

# A study of polarimetric error induced by satellite motion: Application to the 3MI and similar sensors

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**Abstract.** This study investigates the magnitude of the error introduced by the co-registration and interpolation in computing Stokes vector elements from observations by the Multi-viewing, Multi-channel, Multi-polarisation Imager (3MI). The Stokes parameter derivation from the 3MI measurements requires the synthesis of three wide-field-of-view images taken by the instrument at 0.25-second interval with polarizers at different angles. Even though the synthesis of spatially or temporally inhomogeneous data is inevitable for a number of polarimetric instruments, that of 3MI is particularly challenging because of the instrument design that prioritizes the stability during a long life cycle, and that enables the wide-field-of-view and multi-wavelength capability. This study therefore focuses on the 3MI's motion-induced error brought in by the co-registration and interpolation that are necessary for the synthesis of three images. The 2-D polarimetric measurements from the Second-Generation Global Imager (SGLI) are weighted and averaged to produce two proxy datasets of the 3MI measurements, with and without considering the effect of the satellite motion along the orbit. The comparison of these two datasets shows that the motion-induced error is not symmetric about zero and not negligible when the intensity variability of the observed scene is large. The results are analyzed in five categories of pixels, (1) cloud over water, (2) cloud over land, (3) coastlines, (4) clear-sky over water, (5) clear-sky over land. The most spread distribution of normalized polarized radiance ( $L_p$ ) difference is in the cloud-over-water class, and the most spread distribution of degree of linear polarization (DOLP) difference is in the coastline class. The 5th to 95th percentile range of  $L_p$  difference for each class are: (1) [-0.0051:0.012], (2) [-0.0040:0.0088], (3) [-0.0033:0.012], (4) [-0.0033:0.0062], and (5) [-0.0023:0.0032]. The same percentile range of DOLP difference for each class are: (1) [-0.023:0.060], (2) [-0.043:0.093], (3) [-0.019:0.082], (4) [-0.0075:0.014], and (5) [-0.011:0.016]. The medians of the  $L_p$  difference are: (1) 0.00035, (2) 0.000049, (3) 0.00031, (4), 0.000089, and (5) 0.000037 whereas the medians of the DOLP difference are: (1) 0.0014, (2) 0.0015, (3) 0.0025, (4) 0.00027, and (5) 0.00014. A model using Monte Carlo simulation confirms that the magnitude of these errors over clouds are closely related to the spatial correlation in the horizontal cloud structure. For the cloud-over-water category, it is shown that the error model developed in this study can statistically simulate the magnitude and trends of the 3MI's motion-induced error estimated from SGLI data. The obtained statistics and the simulation technique can be utilized to provide pixel-level quality information for 3MI Level 1B products. In addition, the simulation method can be applied to the past, current, and future spaceborne instruments with a similar design.

## 30 1. Introduction

The Multi-viewing, Multi-channel, Multi-polarisation Imager (3MI) is a planned spaceborne sensor on the MetOp Second Generation-A (MetOp-SG-A) satellite platform. The sensor consists of two wide field-of-view cameras with narrow-band wavelength filters, inheriting the legacy of the Polarisation and Directionality of the Earth's Reflectance (POLDER) sensor. The rotating wheel carries 31 filters that enable polarimetric measurements at 9 wavelengths and non-polarimetric measurements at 3 wavelengths (Fougnie et al. 2018). The spatial resolution at nadir is 4 km and the instantaneous swath is 2200 km. The MetOp-SG-A series expects the launch of three identical platforms with seven-year intervals, providing continuous and homogeneous monitoring of the Earth's weather and climate for 21 years. The 3MI sensors on these platforms are anticipated to perform multi-viewing and multi-channel polarimetric observation at unparalleled spatial and temporal scales.

40 As increasingly advanced retrieval techniques are used to extract atmospheric composition parameters from multispectral and polarimetric observations (Knobelspiesse et al. 2012; Fu and Hasekamp 2018; Dubovik et al. 2019), the knowledge and reduction of uncertainties associated to polarimetric measurements become more and more critical. In particular for all techniques relying on optimal estimation, the correct understanding of observational uncertainties, as discussed in details by Povey and Grainger (2015), is pivotal to obtain meaningful and successful retrieval.

45 The best-described uncertainty in the Level 1B product is the radiometric uncertainty. Table 1 summarizes the radiometric requirements of the 3MI sensor according to Fougnie et al. (2018). With no onboard calibration, the 3MI sensor needs to rely on inflight vicarious calibration techniques to monitor and assess the instrument radiometric performances. Among vicarious calibration techniques that are developed for the PARASOL sensor (Fougnie, 2016) and new techniques (e.g. Djellali et al. 2019), some are useful for an independent absolute calibration and others are more suited to perform inter-band or inter-sensor cross calibration. For example, Rayleigh scattering method and new sunglint method can be used to monitor the absolute calibration coefficient, whereas existing sunglint method is designed for inter-band calibration. The temporal evolution of calibration coefficients could be monitored by the calibration over Antarctica, and inter-pixel calibration could be performed over deep convective clouds. The synergies with other sensors of the METOP-SG A platform will also be beneficial (Fougnie et al., 2018), for example through a cross-calibration over relatively invariant target over African and Arabian desert.

55 The radiometric performance of the instrument however is not the only factor driving the overall measurement uncertainties especially for polarimetric observations where the useful quantities (Stokes parameters) are not directly measured but derived, for example, from a set of different radiances. Therefore, the polarimetric performance of the 3MI instrument will depend both on the radiometric accuracy and the process used to derive the Stokes parameters. This paper investigates in particular the uncertainty induced by this derivation process in order to provide instantaneous, realistic, and quantitative estimate of polarimetric error at pixel level for the 3MI instrument or similar sensors.

60 The 3MI instrument derives the first three Stokes parameters ( $I$ ,  $Q$ , and  $U$ ) by synthesizing three wide-field-of-view images that are taken sequentially at 0.25 seconds interval. Each of three images is acquired with linear polarizer oriented in different

directions with polarizing axis being  $-60^\circ$ ,  $0^\circ$  and  $60^\circ$  with respect to the direction of the satellite's orbital motion (along-track direction). However, within the 0.25-second interval, the instantaneous field of view (IFOV) shifts by 1.8 km (0.45 pixel) on the ground because of the motion of the satellite. The shifts between the acquired images lead to the need for the interpolation and co-registration to compensate the satellite's along-track motion before the computation of the Stokes parameters. These non-simultaneous acquisitions therefore introduce a possible source of error in the polarimetric observation by the 3MI sensor due the co-registration and the interpolation required to match the three images.

This kind of error due to the synthesis of spatially or temporally inhomogeneous data is inevitable for polarimetric instruments without a beam splitter, including the 3MI, because it is impossible to measure multiple radiometric quantities along the same line of sight simultaneously and independently. The practical solution is to spatially or temporally change the polarimetric modulation in a way that minimizes the errors, at the same time providing measurements that serves for mission objectives. For the details of the different instrument designs, readers are referred to Dubovik et al. (2019) and references therein. The rotating-filter design of the 3MI and POLDER sensors is suited for the spatially continuous wide field-of-view measurements, but its asynchronous acquisition may result in a significant polarimetric error, particularly over inhomogeneous scenes.

The magnitude of error due to the interpolation and co-registration is expected to be neither spatially uniform nor symmetric about zero, and therefore cannot be removed by spatio-temporal averaging. This is because the intensity in the original images and the polarized normalized radiance ( $L_p$ ) are not linearly related. We define the normalized radiance ( $L$ ) and, in analogy, the polarized normalized radiance as follows:

$$L = \frac{\pi I}{E_0} \quad (1)$$

$$L_p = \frac{\pi}{E_0} \sqrt{Q_i^2 + U_i^2}, \quad (2)$$

where  $I$  is the intensity,  $Q_i$  and  $U_i$  are the second and third elements of Stokes vector in terms of intensity,  $E_0$  is the beam flux of the extraterrestrial solar radiation. The degree of linear polarization (DOLP) is defined as follows:

$$\text{DOLP} = \frac{L_p}{L}. \quad (3)$$

Assuming three ideal linear polarizers with a perfect alignment, the normalized radiance and the polarized normalized radiance can be computed from the original intensity measurements ( $X_{m60}, X_0, X_{p60}$ ) as follows:

$$L = \frac{2}{3} \frac{\pi}{E_0} (X_{m60} + X_0 + X_{p60}) \quad (4)$$

$$L_p = \frac{2\sqrt{2}}{3} \frac{\pi}{E_0} \sqrt{(X_{m60} - X_0)^2 + (X_0 - X_{p60})^2 + (X_{p60} - X_{m60})^2}, \quad (5)$$

where  $X_{m60}$  corresponds to the intensity with the polarizer aligned  $-60^\circ$  off from the along-track direction,  $X_0$  to  $0^\circ$  off, and  $X_{p60}$  to  $+60^\circ$  off. Equation (5) demonstrates that the error in the original images and the normalized polarized radiance are not in linear relation. Rather, the motion-induced error tends to suppress the polarization for strongly polarized target and tends to enhance the polarization for weakly polarized target. This is because  $L_p$  is bounded by  $0 < L_p < L$  (i.e.  $0 < \text{DOLP} < 1$ ), and

any random error near  $L_p = 0$  increases  $L_p$  whereas that near  $L_p = L$  decreases  $L_p$ . From this discussion, we emphasize again that the motion-induced error likely depends on the observation target and the spatial distribution may not be uniform.

95 As the quality of the retrieval product hinges on the quality of the radiance product and ancillary information that delivers the reliability, the quantification of the error triggered by the interpolation and co-registration is significantly useful in the quality control of both Level 1B and Level 2 data products. Some studies have already investigated the impact of the polarimetric accuracy on the performance of retrieval algorithms (e.g. Hasekamp et al. 2019), but the quantification of the error in Level 2 data products is still challenging not only because the retrieval error highly depends on the retrieval algorithm, but also because  
100 the characterization of errors in Level 1B data products is still largely limited to the radiometric uncertainty. By addressing the characteristics of the motion-induced error, this study therefore adds a new dimension to the reliability of the Level 1B and Level 2 data products.

Section 2 describes the data and methods used in this study, Section 3 the results, and Section 4 the discussion on the simulation of the error statistics. Conclusions are given in Section 5.

## 105 **2. Data and methods**

### **2.1 Data**

In this study, we produce 3MI proxy polarimetric measurements from the actual high-resolution polarimetric measurements obtained by the Second-Generation Global Imager (SGLI) aboard the Global Change Observation Mission – Climate (GCOM-C) satellite (Imaoka et al. 2010). The SGLI sensor provides polarized normalized radiances at 1 km nadir resolution within a  
110 1150 km-wide swath. We selected the SGLI data as a source of our proxy data because it provides the global polarimetry at higher resolution than the 3MI, it suffers less from the co-registration and interpolation errors, its orbit and swath are compatible to that of 3MI.

Because of the push-broom design of the SGLI sensor, SGLI's interpolation error is expected to be negligible compared to that introduced by the 3MI's more complex co-registration and interpolation. Figure 1 is a schematic diagram showing the  
115 difference between the observation geometry of the 3MI and that of the SGLI. Both sensors measure the first three elements of the Stokes vector through the measurements of intensity through linear polarizer oriented at three different directions. The pronounced difference is that the 3MI sensor acquires the three wide-field of view images asynchronously, while the SGLI sensor acquires three cross-track profiles of intensity with 170 m offset. Because the SGLI sensor design suffers less from the shift between the acquisition of three images, we treat the SGLI measurement as truth and evaluate the magnitude of error  
120 introduced by the interpolation and co-registration by producing 3MI-proxy data from the SGLI data.

One week of global SGLI Level 1B data near the 2008 September equinox (September 20-26) is used. In this study, we performed our analysis based on the polarimetric data in Level 1B POLDK product and visible, near infrared, and thermal infrared data in Level 1B VNRDK, VNRDL, IRSDK, and IRSDL products. The product name conventions are described in the GCOM-C Data Users Handbook, but in short, the first three letters indicate the subsystem of the SGLI instrument (“POL”

125 for polarization, “VNR” for visible and near infrared, and “IRS” for infrared scanning subsystems), the fourth letter “D” indicates the observation mode (“D” for daytime data), and the last letter indicates the resolution (“K” for 1 km resolution, “L” for aggregated 1 km resolution). As the GCOM-C satellite is in the sun-synchronous orbit at 800 km altitude with descending-node local time of 10:30, the data from the SGLI is valuable to simulate measurements from the 3MI that is anticipated also in the sun-synchronous morning orbit at 830 km altitude.

## 130 2.2 Methods

### 2.2.1 Estimation of the motion-induced error

As the nominal resolution of the 3MI is 4 km and that of the SGLI is 1 km,  $4 \times 4$  SGLI pixels are aggregated to produce a 3MI pixel. We repeat the aggregation for every  $4 \times 4$  SGLI pixel blocks in three original (“Lt\_P2\_m60”, “Lt\_P2\_0”, and “Lt\_P2\_p60”) radiance data in the SGLI Level 1B product. These three datasets correspond to the radiance measured at 0.869  
 135  $\mu\text{m}$  with polarizers at three different directions at  $-60^\circ$ ,  $0^\circ$ , and  $60^\circ$  with respect to the along-track axis of the satellite (i.e.,  $X_{m60}$ ,  $X_0$ ,  $X_{p60}$ ). From the aggregated data, we compute the normalized radiance and polarized normalized radiance by Eqs. (4) and (5). The results are referred to as “reference data” hereafter.

A similar method is applied to produce the 3MI “proxy data” which is compared to the reference data to estimate the magnitude of the error. The proxy data is different from the reference data in that it incorporates the effects of satellite’s motion and  
 140 interpolation. To simulate the motion of satellite between the acquisition of each image (1.8 km), we compute the contribution of every SGLI pixel to the shifted  $4 \times 4$  grid by the following equation:

$$w_0(i) = \frac{1}{16} \int_{i-1}^i \Pi_{4,8}(x - s) dx \quad (6)$$

where  $i$  is the index of line,  $\Pi_{a,b}(x)$  is a boxcar function that is 1 in the interval  $(a, b)$  and 0 otherwise, and  $s$  is the amount of shift in SGLI pixel size (i.e. +1.8 or -1.8 in our case). The results of the calculation is shown in Table 2. The contribution  
 145 factors are multiplied to the measured radiance in every SGLI pixel to perform the weighted average.

After computing the weighted average, we obtain the shifted, aggregated images of “Lt\_P2\_p60” and “Lt\_P2\_m60”. As these two images are shifted with respect to the “Lt\_P2\_0” image, the unshifting is performed as a next step by interpolating the intensity at the pixel center location of the “Lt\_P2\_0” image. The linear interpolation is selected for the simplicity and the locality, but the error estimation described in this subsection as well as the error simulation detailed in Appendix A could be  
 150 performed with other methods of interpolations if deemed necessary for specific applications. The final contribution factors are computed with the following equation:

$$w(i) = \left(1 - \frac{s}{4}\right) w_0(i) + \frac{s}{4} w_0(i + 4 \operatorname{sgn}(s)) \quad (7)$$

where  $\operatorname{sgn}(s)$  is sign of the shift. The results of the computation is summarized in Table 3. From these unshifted aggregated images, we compute the normalized radiance ( $L$ ) and the normalized polarized radiance ( $L_p$ ) by Eqs. (4) and (5), and call it the  
 155 “proxy data”.

The comparison of the proxy and reference data is performed on a pixel-by-pixel basis. In every pixel, the difference of polarized normalized radiance  $\Delta L_p$  and the difference of degree of linear polarization  $\Delta DOLP$  are computed. These differences are attributed to the error induced by the pixel co-registration and the interpolation.

### 2.2.2 Classification of data

160 To further the analysis of the motion-induced error, we classify pixels into five categories: clouds over water, clear-sky over water, clouds over land, clear-sky over land, and coastline. The classification is based on the land-water flag in the SGLI Level 1B dataset and the cloud flag algorithm developed for this study. The activity diagram (flow-chart) of the cloud flag algorithm is shown in Fig. 2 while individual test conditions are listed in Tables 4 (pixels over water) and 5 (pixels over land). To compute cloud flags in the SGLI Level 1B POLDK product's coordinate, other SGLI L1B products are projected onto the POLDK grid.

165 Once the cloud flag is derived, both land-water flag and cloud flag are extended into the along-track directions by 20 SGLI pixels to cover all SGLI pixels used for the error estimation and to minimize the pixels on boundaries. A pixel is classified as "cloud over water" when it is flagged as "confidently cloudy" and "land cover 0%", "clear-sky over water" when it is flagged as "confidently clear" and "land cover 0%", "clear-sky over land" when it is flagged as "confidently clear" and "land cover 100%", "cloud over land" when it is flagged as "confidently cloudy" and "land cover 100%", and "coastline" when land cover

170 is between 5% and 95%. Only pixels with glint angle greater than  $35^\circ$  are collected for cloud-over-water, clear-sky-over-water, and coastline classes to avoid contamination by sun glints.

In every class of data, the normalized polarized radiance differences ( $\Delta L_p$ ) are regrouped according to the along-track Laplacian that is defined as follows:

$$L_{AT} = \frac{\pi}{E_0} (2X_0 - X_{-1} - X_{+1}), \quad (8)$$

175 where  $X_{-1}$  is the  $X_0$  of the adjacent pixel in the negative along-track direction, and  $X_{+1}$  is the  $X_0$  of the adjacent pixel in the positive along-track direction. The along-track Laplacian is a measure of the non-linearity of the local intensity change in the along-track direction. We select this metric because the linear interpolation in Eq. (7) removes the linear error term, and the highest remaining term is characterized by the Laplacian. In other words, we estimate that the major source of the error is the (non-linear) spatial inhomogeneity of the total radiance that pass through the linear interpolation performed in the co-

180 registration.

The DOLP differences ( $\Delta DOLP$ ) are regrouped according to the along-track Laplacian divided by  $L$ , i.e.  $L_{AT}/L$ . This is because we found from the preliminary study that the relation between  $\Delta L_p$  and  $L_{AT}$  does not strongly depend on the value of  $L$ . As the DOLP is defined by Eq. (3), utilizing  $L_{AT}/L$  as a regrouping parameter is deemed a reasonable choice.

### 3. Results

#### 185 3.1 Estimation of the error

The difference of DOLP between the proxy and reference data is shown in Fig. 3 (a) with corresponding visible composite in Fig. 3 (b). The figure covers the western French coast, English Channel, and the southern Great Britain island. Figure 3 (a) shows that the DOLP difference can reach more than 0.2 along the coastlines, particularly in a part where the coastline runs in the cross-track direction. There is little negative DOLP difference near positive values, implying that the distribution of the DOLP difference is not symmetric about zero. Along the edges of thin clouds, for example over the Atlantic in the western part of the Fig. 3, positive and negative DOLP differences are mixed. Note that similar clouds over the ocean and land gives different magnitude of DOLP differences, presumably because of the background normalized radiance ( $L$ ). As the DOLP is divided by  $L$ , errors over dark pixels (e.g. ocean and water near coastlines) tend to be pronounced. For the same reasons, the magnitude of the error is smaller over thick clouds covering the eastern end of English Channel than along coastlines. Figure 3 demonstrates that the magnitude of motion-induced error is not negligible over the scene where intensity variation is large. It is not only over coastlines that the distribution of error is asymmetric about zero. In Figs. 4 and 5, we show histograms of degree of linear polarization (DOLP) and polarized normalized radiance ( $L_p$ ) differences for five different classes of pixels defined in Sect. 2.2.2: cloud over water, clear-sky over water, cloud over land, clear-sky over land, and coastline at wavelength  $\lambda = 0.869 \mu\text{m}$ , in addition to the clear-sky over land at wavelength  $\lambda = 0.674 \mu\text{m}$ . Figures 4 and 5 show that the distributions of the proxy-reference differences are not symmetric about zero and rather skewed to the right (having fat tail in the right end of the histogram) in all classes of data. The tail of DOLP difference histogram is particularly fat for cloud-over-water and coastlines classes, where sharp reflectance gaps near coastal water or cloud edges induce strong polarization artifacts. The asymmetry can be confirmed from the 5th to 95th percentile range and 25th to 75th percentile range (interquartile range) of the estimated DOLP and  $L_p$  error as presented in Table 6. The median of distribution shown in Table 7 also indicates that the distribution is asymmetric not only about zero but also about the median. The clear-sky-over-water class has the most spread distribution of DOLP differences, and the 5th-95th percental range is  $[-0.043; 0.093]$ . On the other hand, the cloud-over-water class has the most spread distribution of  $L_p$  differences, and the 5th to 95th percentile range is  $[-0.0051; 0.012]$ . The asymmetry of the distribution implies that the error cannot be completely cancelled out by computing the spatial average. Figure 6 shows the proxy-reference DOLP differences ( $\Delta\text{DOLP}$ ) as a function of the along-track Laplacian ( $L_{AT}$ ). The red curve indicates the median of  $\Delta\text{DOLP}$  values in each bin of  $L_{AT}$ , and the gray shadow the interquartile range of  $\Delta\text{DOLP}$  values. As the  $L_{AT}$  increases, the median of the error as well as the spread increase. However, an evident difference exists between the clear-sky over land at  $\lambda = 0.869$  and  $\lambda = 0.674$ . The median of  $\lambda = 0.674$  shows a slight increase as a function of  $L_{AP}$  but remains small (within 0.01). At  $\lambda = 0.869$ , for cloud-over-land, cloud-over-water, and clear-sky-over water classes, the spreads of the distributions saturate when  $L_{AT}/L$  increases, while for coastlines the spread of the distribution does not saturate. In the clear-sky-over-land class, the spread reaches a peak at  $L_{AT}/L = 0.15$ . The strong dependence of medians to the along-

track Laplacian imply that the magnitude of the error is predictable from the image of  $X_0$  (intensity with polarizer at  $0^\circ$  off the along track direction), which is used to compute the  $L_{AT}$  and observationally available.

The distribution of polarized normalized radiance difference ( $\Delta L_p$ ) is also shown to be a function of the along-track Laplacian ( $L_{AT}$ ), and Fig. 7 show the increase of median with increasing  $L_p$ . The spectral difference for clear-sky-over-land class still exists, but less pronounced than that for the DOLP. The median of  $\lambda = 0.674 \mu\text{m}$  is closer to 0 than the median of  $\lambda = 0.869$  in the range  $[0:0.02]$  where a majority of pixel exists. It is plausible that the low land inhomogeneity at  $\lambda = 0.674 \mu\text{m}$  results in lower  $L_p$  and DOLP errors. In a similar way as for the DOLP difference, the spreads of distributions for cloudy classes saturate at about  $L_{AT} = 0.1$ , whereas it does not for the coastline class. The spread for the clear-sky pixels over land does not show a maximum as seen in the distribution of the DOLP differences.

The target polarimetric accuracy of the 3MI sensor is  $5 \times 10^{-4}$  in terms of polarized reflectance over homogeneous clear-sky over ocean (Fougnie et al. 2018). Figure 8 shows the fraction of pixels that satisfy this condition as a function of the along-track Laplacian (black points and lines). The blue points and lines indicate the fraction of pixels that satisfy the POLDER specification, which is  $1 \times 10^{-3}$  in terms of polarized normalized radiance. The first point represents the data with  $L_{AT} < 0.005$ , and the interval is 0.005 up to 0.01 (21st bin). Given that 68.2% of data falls within the  $\pm 1$  standard deviation when the error distribution follows the normal distribution, we could interpret that the specification is well satisfied in the bin with the fraction larger than 68.2% (green horizontal line). Over very homogeneous scenes with low along-track Laplacian, indeed we find that the requirements are satisfied for both 3MI and POLDER, but obviously not over as the along-track Laplacian (i.e. inhomogeneity of the scene) increases. This result is consistent with the study by Fougnie et al. (2007), which shows that the POLDER data over homogeneous scene satisfy the requirement.

## 235 4. Discussions

### 4.1 Prediction of error by the Monte Carlo model

The error estimation for the 3MI sensor is possible because the SGLI sensor has a similar swath and orbit as the 3MI with higher spatial resolution and less anticipated motion-induced errors. However, not all sensors have such corresponding sensor to be used for the error estimation. This is our motivation to develop a Monte Carlo model to predict the motion-induced error over cloud-over-water class, which has the highest  $L_p$  error and the normalized radiance structure can be randomly generated using the power-law spectrum and inverse Fourier transform. Technical detail of the method is described in Appendix A.

Figure 9 shows the predicted magnitude of error based on the Monte Carlo simulation for cloudy pixels over water. The simulation predicts the median (red curves) that matches well to the estimation based on the SGLI data (dotted curves). As the empirical 95th percentile of the  $L_{AT}/L$  is 0.39 and that of  $L_{AT}$  is 0.070, the abscissas of Fig. 9 cover the large portion of the plausible range of the data. A slight overestimation of the DOLP difference occurs in the entire range, but the maximum difference is about  $1 \times 10^{-3}$  (i.e. 2% of the median DOLP, 0.041) in the bin  $0.32 < L_{AT}/L < 0.36$ . The difference between



the predicted and estimated normalized polarized radiance is less than  $10^{-3}$  in  $L_{AT} < 0.1$ . The difference reaches  $6.1 \times 10^{-4}$  (i.e. 4.3% of the median  $L_p$ , 0.0032) in the bin  $0.09 < L_{AT} < 0.1$ . Overall, the simulation can predict the median of the error estimation at better than 5% accuracy.

250 The successful prediction of the motion-induced error by the statistical model implies that the error distribution in the cloud-over-water class inferred from the SGLI data is a result of the inherent horizontal structure of clouds. The method is likely be applicable to other spatial scale to predict the magnitude of motion-induced error of the past, current, and future polarimetric instruments sharing similar designs. In the application to other satellite data, it is necessary to collect the four statistics that are used in the simulation, namely, (1) normalized radiance distribution, (2) normalized-radiance-binned sub-pixel inhomogeneity  
255 (weighted variance), (3) normalized-radiance-binned DOLP, and (4) normalized-radiance-binned AOLP. However, most of these statistics are readily available from observations (past and current sensors) or simulations (future sensors). The exception is the sub-pixel inhomogeneity that may be a challenging parameter to obtain if a past or current sensor has no collocated high-resolution imaging measurements, but one could replace it with an alternative measure of the local inhomogeneity, for example, the variance of  $X_0$  in the along-track direction. The modeling technique in this work is therefore particularly helpful for the  
260 preparation for future missions.

#### 4.2 Sensitivity of the Monte Carlo simulation to the assumed power law parameter

In this study, our simulation of the error statistics assumes power-law coefficient ( $-5/3$ ), but it is known that the power-law coefficient varies depending on type of clouds and spatial scale. A well-known example is for the scale break that occurs in the Landsat radiance data over stratocumulus clouds. When the spatial scale is less than a few hundred meters, the power law  
265 coefficient becomes significantly smaller (i.e. the spectrum becomes steeper). Smaller power-law coefficient means that low-frequency structures pronounce more than high frequency structures. As a result, when a lower power-law coefficient is specified, the simulated 2-D normalized radiance field looks more horizontally homogeneous, introducing smaller error in simulated 3MI polarimetric measurements.

To test the sensitivity of our prediction to the specified power-law coefficient, we simulated the error statistics for two other  
270 extreme cases. Figure 10 shows the magnitude of error in the DOLP and  $L_p$  when no correlation between neighboring subpixels is assumed, and Fig. 11 when smaller power-law coefficient ( $-3.0$ ) is assumed.

When there is no spatial correlation in the cloud intensity, the magnitude of simulated error is larger than the estimates based on the SGLI data. The median of SGLI-based estimate is out of the interquartile range of the simulation (gray shading in Fig. 10) for a significant range of  $L_{AT}/L$  and  $L_{AT}$ . On the other hand, Fig. 11 shows that the magnitude of simulated error is slightly  
275 lower when smaller power-law coefficient ( $-3.0$ ) is assumed. In addition, we note that the SGLI error estimation for the clouds-over-land category also shows the slope between these two extremes.

From these results, we propose that the spatial correlation of intensity due to the natural cloud structure should be considered when predicting the statistics of motion-induced error over clouds. For the 3MI sensor, the higher resolution observations

provided by the METImage sensor (Wallner et al, 2017) aboard the same METOP-SG A platform might be used to further  
280 constrain the along track scene spatial correlation and therefore useful to improve the pixel-level polarimetric uncertainty  
estimates.

### 4.3 Application of the results

In this study, we estimated 3MI's motion-induced error from the SGLI data. A straightforward implication of the correlation  
between the motion-induced errors and the along-track Laplacian is that it is possible to predict the quality of polarization data  
285 in every pixel. For example, from the statistics we obtained in this study, the median bias and the standard deviation for every  
pixel can be provided as a function of the  $L_{AT}$ , which is a derivable quantity through  $X_0$ . The challenge of this approach is that  
the view angle of the SGLI is fixed at positive or negative  $45^\circ$  in the along-track direction, and therefore representative of only  
a part of 3MI's view direction. However, as the error estimate shows, the spatial inhomogeneity primarily determines the  
motion-induced error, and statistics obtained in this study are still useful. In addition, the intensity variation over the land is  
290 primarily due to the land surface inhomogeneity, and the month-long or year-long statistics would be beneficial to define the  
standard motion-induced error for aerosol retrieval purposes.

We also confirmed in this study that the motion-induced error over cloud over water class can be predicted with a Monte Carlo  
model. The advantage of the simulation is that it doesn't require the high-resolution polarimetry to perform the error analysis.  
In the application to the 3MI data, among the four required input statistics, three statistics other than cloud subpixel  
295 inhomogeneity are readily available from the 3MI sensor itself. The cloud inhomogeneity parameter can be provided either  
from the collocated METImage sensor, or by replacing with alternative measure of the inhomogeneity, exploiting the stable  
reflectivity power spectrum in the few kilometers scale. As the motion-induced  $L_p$  error for the cloud-over-water class was the  
largest, the simulation technique is helpful to determine the upper limit of the motion-induced  $L_p$  error.

## 5. Conclusions

300 From the high-resolution global polarimetric observation by the SGLI, we estimate the 3MI's polarimetric error induced by  
the co-registration and interpolation that compensates satellite's along-track motion during the acquisition. The estimates show  
that the magnitude of the interpolation error is not negligible nor symmetric about the zero particularly over the locations  
where intensity variation is large.

The asymmetric distribution of the motion-induced error is confirmed in all four categories of analyzed pixels: clear-sky over  
305 land, clouds over land, clouds over water, and coastlines. The coastlines category had the most spread distribution of the degree  
of linear polarization (DOLP) difference, whereas the cloud-over-water class had the most spread distribution of the polarized  
normalized difference ( $L_p$ ) differences. The 9th to 95th percentile range was  $[-0.019; 0.082]$  for the DOLP differences and  
 $[-0.0051; 0.012]$  for the  $L_p$  differences. These differences strongly depend on the along-track Laplacian that characterizes  
the non-linear change of the normalized radiance ( $L_p$  difference), or that divided by the normalized radiance (DOLP

310 difference). As the along-track Laplacian is available from the observation, a pixel-level quality information can be obtained based on the statistics presented in this study. In addition, it is possible to perform the statistical estimation of error when the sub-pixel inhomogeneity is available as an input. Either procedures proposed in this study would help ensure the reliability of the radiance products and downstream applications including retrieval products as well as data assimilation.

The error statistics based on the SGLI data and Monte Carlo simulation agree within 5% in terms of median bias, implying the predictability of the error for cloudy pixels at an arbitrary spatial scale. The sensitivity study on the assumed power-law coefficient proved the need for the spatial correlation to be included in the error prediction. The method of prediction is applicable to past, current and future missions with a polarimetric instrument based on a similar design, paving a way to better predict the performance of the instrument on orbit at the stage of planning. Finally, although simulations presented here are limited to cloudy scenes, similar diagnosis might be made for land surfaces under clear sky conditions for use in aerosol remote sensing applications.

## Appendix

### A. Monte Carlo model of the motion-induced error

The statistics of the error is simulated with a Monte-Carlo model for pixels in cloud-over-water class. In summary, we first generate synthetic 2-D normalized radiance fields by the inverse 2-D Fourier transform, assuming the power-law spectrum of the normalized radiance distribution. We then proceed through with the weighting and aggregation equivalent to the method described in Section 2.1. This process is repeated for 10 million samples to realize meaningful statistics. The details of the method are described in the rest of this Appendix.

The first step is to apply inverse 2-D Fourier transform to the assumed power-law spectrum with Gaussian noise as in the method described by Iwabuchi and Hayasaka (2002). A number of studies show that the intensity spectrum of the cloud field follows the power-law (Cahalan and Snider 1989, Davis et al. 1997, Marshak et al. 1995, 1998, Oreopoulos et al. 2000) and the slope is known to be a function of horizontal spatial scale. For the scale greater than a few hundred meters and less than a few hundred kilometers, the power-law coefficient is between -1.5 and -2.0, and the value increases for the smaller. We select  $-5/3$  (1.666...) as the power-law coefficient in our simulation, as it is the value commonly referred. The impact of this choice is evaluated by the simulations with varied parameter in Section 4.2.

Every synthetic 2-D normalized radiance field that is generated in this way are different. They are however statistically centered at zero, and their variance depends on the prescribed power-law coefficient. In the second step, to make the simulation consistent with the SGLI-based estimation, we scale and add offset to each realization as in the following equation:

$$L_{(i,j)} = ax_{(i,j)} + b, \tag{A1}$$

where  $L_{(i,j)}$  is the final 2-D normalized radiance field,  $x_{(i,j)}$  the output of the inverse Fourier transform,  $a$  the scaling coefficient and  $b$  the offset. The scale  $a$  and offset  $b$  are determined so that the pixel intensity  $\bar{L} = \sum_i w_i L_i$  and weighted

variance  $V = \sum_i w_i (L_i - \bar{L})^2$  follow the observed empirical distribution function (EDF) of normalized radiance  $\hat{F}_L(l)$  and weighted variance  $\hat{F}_V(v; l)$ . These EDFs are computed from the SGLI data upon performing the error estimation described in Section 2.1. The EDF of variance  $\hat{F}_V(v; l)$  is computed for each small normalized radiance interval, spanning from 0 to 0.9 with 0.01 width, from 0.9 to 1 with 0.05 width, and from 1 to 1.5 with 0.5 width. The weight  $w_i$  is the arithmetic mean of final  
345 weights in Table 3 for every line (i.e. for Line 5, it is  $1/16 + 9/320 + 11/320 = 1/240$ ).

The third step is to compute  $X_{1(i,j)}$ ,  $X_{2(i,j)}$ , and  $X_{3(i,j)}$  from the 2-D normalized radiance field  $L_{(i,j)}$ , the angle of linear polarization (AOLP)  $\chi$ , and the degree of linear polarization (DOLP)  $\delta$ . The AOLP are sampled so that it follows the EDF of AOLP  $\hat{F}_\alpha(\alpha; l)$ , and the DOLP are sampled so that it follows EDF of DOLP  $\hat{F}_\delta(\delta; l)$ . The AOLP is assumed constant over subpixels for each realization, but the DOLP is sampled for each subpixel because of the strong intensity-dependence with  
350 weak spatial correlation. Figure A1 shows the strong decreasing trend of the DOLP with intensity. We note here that the statistics of the intensity-binned DOLP and the statistics of AOLP have been found necessary for the reasonable simulation of the polarimetric error. This is presumably because the DOLP varies significantly as a function of reflectivity at cloud boundaries and over thin clouds, and the AOLP determines the relative contribution of error in  $X_1$  and  $X_3$  images to the polarized normalized radiance ( $L_p$ ).

355 Once  $X_{1(i,j)}$ ,  $X_{2(i,j)}$ , and  $X_{3(i,j)}$  are obtained, the last step is to proceed through with the weighting and aggregation equivalent to the method described in Section 2.1. This entire process of 2-D Fourier transform, scaling, and  $X_1$ - $X_2$ - $X_3$  derivation is repeated 10 million times.

### Data availability

GCOM-C/SGLI data used in this study is available from the G-Portal website (<https://gportal.jaxa.jp/gpr/>) by Japan Aerospace  
360 Exploration Agency (JAXA).

### Author contributions

Souichiro Hioki and Jérôme Riedi conceived of the methodology and outlined the project. Souichiro Hioki performed the study and composed the manuscript. Jérôme Riedi encouraged and supervised the project. Mohamed S. Djellali contributed the research activities through discussions on the results.

### 365 Competing interests

The authors declare that they have no conflict of interest.

## Acknowledgements

We appreciate Japan Aerospace Exploration Agency (JAXA) for providing the GCOM-C/SGLI data needed for the research. This research is conducted in a framework of jointly-funded postdoctoral fellowship by Centre National d'Études Spatiales (CNES) and the Make Our Planet Great Again (MOPGA) program by Campus France. The authors are grateful for the financial support and various encouragements by CNES, MOPGA, and the Laboratoire d'Optique Atmosphérique. Our gratitude extends toward Dr. Bertrand Fougnie who provided us valuable comments regarding the 3MI and POLDER mission requirements. It is our pleasure to hereby express our gratitude to three reviewers, Dr. Frans Snik, Dr. Otto Hasekamp, and Dr. Kirk Knobelspiesse, for their constructive and positive comments.

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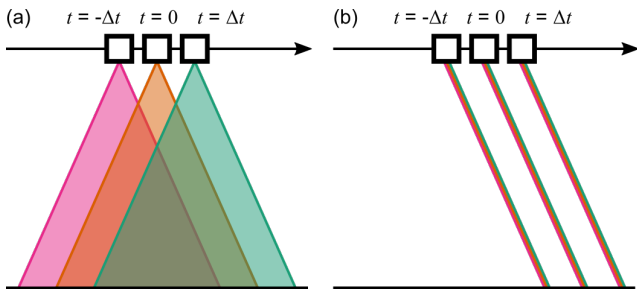


Figure 1. The schematic diagram of the field-of-view by the (a) 3MI and (b) SGLI. The black arrow shows the motion of satellite along the orbit, and the three position of the satellites along the track are shown to highlight asynchronous acquisition by the 3MI sensor.

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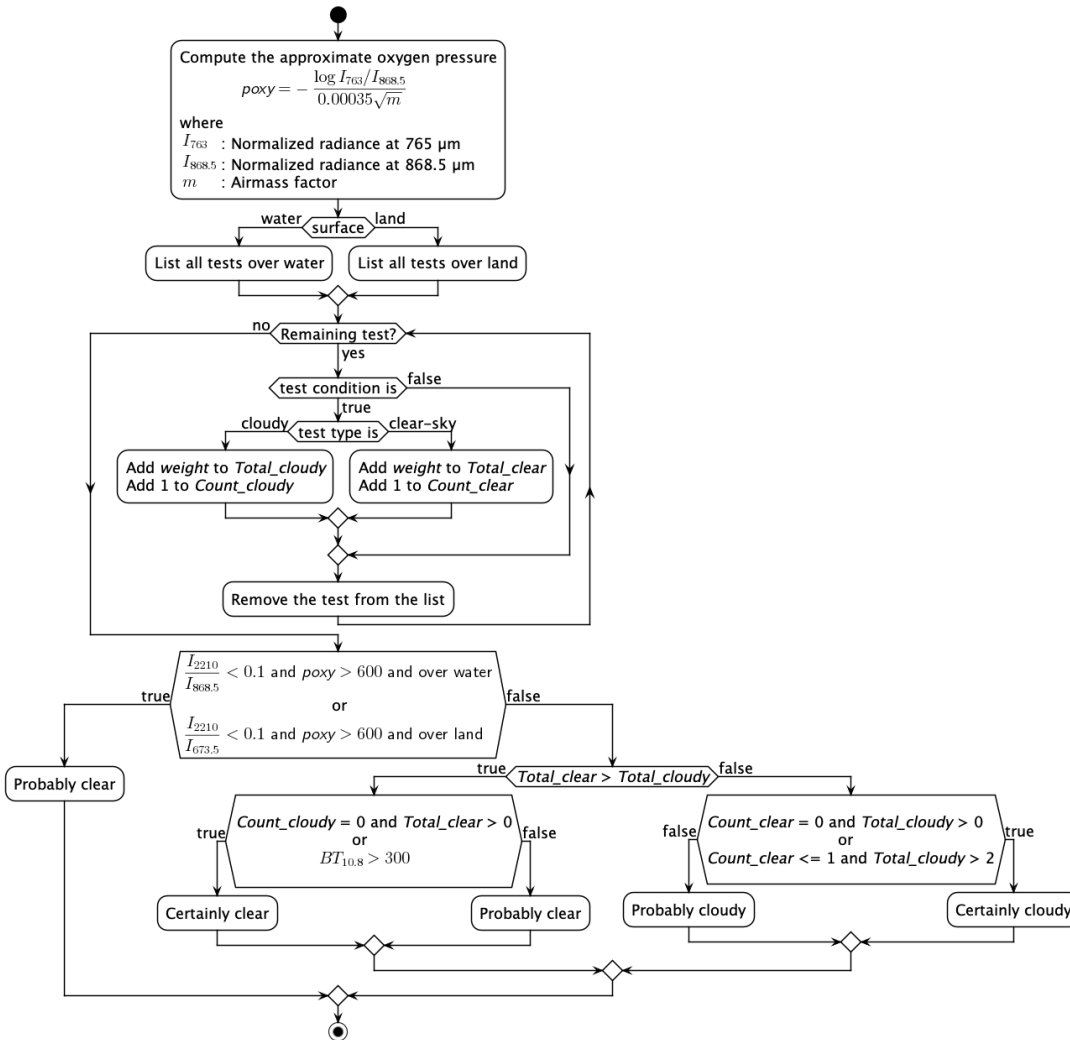
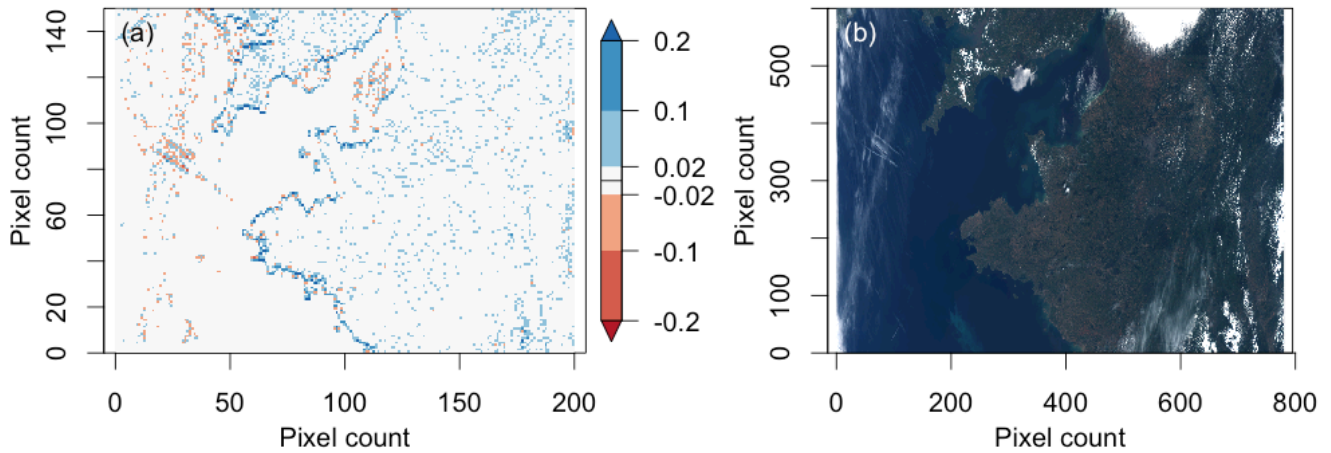
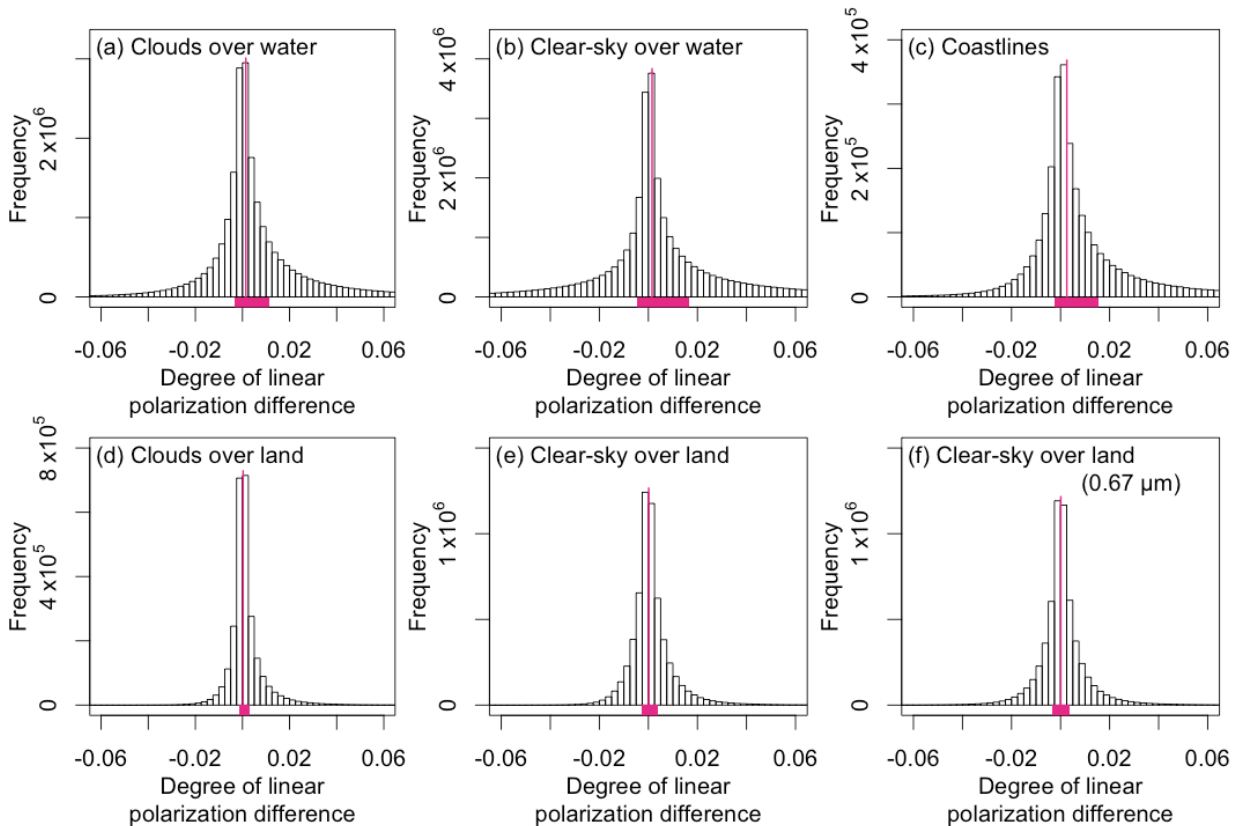


Figure 2. The activity diagram (flow-chart) of the cloud-flag algorithm.

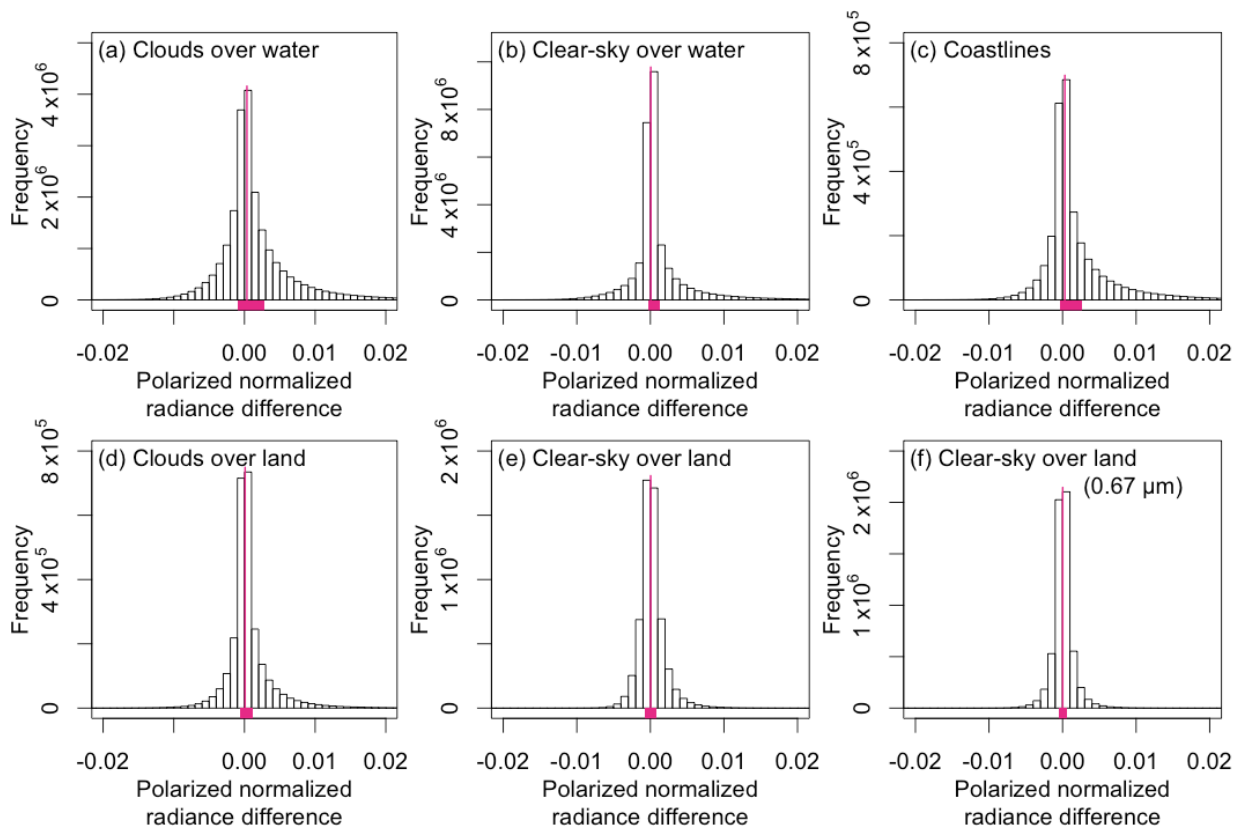


430 **Figure 3. (a) The DOLP difference between proxy and reference data. (b) The visible composite of the SGLI Level 1B data the same zone (visualized by authors, original data by JAXA).**



435 **Figure 4. Histogram of proxy-reference differences in degree of linear polarization (DOLP) for (a) clouds over water, (b) clouds over land, (c) coastlines, (d) clouds over land, (e) clear-sky over land, and (f) clear-sky over land at  $0.674 \mu\text{m}$ . Except for (f), the wavelength is at  $0.869 \mu\text{m}$ . The vertical magenta line indicates the location of the median, and the magenta bar at the bottom indicates the interquartile range.**





**Figure 5. Histogram of proxy-reference differences in normalized radiance ( $L$ ) for (a) clouds over water, (b) clouds over land, (c) coastlines, (d) clouds over land, (e) clear-sky over land, and (f) clear-sky over land at  $0.674 \mu\text{m}$ . Except for (f), the wavelength is at  $0.869 \mu\text{m}$ . The vertical magenta line indicates the location of the median, and the magenta bar at the bottom indicates the interquartile range.**

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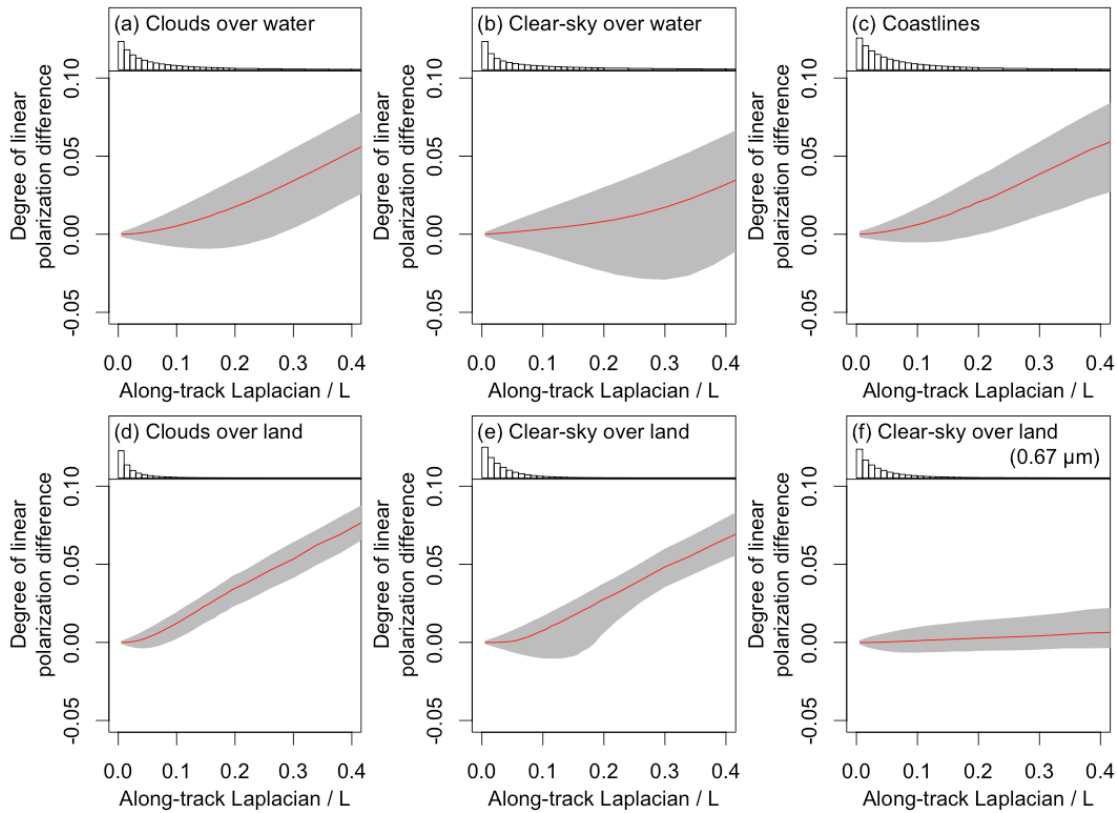


Figure 6. The proxy-reference differences in degree of linear polarization as a function of the along-track Laplacian divided by normalized radiance. Six panels are for: (a) clouds over water, (b) clouds over land, (c) coastlines, (d) clouds over land, (e) clear-sky over land, and (f) clear-sky over land at  $0.674 \mu\text{m}$ . Red curves represent the median and gray shading indicates the interquartile range. Except for (f), the wavelength is at  $0.869 \mu\text{m}$ .

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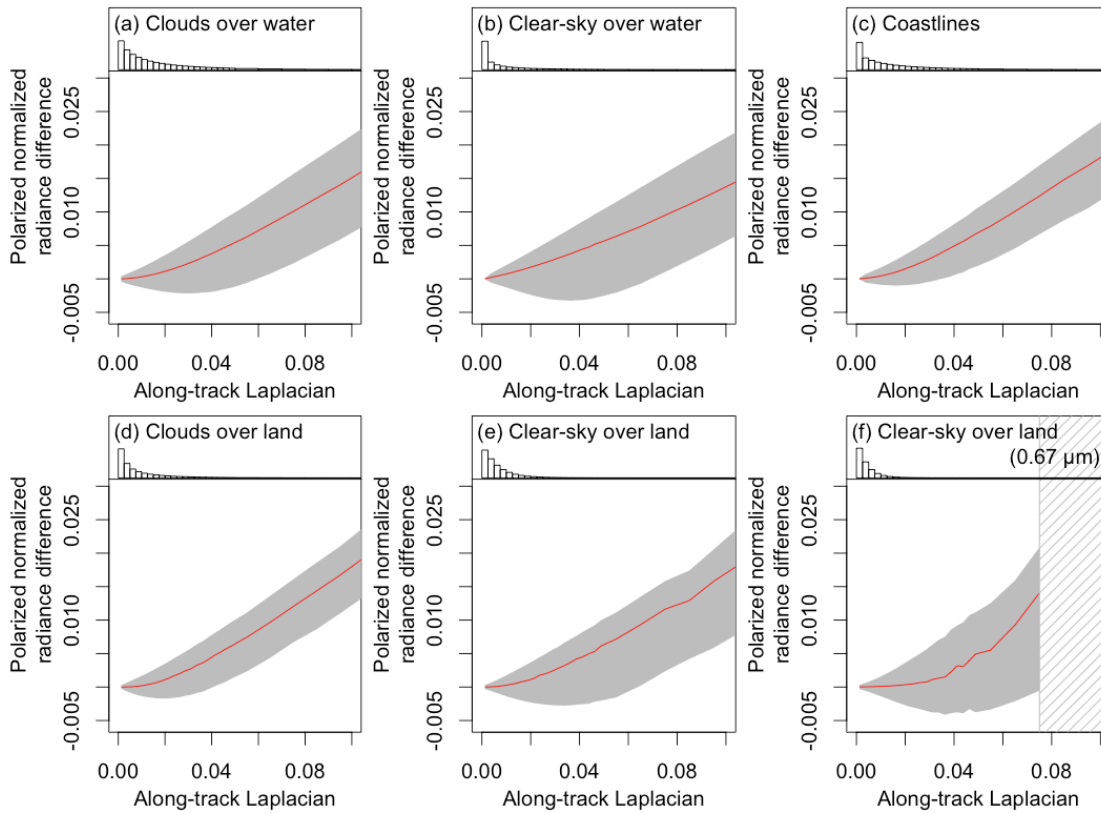
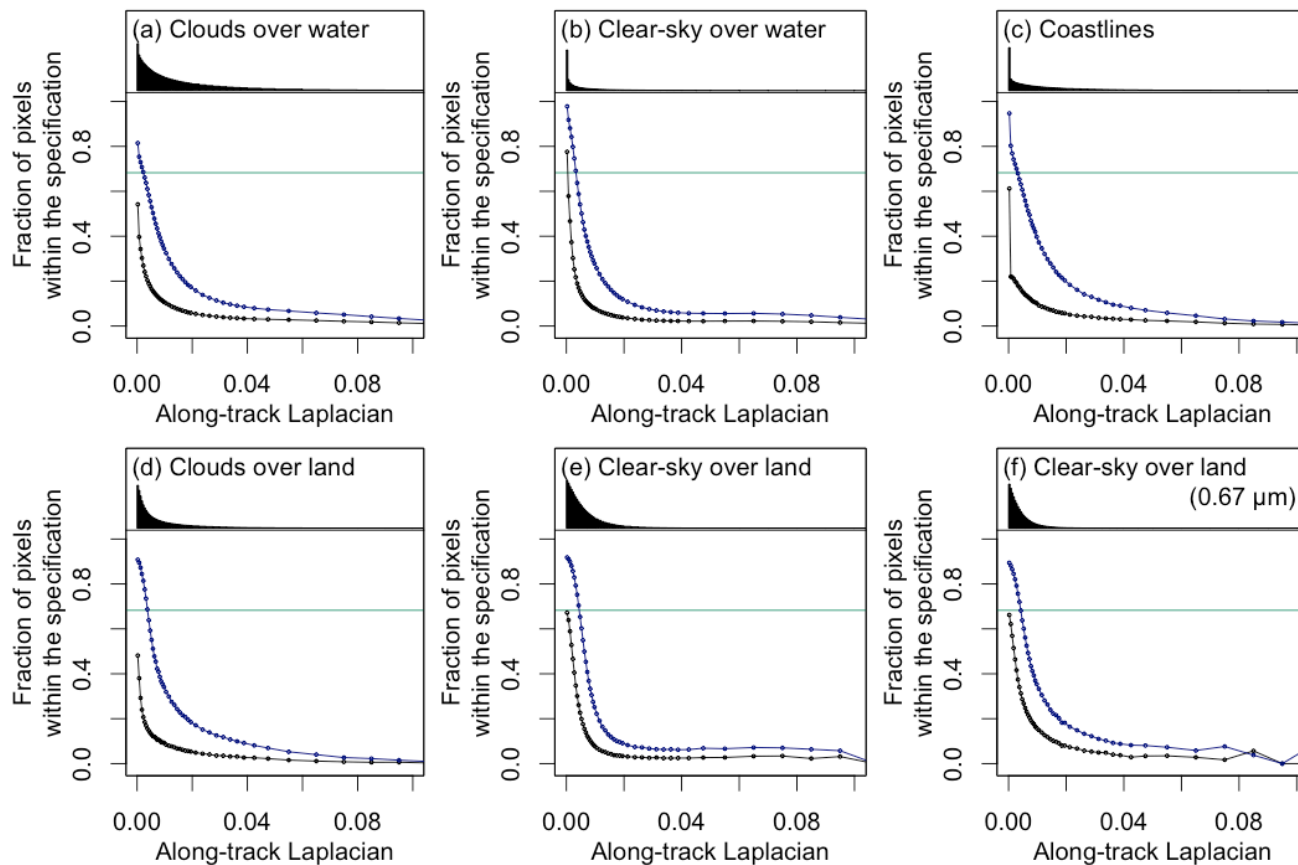


Figure 7. The proxy-reference differences in polarized normalized radiance as a function of the along-track Laplacian. Six panels are for: (a) clouds over water, (b) clouds over land, (c) coastlines, (d) clouds over land, (e) clear-sky over land, and (f) clear-sky over land at  $0.674 \mu\text{m}$ . The top histogram shows the data density along the x-axis. Red curves represent the median and gray shading indicate the interquartile range. Gray hatched area corresponds to the part where statistics is unavailable or unreliable because of limited number of data points. Except for (f), the wavelength is at  $0.869 \mu\text{m}$ .

450



455 **Figure 8.** The fraction of pixels within the POLDER specification (blue) and the 3MI specification (black) in each bin of along-track Laplacian. The density histograms of the along-track Laplacian is presented on the top. The green horizontal line shows the fraction of 0.682, which corresponds to the fraction of data within  $1\sigma$  of a normal distribution.

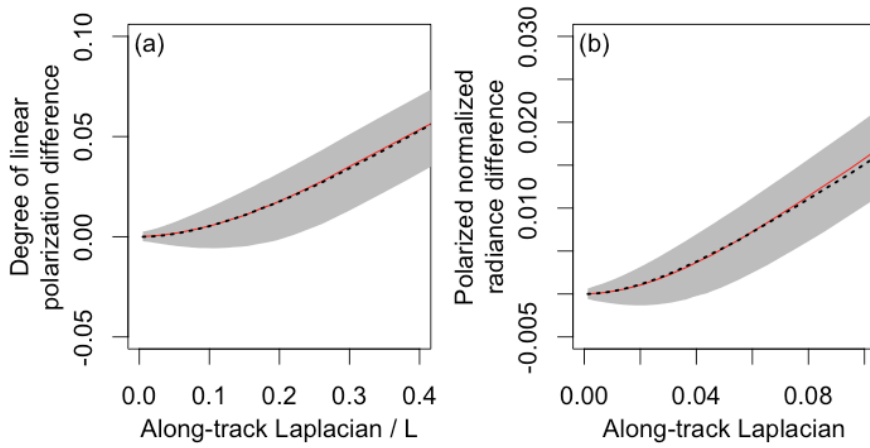


Figure 9. (a) The simulated proxy-reference difference in the degree of linear polarization as a function of the along-track Laplacian divided by normalized radiance (b) The simulated proxy-reference difference in the polarized normalized radiance as a function of the along-track Laplacian. Red curves represent median and gray shading indicates the interquartile range of the simulation. Black dotted curves correspond to the medians of the observation (i.e. Red curves in Figs. 6(a) and 7(a)).

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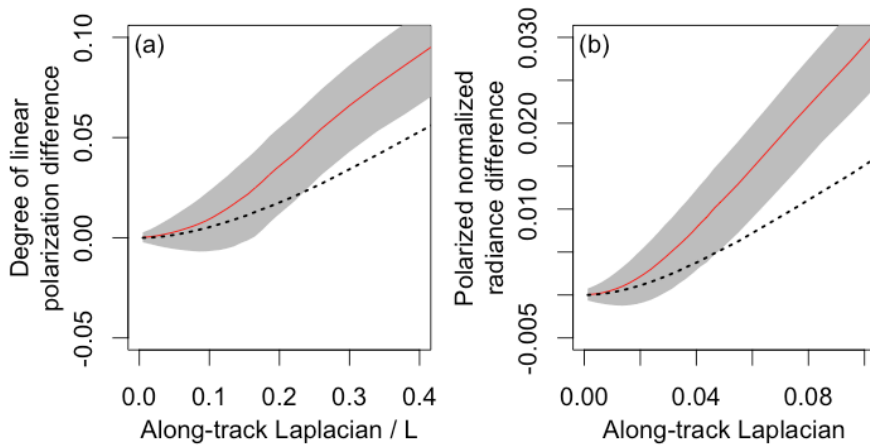
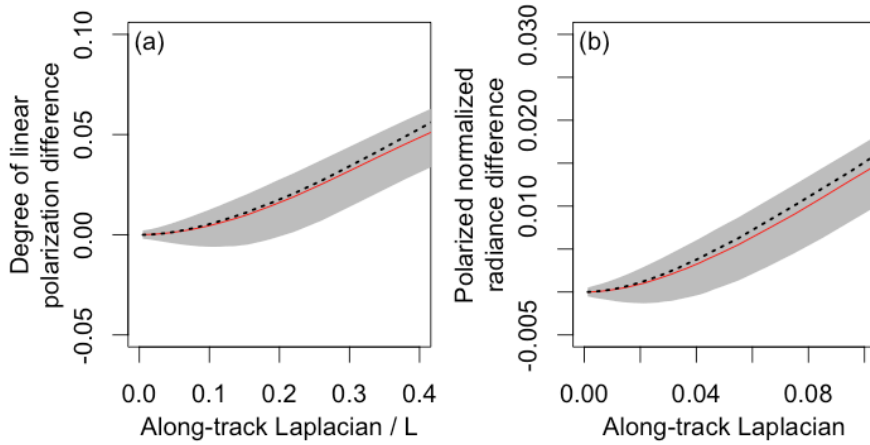


Figure 10. The same as Fig. 8 but without correlation in the cloud field simulation.



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Figure 11. The same as Fig. 8 but with slope of -3.0

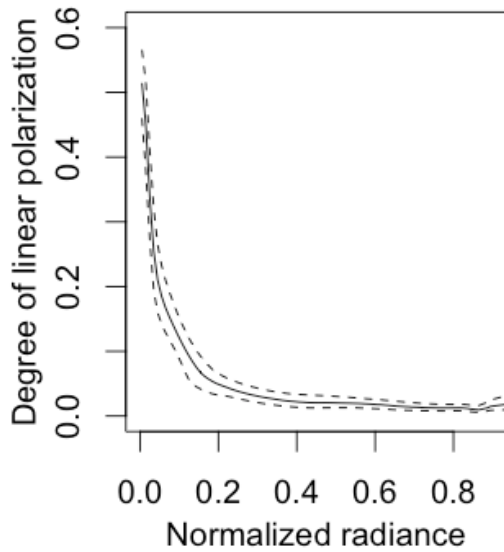


Figure A1. Decreasing trend of the degree of linear polarization for pixels over water with increasing intensity. The solid line is median, dashed lines are 25th and 75th percentile (interquartile range).

470 **Table 1. Specification of the radiometric accuracy for the 3MI instrument (summarized from Fougnie et al. 2018)**

Subject	Requirements (Better than)
Absolute calibration accuracy	2%
Inter-band (spectral) calibration consistency	1%
Lifetime radiometric consistency	1%
Inter-view calibration consistency	2%
Pixel-to-pixel relative calibration consistency within any $10 \times 10$ pixels area	0.1%
Knowledge of instrumental sensitivity to polarization	$10^{-3}$
Signal to noise ratio (SNR) at channel reference radiance value	200

**Table 2. Contribution of SGLI pixels to shifted and unshifted averaging grids for a single 3MI pixel. These weights are intended to simulate the along-track motion of the satellite.**

Line	Weights for the unshifted grid	Weights for the shifted grid (+1.8 km)	Weights for the shifted grid (-1.8 km)
1	0	0	0
2	0	0	0
3	0	0	1/20
4	0	0	1/16
5	1/16	0	1/16
6	1/16	1/80	1/16
7	1/16	1/16	1/80
8	1/16	1/16	0
9	0	1/16	0
10	0	1/20	0
11	0	0	0
12	0	0	0

475 **Table 3. Contribution of SGLI pixels to shifted and unshifted averaging grids for single 3MI pixel. These weights include the effects of satellite's along-track motion and the interpolation.**

Line	Weights for the unshifted grid	Weights for the shifted grid (+1.8 km)	Weights for the shifted grid (-1.8 km)
1	0	0	0
2	0	9/1600	0
3	0	9/320	11/400
4	0	9/320	11/320
5	1/16	9/320	11/320
6	1/16	47/1600	11/320
7	1/16	11/320	47/1600
8	1/16	11/320	9/320
9	0	11/320	9/320
10	0	11/400	9/320
11	0	0	9/1600
12	0	0	0



**Table 4. Tests for the cloud detection algorithm over water.**  $I_{XXX}$  indicates the normalized radiance at wavelength  $XXX$  nm,  $BT_{XX}$  the brightness temperature at  $XX$   $\mu$ m,  $\sigma_{XXX}$  the standard deviation of  $I_{XXX}$  in the concentric box of  $3 \times 3$  pixels.

Test condition	Test type	Weight
$(I_{1630}/I_{868.5} < 1.2)$ and $(BT_{10.8} < 288\text{K})$ and $(I_{673.5} > 0.2)$	Cloudy	1
$I_{673.5} > 0.45$	Cloudy	10
$(I_{673.5} > 0.35)$ and $(\sigma_{673.5} > 0.01)$	Cloudy	10
$(I_{673.5} > 0.15)$ and $(1 < I_{673.5}/I_{868.5} < 1.1)$ and $(BT_{10.8} < 295\text{K})$	Cloudy	10
$(I_{673.5} > 0.2)$ and $(\sigma_{673.5} > 0.005)$ and $(I_{673.5}/I_{1630} < 1.4)$	Cloudy	100
$(BT_{10.8} - BT_{12} < -1\text{K})$ and $(BT_{10.8} < 300\text{K})$	Cloudy	1000
$(I_{1630}/I_{868.5} > 1.3)$ and $(BT_{10.8} > 300\text{K})$	Clear-sky	1
$(I_{673.5}/I_{868.5} < 0.7)$	Clear-sky	10
$(\sigma_{673.5} < 0.1)$ and $(0.2 < I_{673.5} < 0.5)$ and $(1.5 < I_{1630}/I_{673.5} < 10)$	Clear-sky	100
$I_{1630}/I_{673.5} > 2.2$	Clear-sky	100
$(BT_{10.8} - BT_{12})$ and $(BT_{10.8} > 300\text{K})$	Clear-sky	1000
$\left  \frac{I_{868.5} - I_{673.5}}{I_{868.5} - I_{1630}} \right  > 2$	Clear-sky	1000

480

**Table 5. Tests for the cloud detection algorithm over land. The symbols are the same as in Table 4.**

Test condition	Test type	Weight
$(I_{1630}/I_{868.5} < 1.2)$ and $(BT_{10.8} < 288\text{K})$ and $(I_{673.5} > 0.2)$	Cloudy	1
$(I_{868.5} > 0.1)$ or $(\sigma_{868.5} > 0.005)$	Cloudy	10
$I_{1630} > 0.1$	Cloudy	100
$(BT_{10.8} - BT_{12} < -1\text{K})$ and $(BT_{10.8} < 300\text{K})$	Cloudy	1000
$I_{1380} > 0.01$	Cloudy	1000
$(I_{1630}/I_{868.5} > 1.3)$ and $(BT_{10.8} > 300\text{K})$	Clear-sky	1
$(I_{673.5}/I_{868.5} < 0.7)$ and $(I_{868.5} < 0.05)$	Clear-sky	10
$0 < \sigma_{868.5}/I_{868.5} < 0.01$ and $I_{868.5} < 0.1$	Clear-sky	100

**Table 6. The intervals of degree of linear polarization (DOLP) difference and polarized normalized radiance ( $L_p$ ) difference for percentiles that covers 90% and 50% of entire data.**

Percentile range	Pixel class	DOLP difference	$L_p$ difference
[5th:95th]	Cloud over water	[-0.023:0.060]	[-0.0051:0.012]
	Clear-sky over water	[-0.043:0.093]	[-0.0040:0.0088]
	Coastline	[-0.019:0.082]	[-0.0033:0.012]
	Cloud over land	[-0.0075:0.014]	[-0.0033:0.0062]
	Clear-sky over land	[-0.011:0.016]	[-0.0023:0.0032]
	Clear-sky over land (0.674 $\mu\text{m}$ )	[-0.014:0.017]	[-0.0021:0.0023]
[15.9th:84.1th]	Cloud over water	[-0.0074:0.022]	[-0.0020:0.0049]
	Clear-sky over water	[-0.012:0.034]	[-0.00095:0.0027]
	Coastline	[-0.0062:0.029]	[-0.0011:0.0049]
	Cloud over land	[-0.0030:0.0055]	[-0.0012:0.0023]
	Clear-sky over land	[-0.0051:0.0070]	[-0.0011:0.0015]
	Clear-sky over land (0.674 $\mu\text{m}$ )	[-0.0059:0.0070]	[-0.00090:0.00100]
[25th:75th]	Cloud over water	[-0.0033:0.011]	[-0.00090:0.0027]
	Clear-sky over water	[-0.0045:0.016]	[-0.00023:0.0012]
	Coastline	[-0.0026:0.015]	[-0.00034:0.0027]
	Cloud over land	[-0.0016:0.0030]	[-0.00058:0.0012]
	Clear-sky over land	[-0.0029:0.0040]	[-0.00069:0.00087]
	Clear-sky over land (0.674 $\mu\text{m}$ )	[-0.0032:0.0039]	[-0.00050:0.00057]

485

**Table 7. The medians of degree of linear polarization (DOLP) difference and polarized normalized radiance ( $L_p$ ) difference.**

Pixel class	DOLP difference	$L_p$ difference
Cloud over water	0.0014	0.00035
Clear-sky over water	0.0015	0.000049
Coastline	0.0025	0.00031
Cloud over land	0.00027	0.000089
Clear-sky over land	0.00014	0.000037
Clear-sky over land (0.674 $\mu\text{m}$ )	0.000099	0.000020