

Dear Andreas Richter,

Thank you very much for your suggestions.

- **L11: "weighted vertical columns of CO2 mixing ratios" - I'm confused by this formulation. To me, the result of the measurements are vertically averaged CO2 mixing ratios, not columns**

We have changed the wording to: "The integrated-path differential-absorption lidar CHARM-F is installed onboard an aircraft, in order to detect weighted column-integrated dry-air mixing ratios of CO₂." We use the word "column" to indicate that the vertical integration limits correspond to the scanned volume beneath the aircraft, not the entire atmosphere. For clarification we refer to Eq. (3) in Ehret et al. 2017 (<https://doi.org/10.3390/rs9101052>) descriptive for the satellite mission MERLIN and therefore methane, but of course equivalent for CO₂:

$$XCH_4 \equiv \frac{\int_0^{p_T} m_r(p) WF(p, T) dp}{\int_0^{p_T} WF(p, T) dp} = \frac{DAOD}{\int_0^{p_T} WF(p, T) dp} = \frac{\ln \left[\frac{P_{off}(r_T) E_{on}}{P_{on}(r_T) E_{off}} \right] - DAOD_{other\ gases}}{2 \int_0^{p_T} WF(p, T) dp}$$

where

$$WF(p, T) = \frac{\sigma_{on}(p, T) - \sigma_{off}(p, T)}{g(p) M_{air} (1 + M_{H_2O} q(p)_{air})}$$

m_r being the dry-air mixing ratio of CH₄ at a given pressure p , p_T being the pressure at the reflecting surface (target) and q_{dry} is the water vapor mixing ratio with respect to dry air.

- **L95: molecular, absorption => molecular absorption**
Emended
- **L107: " $\Delta\sigma(z)$ is the difference between the absorption cross section of the two laser pulses given in square meter" - not entirely precise as the cross-section is the one of CO₂, not of the laser pulse and the difference is because of the difference in wavelength. What about " $\Delta\sigma(z)$ is the difference between the CO₂ absorption cross section for the two laser wavelengths given in square meter"?**
Emended
- **L107: Cross-section is not explicitly mentioned in the Figure, just "absorption"**
At this point, the Figure depicts the principle of an IPDA lidar schematically. A high cross-section corresponds to a high absorption, while a low cross-section corresponds to a low absorption.
In the Caption we've changed "absorption wavelength" to "absorption line", as a molecule doesn't have a wavelength. Moreover, we've appended the following sentence to the caption: "The black line in (b) schematically depicts the measurement principle, not the actual spectral absorption line shape of CO₂."
If there are no objections from your side, we would like to stick to the label "absorption".
- **Caption Figure 4: "and horizontal spacing of 250 m and 50 m" - not sure how to interpret this**
It's the distance between the individual towers. We've changed the sentence to: "The towers have a height of 120 m and distances of 250 m and 50 m between each other."
- **L228: Errors according to => Errors resulting from**
Emended
- **L230: need not be => need not to be**
Emended
- **L242 and elsewhere: two-tenth: I find this way of separating the error into its components quite unusual, why not say "20% of the uncertainty..."?**

The intention was to not go into the quantitative details of the values of the error components, but to outline their rough attribution fraction. In this way, we thought, we'd guide the reader most straight forward, to the importance of the error attribution by the wind. Moreover, we intended to prevent the reader from confusing the error fractions with the actual values of the errors, since we also give these as percentages in several places.

Be that as it may, we consent that this is an unusual way, but feel it is constructive at this point. To make the attribution more visually accessible, we have changed the written-out attributions into fractional numbers.

We would like to keep it this way, if you disagree, please let us know.

- **Section 4: I'm not sure what the right way of determining the mean wind in the model results really is. For a realistic comparison to the measurements, the right wind would be that of the model run at lower resolution. I would assume, that strong turbulence will lead to strong fluctuations in wind speed and direction over time and altitude, and in a real world application, this will further increase the uncertainty of the assumed wind vector and thus the emission estimate. My concern is, that by trying to find the best wind vector from the simulation, the uncertainty is actually underestimated.**

Measurement uncertainties in a real-world application would certainly add up to that. However, the purpose of our assessment is not to provide an uncertainty estimate. We want to pinpoint to the variations in the retrieved emission rates that arise from inhomogeneities induced by turbulence alone and the potential of avoiding times of strong turbulence. In this consideration, we have tried to keep systematic errors to a minimum. This is the reason why we do not simulate measurement noise, for that matter.

- **L373: higher number of crossings are required => larger number of crossings is required**
Emended

All individual changes can be reviewed in the marked-up manuscript version below.

On behalf of all Co-Authors,
Sebastian Wolff

Determination of the Emission Rates of CO₂ Point Sources with Airborne Lidar

Sebastian Wolff¹, Gerhard Ehret¹, Christoph Kiemle¹, Axel Amediek^{1,†}, Mathieu Quatrevalet¹, Martin Wirth¹, and Andreas Fix¹

5 ¹Deutsches Zentrum für Luft– und Raumfahrt (DLR), Institut für Physik der Atmosphäre, Oberpfaffenhofen, Germany
[†deceased, 28 January 2021](#)

Correspondence to: Sebastian Wolff (sebastian.wolff@dlr.de)

Abstract. Anthropogenic point sources, such as coal-fired power plants, produce a major share of global CO₂ emissions. International climate agreements demand their independent monitoring. Due to the large number of point sources and their global spatial distribution, the implementation of a satellite-based observation system is convenient. Airborne active remote sensing measurements demonstrate that the deployment of lidar is promising in this respect. The integrated-path differential-absorption lidar CHARM–F is installed onboard an aircraft, in order to detect [weighted column-integrated dry-air mixing ratios of weighted vertical columns of CO₂-mixing-ratios](#), below the aircraft along its flight track. During the Carbon Dioxide and Methane mission (CoMet) in spring 2018, airborne greenhouse gas measurements were performed, focusing on the major European sources of anthropogenic CO₂ emissions, i.e., large coal–fired power plants. The flights were designed to transect isolated exhaust plumes. From the resulting enhancement in the CO₂ mixings ratios, emission rates can be derived via the cross–sectional flux method. On average, our results roughly correspond to reported annual emission rates, with wind speed uncertainties being the major source of error. We observe significant variations between individual overflights, ranging up to a factor of 2. We hypothesize that these variations are mostly driven by turbulence. This is confirmed by a high–resolution large eddy simulation that enables us to give a qualitative assessment of the influence of plume inhomogeneity on the cross–sectional flux method. Our findings suggest avoiding periods of strong turbulence, e.g., midday and afternoon. More favorable measurement conditions prevail during nighttime and morning. Since lidars are intrinsically independent of sunlight, they have a significant advantage in this regard.

1 Introduction

25 CO₂ causes the strongest radiative forcing among all anthropogenic greenhouse gases (e.g., Myhre et al. (2014)). Therefore, it plays a crucial role with respect to human-induced climate change. In 2018, CO₂ has reached a global annual average of 407.4 ppm at the Earth’s surface, an increase of 47 % compared to the year ~1750 (Friedlingstein et al., 2019). One-third of all anthropogenic CO₂ emissions stem from localized point sources, in particular coal–fired power plants (Oda and Maksyutov, 2011). For Europe, they even account for 45% of CO₂ emissions (Super et al., 2020). The Paris Climate Agreement aims to
30 reduce anthropogenic greenhouse gas (GHG) emissions by means of *nationally determined contributions* (NDCs), which are

based on national capabilities and the level of economic development (UNFCCC, 2015). Therein it is foreseen that as of 2023 a *global stocktake* will take place every 5 years. This requires independent measurements to verify each nation's emission reports of CO₂, but also of other greenhouse gases, such as CH₄. Currently, there is no independent global emission verification system available, and a complete record of all emissions globally is still far from reality. To achieve this goal, satellite missions are indispensable. Satellite missions are expected to detect CO₂ emissions from large power plants and cities, e.g., the future European Carbon Constellation CO2M (Bézy et al., 2019; Broquet et al., 2018; Kuhlmann et al., 2020), and other mission ideas still in the pre-development phase (Kiemle et al., 2017; Strandgren et al., 2020). Furthermore, CH₄ emissions can also be detected, as is done by GHGSat-D for coal mine ventilation shafts (Varon et al., 2020), or the Sentinel-5 Precursor for the oil and natural gas-producing sector (Pandey et al., 2019; Zhang et al., 2020). Under particularly favorable conditions, it is already possible to detect CO₂ emissions of power plants from space, as is done with data from NASA's OCO-2 mission (Nassar et al., 2017; Reuter et al., 2019). However, at the moment no operating satellite mission is able to quantify emissions from large power plants, on a regular basis. In the development phase for potential missions, airborne measurement campaigns serve as a test of the methods. During the operating phase, they are needed for verification of the space-borne results.

In May/June 2018, the CoMet (Carbon Dioxide and Methane mission) field campaign took place. The objective of CoMet was to investigate the fluxes of the major human-influenced GHG on local, regional, and sub-continental scales. These fluxes were to be determined more precisely than previously possible. Furthermore, supporting activities for GHG stocktaking were provided. The CoMet campaign saw the deployment of a suite of airborne instruments to measure atmospheric CH₄ and CO₂, alongside a variety of ground-based instruments. In particular, the synergetic use of active remote sensing (lidar) (Amediek et al., 2017; Wildmann et al., 2020), passive spectrometry (Krautwurst et al., 2021; Luther et al., 2019), and in situ measurements (Fiehn et al., 2020; Gałkowski et al., 2021; Kostinek et al., 2020) supported by modeling activities (Chen et al., 2020; Nickl et al., 2020), as well as the validation of existing (e.g., Sentinel-5P, GOSAT (Greenhouse Gases Observing Satellite)) and the preparation of upcoming (e.g., MERLIN (Methane Remote Sensing Lidar Mission)) GHG satellite missions were aimed at. Hereby, the German research aircraft HALO (High Altitude and Long Range Research Aircraft) acted as the airborne flagship of that campaign. HALO was equipped with the new airborne CO₂ and CH₄ IPDA (integrated-path differential-absorption) lidar CHARM-F (CO₂ and CH₄ Remote Monitoring-Flugzeug) built and operated by DLR as an airborne demonstrator for the upcoming MERLIN mission (Ehret et al., 2017). CHARM-F simultaneously measures the column-averaged dry-air mixing ratios of carbon dioxide (XCO₂) and methane (XCH₄) between aircraft and ground (Amediek et al., 2017). The influence of other trace gases, in particular H₂O, on the mixing ratio measurements is negligible. As a result of the pulse repetition frequency (50 Hz, double pulse) and divergence (~1.5 mrad) the pattern on the ground is a sequence of overlapping footprints. The vertical column measurements are insensitive to vertical redistribution of the trace gases. The insensitivity towards optically thin clouds, aerosol layers, and varying surface albedo, and the instrument design with e.g., active laser frequency control is a further strong asset of the IPDA lidar approach. Albedo variations basically affect the measurement precision (statistical uncertainty), whereas the influence on the bias is negligible (Amediek et al., 2009).

During the CoMet campaign, HALO probed various local plumes of different coal-fired power plants. As a case study, the paper in hand focuses on the measurement flight of 23 May 2018, where the CO₂ exhaust plume of the power plant Jämschwalde, close to the Polish-German border was surveyed. The specific goal is to quantify the CO₂ fluxes of the power plant. An established method for quantifying emission rates of point sources is the *cross-sectional flux method*, which is a product of mean wind speed and an integrated concentration enhancement along a cross-sectional overflight of the exhaust plume. This principle has been applied for air-/space-borne nadir-viewing remote sensing (Krings et al., 2018; Menzies et al., 2014; Varon et al., 2018; Reuter et al., 2019), mobile ground-based sun-viewing remote sensing (Luther et al., 2019), as well as airborne in situ measurements (Cambaliza et al., 2014; Conley et al., 2016; Fiehn et al., 2020; White et al., 1976). Amediek et al. (2017) have described how this principle can be realized with CHARM-F. Using CHARM-F data from the respective overflights, we strive to accurately assess the error and advance the general methodology.

When determining the cross-sectional flux, one of the major error sources is the local wind field. On the one hand, because the wind speed is directly included in the calculation, on the other hand, because atmospheric turbulence can broaden or constrict the spatial extent of the exhaust plume. This is a well-known problem, which contributes significantly to the measurement error (Kuhlmann et al., 2019; Luther et al., 2019; Strandgren et al., 2020; Varon et al., 2018; Jongaramrungruang et al., 2019; Kumar et al., 2020). Consequently, the observed CO₂ column enhancements between subsequent plume transects may vary considerably, despite a constant emission rate. We hypothesize that these turbulence-induced variations dominate the measurement error of the emission estimates rather than the GHG column measurement uncertainty itself. To assess the impact of this atmospheric turbulence on our measurement results, we perform a large eddy simulation (LES) in order to resolve local plume structures. By doing so, we can compare different ambient weather and turbulence conditions. We aim to separate more and less favorable conditions, to determine an adequate distance between emission source and measurement locations, and to find out how many independent plume measurements will be necessary, in order to obtain an appropriate emission rate accuracy, as a function of those environmental conditions.

This paper is organized as follows: Section 2 introduces the IPDA lidar method, describes the retrieval of the emission rate, and the methodical errors. Section 3 reports on the plume measurement results. Section 4 provides the simulation setup, while the subsequent results are presented in Sect. 5. A discussion is given in Sect. 6, followed by the conclusion in Sect. 7 and the outlook in Sect. 8.

2 Cross-sectional flux method

2.1 Flux calculation

The dataset underlying this work originates from IPDA lidar CHARM-F. A more detailed description of the lidar system can be found in Amediek et al. (2017). At its core, CHARM-F consists of a pulsed, tunable laser source and a detector. Installed on an aircraft or satellite, the nadir-oriented lidar emits two laser pulses that propagate through the atmosphere until they are backscattered at a surface. The two backscattered laser pulses are detected by the lidar. The wavelength of one laser pulse

corresponds to the absorption wavelength of the greenhouse gas under consideration. In the following, this laser pulse is referred to as *online*. Due to molecular absorption the intensity of the online laser pulse decreases while propagating through the atmosphere. The wavelength of the other (*offline*) laser pulse is slightly shifted such that almost no absorption by the greenhouse gas takes place, but the interaction with the remaining atmospheric components is unaltered.

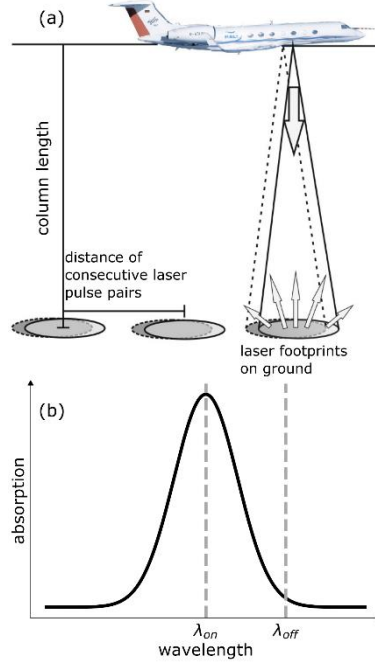


Figure 1: Figure by Amediek et al. (2017). The measurement geometry of a lidar, illustrated by the example of CHARM-F carried on the aircraft HALO. Two laser pulses are emitted towards the earth with a delay of 500 μs . The laser pulse with the wavelength λ_{on} is on the absorption ~~wavelength-line~~ of CO_2 (1572.02 nm), the laser pulse with the wavelength λ_{off} is not (1572.12 nm). By comparing the backscattered intensities, the CO_2 concentration in the measured cone volume can be calculated. The measured volume is usually referred to as a vertical air column, since the column length, i.e., the aircraft's altitude above ground (~ 6500 m), is very large compared to the diameter of the reflecting surfaces (~ 10 m). The distance of consecutive laser pulse pairs is 3 m. The black line in (b) schematically depicts the measurement principle, not the actual spectral absorption line shape of CO_2 .

100 Using a beam splitter, a small part of both the online and the offline laser pulse energy ($E_{\text{on/off}}$) is deflected onto a detector while still in the lidar system. Together with the radiation fluxes entering the lidar telescope $P_{\text{on/off}}$ the differential optical absorption depth (DAOD) can be calculated (Ehret et al., 2008):

$$DAOD = \frac{1}{2} \cdot \ln \left(\frac{P_{\text{off}}/E_{\text{off}}}{P_{\text{on}}/E_{\text{on}}} \right) \quad (1)$$

Note that for the DAOD a single value is obtained for the entire vertical air column. It is a metric for the greenhouse gas
105 concentration of the measured column and is also defined by the following relationship:

$$DAOD = DAOD_b + \Delta DAOD = DAOD_b + \frac{1}{M} \int_0^l \Delta \sigma(z) \cdot \Delta c(z) dz \approx DAOD_b + \frac{\overline{\Delta \sigma}}{M} \int_0^l \Delta c(z) dz \quad (2)$$

Here, DAOD_b is the background differential absorption optical depth, ΔDAOD is the enhancement in the DAOD induced by the plume, M is the molecular mass of CO₂ in gram, and Δc(z) is the enhanced CO₂ density induced by the plume in gram per cubic meter. Δσ(z) is the difference between the CO₂ absorption cross section ~~of for~~ the two laser ~~pulses-wavelengths~~ given in square meter (cf. Fig. 1). It is referred to as the differential-absorption cross section. Generally, Δσ(z) is not constant over the plume's vertical extension, due to the decreasing pressure with altitude. However, the decreases in pressure associated with typical vertical plume extensions are small. As an approximation, we use the mean value over the vertical extent of the plume $\overline{\Delta\sigma}$. This aspect is discussed in more detail in Sect. 3. The vertical integral limits are the ground (z = 0 m) and the respective height of the aircraft fl. Variations in flight altitude, as well as topography, may cause variations in the surveyed column length and thus ultimately in the measured DAOD. In this study, these variations are negligible, since the flight altitude was deliberately kept constant and the topography around the power plant under consideration is sufficiently flat.

This DAOD dataset is used to determine the CO₂ emission rate of a point source utilizing the flux calculation method introduced by Amediek et al. (2017). As schematically depicted in Fig. 2, a crossing of the exhaust plume leads to a DAOD enhancement. This is caused by the additional absorption of laser radiation by the CO₂ molecules of the plume. The instantaneous flux through the lidar cross-section, in the moment of the overflight, is given in kilogram per second and denoted by q:

$$q = A \cdot \frac{M}{\overline{\Delta\sigma}} \cdot u \cdot \sin(\varphi) \quad (3)$$

Given in meter, the parameter A corresponds to the integrated DAOD enhancement over the background DAOD in the direction of the aircraft flight track as shown in Fig. 2b. In the following, it is referred to as *integrated enhancement*. The mean horizontal wind speed u is given in meter per second and the angle between the wind direction and the aircraft's flight direction is denoted as φ (in the following referred to as relative wind direction). Furthermore, it is assumed that no uptake by the soil takes place when the gas plume hits the ground and that the flight altitude is high enough (i.e., well above the Planetary Boundary Layer) to cover the entire vertical extent of the plume.

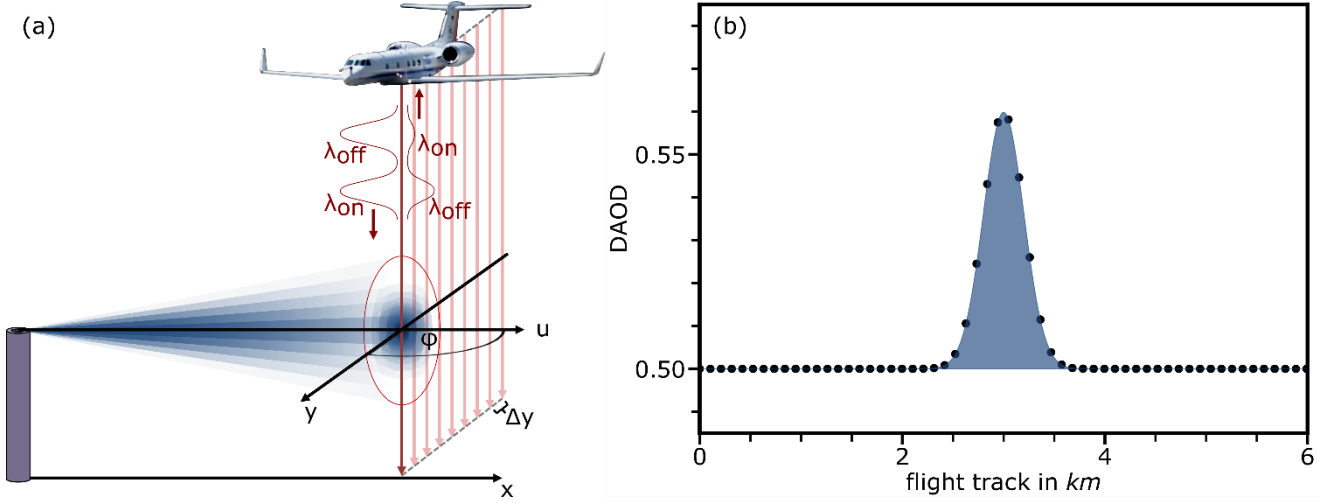


Figure 2: Crossing an exhaust plume illustrated by the example of CHARM-F carried on the aircraft HALO. (a) Two laser pulses are emitted towards the earth with a short delay. The laser pulse with the wavelength λ_{on} is on the absorption wavelength of CO_2 , the laser pulse with the wavelength λ_{off} is not. By comparing the backscattered intensities, the DAOD can be calculated (see Sect. 2.1). An ideal exhaust plume of a point source has a Gaussian-shaped mean concentration distribution both horizontally and vertically. (b) A perpendicular crossing of the plume yields a Gaussian-shaped DAOD dataset.

The two closely spaced sounding wavelengths are selected in such a way that the impact from unknown particles is minimized while keeping the absorption by water vapor is as low as possible. This is due to the very weak water vapor differential-absorption cross section, which is more than 4 orders of magnitude smaller than the differential-absorption cross section for CO_2 . Thus the influence of additional water vapor in the plume released by the cooling or coal drying systems of the power plant is negligible (Kiemle et al., 2017). Moreover, the selected CO_2 absorption line is sufficiently temperature-insensitive, such that the influence of temperature variations within the plume can be neglected (see also Kiemle et al. (2017)). Under these conditions, the flux error is mainly driven by uncertainties of the four parameters A , $\overline{\Delta\sigma}$, u , and φ . Assuming that these parameters are not correlated, the relative accuracy in the flux calculation can then be estimated by error propagation means:

$$\frac{\delta q}{q} = \sqrt{\left(\frac{\delta A}{A}\right)^2 + \left(\frac{\delta(\overline{\Delta\sigma})}{\overline{\Delta\sigma}}\right)^2 + \left(\frac{\delta u}{u}\right)^2 + \left(\frac{\delta \varphi}{\tan(\varphi)}\right)^2} \quad (4)$$

With $\delta A/A$, $\delta(\overline{\Delta\sigma})/\overline{\Delta\sigma}$, $\delta u/u$ denoting the relative uncertainties of these parameters. From this, it is obvious that crossing the plume perpendicular to the wind direction as displayed in Fig. 2a would give the highest accuracy for any fluctuation of the wind direction $\delta\varphi$. On the other hand, atmospheric conditions at low wind speeds or situations with high atmospheric turbulence are in general less favorable because of the high uncertainty in the mean wind speed and wind direction. Varon et al. (2018) have identified 2 m/s as the minimum threshold of wind speed for the applicability of the cross-sectional flux method.

This minimum value is also referred to by Sharan et al. (1996), arguing that above this threshold, advection dominates over diffusion.

145 2.2 Background separation

For the calculation of the integrated enhancement A and its uncertainty, it is crucial to distinguish between the DAOD value attributable to the background concentration of CO_2 and the fraction attributable to the exhaust plume of the point source. As shown in Eq. (2), the measured DAOD along the flight track is the sum of background term DAOD_b and the enhancement due to the plume interaction ΔDAOD . A complicating factor is that the background term may not be constant. There are small
150 variations in local CO_2 concentration from other anthropogenic sources (traffic, cities, etc.) or local interaction with the biosphere. Also, small CO_2 gradients caused by the sounding of different air masses in the vicinity of the plume may have an impact on the background term. In the following, we describe a suitable method that enables us to extract ΔDAOD from the measured dataset, while allowing the background term to be variable.

An example of the plume extraction procedure is shown in Fig. 3. The plume must first be detected as an enhancement not
155 attributable to noise in the data. For this, we examine a 0.2 km running mean of the DAOD dataset (Fig. 3a). The choice of 0.2 km is made because it corresponds to the diameter of the pixels of the simulation (see Sect. 4). The larger the window for the running mean, the less noise is present and the clearer the plume enhancement can be seen. Then again, peaks threaten to be blurred if the window width becomes too large.

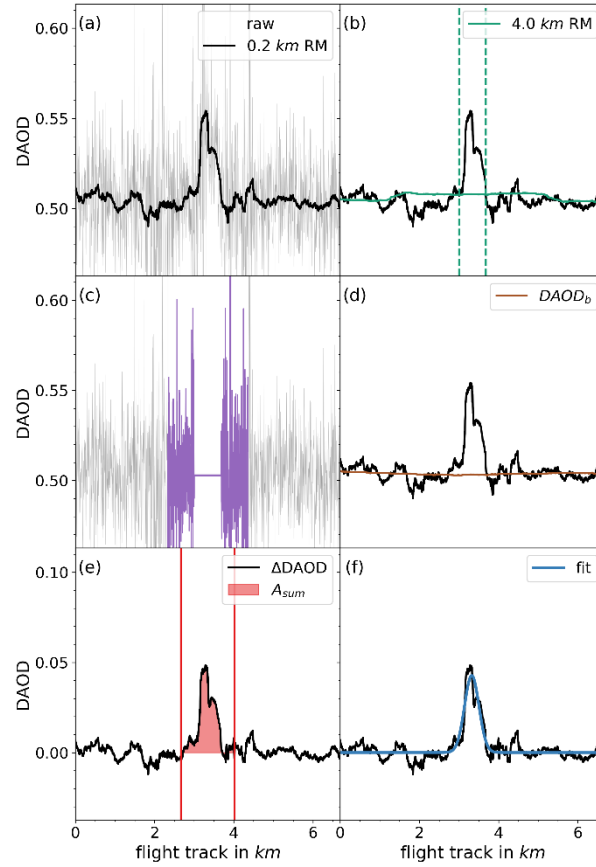


Figure 3: Plume crossing at a point source distance of 1.53 km. In (a) the gray curve shows the raw data, with a standard deviation of 5.2 %, while the black curve shows a 0.2 km (64 data points) running mean (RM), with a standard deviation reduced to 0.9 %. In (b) the green curve is a 4 km (1293 data points) RM. Green vertical dashed lines mark the intersections between the 0.2 km RM and 4 km RM, which are defined as the plume's limits. Colored purple in (c) shows the region of the data used to construct a mean value of the data before and after the plume's limits. This mean value is used to bypass the plume enhancement and is also colored purple. In (d) again a 4 km running mean over the bypassed dataset is shown in brown. This data, which has slight variability, is used as the background term $DAOD_b$. Finally, in (e) and (f) the enhanced term $\Delta DAOD$, i.e., difference between 0.2 km RM and $DAOD_b$, is plotted in black. Note the different scales on the y-axis. In (e) the area underneath the curve is colored red, as an example of the parameter A_{sum} determined with a Riemann sum. Alternatively, a Gaussian fit can be applied to $\Delta DAOD$, providing the parameter A_{fit} as a fit-parameter, as shown as a blue line in (f).

Starting from the middle of the plume enhancement we define the plume's limits as the intersections between the 0.2 km running mean (RM) and another 4 km running mean (Fig. 3b). Applying a running mean broadens and flattens the plume. For larger running mean widths, such as 4 km, the flattening is so severe that the plume is only distinguishable from the background as a raised plateau (see Fig. 3b). The limits are then defined as the intersections between the 0.2 km running mean and the 4 km running mean. For the calculation of this mean we consider a window with a width equal to that of the plume, colored violet in Fig. 3c. At last, we execute another 4 km running mean over the raw dataset, with bypassed plumes, resulting in the

165 background term $DAOD_b$, shown in brown in Fig. 3d. This procedure allows for a variability in the background term on a scale of a few hundred meters. Smaller scale gradients cannot be attributed to the background and are incorporated in the enhancement term $\Delta DAOD$, thereby not being distinguishable from noise.

The mean wind speed u and its mean relative direction ϕ are extracted from model data provided by ECMWF. The molecular mass M and the differential-absorption cross section $\Delta\sigma$ are physical properties of CO_2 and available in various databases such as HITRAN2016 (Gordon et al., 2017). The only parameter that results from a measurement by CHARM-F, or a respective simulation, is the integrated enhancement A . For this purpose Amediek et al. (2017) described two distinct methods. The first method is a Riemann sum over all enhancement values $\Delta DAOD_i$, multiplied with their respective spatial distance Δy_i between two successive data points:

$$A_{sum} = (\sum_i \Delta DAOD_i \cdot \Delta y_i) \quad (5)$$

175 The second method makes use of the fact that, on average, the plume is subject to Gaussian dispersion behavior. According to the function $F(y)$ in Eq. (6), a nonlinear least squares fit is applied to the $\Delta DAOD$ values of the plume.

$$F(y) = \frac{A_{fit}}{A_2 \cdot \sqrt{2\pi}} \cdot e^{-\frac{1}{2} \cdot \left(\frac{y-A_1}{A_2}\right)^2} \quad (6)$$

By doing so the integrated enhancement is obtained as the fit parameter A_{fit} . A_1 is the peak's position along the flight track and A_2 the turbulent dispersion parameter, which is a measure for the width of the plume. The fit method yields very low values for the uncertainty of the parameter A . However, the Riemann sum is not depending on any model assumption for the calculation of the integrated $\Delta DAOD$ along the flight track. Both methods were investigated in the course of this work and showed nearly identical results. Therefore, the results in Table 1 correspond to the mean value of the two methods.

3 Airborne measurements

In this work the measurement flight of HALO on 23 May 2018 between 10:24 and 11:36 is investigated. Located in the south-east of the German federal state of Brandenburg, close to the Polish-German border, the *Lausitz Energie Kraftwerke AG* (LEAG) operates the coal-fired power plant Jänschwalde. It is one of the largest power plants in Europe, both in terms of annual electricity generation and annual CO_2 emissions. For the year 2017, the power plant operators have reported an emission quantity of 24.0 Tg(CO_2) to the European Environment Agency (E-PRTR, 2020). The exhaust gases of this power plant are emitted through the cooling towers at a height of ~ 120 m. Figure 4 shows the flight track of the aircraft, along with a picture of the cooling towers. In total, the point source was flown over seven times downwind, two times upwind, and once directly overhead the cooling towers. In three of the downwind overflights, no enhancement in $DAOD$ is visible. For these transects, the distance to the point source is greater than 4.6 km. At such distances, it can be assumed that the exhaust gases are too diluted with the surrounding air to generate a measurable signal.

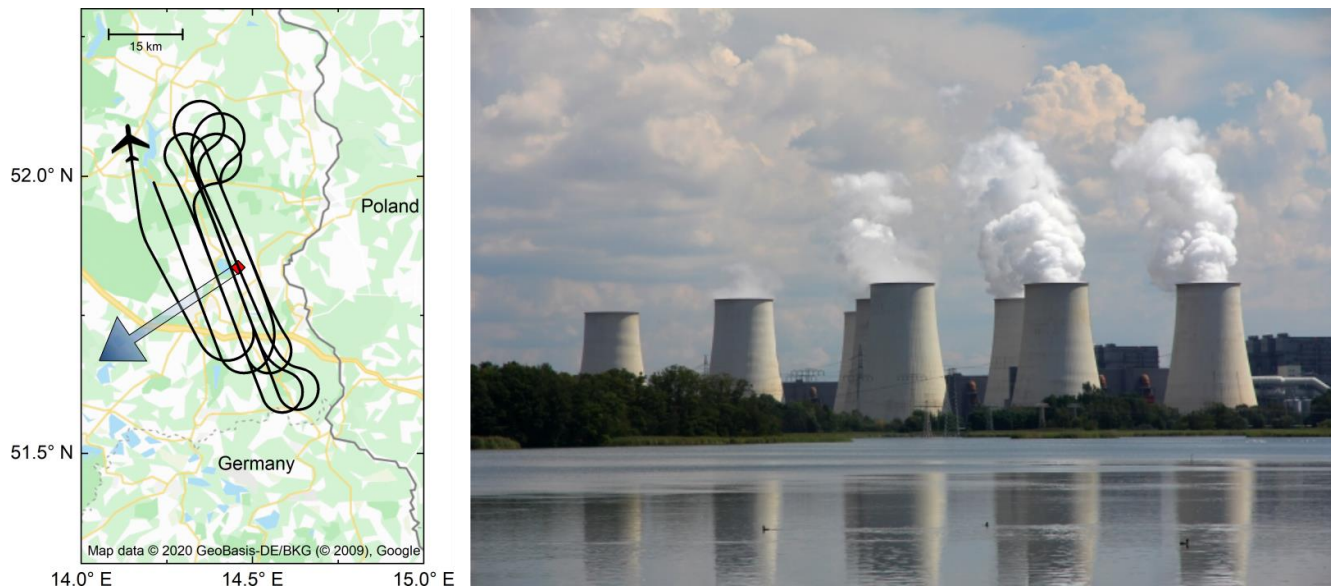


Figure 4: Flight track of HALO in the vicinity of the coal-fired power plant Jämschwalde. The black line on the left depicts the flight track of HALO between 10:24 and 11:36 on the 23 May 2018. The red square marks the position of the power plant Jämschwalde. The arrow shows the mean wind direction during the observation period. The right picture shows the nine cooling towers facing southwest. There the exhaust is released. The towers have a height of 120 m and distances of 250 m and 50 m between each other, horizontal spacing of 250 m and 50 m.

In order to evaluate the uncertainty of the calculated integrated enhancement, a total of 15 different data subsets centered to the plume's position, with varying width, are examined. To ensure that the Riemann sum completely covers the plume, the smallest subset is twice as wide as the plume limits, determined according to Fig. 3. The width of the remaining subsets is expanded by 400 m each.

To further evaluate Eq. (3) the differential-absorption cross section $\Delta\sigma$ is calculated using the Voigt-profile model with input from HITRAN 2016 database for the line parameters (Gordon et al., 2017). This calculation requires the knowledge of pressure and temperature profiles, which are extracted from the simulation introduced in Sect. 4. For the lidar measurements, the online wavelength was tuned to the CO_2 absorption line center at $\lambda_{\text{on}} = 1572.02$ nm, while the offline wavelength was adjusted to $\lambda_{\text{off}} = 1572.12$ nm in the wing of this line (cf. Fig. 1b). Based on this wavelength selection and a flight altitude of 8000 m, the background DAOD_b is approximately 0.5, while the plume causes a ~ 10 % enhancement to this value (~ 0.05), as depicted in Fig. 3. The absorption cross section is not constant over the plume's vertical extension, mainly due to the decreasing pressure and resulting decrease in collisional line broadening with altitude. The relative change in the absorption cross section along the vertical course of the plume depends on the exact online position with respect to the absorption line center. To take a possible cross section change for our measurements into account, representative mean values for the distances at $x_1 \approx 1500$ m and $x_2 \approx 4700$ m (see Table 1) are calculated using the slender plume approximation (Amediek et al., 2017; Seinfeld and Pandis, 1997):

$$210 \quad \overline{\Delta\sigma}(x_{1,2}) = \frac{\int_0^{\max} \Delta\sigma(z) \cdot \left(e^{-\frac{(z-h)^2}{2 \cdot (\sigma_z(x_{1,2}))^2}} + e^{-\frac{(z+h)^2}{2 \cdot (\sigma_z(x_{1,2}))^2}} \right) dz}{\int_0^{\max} \left(e^{-\frac{(z-h)^2}{2 \cdot (\sigma_z(x_{1,2}))^2}} + e^{-\frac{(z+h)^2}{2 \cdot (\sigma_z(x_{1,2}))^2}} \right) dz} \quad (7)$$

In this equation, the ground ($z = 0$ m) and $\max = 4000$ m denote the integration boundaries. h is the height of the cooling towers. The key parameter in this equation is the turbulence parameter σ_z , which is a proxy for the plume extension in the vertical direction, at the respective distance. Different expressions for this parameter for various atmospheric stability conditions can be found in the literature, e.g., Seinfeld and Pandis (1997).

215 Assuming a moderately turbulent atmosphere, we found plume widths of $\sigma_z = 170$ m and 600 m for the two distances. However, if the atmospheric turbulence is less pronounced, the vertical plume widths are only $\sigma_z = 90$ m and 250 m, respectively. Due to the lack of further information on turbulence characteristics during our measurements, we consider both plume widths in the calculation below. The change of $\Delta\sigma(z)$ versus altitude above ground in Eq. (8) is calculated at grid cell spacing of 1 m in the vertical direction using the following 2nd order polynomial function:

$$220 \quad \Delta\sigma(z) = 7.10652 \cdot 10^{-27} m^2 + 8.60755 \cdot 10^{-31} m \cdot z + 8.02673 \cdot 10^{-35} \cdot z^2 \quad (8)$$

Consequently the differential-absorption cross section at the height of the ground (70 m a.s.l.), corresponds to $\Delta\sigma(z = 0 \text{ m}) = 7.10652 \cdot 10^{-27} m^2$. The constant factors of this equation are the result of fitting this function to some representative cross section values from Voigt-profile calculations over the altitude range of 4000 m. The deviations of this approximation to the *exact* Voigt-profile calculations are less than 0.1 %, which is regarded negligible. Finally, Eq. (7) gives the following results:

$$225 \quad \overline{\Delta\sigma}(x_1 = 1500 \text{ m}) = 7.27 \cdot 10^{-27} m^2 \pm 0.04 \cdot 10^{-27} m^2 \quad \text{and} \quad \overline{\Delta\sigma}(x_2 = 4700 \text{ m}) = 7.47 \cdot 10^{-27} m^2 \pm 0.24 \cdot 10^{-27} m^2.$$

The overscore indicates the mean value of the aforementioned turbulence scenarios with corresponding plume vertical widths at each distance and the errors indicate the differences. Close to the source (~ 1500 m), the relative cross section uncertainty is ~ 0.6 % and therefore negligible, whereas, at a distance of 4700 m, the relative error is ~ 3.2 % and not negligible in the overall error budget outlined by Eq. (4).

230 Possible systematic errors, due to uncertainties of the line parameters, are less than 2 % (Gordon et al., 2017). Errors ~~according to~~ resulting from the wavelength setting with the CHARM-F instrument are considered very small compared to the other contributors and therefore need not to be extensively discussed in this study (~ 0.5 %, see Amediek et al. (2017)).

The wind data are taken from operational analysis data of the ECMWF model. This is done by first interpolating the 4-dimensional gridded model data onto the flight path at the altitude of the power plant's exhaust shaft. Secondly, a mean value
235 of the wind speed and direction along the flight track, together with an estimate of their relative errors are calculated according to Ackermann (1983).

Table 1: Flight measurement results of individual crossings for the Jämschwalde power plant on 23 May 2018, following the nomenclature of Eq. (3)

Crossing			Measurement					
local time	flight track in km	distance in km	A in m	$\overline{\Delta\sigma}$ in 10^{-27} m ²	q in kg(CO ₂)/s	mean q in kg(CO ₂)/s	mean u in m/s	mean φ in °
10:50	200	1.46	15.36 ± 0.67	7.27 ± 0.04	760 ± 60	650 ± 240	5.06 ± 0.36	103.34 ± 6.40
10:57	268	4.77	9.04 ± 0.42	7.47 ± 0.24	470 ± 40			
11:10	388	1.67	19.29 ± 0.46	7.27 ± 0.04	950 ± 80			
11:27	536	1.78	8.45 ± 1.11	7.27 ± 0.04	420 ± 40			

Table 1 shows the measured integrated enhancements, the wind data, and the resulting fluxes for the four exploitable overflights, alongside the obtained mean values, under the assumption that during the measurement both the wind direction, as well as the wind speed were reasonably constant. The flight segments were not exactly perpendicular to the mean wind direction. With a relative angle of $\varphi = 103^\circ$ a correction factor of $\sin(103^\circ) = 0.97$ is applied (see Eq. (3)). The mean wind speed is well above the threshold of 2 m/s, introduced at the end of Sect. 2.1.

The individual flux uncertainties, calculated with Eq. (4), are relatively small and range between 8–10 %. It is to be emphasized that the integrated enhancement A is the only parameter in the calculation of the instantaneous flux in Eq. (3), coming from the IPDA lidar measurement itself. On average, ~~two-tenth~~ ^{$\frac{2}{10}$} of this individual measurement uncertainty is due to the uncertainty of the integrated enhancement $\delta A/A$. Taken together, ~~one-tenth~~ ^{$\frac{1}{10}$} can be attributed to the uncertainty of the mean differential-absorption cross section of CO₂ $\delta(\overline{\Delta\sigma})/\overline{\Delta\sigma}$ and the mean relative wind direction $\delta\varphi/\tan(\varphi)$. The major contributor to the flux uncertainty, however, is the uncertainty of the mean wind speed $\delta u/u$, which accounts for ~~two-thirds~~ ^{$\frac{7}{10}$} .

The reported value of 760 kg(CO₂)/s (24.0 Tg(CO₂)/yr) (E-PRTR, 2020) lies within the error range of the mean value of 650 $\pm$ 240 kg(CO₂)/s (20.3 $\pm$ 7.9 Tg(CO₂)/yr). Nevertheless, the variations between the individual crossings are very large, both in the integrated enhancement A, as well as in the calculated fluxes. The second and third crossings differ by approximately a factor of 2 (see Table 1). These variations cannot be explained by our uncertainty estimation, but rather by atmospheric turbulence that distorts the plume. Therefore, this work further investigates the influence of atmospheric turbulence and the resulting inhomogeneity in the propagation of exhaust plumes. To achieve this, we make use of the mesoscale numerical weather prediction system model WRF (Weather Research and Forecasting model).

To investigate the influence of atmospheric turbulence and the resulting inhomogeneity in the propagation of exhaust plumes, we use WRF-ARW, the Advanced Research Version of the Weather Research and Forecasting model (Skamarock et al., 2008). It is a well-established platform to investigate the transport of plumes (Zhao et al., 2019; Bhimireddy and Bhaganagar, 2018; Yver et al., 2013). The model configuration can be found in Table 2.

Table 2: WRF model configuration

	Setting	Reference
WRF version	WRF 3.8.1	Skamarock et al. (2008)
Dynamical solvers	Advanced Research WRF	
Meteorological boundary conditions	Operational ECMWF analysis	ECMWF (2018)
Simulated time span	06:00 UTC on 21 June – 06:00 UTC on 24 June in 2018	
Spin-up	6 h	
Number of vertical layers	56	
Model top	200 hPa	
Radiation	Rapid Radiative Transfer Model Scheme (ra_lw_physics = ra_sw_physics = 4)	Iacono et al. (2008)
Microphysics	Morrison 2-moment Scheme (mp_physics = 10)	Morrison et al. (2009)
Land surface model	Unified Noah Land-Surface Model (sf_surface_physics = 2)	Tewari et al. (2004)
Surface layer physics	Revised MM5 Scheme (sf_sfclay_physics = 1)	Jimenez et al. (2012)

260 Considering typical source distances of the measurement crossings (see Table 1), in addition to the spread of the plumes (see Fig. A1), it is clear that our investigations need to be implemented with a horizontal resolution in the sub-kilometer range. To achieve this, we introduce three nested domains, with the coordinates of the middle cooling tower as the center of the domains (see Fig. 5). The domain configurations can be found in Table 3. As meteorological initial and boundary conditions, operational ECMWF analysis data is used with a horizontal resolution of 9 km.

Table 3: Configuration of quadratic domains

Domain	D1	D2	D3
Horizontal resolution	5 km	1 km	0.2 km
Computational time step	30 s	5 s	1 s
Number of grid points	100	150	175
Domain size, W-E and S-N	500 km	150 km	35 km
Planetary Boundary Layer Physics	MYNN Level 2.5 Nakanishi and Niino (2009)	MYNN Level 2.5 Nakanishi and Niino (2009)	LES PBL Moeng et al. (2007)
Eddy coefficient option	2d Deformation (km_opt = 4)	2d Deformation (km_opt = 4)	3d TKE (km_opt = 2)
Turbulence and mixing option	Simple diffusion (diff_opt = 1)	Simple diffusion (diff_opt = 1)	Full diffusion (diff_opt = 2)

As suggested by Powers et al. (2017) we run the inner domain D3 as a large eddy simulation (WRF-LES). This makes it possible to resolve local turbulence (Moeng et al., 2007). Several studies show that WRF-LES is an adequate tool to model plume trajectories, in conjunction with turbulence and passive tracer dispersion (Nunalee et al., 2014; Nottrott et al., 2014). Only the plume of the power plant is simulated, without any CO₂ background field. WRF-ARW has the option to predefine a tracer variable $tr(t,x,y,z)$ which has the properties of a passive tracer, as used in Blaylock et al. (2017). It represents a four-dimensional field of space-time. A detailed description of the calculation of simulated DAOD can be found in Appendix A. Therein Eq. (A3) is used to calculate the DAOD enhancement corresponding to the horizontal dispersion of the tracer, as shown in Fig. 6.

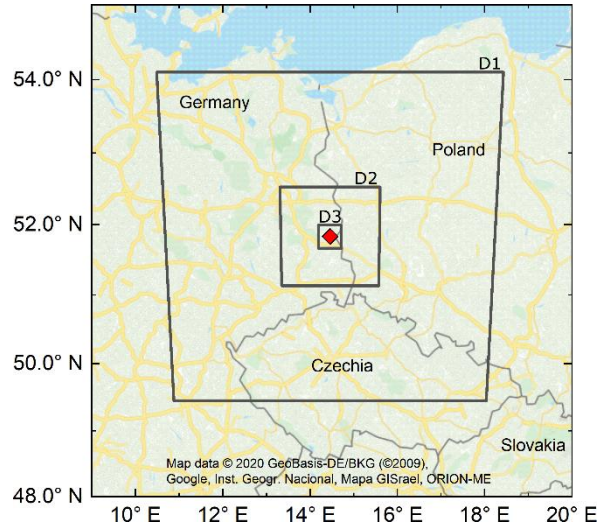


Figure 5: Location of three times nested domains (black squares) of the WRF simulation. They are centered to the power plant Jämschwalde (red square). The domains have a side length of 500 km (D1), 150 km (D2), 35 km (D3) and a horizontal resolution of 5 km (D1), 1 km (D2) and 0.2 km (D3). Vertically, 57 eta levels are introduced ranking from the ground up to a top layer pressure of 200 hPa.

The WRF simulation provides a data output every 2 minutes. One virtual plume crossing is evaluated for each output time step at a point source distance of 1.5 km. This corresponds to our measurements (see Table 1). Since neither background field nor noise is simulated, it does not matter at which distance to the point source the virtual flyover takes place. Nevertheless, we try to match the virtual survey as closely as possible to real conditions. Just as in the real measurement, the virtual crossings are arranged perpendicular to the propagation direction of the plume (cf. Sect. 2.1). However, in a turbulent atmosphere, it is not trivial to precisely identify this direction of propagation. In this work, we consider the center of mass of the emitted tracers within a radius of twice the point source distance, i.e., 3 km. A connecting line between this center of mass and the point source corresponds to the propagation direction.

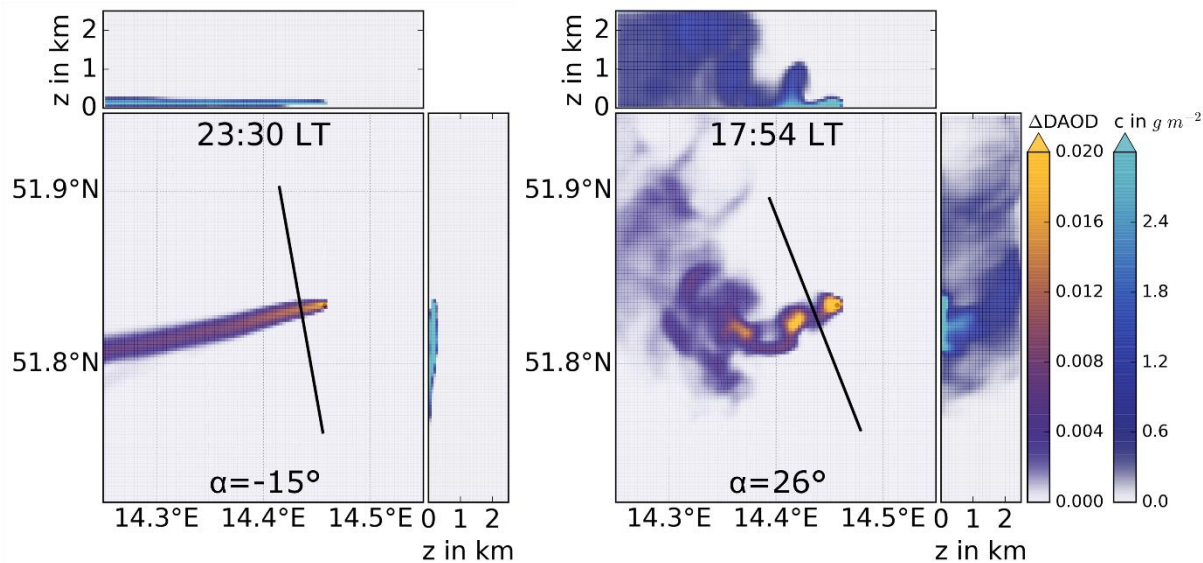


Figure 6: Exemplary snapshots of simulated exhaust plumes. The flight track of the virtual plume overflight is shown as a black line. At the top of the respective middle panel the local time is given in Central European Summer Time (CEST, i.e., UTC+2), at the bottom α denotes the local solar altitude. The first colorbar represents the DAOD enhancement and refers to the respective middle panel, which shows the horizontal dispersion of the plume. The second colorbar represents the mass per area and refers to the top and right panels, which show the vertical dispersion. In a corresponding measurement, DAOD enhancement values beneath 0.008 would not be distinguishable from noise and are therefore displayed blue. Values higher than 0.01 exceed the noise and can be identified as plume enhancement in a real measurement. A Δ DAOD value of 0.02 corresponds to an enhancement of 4 % with respect to a background of 0.5 (cf. Fig. 3). The color maps follow the guidelines for a perception-based color map presented by Stauffer et al. (2015).

For the calculation of the virtually retrieved emission rate, the mean wind speed and direction are needed (see Eq. (3)). To obtain these from the simulation, the following procedure is performed. First, for each data output step the horizontal wind components at the mean height of the plume are retrieved by vertical integration, weighted with tracer mass content. Second, the resulting 2D wind field is linearly interpolated onto the virtual flight path, yielding a 1D field with the horizontal wind components along the flight track. Last, the wind components are integrated, weighted with the DAOD along the flight track, resulting in the mean wind used for calculation.

5 Simulation results

WRF is able to simulate realistic plume dispersion. The DAOD enhancement values correspond to our measurements. Exemplary snapshots of the simulated plume during the course of a whole day can be found in Appendix A in Fig. A2. Additionally, an animated GIF of the simulated plume can be found under <https://doi.org/10.5281/zenodo.4266513> (Wolff, 2020). In the nocturnal absence of solar irradiation, the turbulence decreases, leading to narrow, homogeneous plume dispersion, within a laminar flow. The exhaust plume follows Gaussian behavior, as depicted in Fig. 6 at 23:30. Contrary to this, we find boundary layer turbulence during daytime.

Strong solar heating of the surface generates convective air masses, which in turn cause a cascade of eddies. Consequently,
 295 locally reverse and counter-gradient flow, i.e., flow opposite to the main wind direction, emerges. This results in local *puffs* of
 above-average column concentration enhancements within the exhaust plume, while eddy-generated local flow in the same
 direction as the ambient wind causes *constrictions* of lower column concentrations in a plume (Stull, 1988). Such plume
 structures deviate from Gaussian behavior, as can be seen in Fig. 6 at 17:54.

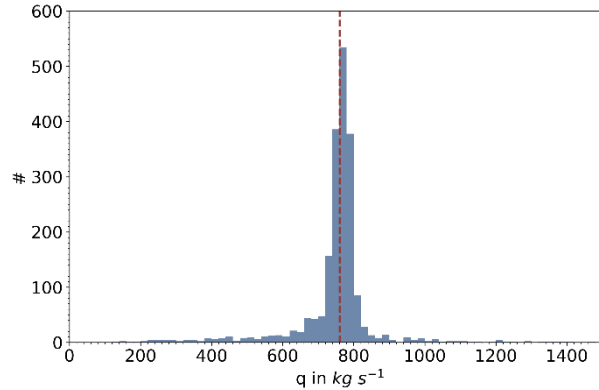


Figure 7: Histogram of virtually retrieved emission rates. The histogram shows a slightly skewed distribution towards smaller emission rates than the input emission rate (red dashed line). It depicts all 1980 emission rates retrieved over 66 simulated hours between 12 UTC on 21 May and 6 UTC on 24 May.

Locally increased CO_2 column concentration results in a high value in the integrated enhancement A , in contrast to an
 300 overflight over a constriction. Following Eq. (3) this corresponds to a high value of the emission rate q . It should also be
 stressed that the spatial extent of such puffs is smaller than that of complementary constrictions. Therefore, a skewed
 distribution of the retrieved emission rates is to be expected, as Fig. 7 confirms.

On 23 May 2018, four measurement flyovers of the power plant Jämschwalde took approximately one hour, as presented in
 Sect. 3. As spin-up we discard the first 6 hours of the simulation (see Table 2). That is 66 hours of simulation, which leaves us
 305 with a total of 1980 virtual plume flyovers. The corresponding results of the emission rate, which are calculated using Eq. (3),
 are displayed as a histogram in Fig. 7 and as a time series in Fig. 8a.

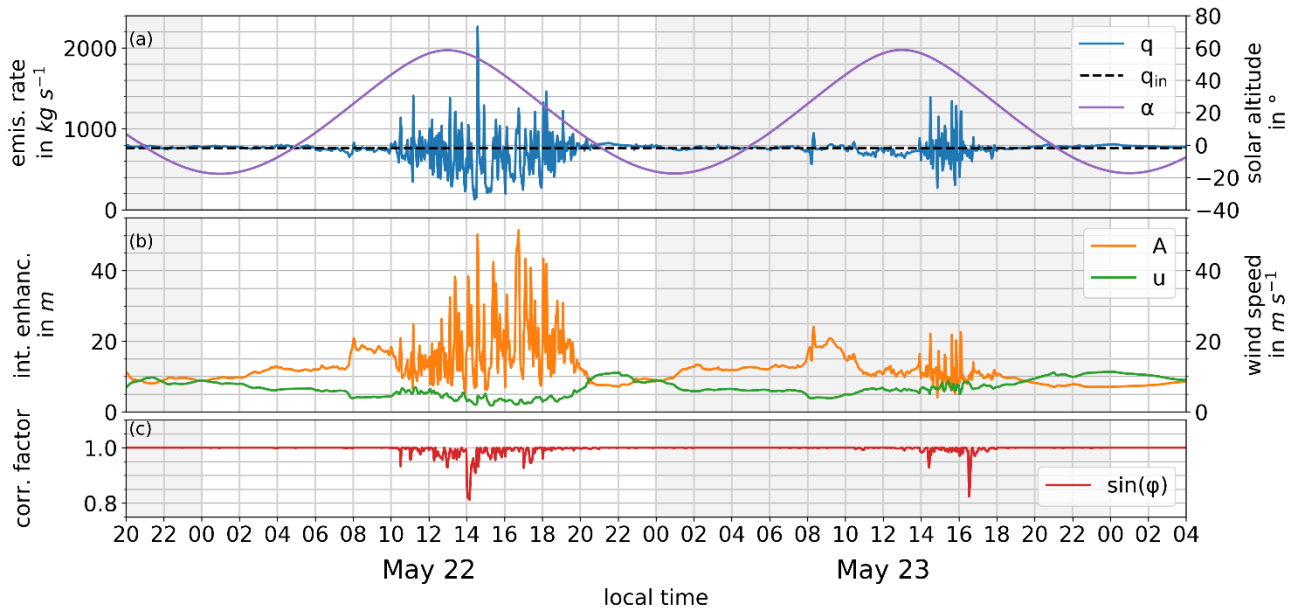


Figure 8: Virtual overflight results in the course of the day. In (a) it can be seen that rising solar altitude α entails turbulence. Especially, midday turbulence causes deviations of the retrieved emission rates q from the input emission rate q_{in} . In (b) the integrated enhancement A shows equivalent behavior, while the variations in wind speed u are comparatively small. It is during the midday turbulence, that the virtual flight tracks are not exactly perpendicular to the instantaneous wind direction at the plume crossing, which becomes apparent in the correction factor $\sin(\varphi)$ in (c). In the night hours, as well as the morning the retrieved emission rates agree very well with the input emission rate q_{in} . The wind speed u surpasses the threshold value of 2 m/s at all times.

In Fig. 8a it can be seen how the diurnal course of solar altitude α influences the retrieved emission rates q . The random occurrence of inhomogeneities in the plume propagation, caused by local turbulence, leads to large variations in the results of successive crossings. Turbulence lags behind solar altitude because the surface needs time to heat up. It is also apparent that the emission rate deviations vary from day to day, both in intensity, as well as in dwell time.

The implications for the measurement results can be reduced by averaging over a multitude of retrieved emission rates. Next, we investigate how often the exhaust plume must be surveyed, to achieve a mean emission rate with satisfactory accuracy. From experience with the Janschwalde measurement presented in Sect. 3, as well as other point source measurements during the CoMet campaign, which are not presented in this work, we assume a time delay in the range of 6 to 18 minutes between two successive crossings. With typical wind speeds in the range of 5–8 m/s and spatial scales of puffs and constrictions of about 1–2 km, our range of time delay exceeds the residence time of coherent plume structures, thus preventing repeated measurements of identical air masses. The model setup provides one measurement every 2 minutes, resulting in a vast number of permutations of successive virtual crossings available for merging (see Table A1). For each of these permutations, a mean value is calculated, which is then compared with the initiated emission rate q_{in} . To evaluate the turbulence-induced inhomogeneity in the daily course, we compare two-hour time frames. We execute a total of 60 virtual overflights in such a

two-hour time frame. The number of possible permutations increases exponentially to 5000 if four crossings are merged and even on to 312500 if seven crossings are merged (see Table A1). This high number of permutations is based on the identical 60 single crossing emission rates, which are displayed in the histograms in Fig.9.

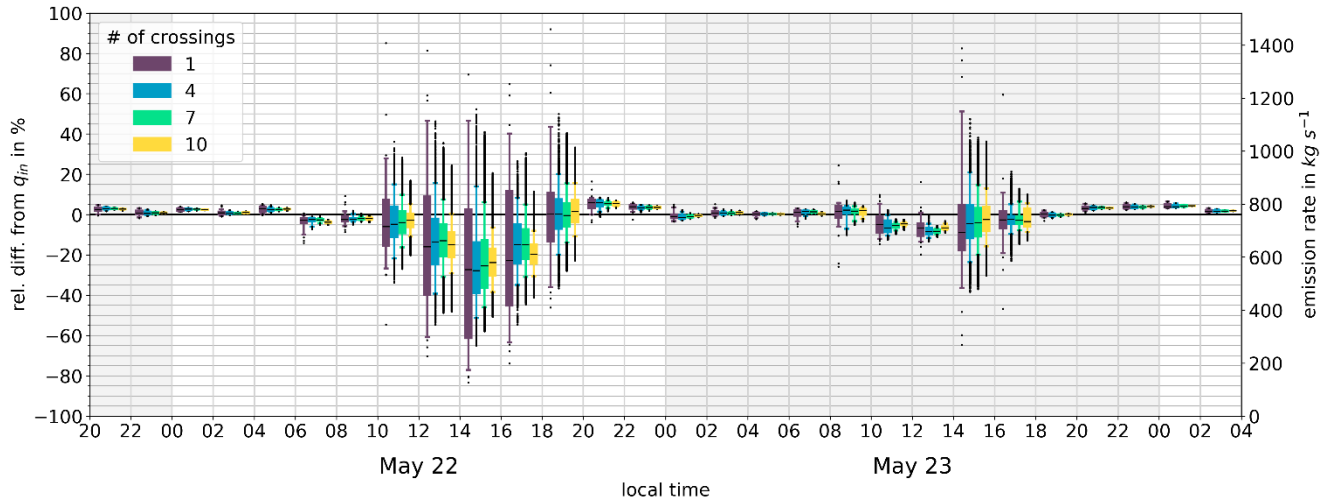


Figure 9: Box-whisker-plot of the relative difference to the input emission rate q_{in} within two-hour time frames. The right axis shows the associated retrieved emission rates. The width of the distribution decreases with a higher number of crossings. For all time frames it can be stated that with an increasing number of merged crossings the width of the distribution decreases. The largest differences to q_{in} are observed in the afternoon. Different colors represent a different number of virtual crossings merged for averaging. The inner boxes range from the first to the third quartile, thus containing 50 % of the values. The median is marked within as a black dash. The upper whisker is drawn up to the 95th percentile, while the lower whisker is drawn to the 5th percentile. Consequently 90% of the values are in between the two whiskers. All values outside the whiskers are outliers and plotted as dots.

Figure 9 presents the resulting distribution of this relative difference to the input emission rate as a box-whisker-plot. The spread of the respective box-whisker-plot is an indicator of turbulence. It is evident that with an increasing number of overflights merged for averaging the spread of the relative differences decreases, while the measurement precision increases. A high emission rate measured by a single overflight scanning a puff is compensated if the subsequent overflight measures a lower emission rate. With a higher number of overflights averaged, it is more likely to measure both high and low concentration air masses. Yet, although the precision can be improved by increasing the number of overflights, even for ten overflights it is inferior to the precision of nighttime measurements. Additionally, not only the precision but also the accuracy is compromised during times of strong turbulence, i.e., in the afternoon. As aforementioned, the spatial extent of turbulence-induced puffs is smaller than the one of the complementary constrictions. Therefore, such puffs are likely to be less frequent and only partially scanned when measured at a low sampling frequency. Consequently, the retrieved emission rates will be biased low. This is an effect that occurs especially during strong turbulence. In Fig. 9 a strongly turbulent day (22 May) is compared to a less turbulent day (23 May). Both precision and accuracy are superior on a less turbulent day.

In contrast, the night hours show little turbulence and high precision. Even with a single overflight, small differences to the true emission rate are to be expected. Here, a higher number of overflights will only cause minor improvements. At this point, it should be mentioned that the representation of nightly plume propagation must be critically reviewed. The plume height decreases so much that the propagation takes place only in the lowest four model layers. The fact that a bias of approx. $\pm 5\%$ remains at night is not surprising from this point of view. This study should therefore be understood as a qualitative assessment. The key finding is that avoiding situations of high turbulence brings an enormous improvement for both precision and accuracy. Even with a significantly higher number of measurement overflights, a comparable improvement cannot be attained.

6 Discussion

Regarding the lidar measurements during the CoMet campaign on 23 May 2018, we find that the mean emission rate, derived from repeated plume overflights, is in rough agreement with the average emission reported by the power plant operator for the year 2017. The cross-sectional flux method is straight forward to apply. The exhaust plume generates column enhancements in the differential absorption optical depth (DAOD), with a good signal-to-noise ratio, in the order of 10 %. The product of enhanced column concentration integrated along the flight track and mean wind speed, provides the flux through the lidar cross-section, at the instant of the overflight. This instantaneous flux of an individual overflight measurement can be determined with an error ranging between 8–10 %. This error is mainly driven by uncertainties of the integrated enhancement, the mean differential-absorption cross section, the mean relative wind direction, and the mean horizontal wind speed. On average, we find that ~~two-tenth~~ $\frac{2}{10}$ of the flux error can be attributed to uncertainty in the determination of the integrated enhancement, i.e., the integrated enhancement of the DAOD signal, which is the only parameter that needs to be derived from the IPDA lidar measurement. ~~One-tenth~~ $\frac{1}{10}$ can be attributed to the uncertainties of the mean differential-absorption cross section of CO₂ and the relative wind direction, taken together. The main source of error, however, is the mean horizontal wind speed, with a contribution of ~~two-thirds~~ $\frac{7}{10}$. This highlights the need for more accurate wind information. Future studies will examine CHARM-F measurements in the Upper Silesian Coal Basin to determine CH₄ emissions from coal mines. In this area, ground-based Doppler wind lidars have been installed. It is expected that nudging the simulation towards the wind soundings will result in an improvement of the wind vector estimation, ultimately reducing the overall error in the flux determination.

It is necessary to distinguish between instantaneously measured flux and actual emission rate. In theory, an exhaust plume behaves Gaussian on average and the mean emission rate of the point source lies within the error range of the instantaneously measured fluxes. Contrary to this, our overflights reveal large variations between the individually retrieved instantaneous fluxes, which cannot be attributed to measurement uncertainties. These variations do not occur because the measurement error increases, but because plume segments with varying CO₂ content are probed. The actual measurement error is minor compared to these variations (cf. Table 1). As described in Sect. 5, strong solar heating causes turbulence, which forces the plume to

deviate from Gaussian behavior. This deviation can be restricted by averaging over a multiple of instantaneous fluxes, as the results from our measurement flights suggest.

To analyze this effect in more detail, we employ the atmospheric transport model WRF in a high-resolution large eddy simulation (LES) setup. We find that the model simulates realistic plume dispersion. Typical DAOD values, as well as turbulence-induced distortions, show the same order of magnitude as our measurements. However, as we evaluate only four overflights in the measurement, we cannot make any statement about the absolute accuracy of the simulation, which is also not the intention of this work. Qualitatively, the simulation provides the following insights. During the night the plumes are weakly distorted and have a Gaussian shape because laminar flow dominates. Over the course of the day, turbulence increases, reaching its peak in the mid-afternoon and distorting the plumes to non-Gaussian shapes. Thus, with increasing turbulence, a higher-larger number of crossings are-is required for averaging in order to obtain sufficient emission rate precision. According to our simulation, nighttime measurements require fewer overflights. Under such conditions, even a single instantaneous cross-sectional flux measurement yields an accuracy of up to ~95 %. In cases of very pronounced turbulence (i.e., in the afternoon), even an impractically high number of overflights will neither reach the precision, nor the accuracy of a single nighttime overflight.

At this point, we cannot derive any limits for solar altitude or local times that should be avoided, as the simulation reveals that the turbulence intensity varies from day to day (see Fig. 8 and Fig. 9). Generally, we find that the most significant turbulence occurs in the afternoon. For future campaign planning, we recommend to also perform measurements at night or in the morning, which is possible with lidar.

7 Conclusion

The present study continues the investigations by Amediek et al. (2017) on the quantification of fluxes of local greenhouse gas emission sources using the integrated-path differential-absorption (IPDA) lidar CHARM-F and the cross-sectional flux method. While the preceding study was concentrated on CH₄ emissions from hard coal mines, here, we exploit the results from the CoMet campaign in 2018. We investigate CO₂ plume overflights of the coal-fired power plant Jänschwalde, conducted to quantify its emission rate and to assess how accurately the cross-sectional flux method can be applied. Since CHARM-F measures both greenhouse gases simultaneously, our findings also apply to isolated CH₄ point sources.

With regard to cross-sectional flux measurements, the current work suggests avoiding mid-afternoon periods of strong turbulence. On the one hand, this is because the uncertainties in the wind speed are most pronounced at these times, being the major source of error in a single measurement. On the other hand, this is due to the distortions of exhaust plumes in a turbulent wind field, which lead to substantial deviations from Gaussian plume dispersion. Under strong turbulence, the cross-sectional flux method cannot provide an accurate measurement of the emission rate, not even in the average of a vast number of overflights. Therefore, measurement flights performed during nighttime are beneficial. In this respect, intrinsic independence from solar irradiation is a clear advantage of active remote sensing over passive approaches. Whenever sunlight is needed to

perform the measurement, less turbulent conditions, for example in the morning after sunrise, or winter, should be preferred. Further, it shall be pointed out that, with a lidar, cross-sectional plume measurements can also be performed over water bodies, whose detrimental reflective properties often impede the use of passive remote sensing (Gerilowski et al., 2015; Krautwurst et al., 2021; Larsen and Stamnes, 2006). Therefore, plumes from offshore installations can also be addressed with this approach. Independent of the location of the point source, there are restrictions regarding the adequate distance of a plume overflight to the point source. We report that at a point source distance of more than 4.6 km no enhancement is visible and therefore no plume detection can be performed. In addition to that, we find that the uncertainty of the mean differential-absorption cross section increases with a larger vertical extension of the plume, which correlates with distance. At a point source distance of 1.5 km, this uncertainty is negligible. Concerning the detectability of the plume, we can locate distinct enhancements at a distance of 1.5 km. Nevertheless, the closer to the point source the overflight takes place, the more constrained the plume and consequently the more pronounced the column enhancement is. It must be considered, however, that the horizontal extension is also smaller and thus fewer data points lie within the plume. In the case of CHARM-F, this can be compensated by a higher repetition rate.

8 Outlook

Apart from the CHARM-F measurements, the CoMet campaign also saw the deployment of other airborne instruments to measure atmospheric CH₄ and CO₂, supported by a variety of ground-based, in situ and remote sensing instruments. They were predominantly based in the vicinity of one of the major hot-spot regions of CH₄ emissions in Europe, the Upper Silesian Coal Basin (USCB). Investigations of local and regional CH₄ emissions from this region are, in view of the preparation for the upcoming MERLIN mission, a particular field of interest. The possibility to synergistically use active remote sensing (lidar), passive spectrometry, and in situ measurements supported by modeling activities, allow for unique cross comparisons, which are beyond the scope of the present paper. Such cross comparisons will be subject of subsequent investigations, as well as other HALO measurement flights, as it flew along latitudinal trajectories, performed regional survey flights (e.g., over the Mount Etna) and also probed the local plume of not only Jänschwalde, but also Bełchatów in Poland, which is considered Europe's largest coal-fired power plant, in terms of CO₂ emission. The measured data can make an important contribution to the validation of existing satellite missions (e.g., Sentinel-5P, GOSAT). Further aircraft campaigns (e.g., CoMet-2.0) are foreseen which will provide additional opportunities for methodical refinements, including advancements on model-measurement synergies.

Appendix A

Figures of individual HALO crossings on 23 May 2018:

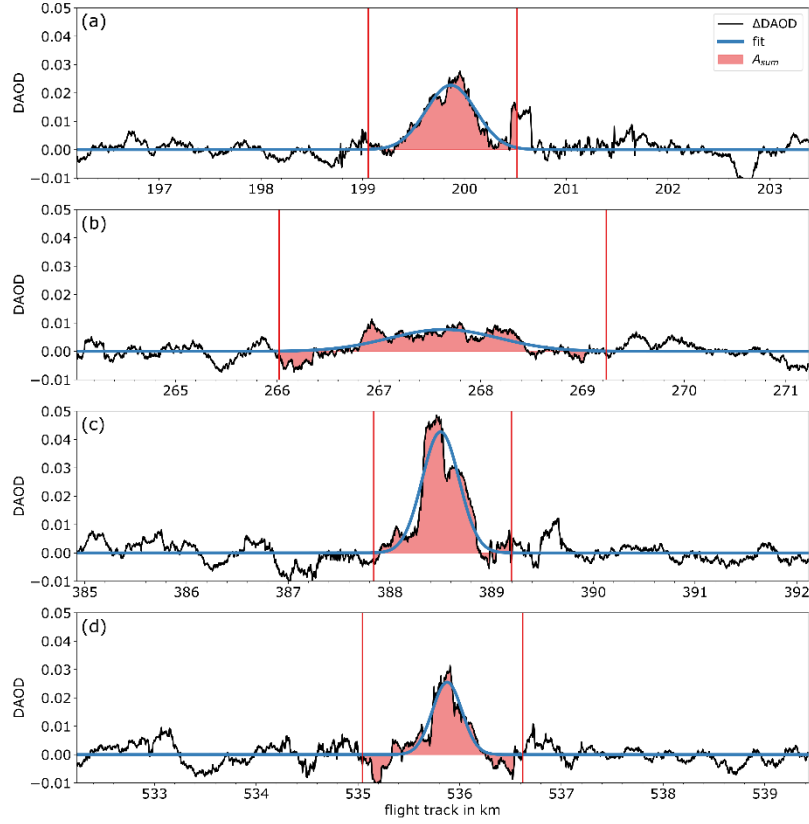


Figure A1: Individual transects listed in Table 1. Red vertical lines mark the smallest data extract used for the Riemann sum, as described in Sect. 3.

Calculation of simulated DAOD:

At the initialization position of the power plant, the value of the tracer variable is increased by the value 1 at each time step.

430 In this study, it is defined only in the inner domain D3.

$$tr(t + \Delta t, x, y, z) = tr(t, x, y, z) + 1 \quad (\text{A1})$$

Here, Δt corresponds to the computational time step of the third domain, i.e., one second (Table 3). At the same time the tracer is distributed in the domain D3 by advection and turbulent dispersion. The corresponding mass concentration $c(t, x, y, z)$ at any grid point x, y, z at time t is obtained as follows:

$$435 \quad c(t, x, y, z) = tr(t, x, y, z) \cdot \frac{q_{in} \cdot \Delta t}{\Delta x \cdot \Delta y \cdot \Delta z(t, x, y, z)} \quad (\text{A2})$$

For the input emission rate q_{in} a constant value of 760 kg(CO₂)/s (24.0 Tg(CO₂)/yr) is initialized, which corresponds to the total annual emission for the year 2017 reported to the European Environment Agency by the operators (E-PRTR, 2020). Δx and Δy correspond to the temporally and spatially constant horizontal size of a grid point (0.2 km). The vertical layer size $\Delta z(t, x, y, z)$ corresponds to the spatial distance between two model levels. In the simulation this distance is computed in pressure coordinates and depends on all four dimensions. Since the pressure varies only slightly between successive time steps, the temporal dependence of Δz is small. At locations with flat topography the dependence of Δz on the horizontal coordinates x and y is also small, at locations with large topographic changes (e.g., steep slopes) the dependence is more significant. The product $\Delta x \cdot \Delta y \cdot \Delta z(t, x, y, z)$ corresponds to the volume of the respective grid box. Within this volume the value of the tracer variable and thus the concentration is constant.

445 In order to compare the simulated data with an IPDA lidar measurement, the concentration array must be summed up vertically and multiplied by the quotient of the mean differential-absorption cross section and the molecular mass:

$$DAOD_{wrf}(t, x, y) = \frac{\overline{\Delta\sigma}}{M} \cdot \sum_{j=1}^{j_{top}} c(t, x, y, z_j) \cdot \Delta z_j(t, x, y, z) \quad (A3)$$

The index j marks the respective vertical layer. Consequently $j \in \{1, 56\}$ applies, and z_j is defined to correspond to the lower edge of the respective layer.

450

Exemplary snapshots of simulated DAOD:

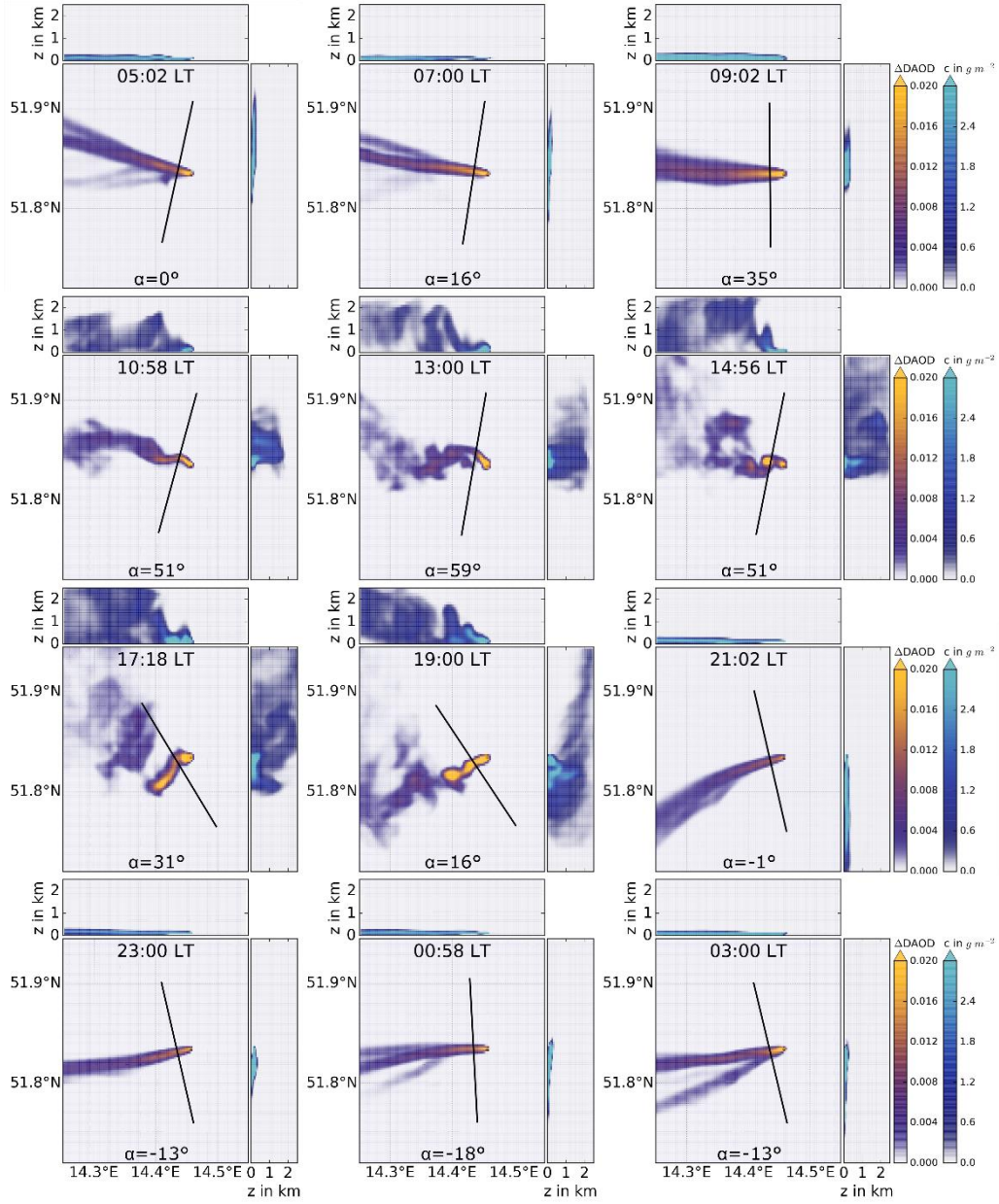


Figure A2: Exemplary snapshots of simulated plume and virtual flight track. At the respective top local time is given in Central European Summer Time (CEST, i.e., UTC+2), at the bottom α denotes the local solar altitude. The daily solar irradiation causes a deep, convective boundary layer with turbulent plume dispersion within. In the nocturnal absence of solar irradiation, the boundary layer shrinks, leading to narrow, homogeneous plume dispersion, within a laminar flow. Every two minutes a virtual measurement is performed yielding 60 measurements within a time frame of 2 hours. One representative snapshot within the two-hour time frame is shown. Some snapshots show disjointed exhaust plumes. This is due to vertical wind shearing and the resulting different vertical advection directions.

Table A1: Number of possible permutations of successive virtual crossings used for averaging

# of measurements	# of possible permutations
1	60
4	5000
7	312500
10	9765625

Data availability.

The data are available from the author upon request and will be made publicly available through the HALO Data Base www.halo.dlr.de/halo-db/ in due time.

455 *Author contribution.*

SW analyzed the measurement data, performed the simulation and wrote most of the manuscript. AF, CK and GE supervised the measurement data analysis, as well as the simulation post processing. AA, AF, MQ and MW developed the lidar system and operated it during CoMet. AF was principal investigator of the CoMet mission. AA, AF, CK and GE designed the measurement flights. AF, CK, GE and MQ contributed to the manuscript’s text and figures.

460 *Competing interests.*

The authors declare that they have no conflict of interest.

Acknowledgements.

We thank Bastian Kern, Sabrina Arnold (both DLR Institut für Physik der Atmosphäre, Oberpfaffenhofen, Germany), and Friedemann Reum (SRON Netherlands Institute for Space Research, Utrecht, Netherlands) for the helpful comments on a previous version of the paper. We further gratefully acknowledge Michał Gałkowski (Max Planck Institute for Biogeochemistry, Jena, Germany), Johannes Wagner (DLR Institut für Physik der Atmosphäre, Oberpfaffenhofen, Germany, now at Deutsches Patent- und Markenamt, Munich, Germany) and Andreas Luther (DLR Institut für Physik der Atmosphäre, Oberpfaffenhofen, Germany) for advising the simulation setup. We would like to thank DLR flight experiments for excellent operations during CoMet.

We acknowledge financial support by BMBF (German Federal Ministry of Education and Research) through its AIRSPACE project (grants no. 01LK1701A/B/C), the German Science Foundation (Deutsche Forschungsgemeinschaft, DFG) within DFG Priority Program SP 1294 “Atmospheric and Earth System Research with the Research Aircraft HALO (High Altitude and Long Range Research Aircraft)”. The HALO flights also received support in the frame of DLR project ”KliSAW” and from
475 the Max Planck Society.

References

- Ackermann, G. R.: Means and Standard Deviations of Horizontal Wind Components, 22, 959-961, [https://doi.org/10.1175/1520-0450\(1983\)022%3C0959:MASDOH%3E2.0.CO;2](https://doi.org/10.1175/1520-0450(1983)022%3C0959:MASDOH%3E2.0.CO;2), 1983.
- Amediek, A., Fix, A., Ehret, G., Caron, J., and Durand, Y.: Airborne lidar reflectance measurements at 1.57 μm in support
480 of the A-SCOPE mission for atmospheric CO₂, *Atmos. Meas. Tech.*, 2, 755-772, <https://doi.org/10.5194/amt-2-755-2009>, 2009.
- Amediek, A., Ehret, G., Fix, A., Wirth, M., Budenbender, C., Quatrevalet, M., Kiemle, C., and Gerbig, C.: CHARM-F-a new
airborne integrated-path differential-absorption lidar for carbon dioxide and methane observations: measurement
performance and quantification of strong point source emissions, *Appl Optics*, 56, 5182-5197,
485 <https://doi.org/10.1364/AO.56.005182> 2017.
- Bézy, J., Sierk, B., Löscher, A., Meijer, Y., Nett, H., and Fernandez, V.: The European Copernicus Anthropogenic CO₂
Monitoring Mission, IGARSS 2019 - 2019 IEEE International Geoscience and Remote Sensing Symposium, 8400-8403,
<https://doi.org/10.1109/IGARSS.2019.8899116>, 2019.
- Bhimireddy, S. R., and Bhaganagar, K.: Short-term passive tracer plume dispersion in convective boundary layer using a high-
490 resolution WRF-ARW model, *Atmospheric Pollution Research*, 9, 901-911, <https://doi.org/10.1016/j.apr.2018.02.010>, 2018.
- Blaylock, B. K., Horel, J. D., and Crosman, E. T.: Impact of Lake Breezes on Summer Ozone Concentrations in the Salt Lake
Valley, *Journal of Applied Meteorology and Climatology*, 56, 353-370, <https://doi.org/10.1175/JAMC-D-16-0216.1>, 2017.
- Broquet, G., Bréon, F. M., Renault, E., Buchwitz, M., Reuter, M., Bovensmann, H., Chevallier, F., Wu, L., and Ciais, P.: The
495 potential of satellite spectro-imagery for monitoring CO₂ emissions from large cities, *Atmos. Meas. Tech.*, 11, 681-708,
<https://doi.org/10.5194/amt-11-681-2018>, 2018.
- Cambaliza, M. O. L., Shepson, P. B., Caulton, D. R., Stirn, B., Samarov, D., Gurney, K. R., Turnbull, J., Davis, K. J., Possolo,
A., Karion, A., Sweeney, C., Moser, B., Hendricks, A., Lauvaux, T., Mays, K., Whetstone, J., Huang, J., Razlivanov, I.,
Miles, N. L., and Richardson, S. J.: Assessment of uncertainties of an aircraft-based mass balance approach for quantifying
500 urban greenhouse gas emissions, *Atmos. Chem. Phys.*, 14, 9029-9050, <https://doi.org/10.5194/acp-14-9029-2014>, 2014.
- Chen, J., Gerbig, C., Marshall, J., and Totsche, K. U.: Short-term forecasting of regional biospheric CO₂ fluxes in Europe
using a light-use-efficiency model (VPRM, MPI-BGC version 1.2), *Geosci. Model Dev.*, 13, 4091-4106,
<https://doi.org/10.5194/gmd-13-4091-2020>, 2020.
- Conley, S., Franco, G., Faloona, I., Blake, D. R., Peischl, J., and Ryerson, T. B.: Methane emissions from the 2015 Aliso
505 Canyon blowout in Los Angeles, CA, *Science*, 351, 1317-1320, <https://doi.org/10.1126/science.aaf2348>, 2016.
- E-PRTR: The European Pollutant Release and Transfer Register (E-PRTR), Member States reporting under Article 7 of
Regulation (EC) No 166/2006, 2020, EEA, [https://www.eea.europa.eu/data-and-maps/data/member-states-reporting-art-7-
under-the-european-pollutant-release-and-transfer-register-e-prtr-regulation-23#tab-european-data](https://www.eea.europa.eu/data-and-maps/data/member-states-reporting-art-7-under-the-european-pollutant-release-and-transfer-register-e-prtr-regulation-23#tab-european-data), access: November 5,
2020.
- 510 ECMWF: Part III : Dynamics and numerical procedures, in: IFS Documentation CY45R1, IFS Documentation, 3, ECMWF,
<https://www.ecmwf.int/en/elibrary/18713-part-iii-dynamics-and-numerical-procedures>, 2018.

- Ehret, G., Kiemle, C., Wirth, M., Amediek, A., Fix, A., and Houweling, S.: Space-borne remote sensing of CO₂, CH₄, and N₂O by integrated path differential absorption lidar: a sensitivity analysis, *Applied Physics B*, 90, 593-608, <https://doi.org/10.1007/s00340-007-2892-3>, 2008.
- 515 Ehret, G., Bousquet, P., Pierangelo, C., Alpers, M., Millet, B., Abshire, J. B., Bovensmann, H., Burrows, J. P., Chevallier, F., Ciais, P., Crevoisier, C., Fix, A., Flamant, P., Frankenberg, C., Gibert, F., Heim, B., Heimann, M., Houweling, S., Hubberten, H. W., Jockel, P., Law, K., Low, A., Marshall, J., Agusti-Panareda, A., Payan, S., Prigent, C., Rairoux, P., Sachs, T., Scholze, M., and Wirth, M.: MERLIN: A French-German Space Lidar Mission Dedicated to Atmospheric Methane, *Remote Sens.*, 9, 1052, <https://doi.org/10.3390/rs9101052>, 2017.
- 520 Fiehn, A., Kostinek, J., Eckl, M., Klausner, T., Galkowski, M., Chen, J., Gerbig, C., Röckmann, T., Maazallahi, H., Schmidt, M., Korbeň, P., Nečki, J., Jagoda, P., Wildmann, N., Mallaun, C., Bun, R., Nickl, A. L., Jöckel, P., Fix, A., and Roiger, A.: Estimating CH₄, CO₂ and CO emissions from coal mining and industrial activities in the Upper Silesian Coal Basin using an aircraft-based mass balance approach, *Atmos. Chem. Phys.*, 20, 12675-12695, <https://doi.org/10.5194/acp-20-12675-2020>, 2020.
- 525 Friedlingstein, P., Jones, M. W., O'Sullivan, M., Andrew, R. M., Hauck, J., Peters, G. P., Peters, W., Pongratz, J., Sitch, S., Le Quéré, C., Bakker, D. C. E., Canadell, J. G., Ciais, P., Jackson, R. B., Anthoni, P., Barbero, L., Bastos, A., Bastrikov, V., Becker, M., Bopp, L., Buitenhuis, E., Chandra, N., Chevallier, F., Chini, L. P., Currie, K. I., Feely, R. A., Gehlen, M., Gilfillan, D., Gkritzalis, T., Goll, D. S., Gruber, N., Gutekunst, S., Harris, I., Haverd, V., Houghton, R. A., Hurtt, G., Ilyina, T., Jain, A. K., Joetzjer, E., Kaplan, J. O., Kato, E., Klein Goldewijk, K., Korsbakken, J. I., Landschützer, P., Lauvset, S.
- 530 K., Lefèvre, N., Lenton, A., Lienert, S., Lombardozzi, D., Marland, G., McGuire, P. C., Melton, J. R., Metzl, N., Munro, D. R., Nabel, J. E. M. S., Nakaoka, S. I., Neill, C., Omar, A. M., Ono, T., Peregon, A., Pierrot, D., Poulter, B., Rehder, G., Resplandy, L., Robertson, E., Rödenbeck, C., Séférian, R., Schwinger, J., Smith, N., Tans, P. P., Tian, H., Tilbrook, B., Tubiello, F. N., van der Werf, G. R., Wiltshire, A. J., and Zaehle, S.: Global Carbon Budget 2019, *Earth Syst. Sci. Data*, 11, 1783-1838, <https://doi.org/10.5194/essd-11-1783-2019>, 2019.
- 535 Galkowski, M., Jordan, A., Rothe, M., Marshall, J., Koch, F. T., Chen, J., Agusti-Panareda, A., Fix, A., and Gerbig, C.: In situ observations of greenhouse gases over Europe during the CoMet 1.0 campaign aboard the HALO aircraft, *Atmos. Meas. Tech.*, 14, 1525-1544, <https://doi.org/10.5194/amt-14-1525-2021>, 2021.
- Gerilowski, K., Krings, T., Hartmann, J., Buchwitz, M., Sachs, T., Erzinger, J., Burrows, J. P., and Bovensmann, H.: Atmospheric remote sensing constraints on direct sea-air methane flux from the 22/4b North Sea massive blowout bubble plume, *Marine and Petroleum Geology*, 68, 824-835, <https://doi.org/10.1016/j.marpetgeo.2015.07.011>, 2015.
- 540 Gordon, I. E., Rothman, L. S., Hill, C., Kochanov, R. V., Tan, Y., Bernath, P. F., Birk, M., Boudon, V., Campargue, A., Chance, K. V., Drouin, B. J., Flaud, J.-M., Gamache, R. R., Hodges, J. T., Jacquemart, D., Perevalov, V. I., Perrin, A., Shine, K. P., Smith, M.-A. H., Tennyson, J., Toon, G. C., Tran, H., Tyuterev, V. G., Barbe, A., Császár, A. G., Devi, V. M., Furtenbacher, T., Harrison, J. J., Hartmann, J.-M., Jolly, A., Johnson, T. J., Karman, T., Kleiner, I., Kyuberis, A. A.,
- 545 Loos, J., Lyulin, O. M., Massie, S. T., Mikhailenko, S. N., Moazzen-Ahmadi, N., Müller, H. S. P., Naumenko, O. V., Nikitin, A. V., Polyansky, O. L., Rey, M., Rotger, M., Sharpe, S. W., Sung, K., Starikova, E., Tashkun, S. A., Auwera, J. V., Wagner, G., Wilzewski, J., Wcisło, P., Yu, S., and Zak, E. J.: The HITRAN2016 Molecular Spectroscopic Database, *Journal of Quantitative Spectroscopy and Radiative Transfer* Volume: 203, <https://doi.org/10.1016/J.JQSRT.2017.06.038>, 2017.
- 550 Iacono, M. J., Delamere, J. S., Mlawer, E. J., Shephard, M. W., Clough, S. A., and Collins, W. D.: Radiative forcing by long-lived greenhouse gases: Calculations with the AER radiative transfer models, *J. Geophys. Res.*, 113, <https://doi.org/10.1029/2008jd009944>, 2008.
- Jimenez, P. A., Dudhia, J., Gonzalez-Rouco, J. F., Navarro, J., Montavez, J. P., and Garcia-Bustamante, E.: A Revised Scheme for the WRF Surface Layer Formulation, *Monthly Weather Review*, 140, 898-918, <https://doi.org/10.1175/Mwr-D-11-00056.1>, 2012.
- 555 Jongaramrungruang, S., Frankenberg, C., Matheou, G., Thorpe, A. K., Thompson, D. R., Kuai, L., and Duren, R. M.: Towards accurate methane point-source quantification from high-resolution 2-D plume imagery, *Atmos. Meas. Tech.*, 12, 6667-6681, <https://doi.org/10.5194/amt-12-6667-2019>, 2019.
- Kiemle, C., Ehret, G., Amediek, A., Fix, A., Quatrevalet, M., and Wirth, M.: Potential of Spaceborne Lidar Measurements of
- 560 Carbon Dioxide and Methane Emissions from Strong Point Sources, *Remote Sens.*, 9, 1137, <https://doi.org/10.3390/rs9111137>, 2017.

- Kostinek, J., Roiger, A., Eckl, M., Fiehn, A., Luther, A., Wildmann, N., Klausner, T., Fix, A., Knote, C., Stohl, A., and Butz, A.: Estimating Upper Silesian coal mine methane emissions from airborne in situ observations and dispersion modeling, *Atmos. Chem. Phys. Discuss.*, 2020, 1-24, <https://doi.org/10.5194/acp-2020-962>, 2020.
- 565 Krautwurst, S., Gerilowski, K., Borchardt, J., Wildmann, N., Gałkowski, M., Swolkien, J., Marshall, J., Fiehn, A., Roiger, A., Ruhtz, T., Gerbig, C., Necki, J., Burrows, J. P., Fix, A., and Bovensmann, H.: Quantification of CH₄ coal mining emissions in Upper Silesia by passive airborne remote sensing observations with the MAMAP instrument during CoMet, *Atmos. Chem. Phys. Discuss.*, 2021, 1-39, <https://doi.org/10.5194/acp-2020-1014>, 2021.
- 570 Krings, T., Neininger, B., Gerilowski, K., Krautwurst, S., Buchwitz, M., Burrows, J. P., Lindemann, C., Ruhtz, T., Schüttemeyer, D., and Bovensmann, H.: Airborne remote sensing and in situ measurements of atmospheric CO₂ to quantify point source emissions, *Atmos. Meas. Tech.*, 11, 721-739, <https://doi.org/10.5194/amt-11-721-2018>, 2018.
- Kuhlmann, G., Broquet, G., Marshall, J., Clément, V., Löschner, A., Meijer, Y., and Brunner, D.: Detectability of CO₂ emission plumes of cities and power plants with the Copernicus Anthropogenic CO₂ Monitoring (CO₂M) mission, *Atmos. Meas. Tech.*, 12, 6695-6719, <https://doi.org/10.5194/amt-12-6695-2019>, 2019.
- 575 Kuhlmann, G., Brunner, D., Broquet, G., and Meijer, Y.: Quantifying CO₂ emissions of a city with the Copernicus Anthropogenic CO₂ Monitoring satellite mission, *Atmos. Meas. Tech.*, 13, 6733-6754, <https://doi.org/10.5194/amt-13-6733-2020>, 2020.
- Kumar, P., Broquet, G., Yver-Kwok, C., Laurent, O., Gichuki, S., Caldow, C., Cropley, F., Lauvaux, T., Ramonet, M., Berthe, G., Martin, F., Duclaux, O., Juery, C., Bouchet, C., and Ciais, P.: Mobile atmospheric measurements and local-scale inverse estimation of the location and rates of brief CH₄ and CO₂ releases from point sources, *Atmos. Meas. Tech. Discuss.*, 2020, 1-27, <https://doi.org/10.5194/amt-2020-226>, 2020.
- 580 Larsen, N., and Stamnes, K.: Methane detection from space: use of sunglint, *Optical Engineering*, 45, 016202, <https://doi.org/10.1117/1.2150835>, 2006.
- Luther, A., Kleinschek, R., Scheidweiler, L., Defratyka, S., Stanisavljevic, M., Forstmaier, A., Dandocsi, A., Wolff, S., Dubravica, D., Wildmann, N., Kostinek, J., Jöckel, P., Nickl, A. L., Klausner, T., Hase, F., Frey, M., Chen, J., Dietrich, F., Necki, J., Swolkien, J., Fix, A., Roiger, A., and Butz, A.: Quantifying CH₄ emissions from hard coal mines using mobile sun-viewing Fourier transform spectrometry, *Atmos. Meas. Tech.*, 12, 5217-5230, <https://doi.org/10.5194/amt-12-5217-2019>, 2019.
- 585 Menzies, R. T., Spiers, G. D., and Jacob, J.: Airborne Laser Absorption Spectrometer Measurements of Atmospheric CO₂ Column Mole Fractions: Source and Sink Detection and Environmental Impacts on Retrievals, *Journal of Atmospheric and Oceanic Technology*, 31, 404-421, <https://doi.org/10.1175/JTECH-D-13-00128.1>, 2014.
- Moeng, C.-H., Dudhia, J., Klemp, J., and Sullivan, P.: Examining Two-Way Grid Nesting for Large Eddy Simulation of the PBL Using the WRF Model, *Monthly Weather Review*, 135, 2295-2311, <https://doi.org/10.1175/MWR3406.1>, 2007.
- Morrison, H., Thompson, G., and Tatarskii, V.: Impact of Cloud Microphysics on the Development of Trailing Stratiform Precipitation in a Simulated Squall Line: Comparison of One- and Two-Moment Schemes, *Monthly Weather Review*, 137, 991-1007, <https://doi.org/10.1175/2008MWR2556.1>, 2009.
- 595 Myhre, G., Shindell, D., Bréon, F.-M., Collins, W., Fuglestad, J., Huang, J., Koch, D., Lamarque, J.-F., Lee, D., Mendoza, B., Nakajima, T., Robock, A., Stephens, G., Takemura, T., and Zhan, H.: Anthropogenic and Natural Radiative Forcing, in: *Climate Change 2013 – The Physical Science Basis: Working Group I Contribution to the Fifth Assessment Report of the Intergovernmental Panel on Climate Change*, edited by: Intergovernmental Panel on Climate, C., Cambridge University Press, Cambridge, 659-740, https://www.ipcc.ch/site/assets/uploads/2018/02/WG1AR5_Chapter08_FINAL.pdf, access: 12.08.2020, 2014.
- 600 Nakanishi, M., and Niino, H.: Development of an Improved Turbulence Closure Model for the Atmospheric Boundary Layer, *Journal of the Meteorological Society of Japan. Ser. II*, 87, 895-912, <https://doi.org/10.2151/jmsj.87.895>, 2009.
- 605 Nassar, R., Hill, T. G., McLinden, C. A., Wunch, D., Jones, D. B. A., and Crisp, D.: Quantifying CO₂ Emissions From Individual Power Plants From Space, 44, 10,045-010,053, <https://doi.org/10.1002/2017GL074702>, 2017.
- Nickl, A. L., Mertens, M., Roiger, A., Fix, A., Amediek, A., Fiehn, A., Gerbig, C., Gałkowski, M., Kerkweg, A., Klausner, T., Eckl, M., and Jöckel, P.: Hindcasting and forecasting of regional methane from coal mine emissions in the Upper Silesian Coal Basin using the online nested global regional chemistry–climate model MECO(n) (MESSy v2.53), *Geosci. Model Dev.*, 13, 1925-1943, <https://doi.org/10.5194/gmd-13-1925-2020>, 2020.
- 610

- Nottrott, A., Kleissl, J., and Keeling, R.: Modeling passive scalar dispersion in the atmospheric boundary layer with WRF large-eddy simulation, *Atmospheric Environment*, 82, 172-182, <https://doi.org/10.1016/j.atmosenv.2013.10.026>, 2014.
- Nunalee, C. G., Kosović, B., and Bieringer, P. E.: Eulerian dispersion modeling with WRF-LES of plume impingement in neutrally and stably stratified turbulent boundary layers, *Atmospheric Environment*, 99, 571-581, <https://doi.org/10.1016/j.atmosenv.2014.09.070>, 2014.
- Oda, T., and Maksyutov, S.: A very high-resolution (1 km×1 km) global fossil fuel CO₂ emission inventory derived using a point source database and satellite observations of nighttime lights, *Atmos. Chem. Phys.*, 11, 543-556, <https://doi.org/10.5194/acp-11-543-2011>, 2011.
- Pandey, S., Gautam, R., Houweling, S., van der Gon, H. D., Sadavarte, P., Borsdorff, T., Hasekamp, O., Landgraf, J., Tol, P., van Kempen, T., Hoogeveen, R., van Hees, R., Hamburg, S. P., Maasakkers, J. D., and Aben, I.: Satellite observations reveal extreme methane leakage from a natural gas well blowout, *P Natl Acad Sci USA*, 116, 26376-26381, <https://doi.org/10.1073/pnas.1908712116>, 2019.
- Powers, J. G., Klemp, J. B., Skamarock, W. C., Davis, C. A., Dudhia, J., Gill, D. O., Coen, J. L., Gochis, D. J., Ahmadov, R., Peckham, S. E., Grell, G. A., Michalakes, J., Trahan, S., Benjamin, S. G., Alexander, C. R., Dimego, G. J., Wang, W., Schwartz, C. S., Romine, G. S., Liu, Z., Snyder, C., Chen, F., Barlage, M. J., Yu, W., and Duda, M. G.: The Weather Research and Forecasting Model: Overview, System Efforts, and Future Directions, *Bull. Amer. Meteor. Soc.*, 98, 1717-1737, <https://doi.org/10.1175/BAMS-D-15-00308.1>, 2017.
- Reuter, M., Buchwitz, M., Schneising, O., Krautwurst, S., O'Dell, C. W., Richter, A., Bovensmann, H., and Burrows, J. P.: Towards monitoring localized CO₂ emissions from space: co-located regional CO₂ and NO₂ enhancements observed by the OCO-2 and S5P satellites, *Atmos. Chem. Phys.*, 19, 9371-9383, <https://doi.org/10.5194/acp-19-9371-2019>, 2019.
- Seinfeld, J. H., and Pandis, S. N.: *Atmospheric Chemistry and Physics: From Air Pollution to Climate Change*, Wiley, 9781118947401, 1997.
- Sharan, M., Yadav, A. K., Singh, M. P., Agarwal, P., and Nigam, S.: A mathematical model for the dispersion of air pollutants in low wind conditions, *Atmospheric Environment*, 30, 1209-1220, [https://doi.org/10.1016/1352-2310\(95\)00442-4](https://doi.org/10.1016/1352-2310(95)00442-4), 1996.
- Skamarock, W., Klemp, J., Dudhia, J., Gill, D., Barker, D., Duda, M., Huang, X., Wang, W., and Powers, J.: A description of the advanced research WRF Version 3, NCAR technical note, Mesoscale and Microscale Meteorology Division, National Center for Atmospheric Research, Boulder, Colorado, USA, <https://doi.org/10.5065/D68S4MVH>, 2008.
- Stauffer, R., Mayr, G. J., Dabernig, M., and Zeileis, A.: Somewhere Over the Rainbow: How to Make Effective Use of Colors in Meteorological Visualizations, *Bull. Amer. Meteor. Soc.*, 96, 203-216, <https://doi.org/10.1175/BAMS-D-13-00155.1>, 2015.
- Strandgren, J., Krutz, D., Wilzewski, J., Paproth, C., Sebastian, I., Gurney, K. R., Liang, J., Roiger, A., and Butz, A.: Towards spaceborne monitoring of localized CO₂ emissions: an instrument concept and first performance assessment, *Atmos. Meas. Tech.*, 13, 2887-2904, <https://doi.org/10.5194/amt-13-2887-2020>, 2020.
- Stull, R. B.: *An introduction to boundary layer meteorology*, Springer Science & Business Media, 978-94-009-3027-8, 1988.
- Super, I., Dellaert, S. N. C., Visschedijk, A. J. H., and Denier van der Gon, H. A. C.: Uncertainty analysis of a European high-resolution emission inventory of CO₂ and CO to support inverse modelling and network design, *Atmos. Chem. Phys.*, 20, 1795-1816, <https://doi.org/10.5194/acp-20-1795-2020>, 2020.
- Tewari, M., Chen, F., Wang, W., Dudhia, J., LeMone, M., Mitchell, K., Ek, M., Gayno, G., Wegiel, J., and Cuenca, R.: Implementation and verification of the unified NOAA land surface model in the WRF model, 20th conference on weather analysis and forecasting/16th conference on numerical weather prediction, 2165-2170, <https://ams.confex.com/ams/84Annual/webprogram/Paper69061.html>, 2004.
- UNFCCC: The Paris Agreement, 2015, United Nations Framework Convention on Climate Change, <https://unfccc.int/process-and-meetings/the-paris-agreement/the-paris-agreement>, access: 11.08.2020.
- Varon, D. J., Jacob, D. J., McKeever, J., Jervis, D., Durak, B. O. A., Xia, Y., and Huang, Y.: Quantifying methane point sources from fine-scale satellite observations of atmospheric methane plumes, *Atmos. Meas. Tech.*, 11, 5673-5686, <https://doi.org/10.5194/amt-11-5673-2018>, 2018.
- Varon, D. J., Jacob, D. J., Jervis, D., and McKeever, J.: Quantifying Time-Averaged Methane Emissions from Individual Coal Mine Vents with GHGSat-D Satellite Observations, *Environmental Science & Technology*, <https://doi.org/10.1021/acs.est.0c01213>, 2020.

- 660 White, W. H., Anderson, J. A., Blumenthal, D. L., Husar, R. B., Gillani, N. V., Husar, J. D., and Wilson, W. E., Jr.: Formation
and transport of secondary air pollutants: ozone and aerosols in the St. Louis urban plume, *Science*, 194, 187-189,
<https://doi.org/10.1126/science.959846> 1976.
- Wildmann, N., Päschke, E., Roiger, A., and Mallaun, C.: Towards improved turbulence estimation with Doppler wind lidar
velocity-azimuth display (VAD) scans, *Atmos. Meas. Tech.*, 13, 4141-4158, <https://doi.org/10.5194/amt-13-4141-2020>,
665 2020.
- Wolff, S., 2020, Animated GIF of simulated plume and virtual flight tracks, Zenodo, <http://doi.org/10.5281/zenodo.4266513>
- Yver, C., Graven, H., Lucas, D. D., Cameron-Smith, P., Keeling, R., and Weiss, R.: Evaluating transport in the WRF model
along the California coast, *Atmos. Chem. Phys.*, 13, <https://doi.org/10.5194/acp-13-1837-2013>, 2013.
- 670 Zhang, Y., Gautam, R., Pandey, S., Omara, M., Maasakkers, J. D., Sadavarte, P., Lyon, D., Nesser, H., Sulprizio, M. P., and
Varon, D. J.: Quantifying methane emissions from the largest oil-producing basin in the United States from space, *Science
Advances* 6, 5120, <https://doi.org/10.1126/sciadv.aaz5120>, 2020.
- Zhao, X., Marshall, J., Hachinger, S., Gerbig, C., Frey, M., Hase, F., and Chen, J.: Analysis of total column CO₂ and CH₄
measurements in Berlin with WRF-GHG, *Atmos. Chem. Phys.*, 19, 11279-11302, [https://doi.org/10.5194/acp-19-11279-](https://doi.org/10.5194/acp-19-11279-2019)
2019, 2019.
- 675