The high frequency response correction of eddy covariance fluxes. Part ~~1~~2: an experimental approach for analysing noisy measurements of small fluxes

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Abstract. Fluxes measured with the eddy covariance (EC) technique are subject to flux losses at high frequencies (low-pass filtering). If not properly corrected for, these result in systematically biased ecosystem-atmosphere gas exchange estimates. This loss is corrected using the system's transfer function which can be estimated with either theoretical ~~and~~ or experimental approaches. In the experimental approach, commonly used for closed-path EC systems, the low-pass filter transfer function (H) can be derived from the comparison of either (i) the measured power spectra of sonic temperature and the target gas mixing ratio or (ii) the cospectra of both entities with vertical wind speed. In this study, we compare the power spectral approach (PSA) and cospectral approach (CSA) in the calculation of H for a range of attenuation levels and signal-to-noise ratios (SNRs). For a systematic analysis, we artificially generate a representative dataset from sonic temperature (T) by attenuating it with a first order filter and contaminating it with white noise, resulting in various combinations of time constants and SNRs. For PSA, we use two methods to account for the noise in the spectra: the first is the one introduced by Ibrom et al. (2007a) (PSA_{I07}), where the noise and H are fitted in different frequency ranges and the noise is removed before estimating H. The second is a novel approach that uses the full power spectrum to fit both H and noise simultaneously ($PSA_{\sim A20 A21}$). For CSA, we use ~~three different methods: (1) a plain version of Lorentzian equation describing the H (CSA_H), (2) a~~ a method utilizing the square-root of the H ~~($CSA_{\sqrt{H}}$), and (3) a square-root of the H~~ with shifted vertical wind velocity time series via cross-covariance maximisation ($CSA_{\sqrt{H},sync}$). PSA_{I07} tends to overestimate the time constant when low-pass filtering is low, whilst the new $PSA_{\sim A20}$ ~~successfully estimates~~ $A21$ and $CSA_{\sqrt{H},sync}$ successfully estimate the expected time constant regardless of the degree of attenuation and SNR. ~~CSA_H underestimates the time constant with decreasing accuracy as attenuation increases due to the omission of the quadrature spectrum. $CSA_{\sqrt{H}}$ overestimates, but its accuracy increases with time-lag correction in the $CSA_{\sqrt{H},sync}$.~~ We further examine the effect of the time constant obtained with the different implementations of PSA and CSA on cumulative fluxes using estimated time constants in frequency response correction. For our example time series, the fluxes corrected using time constants derived by PSA_{I07} show a bias ~~of ±2%. PSA_{A20} showed a similar variation, yet slightly better accuracy. CSA_H underestimated fluxes by up to 4%, while $CSA_{\sqrt{H}}$ overestimated them by up to 3%, a bias which was mostly eliminated with time-lag correction in the CSA~~between 0.1 and 1.4%. PSA_{A21} showed almost no bias,

while CSA$_{\sqrt{H},sync}$ ~~(−2% to 1%)~~showed bias of $\pm 0.4\%$. The accuracies of both PSA and CSA methods were not significantly affected by SNR level, instilling confidence in EC flux measurements and data processing in setups with low SNR. Overall we show that, when using power spectra for the empirical estimation of parameters of H for closed-path EC systems the new PSA$_{\text{A20}~\text{A21}}$ outperforms PSA$_{I07}$, while when using cospectra the CSA$_{\sqrt{H},sync}$ approach provides ~~the most~~ accurate results.

5   These findings are independent of the SNR value and attenuation level.

1   Introduction

Vertical turbulent fluxes of momentum, energy, and gases between the atmosphere and the biosphere measured by the eddy covariance (EC) technique are subject to both low and high frequency losses (Foken and Napo, 2008; Aubinet et al., 2012). The physical limitations in instrument response times, spatial separation of instruments, line averaging, and air transport through

10   the sampling tubes cause high frequency losses (Aubinet et al., 1999).

    The EC sampling system acts as a low-pass filter on the flux and the signal loss must be compensated with the frequency response correction (FRC) during post-processing. The first step in the FRC is the description of the effect of the low-pass filtering of the measurement system, and for this, the transfer function approach has been widely used since it was first proposed by Moore (1986). The joint transfer function (H) that describes the low-pass filtering of the whole EC system can be determined

15   theoretically or experimentally (Foken and Napo, 2008; Aubinet et al., 2012). The theoretical approach involves ~~a convolution of~~ various specific transfer functions that are estimated to represent different causes of flux loss. Conversely, in the experimental approach H is estimated from *in situ* measurements. Due to its simplicity, many studies have implemented the theoretical approach, which typically works well with fluxes measured by open-path EC systems as well as momentum fluxes and sensible heat fluxes measured by sonic anemometers (Aubinet et al., 2012). However, for complex EC systems the necessary information

20   to calculate H is not available and needs to be estimated empirically. In addition, the time response of the system can vary with relative humidity (Ibrom et al., 2007a), tube aging ~~Mammarella et al. (2009)~~(Mammarella et al., 2009), and variations in the flow regime in the tube. Thus, the theoretical approach is not preferred for gas fluxes measured with closed-path EC systems, for which the experimental approach is therefore recommended (Aubinet et al., 2012; Sabbatini et al., 2018; Nemitz et al., 2018).

25   In the experimental approach for closed-path systems, H is usually estimated from either the measured power spectra (i.e. PSA) or cospectra (i.e. CSA) of sonic temperature and the mixing ratio of the target gas (χ). Different studies use either PSA (Ibrom et al., 2007a; Nordbo et al., 2011; Fratini et al., 2012; Sabbatini et al., 2018) or CSA (Aubinet et al., 1999; Humphreys et al., 2005; Mammarella et al., 2009; Peltola et al., 2013). Also, some software packages used for EC flux calculation are based on PSA ~~(e.g. EddyPro, see Biosciences, 2020)~~(e.g. EddyPro, see LI-COR Biosciences, 2020), while others are based on

30   CSA (e.g. EddyUH, see Mammarella et al., 2016).

    Interestingly, there has not been much debate to date whether to use power spectra or cospectra to determine the time constant of the H (or response time), which characterizes the EC system's high-frequency response. Only recently, Wintjen et al. (2020) investigated the optimal method for high frequency response correction, for fluxes of nitrogen compounds, recommending

CSA. Ibrom et al. (2007a) argued for using PSA as the vertical wind speed (w) does not contain any relevant information for the spectral attenuation of the gas collection and data acquisition system, allowing to describe ~~sensor related~~ sensor-related attenuation independently. This should in principle provides a better estimation of the time constant of the gas analysis system, because the spectral data is not mingled with other components, such as, e.g., sensor separation. In this approach, the effect of sensor separation is then treated explicitly with an additional correction step (Horst and Lenschow, 2009). In most cases the instrumental noise becomes visible in the high frequency range of χ' power spectra, and this has to be dealt with before the time constant of the gas sampling system can be estimated. The noise removal procedure is not well established, and this represents a major uncertainty in the PSA approach. This paper explores this uncertainty and proposes a novel, more robust approach to account for the noise in PSA.

~~This~~ On the other hand, this noise is often assumed not to correlate with the fluctuations in w, and therefore it does not contribute to the cospectra between w and χ. If this holds, this makes the CSA attractive for the estimation of the time constant, because then the noise would effectively ~~be~~ disappear from the measured signal. ~~On the other hand~~Yet, the use of the CSA relies on the correct determination of the time lag between w and χ, which may be difficult in case of small fluxes due to noisier cross-correlation function, making the search for the absolute maximum harder (Langford et al., 2015). Due to the above-mentioned reasons, empirically determined H can be a source of uncertainty for the FRC (Lee et al., 2004). Additionally, the CSA approach inadvertently accounts for the phase shift caused by low-pass filtering, a topic discussed in our companion paper (Peltola et al., 2021).

EC measurements conducted under ~~low flux~~ low-flux conditions result in relatively ~~higher noise in signal~~ high signal noise, i.e. low signal-to-noise ratio (SNR) (Smeets et al., 2009). EC fluxes with low SNR are ~~typically~~ normally found in many ecosystems especially for methane (CH_4) and nitrous oxide (N_2O) as well as for other ~~gases and~~ non-H_2O and non-CO_2 gas species and aerosol particles, in which any implementation of the FRC becomes uncertain (Rannik et al., 2015; Nemitz et al., 2018; Oosterwijk et al., 2018). Low SNR can also be observed for CO_2 at specific ecosystems (e.g. lakes), and seasons (e.g., senescence, winter dormancy), for CH_4 over well-drained soils or peatlands during winter, for N_2O in long periods outside the high emission periods (e.g. fertilizer applications, freeze-thaw cycles, or rain events), all of which, although small, ~~ultimately~~ significantly contribute to the ~~final flux estimates~~long-term flux budgets, and, hence must be corrected ~~from~~ to reduce the systematic bias. Thus, investigation of uncertainties in commonly used FRC methods is of great importance ~~in order to obtain~~ for obtaining unbiased, harmonized and continuous time series of gas fluxes measured by EC technique.

To our knowledge, the uncertainty in fluxes caused by the use of the PSA and the CSA have not been investigated systematically so far, motivating this study, which hypothesizes that the success of the PSA and CSA usage in FRC depends on the attenuation condition and the level of SNR. Consequently, we expect to see substantially different time constants, correction factors, and eventually different overall magnitudes of correction estimates with respect to the attenuation and SNR conditions. To test this hypothesis, we need a scalar dataset, which represents different attenuation levels and noise conditions. Assuming spectral similarity between scalars, we apply different levels of attenuation and noise to sonic temperature time series (T) in order to generate a proxy representing attenuated gas concentration dataset (e.g. CH_4, N_2O) with known characteristics. We use a ~~first order~~ first-order low-pass filter, which solely depends on a single time constant (τ_{LPF}), to attenuate the signal. Then,

we systematically contaminate the signal with white noise. We then assess which analysis approach most closely retrieves the true time constant used to degrade the flux in the first place. ~~Firstly~~First, we try to retrieve the system time constants using the PSA and CSA, then compare those with original values (i.e., τ_{LPF}). ~~Secondly~~Second, in order to demonstrate how variation in time constant estimation further affects the cumulative fluxes, we run a low-pass filter ~~a one month T time series~~ over one

5   month-long time series of T, and correct the attenuation with the FRC of Fratini et al. (2012) via implementing the time constants calculated in the first step. In Sect. 2, the theory of experimental FRC is summarized. In Sect. 3, materials used in this study and methods are explained. Results and discussion are then interpreted in Sect. 4.

2   Theory

2.1   Background of methods typically used to determine the system time response

10   In order to calculate the true unattenuated (i.e. frequency-response corrected) covariance ($\overline{w'\chi'}_{\text{corr}}$) with the transfer function method, the measured covariance ($\overline{w'\chi'}_{\text{meas}}$) is multiplied by a correction factor (F_{corr}):

$$\overline{w'\chi'}_{\text{corr}} = \overline{w'\chi'}_{\text{meas}} F_{corr}. \tag{1}$$

One way to calculate F_{corr} is to estimate the ratio of the integrated unbiased and biased cospectra as a function of frequency. In order to define the co-spectrum of the unattenuated scalar under the assumption that the normalized cospectrum of all scalars

15   has the same form (i.e scalar similarity), either the cospectra model (see Mammarella et al., 2009) or the measured cospectra (see Fratini et al., 2012) of T are used as a reference. Many studies used the surface layer models described by Kaimal et al. (1972) and based on Kansas experiments (see Moore, 1986). The attenuated cospectra are obtained by ~~convolution~~ multiplication of the reference cospectra with the transfer function (H), which characterizes the filtering of the EC system.

Another way to calculate F_{corr} is to simulate the attenuation with a recursive filter in time, rather than in frequency space,

20   in which F_{corr} is defined as the ratio of the unattenuated and attenuated co-variances (see Goulden et al., 1997). In addition, based on the same approach, an experimental method was proposed by Ibrom et al. (2007a) to parameterise the correction factor separately for stable and unstable stratifications, using meteorological data. For this method, a further modification was later suggested by Fratini et al. (2012) for the processing of large fluxes.

Regardless of the method chosen, H needs to be obtained either theoretically or empirically before F_{corr} can be calculated.

25   In empirical approach, H can be determined using *in situ* measurements as a ratio of the normalized power spectra (for PSA) or cospectra (for CSA) of the attenuated scalar to those of an unattenuated scalar, e.g., T. In both approaches, in order to reduce the uncertainties on the low frequency part of the spectra, and to fulfill the assumption of spectral similarity, data must be selected from periods with rigorous stationary turbulent mixing. In addition, the power spectra and cospectra of T and χ should be normalized with their standard deviations so that they can be compared with each other (see their Eq. 2 in Ibrom

30   et al., 2007a).

For the PSA, H can be calculated using the power spectra of χ and T (Eq. (2)), where the effect of sensor separation should additionally be treated via the method proposed by Horst and Lenschow (2009). For PSA, H is derived as:

$$H_{PSA}(f) = \left[\frac{S_\chi(f)}{\sigma_\chi^2}\right]\left[\frac{S_T(f)}{\sigma_T^2}\right]^{-1}, \tag{2}$$

where S_χ indicates the power spectrum of measured target gas mixing ratio, S_T is the power spectrum of T, and variances (σ_χ^2 and σ_T^2) are calculated across the frequency range over which no attenuation occurs. Instrumental noise often becomes dominant in the high frequency range of the power spectrum and also contributes to ~~σ_s. Where instrumental noise is large, the power spectrum asymptotically approaches a line of slope +1 at the high frequency end (~~σ_χ (see blue line in Fig. 1)~~which represents the fact that white noise affects all frequencies equally, but is multiplied by f in this representation (see Sect. 2.2).~~ Thus, prior to calculation of Eq. (2), the noise contribution to the power spectra of S_χ should be removed ~~and this is typically done by fitting a line to the high frequency end~~ (Ibrom et al., 2007a). Finally, the frequency dependence of H_{PSA} can be ~~be~~ described through a sigmoidal curve which is characterised by the time constant (τ) of the measurement system (see for more details Peltola et al., 2021, and references therein):

$$H_{emp}(f) = \frac{1}{1 + (2\pi f \tau)^2}. \tag{3}$$

For PSA, Ibrom et al. (2007a) updated Eq. (2) by introducing a normalisation factor, which is used to secure the spectral similarity especially for small fluxes. As described in their Eq. (6), the time constant and the normalisation factor (F_n) are obtained via fitting the following equation to the dampened and ~~noise free~~ noise-free χ data:

$$\frac{S_\chi(f)}{\sigma_\chi^2} = \frac{S_T(f)}{\sigma_T^2} F_n \frac{1}{1 + (2\pi f \tau)^2}. \tag{4}$$

In our study, we follow the same procedure (hereafter PSA$_{I07}$) for the time constant calculation for the PSA, which is summarized in Sect. 3.2. In addition to PSA$_{I07}$, we used a new comprehensive method for PSA, which is summarized in Sect. 2.2.

Alternatively, for the CSA, H is calculated as

$$H_{CSA}(f) = \left[\frac{Co_{w\chi}(f)}{\overline{w'\chi'}}\right]\left[\frac{Co_{wT}(f)}{\overline{w'T'}}\right]^{-1}, \tag{5}$$

where f is the natural frequency, $Co_{w\chi}$ indicates the cospectrum of measured w and target gas mixing ratio χ; Co_{wT} is the cospectrum of measured kinematic heat flux, $\overline{w'\chi'}$ and $\overline{w'T'}$ are covariances calculated across a frequency range where the cospectra are not attenuated.

For CSA, τ is obtained ~~similar to PSA~~ via fitting H_{emp} to Eq. (5), however, there is an ongoing debate on whether the correct transfer function for the cospectra would be $\sqrt{H_{emp}}$, instead of H_{emp} (Moore, 1986; Eugster and Senn, 1995; Horst, 1997, 2000; Fratini et al., 2012; Hunt et al., 2016)~~as discussed throughouly by Peltola et al. (2021)who also provide a mathematical derivation on the subject. Since both forms exist widely in the literature, here we~~, which is related to the low-pass filtering time-lag (i.e. phase shift) as discussed thoroughly by Peltola et al. (2021). They showed that the phase shift effect can be well approximated when square-root is used. We therefore opt to apply ~~both approaches to CSAto demonstrate discrepancies between the approaches~~$\sqrt{H_{emp}}$ to CSA.

2.2 ~~A new approach to estimate~~ Estimating the time constant from a noise-contaminated power spectrum

In the PSA$_{I07}$ application to noisy data, the time constant is typically obtained via two separate fitting procedure steps following the approach of Ibrom et al. (2007a) as illustrated in Fig. 1 for a noisy spectrum. First ~~the noise part~~, in order to remove the noise, the noise part of the attenuated-noisy power spectra (blue solid line) is fitted with a line of an unconstrained slope

5 (blue dashed line) ~~and then the transfer function is fitted (black solid line). This~~ within the marked-frequency domain in the high-frequency end, then the line is extended towards lower frequencies and subtracted from attenuated-noisy power spectra, yielding noise-free power spectra (black line) represented with the term $\frac{S_\chi(f)}{\sigma_\chi^2}$ in Eq. (4). The unattenuated and noise free spectra of T (i.e. term $\frac{S_T(f)}{\sigma_T^2}$ in Eq. (4)) is represented with red line. Second, the time constant is obtained via fitting Eq. (4) within the marked-frequency domain.

10 Regarding the noise removal procedure, this approach can be problematic as we will show in Sec. 4.1 below, because if the resulting line (blue-dashed line in Fig. 1) has a slope less than unity, its extrapolation to lower frequencies erroneously removes the true signal. ~~By contrast, a line with a predefined slope of 1 can only be fit for very noisy spectra where the 1:1 is fully reached.~~ In addition, the frequency domains used for fittings should be determined visually, requiring expertise in micrometeorology and signal processing, which limits its effective application in the research community.

15 Here we introduce a new alternative approach (hereafter PSA$_{A20}$ ~~), which~~ $_{A21}$) that overcomes above-mentioned shortcomings as we will show in Sec. 4.1 below. It performs the estimation of the time constant and accounts for instrument ~~noise~~ without removal in a single non-linear comprehensive fitting step. In this approach, the time constant is yielded via fitting Eq. (7) to directly attenuated-noisy power spectra (blue-solid line). The fitting is performed across the entire frequency domain (Fig. 1), indicating that the visual inspection is not needed. The brief derivation of Eq. (7) is shown below.

20 Equation (4) can be extended to the following equation, which includes also the noise component of the scalar:

$$f\frac{S_\chi(f)}{\sigma_\chi^2} = f\frac{S_T(f)}{\sigma_T^2}F_n\frac{1}{1+(2\pi f\tau)^2} + f\frac{S_{\chi,n}(f)}{\sigma_\chi^2}, \tag{6}$$

where $S_{\chi,n}(f)$ is the power spectrum of the noise in χ. Here it is assumed that the noise and signal in measured χ time series are uncorrelated and hence two independent and additive components of the time series. In the case of white noise, Eq.(6) can be simplified to

25 $$f\frac{S_\chi(f)}{\sigma_\chi^2} = f\frac{S_T(f)}{\sigma_T^2}F_n\frac{1}{1+(2\pi f\tau)^2} + fb, \tag{7}$$

where b is the ~~y-axis intercept of the power spectra of the white noise multiplied with f~~ ratio between noise variance and variance used to normalise the χ power spectrum, which is shown linearly in log-log scale. All terms in the equation have been multiplied by f because this is the standard normalisation used to depict the spectral density functions (Fig. 1). The detailed derivation of Eq. (7) can be found in Appendix A.

30 ~~In this approach, the frequency ranges used for fitting both for transfer function and noise are not separated, hence the fitting is performed across the entire frequency domain.~~
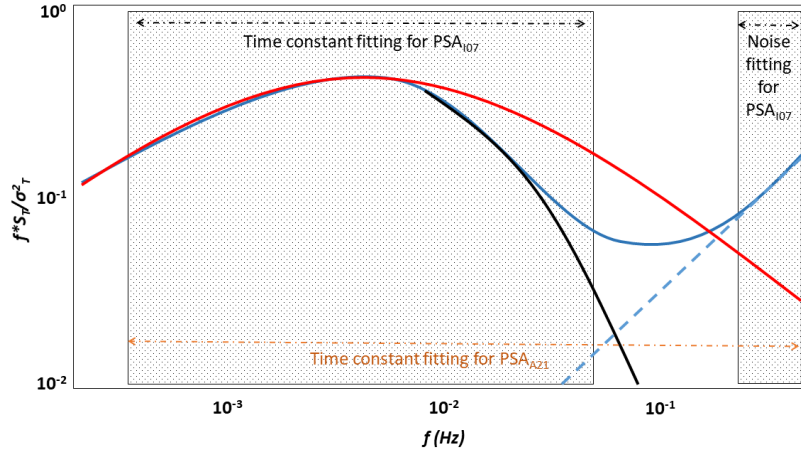
Figure 1. A diagram illustrating ~~two-steps~~ fitting procedures ~~(i.e. noise removal and transfer function) to estimate time constant~~ for PSA~~$_{I07}$~~methods. Shown are the spectra of unattenuated and noise-free ~~scalar~~ temperature (red line), and spectra of low-pass filtered and noisy scalar (~~dark blue~~blue-solid line) and after (black ~~line~~) noise removal. ~~The blue-dotted lines are~~ For PSA$_{I07}$, the ~~curves fitted~~ noise is detected via fitting a line (blue-dashed) to the ~~high frequency~~ high-frequency end of ~~blue line~~noisy scalar over the frequency range highlighted. Then, ~~then~~ it is extended towards lower frequencies, and subtracted from the noisy spectrum, yielding noise-free spectra. ~~The shaded areas mark~~ Later, the time constant is calculated via fitting Eq. (4) to noise-free spectra over the frequency range ~~used for~~highlighted. For PSA$_{A21}$, the time constant is obtained from one comprehensive fitting ~~for noise removal and transfer function~~Eq. (7) to noisy spectra over the whole frequency range highlighted.

3 Materials and methods

3.1 Sites description and measurements

Two datasets measured with sonic anemometer in an EC set up from the Siikaneva fen site were mainly used in this study. The site is located in Southern Finland ($61^o49.9610'$ N, $24^o11.5670'$ E; 160 m a.s.l). The data were measured with 10 Hz sampling frequency using a 3-D sonic anemometer (Model USA-1; Metek GmbH, Elmshorn, Germany). Further details about the site and measurements can be found in Peltola et al. (2013).

The first dataset (D_1) was used for the time constant calculation (see Sect. 3.2). It contained 70 half-hourly EC data records measured in fully turbulent daytime conditions in the period from May to September 2013 with an average sensible heat flux of 114.3 W m^{-2}, friction velocity of 0.3 m s^{-1}, and wind speed of 2.1 m s^{-1}.

The second dataset (D_2) was used for the cumulative flux calculation based on T (see Sect. 3.3). This dataset was measured between May 1 and May ~~31~~ 30 2013 and consisted of 1440 half-hourly periods for which fluxes were calculated.

Lastly, to demonstrate the performances of different methods in real-world data, we used CO_2 dataset (D_3) measured with 10 Hz sampling frequency using an infrared gas analyzer (LI-7000, LI-COR, Lincoln, NE, USA). The measurements were simultaneously done with D_1 at the same set up at 2.75 m above the peat surface, where the center of the sonic anemometer was displaced 25 cm vertically above the intake of gas analyzer. The air was drawn to the analyzer through a 16.8 m long heated inlet sampling line.

3.2 Data processing for time constant estimation

The data processing flow for all variants of PSA and CSA is summarized in Fig. 2. In order to generate the artificial dataset, which represents various known levels of SNR and attenuation, we first applied commonly used EC data processing procedures, i.e., de-spiking, two-dimensional coordinate rotation of the wind velocity vector, and linear de-trending to D_1. We ~~did not apply the time-lag correction because we assumed that there was no time-lag between T and w, both of which measured with the same instrument. We~~ then degraded each half-hourly T time series with a first order low-pass filter in the spectral domain (see Sect. 3.2.1) and contaminated it with prescribed amount of white noise in the time domain (see Sect. 3.2.2).

For PSA, we calculated power spectra of T, following Sabbatini et al. (2018), normalised it by the total variance calculated within the frequency range of 0.0012 and 0.05 Hz, and averaged it into a logarithmically equally distanced frequency base. Then we took an ensemble average of the 70 power spectra. For PSA_{I07}, we first removed the noise from the power spectra (see Sect. ~~??~~2.2), then ~~retrieve~~ retrieved the time constant (i.e. $\tau_{PSA_{I07}}$) via fitting Eq. (4) within a frequency range, the lower limit of which is 0.01 Hz, while the optimal higher limit is defined via visual inspection. For $PSA_{\sout{A20}A21}$, we obtained the time constant (i.e. $\tau_{PSA_{\sout{A20}}}\tau_{PSA_{A21}}$) via fitting Eq. (4) using the entire frequency domain.

~~Low-pass~~ In practice there is no time-lag between T and w as both variables are measured with the same instrument. However, low-pass filtering introduces a time-lag in the scalar of interest in addition to any physical time-lag that may be caused by transport through sampling lines and/or sensor separation ~~(Massman, 2000; Ibrom et al., 2007b)~~ (Massman, 2000; Ibrom et al., 2007b; Peltola et al., 2021). In our case, since the scalar of interest is represented by the attenuated T, ~~this~~ the time-lag ~~occurs~~ occurring between T and w ~~, two entities that are not separated by a further physical time-lag. In order to demonstrate the effect of low-pass induced time-lag on the time constant estimation in CSA, we generated a dataset in which the time-lag~~ was adjusted via the maximisation of the ~~crosscovariance, which was explored in addition to the original not time-lag adjusted dataset~~cross-covariance for the time constant estimation in CSA. Next, we calculated cospectra of T and w~~of both datasets~~, normalised it with the total ~~covariances~~covariance calculated within the frequency range of 0.0012 and 0.05 Hz, and averaged the data into exponentially spaced frequency bins. Then we calculated ensemble averages. Lastly, we derived the time constants for the original dataset (i.e. $\tau_{CSA_{\sqrt{H},sync}}$) via fitting the square-root of Eq. (3)~~, while for time-lag corrected dataset, i. e. τ_{CSA_H} via fitting Eq. (3), and (i.e. $\tau_{CSA_{\sqrt{H}}}$) via fitting square-root of Eq. (3). All fits were ~~. The fit was estimated for the frequency range from 0.01 to 2 Hz. ~~For a more complete analysis on the effect of low-pass induced time-lag on time constant estimation see the companion paper (Peltola et al., 2021).~~

In summary, for ~~the two methods of PSA and three methods of CSA~~three methods (two PSAs and one CSA), we assessed 45 different conditions each, combining five different attenuation levels with nine different SNRs. We repeated the same procedure

100 times to account for the uncertainty associated with the white noise generation, and thus obtained 100 different values for the time constant for all attenuation and SNR levels for both PSA and CSA. The relevant results are shown in Sect. 4.2.
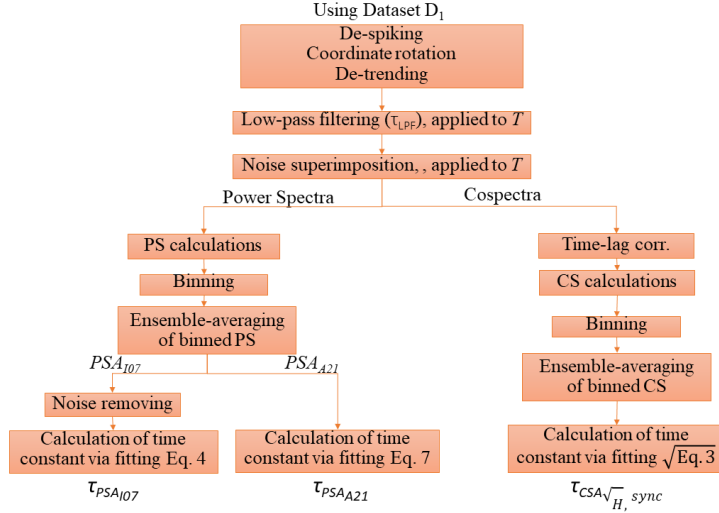
Figure 2. Flow chart of the data processing for time constant calculation using the dataset D_1. τ_{LPF} is the time constant of the first order filter. $\tau_{PSA_{I07}}$ and ~~$\tau_{PSA_{A20}}$~~ $\tau_{PSA_{A21}}$ represent the estimated time constants with power spectra (PSA), while $\tau_{CSA_{\sqrt{H},sync}}$, ~~$\tau_{CSA_{\sqrt{H}}}$ and~~ ~~τ_{CSA_H}~~ with cospectra (CSA)~~approaches~~. H is the spectral transfer function.

3.2.1 Low-pass filtering

The dynamic performance of any EC measurement system can be approximated with a linear first-order non-homogeneous ordinary differential equation (Massman and Lee, 2002):

$$\tau_{LPF}\frac{d\chi_O}{dt} + \chi_O(t) = \chi_I(t), \tag{8}$$

where χ_O is the output of a scalar sensor, $\chi_I(t)$ is the true scalar concentration (i.e., input) and τ_{LPF} is the characteristic time constant of the sensor response (Massman and Lee, 2002). The spectral response ($h_{LPF}(\omega)$) of such system can be obtained by the Fourier transform of the ratio of the output signal to the input signal, i.e. χ_O/χ_I (Horst, 1997):

$$h_{LPF}(\omega) = \frac{1}{1 - j\omega\tau_{LPF}}, \tag{9}$$

where $\omega = 2\pi f$ and $j = \sqrt{-1}$.

The desired (i.e. low-pass filtered) output data in the frequency domain can be estimated as

$$Z_O = h_{LPF}(\omega)Z_I. \tag{10}$$

where Z_I is the Fourier transform of χ_I. From this, the low-pass filtered time series χ_O can be acquired by applying the inverse Fourier transform to Z_O and taking the real part. In practice, the complex conjugate of h_{LPF} is used to derive the correct temporal lag (scalar lag with respect to w).

We followed this procedure to filter T with five different τ_{LPF} values, i.e. 0.1, 0.2, 0.3, 0.4 and 0.5 s, corresponding to f_c values of 1.60, 0.80, 0.53, 0.40 and 0.32 Hz, respectively.

3.2.2 Noise superimposition

In this study we use Gaussian white noise, which has equally distributed spectral densities across all frequencies (Stull, 2012), to contaminate the filtered signal in ~~time space~~time-space. In order to generate time series with varying levels of SNR, we first generated white noise with unit standard deviation and multiplied the white noise with the standard deviation of the original T time series with different ratios (e.g. from 0.1 to 0.9). This represents the amount of noise compared to the amount of signal (e.g. from 10 to 90%). We then added this noise to the filtered signal. As a result, we obtained SNR values of 10.0, 5.0, 3.3, 2.5, 2.0, 1.6, 1.4, 1.2, and 1.1, which are equal to the ratio of the standard deviation of T and the standard deviation of white noise.

3.2.3 ~~Noise removal~~

~~The instrumental noise is often removed via the approach introduced by (Ibrom et al., 2007a), in which, to detect the noise, a line with unconstrained slope is fitted to the power spectra in logarithmic frequency space at a certain frequency range, which is assumed to be solely dominated by noise. Then, the fitted line is extrapolated towards lower frequencies and finally subtracted from the original spectra in logarithmic frequency space as described in Ibrom et al. (2007a) (cf. dashed lines in Fig. 4). The boundaries of the frequency domain of fitting are defined by visual inspection of the power spectra. In our study, the optimal frequency domains used for noise fitting were detected as 3, 2.6 and 2.3 to 5 Hz for the different attenuation level of 0.1, 0.2 and 0.3 s, respectively. For attenuation levels of 0.4 and 0.5 s, we used the frequency range of 2 to 5 Hz.~~

3.3 Data processing when estimating long-term budgets

Data processing steps when estimating the long-term budgets using the D_2 dataset are summarized in Fig. 3.

We applied regular EC data processing, which included de-spiking, coordinate rotation, de-trending. Next, the T time series were deteriorated with values of ~~τ~~τ_{LPF} that varied between 0.1 and 0.5 s to mimic a realistic range of scalar attenuations (mimicking the conditions, e.g., of CH_4, N_2O). Later, the low-pass induced time-lag was accounted for via maximisation

of the cross-covariance, which was followed by the calculation of the covariances. Then we applied the frequency response correction using Eq. (1), where F_{corr} was estimated using the method proposed by Fratini et al. (2012)[1]:

$$F_{corr} = \frac{\int\limits_{f=f_{min}}^{f_{max}} CO(f)df}{\int\limits_{f=f_{min}}^{f_{max}} CO(f)\sqrt{H_{emp}(f)}df}, \tag{11}$$

where CO equals the current T cospectrum when the absolute sensible heat fluxes exceeded 15 W m^{-2}. For small fluxes we

5 used a ~~site specific~~ site-specific cospectral model (see Appendix C) for CO instead of parameterisation of F_{corr} proposed by Ibrom et al. (2007a). To make sure that the analysis was not affected by low data quality, we removed the fluxes with low friction velocity ($u_* < 0.2\ ms^{-1}$), unrealistic sensible heat fluxes and non-stationary conditions (Foken and Wichura, 1996), eliminating 553 half-hourly data points out of 1440 (ca. 38%).

The time constant (τ) in H_{emp} is either estimated by PSA (i.e., $\tau_{PSA_{I07}}$ and ~~$\tau_{PSA_{A20}}$~~ $\tau_{PSA_{A21}}$) or CSA (i.e., $\tau_{CSA_{\sqrt{H},sync}}$,

10 ~~$\tau_{CSA_{\sqrt{H}}}$ and τ_{CSA_H}~~), and this yielded cumulative fluxes $F_{PSA_{I07}}$, ~~$F_{PSA_{A20}}$~~ $F_{PSA_{A21}}$, $F_{CSA_{\sqrt{H},sync}}$, ~~$F_{CSA_{\sqrt{H}}}$ and F_{CSA_H}~~, respectively. For simplicity, in the FRC only median values of time constants of PSA and CSA ensembles estimated were used for each combination of SNR and attenuation. The reference fluxes (F_{REF}) were also estimated with F_{corr} ~~calculated as the ratio of unattenuated and attenuated covariances $\overline{T'w'}$, and maximisation of cross-covariance was used to account for the time-lag induced by the low-pass filter~~ using τ_{LPF}. We present the differences between cumulative fluxes as relative differences with re-

15 spect to the reference (F_{REF}) in %. In particular, as an example, the relative bias for PSA_{I07} is calculated as $100(F_{PSA_{I07}} - F_{REF})/F_{REF}$, while for ~~$CSA_H$ as $100(F_{CSA_H} - F_{REF})/F_{REF}$~~ $CSA_{\sqrt{H},sync}$ as $100(F_{CSA_{\sqrt{H},sync}} - F_{REF})/F_{REF}$ for several attenuation and SNR conditions. The relevant results are shown in Sect. 4.3.

4 Results and Discussion

4.1 Time constant estimation with PSA

20 In order to ~~provide an illustration of~~ illustrate the important steps in the data analysis in PSA (e.g. low-pass filtering, noise superimposition and noise removal only for PSA_{I07}), here we show how the shape of power spectra changes on a logarithmic scale for a few SNR values (5, 3.3 and 2.5) and low-pass filtering conditions (Fig. 4). The low-pass filter time-constants (τ_{LPF}) of 0.1, 0.3 and 0.5 s result in f_c values beyond which the signals become attenuated of ca. 1.6, 0.5 and 0.3 Hz. As the time constant increases, f_c decreases, causing stronger attenuation. Referring to the upper panel of Fig. 4, for constant attenuation

25 ($\tau_{LPF} = 0.1$ s), if the SNR decreases, noise becomes more visible and the line fit to the noise becomes more consistent. Similarly, referring to the left panel of Fig. 4, for constant SNR (e.g. for SNR=5), from top to bottom, as attenuation increases, the slope of the fit increases and therefore, the goodness of fit increases (Table 1). As discussed in Sect. 2.2, white noise

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[1]Here we preferred using the square-root to describe the true transfer function as it is a good approximation when maximisation of the cross-covariance is used for the time-lag correction as shown by Peltola et al. (2021).
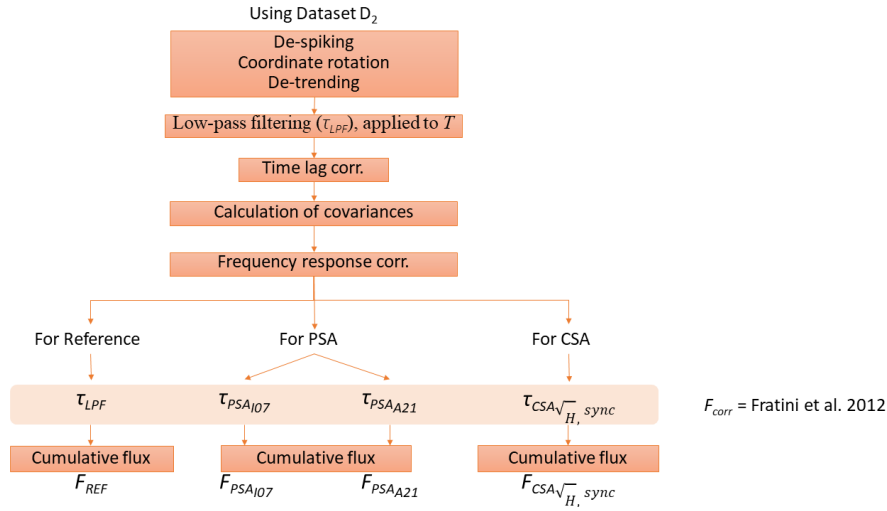
Figure 3. Flow chart of the data processing for the cumulative flux calculation using T of dataset D_2. ~~F_{REF} refers to reference cumulative flux obtained via frequency response correction applied, where the correction factor (F_{corr}) is calculated as the ratio of covariances of unattenuated and attenuated of T and w.~~ $F_{PSA_{I07}}$, ~~$F_{PSA_{A20}}$~~ $F_{PSA_{A21}}$, $F_{CSA_{\sqrt{H},sync}}$, ~~$F_{CSA_{\sqrt{H}}}$~~ and ~~F_{CSA_H}~~ F_{REF} are the cumulative fluxes corrected via following Fratini et al. (2012), where F_{corr} is calculated via implementing the time constants (for PSA; $\tau_{PSA_{I07}}$ and ~~$\tau_{PSA_{A20}}$~~ $\tau_{PSA_{A21}}$, for CSA; $\tau_{CSA_{\sqrt{H},sync}}$, ~~$\tau_{CSA_{\sqrt{H}}}$ and τ_{CSA_H}~~ for reference; τ_{LPF}) calculated in previous section.

Table 1. Results of the noise removal procedure applied in the power spectra approach following Ibrom et al. (2007a) (PSA_{I07}): the values indicate the slopes of ~~the~~ fitted line to the ~~high frequency~~ high-frequency end of the spectrum in Fig. 4, with the coefficient of determination (R^2) shown in the parenthesis, as a function of τ_{LPF} and SNR. Note that for accurate noise removal the slopes should equal one.

	SNR=5	SNR=3.3	SNR=2.5
τ_{LPF}=0.1 s	0.57 (0.93)	0.78 (0.98)	0.87 (0.99)
τ_{LPF}=0.3 s	0.91 (0.99)	0.96 (0.99)	0.97 (0.99)
τ_{LPF}=0.5 s	0.96 (0.99)	0.98 (0.99)	0.99 (0.99)

causes a slope of one, and thus any discrepancies from one results in overestimated noise removal. Based on Fig. 4 alone, it is evident that removing the noise from power spectra can be done with higher accuracy when the ~~high frequency~~ high-frequency attenuation increases and/or SNR decreases.

The results of the time constant estimation are shown in Fig. 5a, and 5b for PSA_{I07} and $PSA_{\sim A20~ A21}$, respectively. Results are presented as medians with 25th and 75th percentile ranges for the repeat simulations. It can be seen that for PSA_{I07} the interquartile range (IQR) expands as the amount of noise increases, while for $PSA_{\sim A20~ A21}$ it is small and almost constant with only a slight increase.
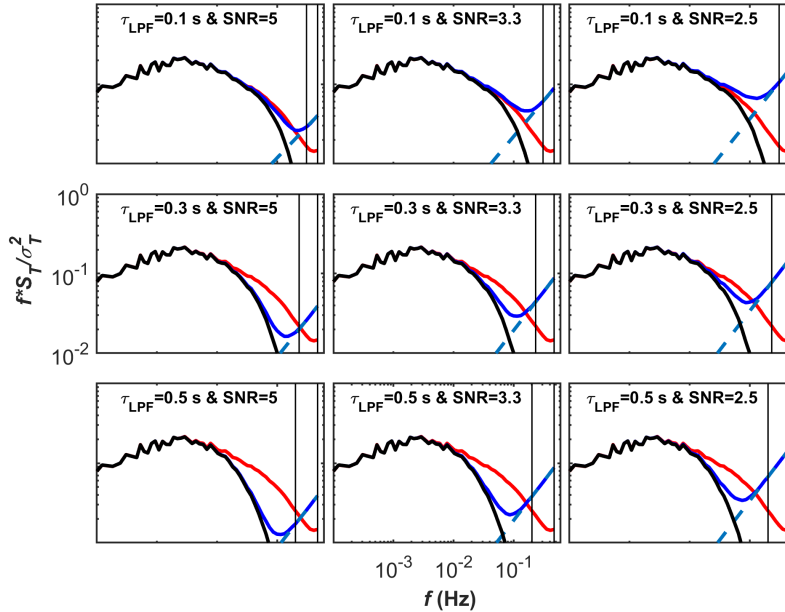
Figure 4. Effect of several low-pass filtering (τ_{LPF}= 0.1, 0.3, and 0.5 s) and SNR (5, 3.3 and 2.5) on spectra of sonic temperature (T) of 70 half-hourly data illustrated in logarithmic scale, where f is natural frequency, S_T is spectral density, σ_T^2 is ~~the~~ the variance of T. Shown are the spectra of raw measured sonic temperature (red lines), and of the artificially deteriorated (i.e. low-pass filtered and noise superimposed) sonic temperature before (dark blue) and after (black) noise removal following Ibrom et al. (2007a), through subtraction of the linear fit (blue dashed lines) to the ~~high frequency~~ high-frequency end of the deteriorated spectra. The vertical lines mark the frequency range used for fitting for ~~the~~ noise removal. The lower thresholds of the frequency range are 3, 2.3 and 2 Hz for the attenuation levels of 0.1, 0.3 and 0.5 s, respectively.

For PSA$_{I07}$, the optimal frequency domains used for noise fitting were detected as 3, 2.6 and 2.3 to 5 Hz for the different attenuation levels of 0.1, 0.2 and 0.3 s, respectively. For attenuation levels of 0.4 and 0.5 s, we used the frequency range of 2 to 5 Hz.

PSA$_{I07}$ overestimates the time constants with improving accuracy from low attenuation to high attenuation conditions regardless of the SNR values. The overestimation is likely due to the noise removal procedure, which further attenuates the high-frequency end of the spectra via removing the part of the signal together with noise (i.e. the noise is fitted with a slope < 1). In this approach, the accuracy of the noise removal procedure can be improved by visual inspection and adjustment of the fitting range to provide slopes close to one, and thus better fitting parameters. However, especially for low attenuation conditions (e.g. 0.1, 0.2 s), the frequency range is not sufficient to detect the noise statistically, meaning that the linear fitting
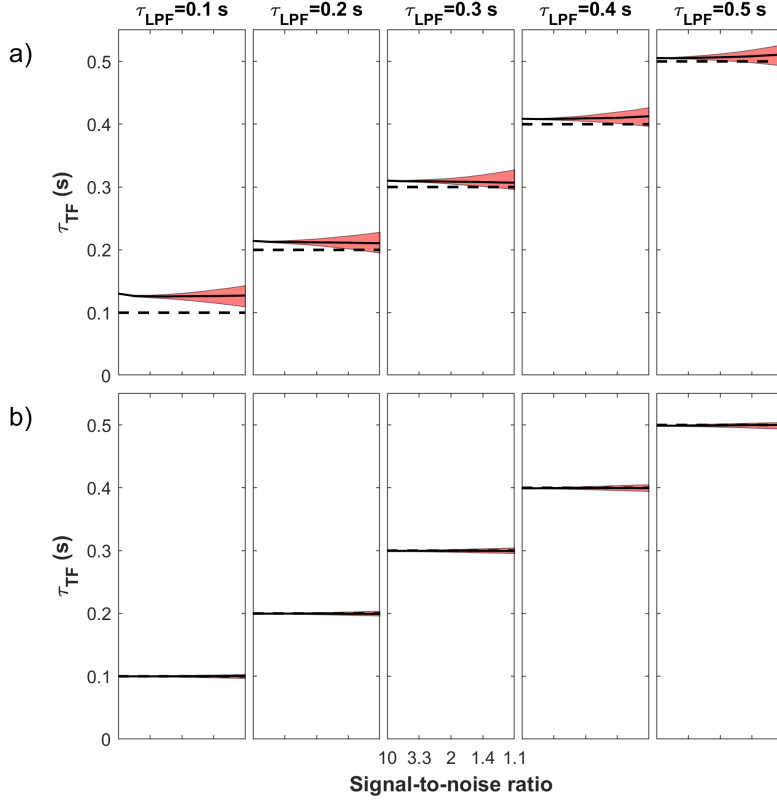
Figure 5. Time constants calculated using the power spectra approach, comparing (a) PSA_{I07}, and (b) ~~PSA_{A20}~~ PSA_{A21}, in several low-pass filtering ~~condition~~ conditions (τ_{LPF}=0.1 - 0.5 s) as a function of signal-to-noise ratio (SNR) over the range 10-1.1, which correspond to the amount of noise (e.g. 10-90 %). The solid ~~red~~ black curve represents the median, while the shaded area ~~represent~~ represents inter-quartile ranges. The dashed line corresponds to the expected value (τ_{LPF}), which was used for the artificial low-pass filtering.

method is not ideal for differentiating in the spectral power the noise contribution from the real variations due to turbulence. In addition to the shortcoming of the linear fitting, the visual inspection of both detecting the frequency ranges for noise removal and the H fitting constitutes another uncertainty source due to its subjectivity. It requires expertise on the topic, and is hard to ~~automise~~ automate when using software used for flux calculations (e.g., EddyPro). Moreover, in some cases, the optimal visual inspection might not be sufficient as the low attenuation results in our study suggest. In our case we could not further improve the accuracy even though the exact attenuation and SNR level were known, which is not the case with ~~real world~~ real-world data.

14

PSA~~A20~~ A21 successfully estimates the time constants regardless of the attenuation and SNR level. This is due to using the whole frequency range for fitting without separating the superimposed attenuated signal and noise. The most important advantage of the PSA~~A20~~ A21 is that it does not require visual inspection.

We assumed that the noise contaminating the signal is white noise, which may not always be the case in ~~real world~~ real-world data. Thus, the accuracy of the PSA~~A20~~ A21 depends on knowledge of the nature of the noise, which should be determined in advance, and implemented in Eq. (6) by adjusting the last term that characterises the noise. This said, in many EC studies, the type of ~~the~~ noise is attributed to white noise (e.g., Launiainen et al., 2005; Peltola et al., 2014; Rannik et al., 2015; Gerdel et al., 2017; Wintjen et al., 2020)[2], but brown noise in other studies (Wintjen et al., 2020). A simple approach to characterise the type of noise is either by examining the ~~high frequency~~ high-frequency end of spectra, which is similar to our study, or through the Allan variance, e.g. Werle et al. (1993). Alternatively, we conducted a brief investigation into the type of noise by comparing the power spectra of measurements with very low SNR and those of white and blue noise (see Appendix B). It should be noted, however, that there are situations when noise is complex and difficult to predict $a\ priori$.

4.2 Time constant estimation with CSA

Figure 6 illustrates the time-lag corrected cospectra of three low-pass filtered cases (i.e. τ=0.1, 0.3 and 0.5 s) with most noisy conditions (i.e. lowest SNR of 1.1) in addition to ~~raw~~ the unattenuated and noise free cospectra (i.e. original)~~cospectra~~. It shows that ~~noise contamination does not affect the shape~~ the white noise contamination did not cause linear increase in the high-frequency end of the cospectra~~.~~, enabling the time-constant calculation without additional procedure related to noise removal.

~~CSA_H systematically underestimates the time constant, while, in contrast, $CSA_{\sqrt{H}}$ overestimates, the accuracy of which is further significantly improved when the time-lag correction is applied to the time-series, in~~ $CSA_{\sqrt{H},sync}$ ~~(Fig. 7). The reason for this improvement is discussed in detail in the companion paper (Peltola et al., 2021).~~

~~The accuracy of CSA_H decreases with increasing attenuation. The spectral energy of two variables comprises a real part, i.e. the cospectrum (Co), and an imaginary part, i.e. the quadrature spectrum (Q) (Stull, 2012). The latter is often neglected by assuming the attenuation does not change the phase between the two variables (Horst, 2000). In order to test this assumption we further investigated the effect of Q on the time constant estimation (see Appendix ??). In short, application to a couple of case studies shows that CSA_H can under- or over-estimate the time constant due to neglected Q, depending on the sign of Q~~successfully estimates the time constants (Fig. 7).

~~The bias is larger for higher attenuation since the central term ($2\tau_c Q/Co$ term in Eq. (??)) increases linearly with τ. We showed that (Table ?? and ??), the bias can be eliminated when the ratio of Q over Co, both of which are obtained from unattenuated records, is utilized in the H (Eq. (??)). However, the use of the ratio is not applicable in real-world data of closed-path systems where Q and Co are distorted in case of attenuated time series, hence this uncertainty can be noted as a shortcoming of the CSA.~~

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[2]This also includes Ibrom et al. (2007a), who falsely interpreted the (white) noise as blue. This conclusion, however, was misguided by neglecting the fact that the power spectra were multiplied with f.

~~In the case of $CSA_{\sqrt{H},sync}$, the~~ The variation around the expected values can be attributed to the shortcomings in the maximisation of the ~~crosscovariance~~ cross-covariance used for the time-lag correction, the precision of which is limited to the sampling interval (e.g. 0.1 s). Hence, the importance of the precision of time-lag detection can be noted as a shortcoming of CSA.

5 ~~In practice, the time-lag correction when utilized with the square-root of H can eliminate the above mentioned phase effect, the theoretical premise of which is further investigated in Peltola et al. (2021)~~The use of square-root might be the another reason for the variation as it is an approximation, not an exact representation of the phase shift effect (Peltola et al., 2021).

Lastly, as expected, the level of noise does not affect the accuracy of ~~any of the CSA methods~~ the CSA method at any SNR level as the random noise does not correlate with w, which is a pivotal advantage of the CSA in general. It does, however, add

10 random noise to the result that is greater than in the improved ~~PSA_{A20}~~ PSA_{A21} approach.
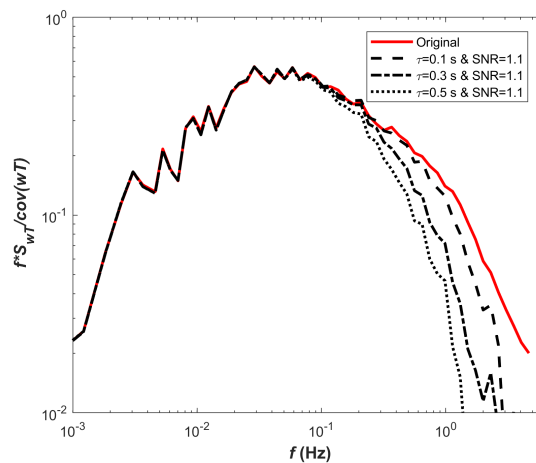
Figure 6. Normalised ensemble cospectra for the original and various attenuated time series (i.e. τ=0.1, 0.3 and 0.5 s). White noise was added at a signal to noise ratio (SNR) of 1.1. The red line represents the ~~non-attenuated~~ unattenuated and ~~noise free~~ noise-free cospectrum, while the dashed, dotted-dashed and dotted lines show the ~~noise contaminated~~ noise-contaminated and low-pass filtered cospectra for the three attenuation levels.

## 4.3 Effect of time constant variations on cumulative fluxes

Figures 8 and 9 ~~illustrates~~ illustrate how variation in the estimation method of the time constant affected the cumulative fluxes in comparison to reference fluxes (see Sect.3.3) calculated using dataset D_2. Fig. 10 shows the correction factors (F_{corr}) for the case with $\tau = 0.3s$ and SNR of two. The values vary between 1 and 1.3, indicating the frequency response correction as

15 high as 30%.
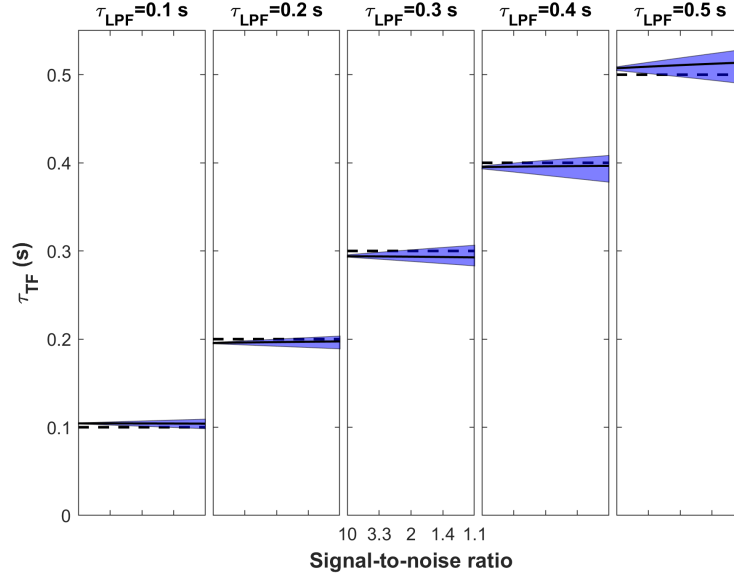
Figure 7. Time constants calculated using the cospectral ~~approaches~~approach, i.e. ~~CSA$_H$ (red), CSA$_{\sqrt{H}}$ (green), and~~ CSA$_{\sqrt{H},sync}$ ~~(blue)~~, for several low-pass filtering condition (τ_{LPF}=0.1 - 0.5 s) as a function of signal-to-noise ratio (SNR) over the range 10-1.1, which correspond to the amount of noise (e.g. 10-90 %). The solid ~~curves represent~~ black line represents the medians, while the shaded areas represent ~~iner-quartile~~ inter-quartile ranges. The dashed line corresponds to the expected value (τ_{LPF}), which was used for the artificial low-pass filtering.

PSA_{I07} based fluxes showed a bias ~~of $\pm2\%$ with negligible response to the SNR level, whereas PSA_{A20} showed a somewhat similar behaviour with slightly better accuracy~~ varying between 0.1 and 1.5%, whereas PSA_{A21} showed almost no bias, reflecting the more accurate time constant estimation previously shown. Fluxes based on $CSA_{\sqrt{H},sync}$ were ~~very~~ close to the expected value with ~~similar biases as the PSA methods. $CSA_{\sqrt{H}}$ overestimates the fluxes up to 3%, while the~~

5 ~~CSA_H method underestimates fluxes by up to 4%~~the bias of $\pm0.4\%$ with negligible response to the SNR level. These findings are ~~partly~~ consistent with the observed biases on time constant estimation, meaning that where the time constant and the low-pass filtering were overestimated (e.g. with the PSA_{I07} especially for τ=0.1 s and ~~$CSA_{\sqrt{H}}$~~$CSA_{\sqrt{H},sync}$ for τ=0.1 and 0.5 s), the spectral correction factor and thus the fluxes were overestimated, too. In summary, the findings indicate that using ~~PSA methods (particularly PSA_{A20}) for~~ the PSA_{A21} for the time constant estimation provides ~~reasonably~~ quite accurate FRC. On

10 the other hand, for CSA ~~methods~~method, $CSA_{\sqrt{H},sync}$ ~~better~~ reasonably approximates the time constants, hence FRC. These results are in agreement with the analysis presented in Peltola et al. (2021), showing that $CSA_{\sqrt{H},sync}$ ~~well~~ approximates the effect of phase shift on the estimation of the time constant and flux correction factor. See more details in Peltola et al. (2021).
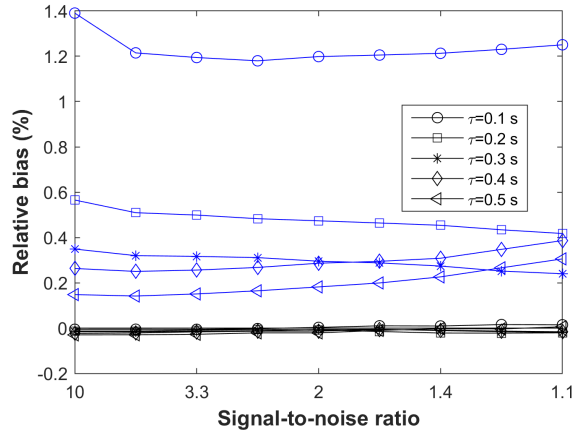
Figure 8. Relative biases of the cumulative fluxes derived with different PSA methods, i.e. PSA_{I07} (blue) and PSA_{A21} (black), compared with the reference flux as a function of SNR for different attenuation time scales (0.1-0.5 s), calculated as, e.g., $100(F_{PSA_{I07}} - F_{REF})/F_{REF}$.
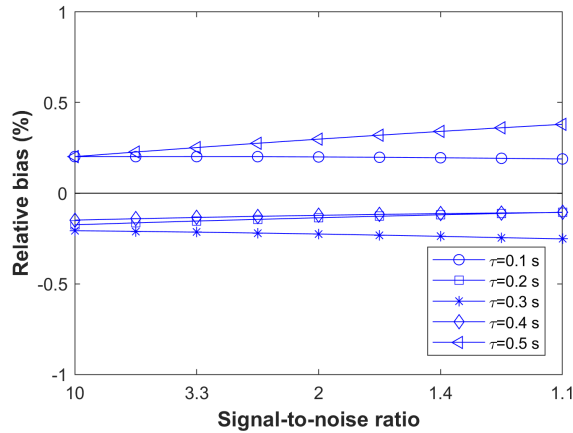
Figure 9. Relative biases of the cumulative fluxes derived with the $CSA_{\sqrt{H}, sync}$ compared with the reference flux as a function of SNR for different attenuation time scales (0.1-0.5 s), calculated as, e.g., $100(F_{CSA_{\sqrt{H}, sync}} - F_{REF})/F_{REF}$.

4.4 Review of typical signal-to-noise ratios and response times encountered during closed-path flux measurements

The range of attenuation and SNR conditions reported in the literature is rather wide and varies depending on ecosystem type, the scalar of interest, data processing, a configuration of instruments, and setup of EC system. Ibrom et al. (2007a) examined fluxes of water vapour and CO_2 measured over a temperate forest, both of which were disturbed by noise in the ~~high frequency~~
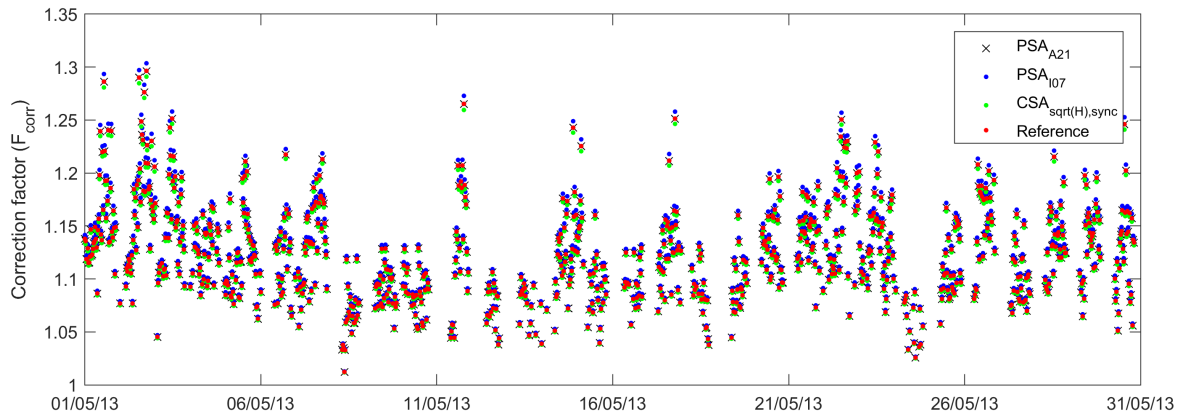
Figure 10. Correction factors (F_{corr}) of half-hourly fluxes calculated with different approaches, i.e. PSA_{A21} (black cross), PSA_{I07} (blue point), $CSA_{\sqrt{H},sync}$ (green point) and the reference (red point) for the case with $\tau = 0.3$s and SNR of two.

high-frequency range of power spectra (see their Fig. 2). They identified an f_c of CO_2 as low as 0.325 Hz (i.e. ca. $\tau = 0.5$ s), indicating strong attenuation, while H_2O showed even stronger attenuation which increased with relative humidity to up to 0.010 Hz (i.e. ca. $\tau = 16$ s) due to the sorption/ desorption effects on the sampling line internal walls. Langford et al. (2015) reviewed SNR values of various gases published in many studies. In their comprehensive analysis (their Fig. 4), the

5   majority of the half-hourly datasets of isoprene and acetone, measured with quadrupole-based Proton Transfer Reaction-Mass Spectrometer (PTR-MS, Ionicon Analytik GmbH, Austria) above ~~broad leaf~~ broad-leaf woodland, roughly showed SNRs of 0.5, 0.3, respectively, and benzene measured (with the same instrument) in the urban environment showed a SNR of 0.3. Additionally, N_2O measured with an older tunable diode laser (Aerodyne Research Inc., Billerica, MA, USA) over managed grassland showed a SNR of one. Rannik et al. (2016) examined the random uncertainties in fluxes measured over forest,

10   lake and peatland ecosystems in the Boreal region. According to their unpublished calculations, the SNRs of CO_2 and H_2O measured with an infrared gas analyzer (~~Li-6262~~LI-6262, LICOR, Lincoln, NE, USA) were 2.6 and 10.3 for the forest site respectively, while the SNRs of CO_2, H_2O and CH_4 measured with two closed-path analysers (i.e. LI-7000, LI-COR~~Inc.~~, Lincoln, NE, USA, for CO_2, H_2O and FMA, Los Gatos ~~research,~~Research, Los Gatos, CA, USA for CH_4) were 2.7, 24.3 and 5.4, respectively. At the same forest site, Kohonen et al. (2019) investigated fluxes of carbonyl sulfide (COS) with a newer

15   generation Aerodyne quantum cascade laser spectrometer (QCLS) (Aerodyne Research Inc., Billerica, MS, USA) that also measures mole fractions of CO_2 and H_2O. They reported high attenuation for their measurement setup (time constant of 0.68 s for their EC system), and high noise disturbance in their power spectra (their Fig. 7) with ~~a~~ an SNR of about one. During the measurement period, COS showed small fluxes near the detection limit, causing uncertainty in the calculation of H. Thus, they calculated the time constant using the cospectra of CO_2, assuming that both fluxes are affected by the same attenuation.

Table 2. Time constants obtained via different approaches (PSA_{I07}, PSA_{A21} and $CSA_{\sqrt{H},sync}$) for CO_2 data from Siikaneva site and relevant statistics.

Method	PSA_{I07}	PSA_{A21}	$CSA_{\sqrt{H},sync}$
τ (s)	0.095	0.075	0.173
Coefficient of determination (R^2) of time constant fitting	0.989	0.993	0.958
Coefficient of determination (R^2) of noise fitting	0.99	-	-
slope of noise fitting	0.82	-	-
frequency range of noise fitting (Hz)	3.5-5	-	-
frequency range of time constant fitting (Hz)	0.01-2	0.01-5	0.01-2
Normalization factor (F_n)	1.017	1.022	-

In addition, N_2O fluxes measured over urban areas (Järvi et al., 2014), and CO_2 fluxes over lake ecosystems (Mammarella et al., 2015) can also be examples of low SNR conditions.

Given the wide range of SNR and attenuation conditions summarised above, we analysed only a limited range of SNR and attenuation. Also, the impact of ~~a~~ the system response time depends on the position of the spectral peak frequency which changes not only with wind speed but also measurement height and surface roughness. Nevertheless, the analysis of the different approaches showed a systematic behaviour with respect to SNR level and attenuation conditions. This provides the opportunity to extend the results of this study beyond the examined values and guides the selection of the right method to find the relevant H.

~~Finally, the~~ The key constraint of the study was that we artificially ~~simulate~~ simulated the various attenuation and SNR conditions. Thus, demonstrating the performance of the methods with real-world data is of great importance. Accordingly, here we provide an example via processing CO_2 data D_3 with the SNR of 2.3. The power spectra and cospectra of CO_2 and T are shown in Fig. 11. The estimated time constants were 0.095, ~~which should be verified with *in situ* measurements.~~ 0.075 and 0.173 s for PSA_{I07}, PSA_{A21} and $CSA_{\sqrt{H},sync}$, respectively. The details and statistics of fitting procedures are summarized in Table 2. The PSA_{A21} fit successfully approximates the noisy CO_2 power spectra ($R^2 = 0.993$), enabling us to assume that the noise is white. However, the slope of the linear noise fit of PSA_{I07} differs from one (0.82). We believe that this is due to the low attenuation, so that the noise cannot become visible similarly as in the case of the artificial data set with low attenuation shown in Fig. 4, resulting in overestimation as it erroneously removes part of the signal together with noise. The differences in time constants obtained via PSA and CSA approaches might be attributed to sensor separation, uncertainties in time-lag correction and the use of square-root in CSA.
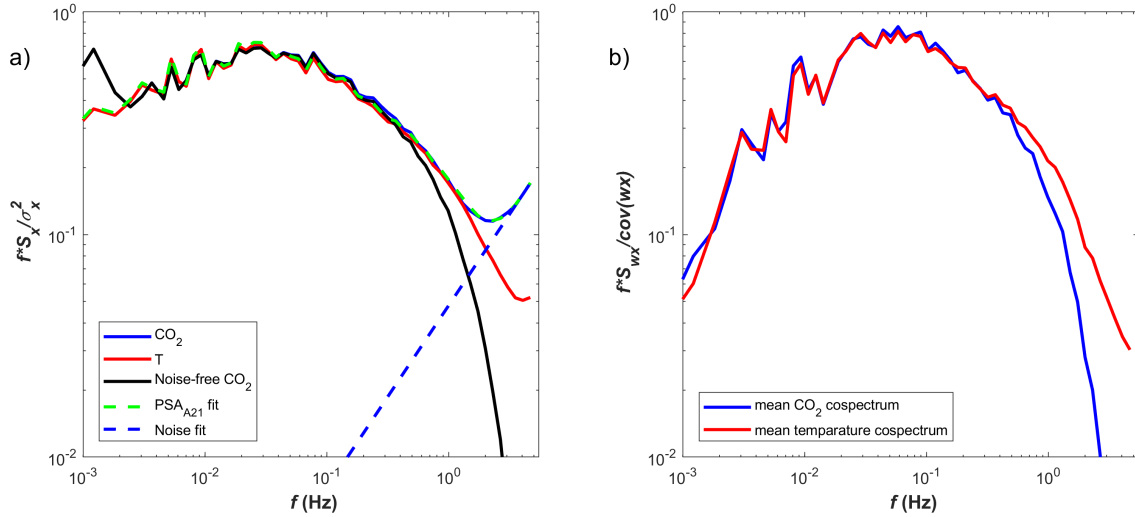
Figure 11. (a) Power spectra of: (1) sonic temperature (red); (2) CO_2 from Siikaneva site measured simultaneously with D_1 (black); (3) noise removed CO_2 (dashed blue); shaded areas show the frequency range used for noise fitting for PSA_{I07}, and time constant fitting for PSA_{I07} and PSA_{A21}. (b) Cospectra of CO_2 (black) and T (red) with vertical wind speed (w).

5 Conclusions

Here we investigated the limitations of two commonly used approaches to empirically estimated the eddy-covariance (EC) transfer function needed for the frequency response correction of measured fluxes by analysing a temperature flux time-series which was synthetically degenerated mimicking slow-response setups and noisy sensors. The first approach (PSA) is based

5   on the ratio of measured power spectra, while the second (CSA) is based on the ratio of measured cospectra. For PSA, we examined two alternative approaches of accounting for the white noise contribution to the power spectra: i.e. PSA_{I07} and $PSA_{\overline{A20}\,A21}$. The latter is newly introduced here and does not require noise removal prior to ~~the~~ the fitting of the response function. For CSA, we examined ~~three approaches: (1) utilising the~~ one approach utilising the square-root of the transfer function (H) ~~suggested by Horst (1997), i.e. CSA_H, (2) using $\sqrt{H}$, i.e. $CSA_{\sqrt{H}}$, and (3) implementing $\sqrt{H}$~~ with shifted w time series

10   via maximisation of the ~~crosscovariance~~cross-covariance, i.e. $CSA_{\sqrt{H},sync}$. We generated an ~~artificially~~ artificial dataset using T with differing degrees of low-pass filtering (simulated damping) and additional random noise. The advantage of using artificial datasets is that the real values of frequency attenuation, SNR and physical time-lag are all known, allowing the precise comparison of the estimations and expected values. PSA_{I07} overestimated the noise contribution and consequently the signal loss and time constant for low attenuation conditions, but better performance was found as attenuation increases. The new

15   $PSA_{\overline{A20}\,A21}$ approach successfully estimated the time constants regardless of the attenuation and SNR level, identifying the noise and signal comprehensively, providing no bias and the lowest random uncertainty in the case of noisy data. However the

approach assumed that the signal is contaminated by white noise, but this is not necessarily always the case. Hence, prior to the calculation of the time constant with this method, the nature of noise must be known. ~~By contrast, systematic differences were found between the results from three approaches based on cospectra, where the choice of the shape of H differs in the literature. CSA_H underestimated the time constants with increasing bias as attenuation increases, the accuracy of which was shown to be affected by neglecting the filtering effects on the quadrature spectrum, which cannot be avoided. $CSA_{\sqrt{H}}$ overestimated the time constants, the bias of which was mostly eliminated when time-lag correction was applied in $CSA_{\sqrt{H},sync}$. See the companion paper (Peltola et al., 2021) for a thorough discussion of the interdependence between~~ showed a slight deviation from expected values. That can be attributed to lack of precision in time-lag estimation ~~via cross-covariance maximisation and frequency response corrections.~~ and the use of square-root.

We then examined the effect of the different approaches to estimate the time constants on the cumulative fluxes: fluxes corrected using the PSA_{I07} based time constants showed the bias ~~of $\pm 2\%$~~ varying between 0.1 and 1.5% in comparison with reference fluxes (see Sect. 3.3), where ~~PSA_{A20} showed similar behaviour, yet slightly better accuracy~~ PSA_{A21} showed almost no bias. By contrast, fluxes corrected using ~~CSA_H based time constants were underestimated by up to 4%, while $CSA_{\sqrt{H}}$ overestimated the fluxes by up to %3, the~~ $CSA_{\sqrt{H},sync}$ showed the bias of ~~which was further reduced with $CSA_{\sqrt{H},sync}$, varying within $\pm 2\%$.~~ 0.4%. This analysis, however, does not account the shortcomings of the method, i.e. Fratini et al. (2012), thus should be read as the sole effect of time constant estimation on the final fluxes. The comparison of commonly used methods are comprehensively done in the companion paper.

The SNR did not affect the accuracy of either PSA or CSA approaches, alleviating concerns on EC flux measurements with low SNR ~~level~~levels.

In summary, for the empirical estimation of parameters of H of closed-path EC systems, our findings showed that $PSA_{\cancel{A20}A21}$ is the most accurate, precise and robust method when power spectra are used. This finding was independent of SNR and degree of attenuation. On the other hand, using the square root of H in $CSA_{\sqrt{H},sync}$, which is a good approximation of the attenuation of cospectra in the presence of phase shifts (Peltola et al., 2021), provided the reasonably correct estimation of τ and F_{corr} when cospectra are ~~used, together~~ computed after with time-lag quantification by cross-covariance maximisation.

Finally, given the constraints of this study, we encourage additional studies based on the real attenuation and SNR conditions, investigating also other ~~type~~types of noise contamination to provide a step forward in efforts to standardise the EC method, which is of great importance to avoid systematic biases of fluxes and improve comparability between different datasets.

Code and data availability. Data to reproduce Figures 4, 5 6, 7, 8, 9, and code to demonstrate PSA_{A21} are available in Aslan (2020).

Appendix A: Derivation of the PSA$_{\cancel{A20}A21}$

In this section, we derive the new approach for the PSA (i.e. PSA$_{\cancel{A20}A21}$) in detail. We assume that the measured χ contains two independent and additive components: the attenuated turbulent signal and the noise. We further assume that scalar similarity

holds (i.e. power spectra of all scalars follow a similar shape). After these assumptions the power spectrum (S_χ) of χ can be written as:

$$S_\chi(f) = \frac{\sigma_\chi^2}{\sigma_T^2} H S_T(f) + S_{\chi,n}(f), \tag{A1}$$

where σ_χ^2 and σ_T^2 are the variances of χ and T related to turbulent signal (no attenuation or noise), $S_T(f)$ is the power spectrum of T, H describes the attenuation of χ due to imperfect instrumentation and $S_{\chi,n}$ is the noise in the χ measurements. Note that here the noise in the T measurements was neglected as being small except in very low turbulence conditions (when eddy-covariance measurements become problematic anyway and fluxes are removed by the u_* filter). Assuming that the instrument measuring χ can be approximated by a first-order linear sensor and reordering terms, this yields:

$$\frac{S_\chi(f)}{\sigma_\chi^2} = \frac{S_T(f)}{\sigma_T^2} F_n \frac{1}{1 + (2\pi f \tau)^2} + \frac{S_{\chi,n}(f)}{\sigma_\chi^2}, \tag{A2}$$

where the proportionality constant F_n was introduced due to the effect that noise adds to σ_χ^2 and thus biases the normalisation (see Ibrom et al., 2007a). The spectral density is best shown in log-log space as wide range of frequencies and spectral densities are well displayed (Stull, 2012), with natural frequency (f) on the x-axis, and spectral density multiplied with f on the y-axis. After multiplication by f, Eq. (A2) becomes:

$$f \frac{S_\chi(f)}{\sigma_\chi^2} = f \frac{S_T(f)}{\sigma_T^2} F_n \frac{1}{1 + (2\pi f \tau)^2} + f \frac{S_{\chi,n}(f)}{\sigma_\chi^2}, \tag{A3}$$

As described in Sect. ~~??~~ 2.2, $f \frac{S_{\chi,n}(f)}{\sigma_\chi^2}$ can be approximated by a model that is linear in frequency in logarithmic space as $f \frac{S_{\chi,n}(f)}{\sigma_\chi^2} = a\log(f) + \log(b)$. In the case of white noise, where $a=1$, this results in a simplified linear model as $f \frac{S_{\chi,n}(f)}{\sigma_\chi^2} = \log(f) + \log(b)$, and in non-logarithmic space as $e^{\log(f) + \log(b)}$, which is fb. Substitution into Eq. (A3) yields:

$$f \frac{S_\chi(f)}{\sigma_\chi^2} = f \frac{S_T(f)}{\sigma_T^2} F_n \frac{1}{1 + (2\pi f \tau)^2} + fb. \tag{A4}$$

It is worth mentioning that this method can be used to retrieve the variance of noise as well, since b equals the ~~ensemble averaged~~ ensemble-averaged noise power spectra ($S_{\chi,n}$) divided with σ_χ^2. However, we do not further examine it as it is not the main interest of this study.

Appendix B: ~~Assessment of the effect of quadrature spectrum on time constant estimation in the CSA~~

~~In Sect. 4.2, we briefly presented the effect of Q on time constant estimation in the CSA_H. In this section, the details are provided.~~

~~The transfer function used in this study (i.e. Eq. (3)) is the simplified version of the transfer function of Horst (2000) (their Eq. (5)) which neglects Q and assumes that the sonic anemometer has a perfect frequency response. The theoretical transfer function including Q can be written as:~~

$$H(f) = \frac{1 + 2\pi f \tau Q / Co}{1 + (2\pi f \tau)^2},$$

where Q is quadrature spectrum and Co is the cospectrum of two variables and τ is the system time constant.

For this particular analysis we used two T datasets, the first of which is D_1 from Siikaneva and second of which is from Hyytiälä (see Peltola et al., 2021). We filtered the data by following the same procedure described in Sect. 3.2.1 with various τ_{LPF} ranging from 0.05 to 1 s. Then, we used different transfer functions (i.e. Eq. (3) and Eq. (**??**)) to obtain time constants to examine the effect of Q.

Table **??** summarises the comparison of the time constants obtained with different transfer functions for CSA_H for Siikaneva. Equation (3) underestimates τ_{CSA_H}, while Eq. (**??**) virtually eliminates this bias. A similar behaviour can be seen in Table **??** for the Hyytiälä dataset.

The results of the two case studies combined indicate that Q biases the time constant estimations, causing either under- or overestimation, depending on the sign of the term $2\pi f \tau Q/Co$ ratio in Eq. (**??**). However, for gas measurements, an accurate calculation of the Q/Co ratio is not feasible due to the physical time lag and high frequency attenuation induced by the sampling system.

Figures **??** and **??** show the ratio of normalized spectral densities of Q and Co of the unattenuated dataset of Siikaneva and Hyytiälä, respectively. Both ratios significantly deviate from zero across the frequency domain.

Time constant estimations in order to assess the effect of quadrature spectrum in the cospectral approach (CSA_H) based on data from the Siikaneva site (dataset D_1). τ_{LPF} indicates the time constant of the first-order filter applied to the T dataset; τ_{CSA_H} represents the time constants obtained via CSA_H with two different transfer functions (i.e. Eq. (3) and Eq. (**??**)), both of which are given with relative biases in the time constant values, respectively. τ_{LPF} (s) τ_{CSA_H} with Eq. (3) (s) Relative bias of Eq. (3) (%) τ_{CSA_H} with Eq. (**??**) (s) Relative bias of Eq. (**??**) (%) 0.05 0.051 1.6 0.050 -1.0 0.1 0.093 -6.8 0.099 -0.9 0.2 0.175 -12.4 0.198 -0.9 0.3 0.260 -13.5 0.298 -0.8 0.5 0.435 -12.9 0.496 -0.7 0.7 0.622 -11.2 0.695 -0.7 1 0.916 -8.4 0.994 -0.6

Time constant estimations in order to assess the effect of quadrature spectrum in the cospectral approach (CSA_H) based on data data from the Hyytiälä site (see Peltola et al., 2021). τ_{LPF} indicates the time constant of the first-order filter applied to the T dataset; τ_{CSA_H} represents the time constants obtained via CSA_H with two different transfer functions (i.e. Eq. (3) and Eq. (**??**)), both of which are given with relative biases in the time constant values, respectively. τ_{LPF} (s) τ_{CSA_H} with Eq. (3) (s) Relative bias of Eq. (3) (%) τ_{CSA_H} with Eq. (**??**) (s) Relative bias of Eq. (**??**) (%) 0.05 0.056 12.6 0.050 -0.6 0.1 0.104 4.3 0.099 -0.7 0.2 0.190 -5.1 0.199 -0.7 0.3 0.275 -8.4 0.298 -0.7 0.5 0.449 -10.3 0.496 -0.8 0.7 0.622 -11.2 0.695 -0.8 1 0.874 -12.9 0.992 -0.8

The ratio of normalised spectral densities of Q and Co of the unattenuated dataset of sonic temperature and vertical wind speed at Siikaneva, representing the ensemble average of dataset D_1 measured over the period from May to September 2013 during daytime with an average sensible heat flux of 114.3 W m^{-2}, friction velocity of 0.3 m s^{-1}, and wind speed of 2.1 m s^{-1}.

The ratio of normalised spectral densities of Q and Co of the unattenuated dataset of sonic temperature and vertical wind speed at Hyytiälä dataset measured over the period from May to August 2019 during daytime when the sensible heat flux was between 90 and 260 W m^{-2}, and the wind speed was between 2.1 and 3.7 m s^{-1}.

Appendix B: Identification of instrumental noise

Here we perform a short analysis to characterise the type of noise in an example ~~high frequency~~ high-frequency CH_4 time series by comparing the spectra of a turbulent scalar with those of artificially generated white and blue noise.

Methane fluxes from an upland forest site can be considered to be greatly affected by instrumental noise because fluxes are
5   small and near the detection limit. Therefore, we used a forest methane mixing ratio dataset to identify the type of noise by comparing its spectra with the spectra of white and blue noise which was artificially generated and with the same standard deviation of the methane dataset.

The data were collected at the SMEAR II station (Station for Measuring Forest ~~Ecosystem- Atmosphere~~ Ecosystem-Atmosphere Relationships), Hyytiälä, Southern Finland ($61^o51'$ N, $24^o17'$ E; 181m a.s.l.) which is Class 1 ICOS ecosystem station. The
10   station is surrounded by extended areas of coniferous forests and the EC tower is located in a 55-year-old (in 2017) Scots pine ($Pinussylvestris$ L.) forest with a dominant tree height of 19 m. The measurements were performed with 10 Hz sampling frequency at a height of 23 m, i.e. approximately 4 m above the forest canopy. A fast response laser absorption spectrometer (G2311-f, Picarro, Santa Clara, CA, USA) was used to measure the CH_4 mixing ratio.

Power spectra of methane were calculated using measurements from the 10 July at 12:00-14:30. The ~~high frequency~~
15   high-frequency range of the normalised frequency weighted CH_4 power spectrum follows the f^{+1} power law scaling, which is consistent with white noise and inconsistent with, e.g., blue noise (Fig. B1).
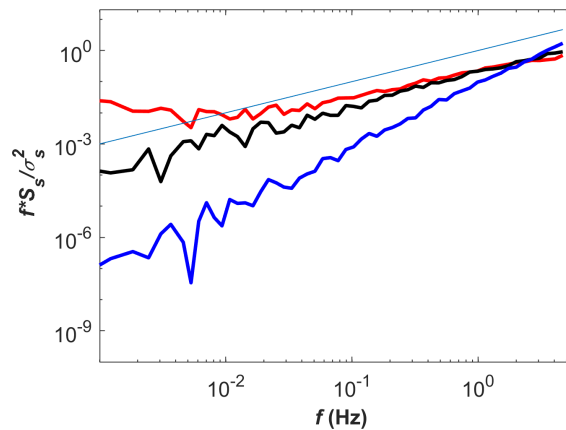
Figure B1. Normalized spectra of methane concentration (red), white noise (black), and blue noise (blue) (fS_s/σ_s^2), all of which have the same standard deviation. ~~Solid~~ The solid straight line is f^{+1} line.

Appendix C: The ~~site specific~~ site-specific cospectral model used in flux calculations

The cospectral model used in flux calculations for small fluxes (i.e. absolute value of sensible heat flux smaller than 15 W m^{-2}) was calculated following Horst (1997)):

$$\frac{fCo(f)}{\overline{w'\chi'}} = \frac{2}{\pi}\frac{n/nm}{1+(n/nm)^2},\tag{C1}$$

where n is the normalised frequency, nm is the cospectral peak frequency, which is derived from in situ measurements in Siikaneva as:

$$nm = \begin{cases} 0.09, & \frac{z-d}{L} \leq 0, \\ 0.09(1+4.5(\frac{z-d}{L})^{0.78}), & \frac{z-d}{L} > 0, \end{cases}\tag{C2}$$

where z is the measurement height, d is the displacement height, and L is the ~~Obkuhov~~ Obukhov length, a measure of atmospheric stability.

References

Aslan, T.: Data and model code for "The high frequency response correction of eddy covariance fluxes. Part 1: an experimental approach for analysing noisy measurements of small fluxes", https://doi.org/10.5281/zenodo.4354432, https://doi.org/10.5281/zenodo.4354432, 2020.

Aubinet, M., Grelle, A., Ibrom, A., Rannik, Ü., Moncrieff, J., Foken, T., Kowalski, A. S., Martin, P. H., Berbigier, P., Bernhofer, C., et al.: Estimates of the annual net carbon and water exchange of forests: the EUROFLUX methodology, in: Advances in ecological research, vol. 30, pp. 113–175, Elsevier, 1999.

Aubinet, M., Vesala, T., and Papale, D.: Eddy covariance: a practical guide to measurement and data analysis, Springer Science & Business Media, 2012.

Biosciences, L.-C.: EddyPro software instruction manual, LI-COR Inc., Lincoln, Nebraska, USA, 2020.

Eugster, W. and Senn, W.: A cospectral correction model for measurement of turbulent NO 2 flux, Boundary-Layer Meteorology, 74, 321–340, 1995.

Foken, T. and Napo, C. J.: Micrometeorology, vol. 2, Springer, 2008.

Foken, T. and Wichura, B.: Tools for quality assessment of surface-based flux measurements, Agricultural and forest meteorology, 78, 83–105, 1996.

Fratini, G., Ibrom, A., Arriga, N., Burba, G., and Papale, D.: Relative humidity effects on water vapour fluxes measured with closed-path eddy-covariance systems with short sampling lines, Agricultural and forest meteorology, 165, 53–63, 2012.

Gerdel, K., Spielmann, F. M., Hammerle, A., and Wohlfahrt, G.: Eddy covariance carbonyl sulphide flux measurements with a quantum cascade laser absorption spectrometer, Atmospheric measurement techniques, 10, 3525, 2017.

Goulden, M. L., Daube, B. C., Fan, S.-M., Sutton, D. J., Bazzaz, A., Munger, J. W., and Wofsy, S. C.: Physiological responses of a black spruce forest to weather, Journal of Geophysical Research: Atmospheres, 102, 28 987–28 996, 1997.

Horst, T.: A simple formula for attenuation of eddy fluxes measured with first-order-response scalar sensors, Boundary-Layer Meteorology, 82, 219–233, 1997.

Horst, T.: On frequency response corrections for eddy covariance flux measurements, Boundary-Layer Meteorology, 94, 517–520, 2000.

Horst, T. and Lenschow, D.: Attenuation of scalar fluxes measured with spatially-displaced sensors, Boundary-layer meteorology, 130, 275–300, 2009.

Humphreys, E. R., Andrew Black, T., Morgenstern, K., Li, Z., and Nesic, Z.: Net ecosystem production of a Douglas-fir stand for 3 years following clearcut harvesting, Global Change Biology, 11, 450–464, 2005.

Hunt, J. E., Laubach, J., Barthel, M., Fraser, A., and Phillips, R. L.: Carbon budgets for an irrigated intensively grazed dairy pasture and an unirrigated winter-grazed pasture, Biogeosciences, 13, 2927–2944, 2016.

Ibrom, A., Dellwik, E., Flyvbjerg, H., Jensen, N. O., and Pilegaard, K.: Strong low-pass filtering effects on water vapour flux measurements with closed-path eddy correlation systems, Agricultural and Forest Meteorology, 147, 140–156, 2007a.

Ibrom, A., Dellwik, E., Larsen, S. E., and Pilegaard, K.: On the use of the Webb–Pearman–Leuning theory for closed-path eddy correlation measurements, Tellus B: Chemical and Physical Meteorology, 59, 937–946, 2007b.

Järvi, L., Nordbo, A., Rannik, Ü., Haapanala, S., Riikonen, A., Mammarella, I., Pihlatie, M., and Vesala, T.: Urban nitrous-oxide fluxes measured using the eddy-covariance technique in Helsinki, Finland., Boreal Environment Research, 19, 2014.

Kaimal, J. C., Wyngaard, J., Izumi, Y., and Coté, O.: Spectral characteristics of surface-layer turbulence, Quarterly Journal of the Royal Meteorological Society, 98, 563–589, 1972.

Kohonen, K.-M., Kolari, P., Kooijmans, L. M. J., Chen, H., Seibt, U., Sun, W., and Mammarella, I.: Towards standardized processing of eddy covariance flux measurements of carbonyl sulfide, Atmospheric Measurement Techniques Discussions, 2019, 1–30, https://doi.org/10.5194/amt-2019-313, https://www.atmos-meas-tech-discuss.net/amt-2019-313/, 2019.

Langford, B., Acton, W., Ammann, C., Valach, A., and Nemitz, E.: Eddy-covariance data with low signal-to-noise ratio: time-lag determination, uncertainties and limit of detection, Atmospheric Measurement Techniques, 8, 4197–4213, 2015.

Launiainen, S., Rinne, J., Pumpanen, J., Kulmala, L., Kolari, P., Keronen, P., Siivola, E., Pohja, T., Hari, P., and Vesala, T.: Eddy covariance measurements of CO, Boreal Environment Research, 10, 569–588, 2005.

Lee, X., Massman, W., and Law, B.: Handbook of micrometeorology: a guide for surface flux measurement and analysis, vol. 29, Springer Science & Business Media, 2004.

Mammarella, I., Launiainen, S., Gronholm, T., Keronen, P., Pumpanen, J., Rannik, Ü., and Vesala, T.: Relative humidity effect on the high-frequency attenuation of water vapor flux measured by a closed-path eddy covariance system, Journal of Atmospheric and Oceanic Technology, 26, 1856–1866, 2009.

Mammarella, I., Nordbo, A., Rannik, Ü., Haapanala, S., Levula, J., Laakso, H., Ojala, A., Peltola, O., Heiskanen, J., Pumpanen, J., et al.: Carbon dioxide and energy fluxes over a small boreal lake in Southern Finland, Journal of Geophysical Research: Biogeosciences, 120, 1296–1314, 2015.

Mammarella, I., Peltola, O., Nordbo, A., Järvi, L., and Rannik, Ü.: Quantifying the uncertainty of eddy covariance fluxes due to the use of different software packages and combinations of processing steps in two contrasting ecosystems, Atmospheric Measurement Techniques, 9, 4915–4933, 2016.

Massman, W. and Lee, X.: Eddy covariance flux corrections and uncertainties in long-term studies of carbon and energy exchanges, Agricultural and Forest Meteorology, 113, 121–144, 2002.

Massman, W. J.: A simple method for estimating frequency response corrections for eddy covariance systems, Agricultural and Forest Meteorology, 104, 185–198, 2000.

Moore, C.: Frequency response corrections for eddy correlation systems, Boundary-Layer Meteorology, 37, 17–35, 1986.

Nemitz, E., Mammarella, I., Ibrom, A., Aurela, M., Burba, G. G., Dengel, S., Gielen, B., Grelle, A., Heinesch, B., Herbst, M., et al.: Standardisation of eddy-covariance flux measurements of methane and nitrous oxide, International Agrophysics, 32, 517–549, 2018.

Nordbo, A., Launiainen, S., Mammarella, I., Leppäranta, M., Huotari, J., Ojala, A., and Vesala, T.: Long-term energy flux measurements and energy balance over a small boreal lake using eddy covariance technique, Journal of Geophysical Research: Atmospheres, 116, 2011.

Oosterwijk, A., Henzing, B., and Järvi, L.: On the application of spectral corrections to particle flux measurements, Environmental Science: Nano, 5, 2315–2324, 2018.

Peltola, O., Mammarella, I., Haapanala, S., Burba, G., and Vesala, T.: Field intercomparison of four methane gas analyzers suitable for eddy covariance flux measurements, Biogeosciences, 10, 3749–3765, https://doi.org/10.5194/bg-10-3749-2013, https://www.biogeosciences.net/10/3749/2013/, 2013.

Peltola, O., Hensen, A., Helfter, C., Belelli Marchesini, L., Bosveld, F. C., van den Bulk, W. C. M., Elbers, J. A., Haapanala, S., Holst, J., Laurila, T., Lindroth, A., Nemitz, E., Röckmann, T., Vermeulen, A. T., and Mammarella, I.: Evaluating the performance of commonly used gas analysers for methane eddy covariance flux measurements: the InGOS inter-comparison field experiment, Biogeosciences, 11, 3163–3186, https://doi.org/10.5194/bg-11-3163-2014, http://www.biogeosciences.net/11/3163/2014/, 2014.

Peltola, O., Aslan, T., Ibrom, A., Nemitz, E., Rannik, , and Mammarella, I.: The high frequency response correction of eddy covariance fluxes. Part 1: the empirical approach and its interdependence with the time-lag estimation, Atmospheric Measurement Techniques Discussions, submitted, 2021.

Rannik, Ü., Haapanala, S., Shurpali, N., Mammarella, I., Lind, S., Hyvönen, N., Peltola, O., Zahniser, M., Martikainen, P., and Vesala, T.: Intercomparison of fast response commercial gas analysers for nitrous oxide flux measurements under field conditions, Biogeosciences, 12, 415–432, 2015.

Rannik, Ü., Peltola, O., Mammarella, I., et al.: Random uncertainties of flux measurements by the eddy covariance technique, Atmospheric Measurement Techniques, 2016.

Sabbatini, S., Mammarella, I., Arriga, N., Fratini, G., Graf, A., Hörtnagl, L., Ibrom, A., Longdoz, B., Mauder, M., Merbold, L., et al.: Eddy covariance raw data processing for CO2 and energy fluxes calculation at ICOS ecosystem stations, International Agrophysics, 32, 495–515, 2018.

Smeets, C., Holzinger, R., Vigano, I., Goldstein, A., and Röckmann, T.: Eddy covariance methane measurements at a Ponderosa pine plantation in California, Atmospheric Chemistry and Physics, 9, 8365–8375, 2009.

Stull, R. B.: An introduction to boundary layer meteorology, vol. 13, Springer Science & Business Media, 2012.

Werle, P., Mücke, R., and Slemr, F.: The limits of signal averaging in atmospheric trace-gas monitoring by tunable diode-laser absorption spectroscopy (TDLAS), Applied Physics B, 57, 131–139, 1993.

Wintjen, P., Ammann, C., Schrader, F., and Brümmer, C.: Correcting high-frequency losses of reactive nitrogen flux measurements, Atmospheric Measurement Techniques, 13, 2923–2948, https://doi.org/10.5194/amt-13-2923-2020, https://www.atmos-meas-tech.net/13/2923/2020/, 2020.