Response to the report of reviewer 1:

Thanks to the reviewer for his time and efforts in reviewing this work. The comments and questions are valuable in improving the clarity of this work. We have responses below with manuscript revised accordingly. Improved retrieval results with doubled spatial resolution are updated in Sec 5. We also made the datasets including all AirHARP retrieval results publicly available with a link specified in the manuscript (https://data.nasa.gov/Earth-Science/FastMAPOL_ACEPOL_AIRHARP_L2/8b9y-7rgh).

The authors use a preexisting radiative transfer (RT) code to train a neural network (NN) to output polarimetric radiances at the angles and wavelengths of the AirHARP instrument. The computationally inexpensive NN forward model is then paired with the inversion module of the preexisting MAPOL algorithm to produce a new hybrid retrieval (FastMAPOL) that is less computationally expensive than the original method. The FastMAPOL retrieval is tested on both synthetic data and real ACEPOL measurements made by the AirHARP instrument and, in both cases, good retrieval performance is observed.

Polarimetric remote sensing has the potential to provide enhanced aerosol information but the large number of free parameters in most multiangle polarimeter (MAP) retrieval algorithms generally prohibits the use of precomputed lookup tables. This fact frequently necessitates computationally expensive online radiative transfer calculations which pose a significant challenge for operational algorithms that need to process very large data volumes. The authors provide a convincing demonstration of a machine learning approach that significantly reduces this computational burden. Care is taken to ensure that the NN reproduces the original RT with high fidelity and tests involving synthetic and real data both show good retrieval performance. The approach appears to be technically sound and has the potential to serve as a foundation for retrieval developments pertaining to PACE and other future missions employing MAPs. Furthermore, the content of the manuscript is well organized, and the material is clearly appropriate for AMT. Therefore, once the comments below have been addressed, I can confidently recommend publication.

Thanks for the summary and the positive comments.

Specific Comments

1. P2, LN21: The list of MAPS in the sentence beginning on this line seems to have an extra "and". It also is inconsistent in its use of the name of sensor or the overarching mission. I would recommend rephrasing.

   Thank you for the suggestion. We have revised the sentence as follows:

   “Several satellite missions plan to carry MAP instruments, which are scheduled to be launched in the time frame of 2023-2024, including the European Space Agency (ESA)’s Multi-viewing Multi-channel Multi-polarisation Imager (3MI) on board the Metop-SG satellites (Fougnie et al, 2018), the National Aeronautics and Space Administration (NASA)’s Multi-Angle Imager for
Aerosols (MAIA) (Diner et al, 2018) and Plankton, Aerosol, Cloud, ocean Ecosystem (PACE) (Werdell et al 2019) missions.”

Details on PACE instruments are provided in the next paragraph in the manuscript.

2. P3, LN22: Did the authors intended to say "...references within)."?
   
   Corrected.

3. P4, LN2: Citation should be inline (no leading parenthesis)
   
   Corrected.

4. P4, LN4: Should read "...benefits of using..."
   
   Corrected.

5. P4, LN32: "have" should be "has"
   
   Corrected.

6. P5, LN8: It would be clearer to say something along the lines of "...observational altitude..." since not all members of the HARP family are aircraft instruments.
   
   Thanks. We have revised the phrase as recommended.

7. P6, LN6: AirHARP's swath width aboard the ER2 should be provided.
   
   Thank you for the suggestion. The following sentence is moved to the first paragraph in Sec 5 with swath width added:

   “AirHARP conducted high spatial resolution measurements with a grid size of 55 m and **swath width of 42km at nadir (up to 60km at far angles)**. We averaged the reflectance and DoLP respectively within a bin box of 10 x 10 pixels (550m × 550 m).”

8. P6, LN8: Is σavg the regular standard deviation of all 100 pixels in the box or is it the standard error of the mean (e.g., σ/sqrt(N)=σ/10)? The latter strikes me as a more appropriate choice as I believe the retrievals are performed on the means of the aggregated 10x10 boxes. The definition of σavg needs to be clarified, and justification for that particular definition should be provided.
   
   Thank you for the discussion. σavg is used to capture the spatial variation of geophysical properties within the bin box, which provides a good uncertainty indicator for field measurement. This is why we used it in our previous noise model. However, how to include σavg in the noise model depends on the assumption of the noise properties. From
our recent tests, we adjusted our approach and further improved our retrieval performance through 1) quality check of the measurement data, 2) adding a constraint in aerosol model, 3) using $\sigma_{\text{avg}}$ to evaluate measurement uncertainty, but not in the noise model. Since $\sigma/\sqrt{N}=\sigma/10$ is much smaller than the calibration uncertainty, our new noise model is similar to what the reviewer suggested. A corresponding discussion is provided in Sec 5:

“To assess the spatial variability of field measurement, we computed the standard deviations for the reflectance ($\sigma_{\text{r,avg}}$) and DoLP ($\sigma_{\text{P,avg}}$) within the bin box. Representative values are provided in Table 5. The values of $\sigma_{\text{r,avg}}$ and $\sigma_{\text{P,avg}}$ at 870nm band are 4.5% and 0.05, respectively, which suggests larger measurement uncertainties at 870nm than other bands probably due to small radiometric magnitudes. Meanwhile, our retrieval tests showed larger coarse mode retrieval uncertainties than synthetic data results. To better constrain retrievals, we assume the coarse mode aerosol as sea salt by setting its imaginary refractive index to zero. All other retrieval parameter range are kept the same as in Table 2. Furthermore, we found our forward model cannot predict the angular variation of DoLP in 440nm band well (with an estimated MAE of 0.04), which contributes a major portion to the cost function and increases both fine and coarse mode retrieval uncertainties. Therefore, we exclude DoLP in 440nm band from our retrievals in this study.”

The corresponding results are updated in Sec 5, and more details are provided in the responses to comments 27-29.

9. P6, LN18: As I understand it, $\sigma_{\text{NN}}$ is actually the difference between the RT code and NN, not the NN's uncertainty in an absolute sense. I would recommend clarifying what is meant by “uncertainty” here.

The reviewer is correct. To evaluate the NN accuracy, we generate a synthetic AirHARP datasets with multiple angle setup. This is more realistic than the single angle used in training data. The NN accuracy is then computed by the RMSE between the NN predictions and the synthetic data. Detailed discussions are in Sec 3.3. We added the following sentence for clarification.

“$\sigma_{\text{NN}}$ is evaluated by comparing with synthetic multi-angle AirHARP measurements discussed in Sec 3.3.”

10. P6, LN32: I generally take "trace gases" to be those gases in the atmosphere other than nitrogen, oxygen, and argon. Was Rayleigh scattering from these three non-trace gases taken into account above the aircraft? Please clarify.

Thank you for the question. Full Rayleigh scatterings is considered. We have revised the sentence to be more precise as follows:
The atmosphere is configured as three layers: a top molecular layer above the aircraft, a molecular layer in the middle below the aircraft, and an aerosol and molecular mixing layer on the bottom with a height of 2 km. Aerosols are assumed to be uniformly distributed in the mixing layer as shown in the left panel of Fig. 1. The same vertical structure of the atmosphere was successfully used in the inversion of RSP data (Gao et al 2019, 2020).

The atmospheric surface pressure is assumed to be one standard atmosphere pressure, which is consistent with the value discussed in Sec 5. Anisotropic molecular Rayleigh scatterings are accounted (Hansen et al 1974). The molecular absorption properties are computed by the hyperspectral line-by-line atmospheric radiative transfer simulator (ARTS) (Buehler et al. 2005) with the molecular absorption parameters of oxygen, water vapor, methane, and carbon dioxide from the HITRAN database (Gordon et al. 2017). The gas absorption of ozone and nitrogen dioxide are from Gorshelev et al. 2014, Serdyuchenko et al. 2014 and Bogumil, K., et al. 2003, respectively. The hyperspectral absorption coefficients are then averaged within the instrument spectral response function and used in the multiple scattering radiative transfer simulation (Zhai et al 2009, 2010, 2018). The molecular profile used is the US standard atmospheric constituent profiles (Anderson et al, 1986)

The following references are added:


Bogumil, K., et al. (2003), Measurements of molecular absorption spectra with the SCIAMACHY pre-flight model: Instrument characterization and reference

11. P7, LN18: The term "visible spectrum" should be replaced with something that also includes HARP's 870 nm NIR channel.

Thank you for the suggestion. We have revised the sentence as follows:

“For the application to AirHARP bands, $p_1$ for the real part of the refractive index is approximately spectrally flat for both the fine and coarse mode aerosols within the AirHARP spectral range.”

12. P7: The vertical profile assumed for the simulated aerosol should be described.

Thank you for the question. The aerosol profile is assumed uniform within 2km range. Please refer to response to comment 10.

13. P9, LN13: Only 14 quantities are listed but it’s stated that the forward calculation uses 15 parameters. The 15th parameter should be included in this summary paragraph (presumably ozone column density?).

Thank you for pointing this out. We have added the ozone density in the sentence as follows:

“In summary, the parameters used to represent the forward model include five volume densities (one for each submode), four independent parameters for the refractive indices of fine and coarse modes, one parameter for wind speed, ozone column density, and Chla.”

14. P9: Should some of the quantities in the equations of section 2.2 have an azimuthal dependence, as well as solar and viewing zenith angle dependence? Why do the equations here show these quantities to be functions of the latter two, but not relative azimuth?

Thank you for the comments. The reviewer is correct. There are dependencies on relative azimuth. We revised the equation by explicitly adding the relative azimuth into the equations (10), (11), (13) and (14).


Corrected.

16. P10, LN11: This sentence needs to be reworked so that it is grammatically correct. Also, it should be specified exactly which angle is less than 1° (viewing zenith angle?).
Thank you for the question. Previously sentence is not accurate. We revised the sentence and add more details:

“To compute the remote sensing reflectance from the multi-angle AirHARP measurement, we only consider the reflectance at the minimum viewing zenith angle for each wavelength and apply the atmospheric correction and BRDF correction as discussed above. For $\theta'_v < 15^\circ$ ($\theta_v < 20^\circ$), the $R_\circ/R$ factor is approximately a constant value of 1, but for larger $\theta'_v$ angles the ratio increases with both wind speed and $\theta'_v$ value (Morel et al 1996, 2002). In this study, we ignored the $R_\circ/R$ factor in Eq. (14), which will not impact Rrs retrievals from synthetic data due to the small viewing zenith angle used, but may cause underestimation of Rrs at the edge of the image, as will be discussed in Sec 4 and 5.”

Sec 4 added more details regarding synthetic data:

“Note that the $R_\circ/R$ factor will not impact the BRDF correction in computing Rrs for the synthetic data, because of the small viewing zenith angle used at the four AirHARP bands, which are 1.22°, 1.17°, 0.03°, 3.52° respectively “

Further discussions are added for field data (please also refer to response to comment 20):

“As discussed in Sec 2.2, we chose the minimum viewing zenith angle available from the measurements after removing the sunglint. The removal of sunglint improves the Rrs calculation for Scene 2 as shown in Fig. 16. Moreover, we ignored the $R_\circ/R$ factor in Eq. 14 which may cause underestimation of the Rrs at the edge of the image where $\theta_v$ can reach as large as 60°. However, it is challenging to analyze its impact at large $\theta_v$ angles. $R_\circ/R$ has a strong dependency on wind speed, but the retrieved wind speeds from current retrievals show large uncertainties. Further work may require a better treatment of sunglint and improved accuracy in wind speed.”

17. P11, L2: A more precise description of the method of random sampling should be given. Are the variables being drawn from a uniform distribution (log-uniform distribution in the case of Chla)?

Thank you for the suggestion. We revised the sentence as follows:

“The solar zenith angle, ozone column density, refractive index, and wind speed are randomly sampled from a uniform distribution. Chla is randomly sampled from a log-uniform distribution.”
18. P12, LN14: Here it is stated that separate NNs are used for reflectance and DoLP. Instead of two separate NNs, another potential approach would have been to use a single NN with an 8-dimensional output (4 reflectance + 4 DoLP values). It would be beneficial if the authors could further elaborate on the pros and cons of these two possible approaches, and their motivation for using the particular 2 network architecture that was ultimately chosen.

Thank you for the questions. We choose the current approach with the consideration of both flexibility and efficiency. Combining two NNs together may lead to better efficiency. However, there are several challenges with this strategy: 1) as shown in the Figure 2 and 3, reflectance and DoLP differ in angular variations which may increase the difficulties in training the neural network without increasing the size of NN: 2) there are different accuracy requirements for reflectance and DoLP, which is easier to control when the two NNs are separated. There could be other ways to combine reflectance with DoLP such as working with I, Q, U directly, which we will explore in future work.

We added the corresponding discussions into Sec. 3.1:

“
To maintain both flexibility and efficiency, we trained two NN models for reflectance and DoLP respectively in the next section. Reflectance and DoLP have different accuracy requirements as discussed in Sec. 2, and also differ in angular variations as shown in the Figs. 2, therefore, it is convenient to control their accuracy through separated training procedures.
“

19. P19, LN 5: Is the added noise uncorrelated in angle, polarization and wavelength? If so, how would the authors expect more realistic calibration errors (which likely will be strongly correlated among these three dimensions) to impact their results?

Thank you for the question. Yes, we assume no correlation in the added noise. We conducted an independent study in which noise was added with correlation in angles, and observed overfitting in retrievals (reduction of $\chi^2$). This is related to the fact that some noise variations are long angular range in nature, which can be similar to some true signals and thus get fitted by the optimization process. The quantified influence depends on the magnitude of the noise and the strength of the correlation (KnobelOE 2012), which requires further study.

20. P22: There is an extra parenthesis in the title of the Chla subplot of Figure 9.

Removed.

21. P22, LN5: The last two sentences of this paragraph have several grammatical errors and are a bit confusing. I suggest rephrasing.
We revised the sentence as follows:

“...For wind speed larger than 3 m/s, the averaged retrieval uncertainty is 1.2 m/s with a small variation less than 0.1 m/s. “

22. P23, LN14: Should read "...less sensitive to outliers." (No "the")

Corrected.

23. P23, LN14: "...applied to the synthetic measurements..."

Corrected.

24. P23, LN23: The sentence starting on this line has several grammatical errors and needs rewriting.

We revised the sentence as follows:

“For 440 nm band, when AOD is less than 0.3, the Rrs retrieval uncertainties are less than 0.0005 sr^{-1}; but the uncertainties become as high as 0.001 sr^{-1} at a larger AOD of 0.5”.

25. P23, LN28: It would be clearer if the phrase "the reduction of" was changed to "reduce".

Revised.

26. P25, FIG12: The figure would be easier to interpret if the caption explained that the "hole" in the middle of the three polar plots was due to water condensation on the lens. I thought it was a plotting artifact, as it lines up the "0°" label, until I read the full condensation explanation later in the text. It might even be good to remove the "0°" tick completely.

In addition to the explanation in the main text, we added a sentence in the caption:

“ The central portion in the viewing angle plots is removed due to water condensation on the lens.“

We prefer to keep the 0 degree symbol to ensure readers understand the central point refers to nadir (with no removal of zenith angles in the plots).

27. P26, LN20: The last sentence needs to have grammatical errors fixed and its meaning clarified.

As discussed for comment 8, we have improved the retrieval performance with a new $\chi^2$ histogram shown below. The discussion of $\chi^2$ is combined with a latter sentence as discussed for the next comment. We revised the sentence as follows:
The histograms of \( \chi^2 \) for all pixels retrieved in each scene are shown in Fig. 14. The most probable \( \chi^2 \) are 1.1, 1.7, and 1.1 respectively.

\[ \text{Figure 14. The histograms of the cost function values over the three scenes as shown in Fig. 12 with total pixel numbers of 13491, 13226, and 9159. Only pixels over the ocean are considered.} \]

28. P27, LN5: More discussion of the along-track stripping in \( \chi^2 \) values should be provided. In many cases, it does not seem to correlate with the number of view angles available. For example, the most prominent ~10 pixel wide dark red strip of \( \chi^2 \) in Figure 15 is actually offset to the right by about five pixels of the band of missing angles at nadir. What is the cause of this artifact?

Thank you for checking the images and questions. We investigated the stripes, and found anomalies from both measurements and retrieved results, which have been corrected (Fig 15). Meanwhile, we have updated the retrievals as discussed in comment 8. The spatial resolutions are also doubled. The new plots are shown below for Figure 15-17. Note that due to the use of smaller uncertainties in the noise model (without contribution from \( \sigma_{avg} \)), the overall value of \( \chi^2 \) increased, but we still have a majority of pixels converging to within \( \chi^2 < 2 \sim 3 \).

More discussion was added to the paragraph (also see response to comment 30):

“For pixels with larger \( \chi^2 \) as shown in Fig. 14, the forward model cannot fit the measured reflectance or DoLP well, which may be due to cloud contamination (Stap et al 2015), land, or residuals of glint. In scene 1, the top region with large \( \chi^2 \) values is mostly due to the impact of thin cloud which is visible from Fig. 13. Larger residuals in the 870nm band between measurement and forward model are also observed. The retrieved AODs are over-estimated in this region. In scene 2, the region with \( \chi^2 > 3 \) correlate closely with the thin clouds (Fig 13), which influence nearby AOD and Rrs retrievals. For scene 3, \( \chi^2 \) becomes larger than 2 when close to the coast. This may be due to complex water properties which are not well represented by the open water bio-optical model used in the simulation.
(Gao et al 2019). The pixels near the coast are also potentially impacted by the bottom effect and adjacency effect of land pixels.”

Fig. 15. The number of viewing angles used in the retrieval ($N_v$), cost function value ($\chi^2$), the retrieved AOD (550 nm) and $R_{rs}$ (550nm) for all pixels in scene 1. The HSRL AODs at 532 nm are indicated by the colored dots in the AOD plot.

Figure 16. Same as Fig. 15 but for scene 2. For $R_{rs}$, viewing angles at least 40° away from the solar specular reflection direction are used to avoid sunglint as shown in Fig. 13.

Figure 17. Same as Fig. 15 but for scene 3. The pixels with large $\chi^2$ are influenced by the land (upper region) and island (lower left). The retrieved AOD and $R_{rs}$ over land pixels are not shown. The location of the AERONET USC_SEAPRISM site is indicated by a red star symbol.
29. P28, FIG15-17: If it is easy to add, it would be informative to include a fourth subplot with the retrieved Rrs in these figures.

Thank you for the suggestion. We have added the Rrs figures as shown above.

30. P29, FIG18-19: I'm struggling to see the value in these two figures given the very coarse across-track averaging. Why resolve along-track data at ~0.5km when averaging across-track at tens of km? In my mind, a better approach might be to average all pixels within a circle of some radius of the HSRL/AERONET/SeaPRISM measurements. Alternatively, these figures could be removed altogether, while still reporting the average values for each of the 3 scenes. (Much of the pixel-level information is already conveyed in figures 15-17).

Thank you for the suggestion. We agree with the reviewer, the original comparison is not ideal, but they are useful to make clear comparison with HSRL. To fix the above-mentioned issue, 1) we conducted new retrievals with a higher resolution, 2) pixels in the along track direction with 4x4 pixels are averaged, and 3) we kept most pixels with a broader criterion in the plots. Both Fig 18 and 19 are updated and shown below.

Discussion for AOD are updated in the paragraph:

“**To compare with the HSRL AOD in the along track direction, the retrieved AOD (550nm) is averaged within a box of 2.2km x 2.2km (4 x 4 pixels). The averaged AOD (550nm) values and the corresponding standard deviations are shown in Fig. 18.** Pixels with Nv>30 and \( \chi^2 <10 \) are considered. The overall averaged values and their standard deviation are also computed and indicated in the plots. The averaged HSRL AODs are 0.079, 0.071 and 0.037 for scenes 1 to 3. The averaged retrieved AOD(550nm) are 0.096, 0.078 and 0.049 with relatively larger retrieval variation of 0.02 to 0.03. For scene 1, most \( \chi^2 \) values are larger than 2, while for the other two scenes, most are less than 2 except for those pixels very close to cloud and coast. The retrieved AOD is larger than that of the HSRL by 0.03 in the overlapped region which may be influenced by the remaining effect of water condensation. In scene 2, the peaks of the retrieved AOD values correspond to the \( \chi^2 \) values larger than 2, which are influenced by the nearby thin cloud. There are no overlapped pixels except the one associated with high AOD peaks, but the general trend of the retrieved AOD agrees with the HSRL results. For scene 3, the retrieved AOD values agree well with the HSRL AOD with an average difference less than 0.01 and \( \chi^2 \) mostly less than 2. However when the pixels are close to the coast, both \( \chi^2 \) and AOD increased significantly as discussed previously.”
Fig. 18 Comparison of the retrieved AOD (550 nm) from AirHARP measurement with the AOD (532 nm) from HSRL for Scenes 1 to 3. The AOD (550nm) from AERONET USC_SeaPRISM site is shown in scene 3. The AirHARP retrieved AOD is averaged with 4x4 pixels (2.2km x 2.2km). The averaged and standard deviations for both AirHARP retrievals and HSRL products are provided in the text. Pixels with Nv>30 and χ²<10 are considered.

Discussions for Rrs in Figure 19 are also updated:

“Fig. 19 shows the mean value and standard deviation of Rrs averaged in the same way as AOD discussed above. There is similar spatial variation between the retrieved Rrs and AOD. Pixels with large Rrs uncertainties are mostly associated with the large AOD uncertainties shown in Fig. 18. The Rrs values at 440nm for the three scenes are 0.0055, 0.0072, and 0.0030sr⁻¹, where the decrease of Rrs from scene 2 to scene 3 may be due to the increase of CDOM close to the coast as demonstrated in Fig. 5. Moreover, Rrs at scene 1 are likely to be under-estimated due to the large χ² and retrieved AOD over the center of scene 1. The averaged Rrs values at 550nm remain approximately constant with a value of 0.0003 sr⁻¹ over all three scenes. Rrs from AERONET USC_SeaPRISM site are indicated in scene 3 of Fig 19 and also compared in Figure 20. …“
Figure 19. Similar to Fig. 18, the retrieved Rrs are computed for the AirHARP band of 440, 550, and 670nm bands. The averaged Rrs and its standard deviation are shown in the legends. For scene 3, Rrs from AERONET USC_SeaPRISM site at wavelengths corresponding to AirHARP bands are indicated by the star symbols.

The comparison with the AERONET (Fig 20) is updated correspondingly:

“To better compare with AERONET results, we only considered the pixels with $\chi^2<2$ and conducted the same averaging (4 x 4 pixels) around the USC_SeaPRISM site for the retrieved AOD and Rrs. The averaged values and their standard deviations are plotted in Fig. 20. The overall retrieved AOD spectrum is similar to AERONET results with a difference smaller than 0.01. The results are similar to the retrieval results from the Research Scanning Polarimeter as reported by Gao et al. (2020). The retrieved Rrs agrees well with the AERONET Rrs with a difference less than 0.001 sr$^{-1}$. Note that this study is done with possible AirHARP measurement uncertainty of 3% in reflectance, which may impact atmospheric correction accuracy.”

Fig 20: Comparisons of the AOD and Rrs from AirHARP retrievals with AERONET products. The retrieval results are averaged with 4×4 pixels (2.2km×2.2 km) around the AERONET USC_SeaPRISM site. This is similar to Fig. 5 and 19 with error bars indicating the standard deviations, but only pixels with $\chi^2<2$ are considered. The AERONET AOD and Rrs spectra are taken from Oct 23, 2017 with the error bars indicating daily variations. HSRL AOD at 532nm is also shown.

31. P30, LN16: Was the speed up factor of FastMAPOL every specified? How long does a retrieval using equivalently accurate RT take with regular MAPOL on the same hardware?

Thank you for the questions. We added the information:
“Comparing to the retrieval speed of approximately 1 hour per pixel using conventional radiative transfer forward model, the computational acceleration is $10^3$ times faster with CPU or $10^4$ times with GPU processors.”

32. P21, LN12: I think the authors intend to say "...HARP2 is likely to have higher accuracy..."

Thank you. I believe the author is referring to P31. We have corrected the sentence.

Furthermore, we have provided the complete dataset from AirHARP retrievals with brief discussion in Sec 5:

“The complete retrieval results, including the aerosol microphysical properties, wind speed, Chla and atmospheric correction related datasets, are provided in Data availability. The retrieval uncertainties for aerosol microphysical properties are relatively large due to the small aerosol optical depths. Chla retrievals are sensitive to the aerosol retrievals, and are more challenging to retrieve accurately at small values as discussed in Sec 4.”