Spectral Calibration of the MethaneAIR Instrument

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Abstract. MethaneAIR is the airborne simulator of MethaneSAT, an area-mapping satellite currently under development with the goal of locating and quantifying large anthropogenic ~~point~~ CH$_4$ point sources as well as diffuse ~~basin-scale emissions~~ emissions at the spatial scale of an oil and gas basin. Built to closely replicate the forthcoming satellite, MethaneAIR consists of two imaging spectrometers. One detects CH$_4$ and CO$_2$ absorption around 1.65 and 1.61 μm, respectively, while the other constrains the optical path in the atmosphere by detecting O$_2$ absorption near 1.27 μm. The high spectral resolution and stringent retrieval accuracy requirements of greenhouse gas remote sensing in this spectral range necessitate a reliable spectral calibration. To this end, on-ground laboratory measurements were used to derive the spectral calibration of MethaneAIR, serving as a pathfinder for the future calibration of MethaneSAT. Stray light was characterized and corrected through Fast Fourier Transform (FFT)-based Van Cittert deconvolution. Wavelength registration was examined and found to be best described by a linear relationship for both bands with a precision of ∼0.02 spectral pixel. The instrument spectral spread function (ISSF), measured with fine wavelength steps of 0.005 nm near a series of central wavelengths across each band, was oversampled to construct the instrument spectral response function (ISRF) at each central wavelength and spatial pixel. The ISRFs were smoothed with a Savitzky-Golay filter for use in a lookup table in the retrieval algorithm. The MethaneAIR spectral calibration was evaluated through application to radiance spectra from an instrument flight over the Colorado Front Range.

15 *Copyright statement.* TEXT

1 Introduction

Methane (CH$_4$) is an influential greenhouse gas due to its high global warming potential, which is estimated to be 56–105 times higher than that of carbon dioxide for a 20-year time period (Howarth, 2014). Given that approximately 60% of global CH$_4$ emissions are anthropogenic (Saunois et al., 2020), the identification and subsequent reduction of these sources represent a
20 significant opportunity for climate change mitigation (Zhang et al., 2020). In quantifying atmospheric CH$_4$, space-based obser-

vation is a powerful tool due to its ability to provide regular coverage on a variety of spatial scales. Currently, the Greenhouse gases Observing SATellite (GOSAT) and TROPOspheric Monitoring Instrument (TROPOMI) aboard the Sentinel-5P satellite collect CH_4 abundance data at a global scale (Yoshida et al., 2011; Hu et al., 2016). These missions have effectively captured regional emission trends as well as significant point sources, but their somewhat coarse spatial resolutions ($\sim$10 km for GOSAT

25 and 7 km for TROPOMI) limit source differentiation and location (Varon et al., 2020). Target-mode satellite instruments may offer much higher spatial resolution for the observation of individual high-emitting facilities within small areas. For example, the GHGSat-D instrument targets CH_4 sources at 50 m resolution within a 12 km^2 area (Varon et al., 2019, 2020; Jervis et al., 2020). Space-based observations at a scale larger than that of GHGSat-D but smaller than that of TROPOMI are not currently operational, but may contribute to a more robust greenhouse gas monitoring system.

30 MethaneSAT is a push broom imaging satellite under development that is designed to operate at ~~such an intermediate scale~~ a scale in between that of current target-mode satellites and global mappers. The mission by MethaneSAT, LLC, a subsidiary of the Environmental Defense Fund, is planned to launch in 2022 (MethaneSAT, LLC, 2020). MethaneSAT aims to characterize oil and gas basin-scale, diffuse CH_4 emissions through a wide swath of ~~$\sim$ 200 km ^{2}~~ 260 km and at the same time locate and quantify large point sources within each target area that is typically 200 $\times$ 140 km^2 ~~(Benmergui et al., 2020a; MethaneSAT, LLC, 2020)~~

35 (Benmergui et al., 2020b; MethaneSAT, LLC, 2020). MethaneSAT detects CH_4 absorption around 1.65 μm and CO_2 absorption near 1.61 μm with one spectrometer. In order to constrain the optical path in the atmosphere, a second spectrometer is dedicated to detect the $O_2\,a^1\Delta_g$ band around 1.27 μm. Although the $O_2\,A$ band ($\sim$0.76 μm) has been commonly used for this purpose, the $O_2\,a^1\Delta_g$ band may be more advantageous ~~given its close proximity~~. Recent advances in separating emitted airglow from backscattered light enable the use of the $O_2\,a^1\Delta_g$ band in remote sensing applications (Sun et al., 2018; Bertaux et al., 2020)

40 . Further, the close spectral proximity of the $O_2\,a^1\Delta_g$ band to the CH_4 ~~band and recent advances in airglow correction (Sun et al., 2018; Bertaux et al., 2020)~~/CO_2 bands is favorable, as any differences in aerosol and cloud optical properties between the bands are reduced (Sun et al., 2018).

MethaneAIR is the airborne simulation instrument for MethaneSAT. It has been designed to replicate the forthcoming satellite as closely as possible. The MethaneAIR instrument was integrated in the National Science Foundation (NSF) Gulfstream

45 V (GV) aircraft operated by the National Center for Atmospheric Research (NCAR). Two engineering flights were conducted in the Colorado Front Range in November 2019. Similarly, airborne simulators have been built and analyzed in support of other future satellites, such as GEOstationary Trace gas and Aerosol Sensor Optimization (GEO-Taso) (Nowlan et al., 2016), GEOstationary Coastal and Air Pollution Events (GEO-CAPE) Airborne Simulator (GCAS) (Nowlan et al., 2018), and Airborne Compact Atmospheric Mapper (ACAM) (Liu et al., 2015). These three instruments have been used as testbeds for the

50 geostationary Tropospheric emissions: Monitoring of pollution (TEMPO) instrument. The test flights from airborne simulators aid in algorithm development while also providing valuable scientific data (Nowlan et al., 2016, 2018; Liu et al., 2015). Indeed, in-flight observations can supplement current ground-based and satellite remote sensing, as is the goal of the airborne SWIR spectrometers Methane Airborne MAPper (Gerilowski et al., 2011), and GreenHouse gas Observations of the Stratosphere and Troposphere (GHOST) (Humpage et al., 2018).

The high spectral resolution and stringent retrieval accuracy requirements of greenhouse gas remote sensing in the short-wave infrared (SWIR) band necessitate a reliable spectral calibration. One of the most important tasks of spectral calibration is characterization of the instrument spectral response function (ISRF), the response of a spectral pixel to photons at different wavelengths. An accurate understanding of the ISRF is crucial for the retrieval of greenhouse gas abundance from the observed radiance spectra. Analysis of column averaged dry-air mole fractions of carbon dioxide (X_{CO_2}) as measured by the Orbiting Carbon Observatory-2 (OCO-2) revealed that uncertainties due to ISRF dominated the total error in land nadir observations (Connor et al., 2016). For CH_4 retrieval in particular, simulations of TROPOMI X_{CH_4} retrievals have indicated high sensitivity to errors in the ISRF (van Hees et al., 2018). The ISRFs are usually characterized through preflight measurements and parameterized with functions ranging in complexity from a simple Gaussian (Munro et al., 2016; Hamidouche and Lichtenberg, 2018) or super-Gaussian (Beirle et al., 2017) to a tailored, weighted sum of multiple functions (van Hees et al., 2018; Liu et al., 2015). In the absence of a satisfactory functional form, a lookup table may be used to describe the ISRF (Day et al., 2011; Lee et al., 2017). Laboratory measurements for ISRF characterization are also used to determine wavelength registration of spectral pixels (Lee et al., 2017).

The ISRF is often determined ~~only~~ within a few spectral sampling intervals away from the central wavelength. However, the spectrum from a given spatial pixel can contain spatial stray light from the other spatial pixels and spectral stray light from all spatial pixels. The MethaneAIR stray light is measured and corrected for following the TROPOMI SWIR band, which is the closest reference to MethaneAIR with a wide across-track swath. The TROPOMI SWIR band stray light was measured extensively in an on-ground calibration campaign. A near-real time stray light correction was incorporated in the TROPOMI operational data processor by approximating the stray light by a pixel-independent far-field kernel and an additional kernel representing the main reflection. This process reduces stray light error, thus increasing gas-column retrieval accuracy (Tol et al., 2018).

This work presents the spectral calibration of the MethaneAIR instrument, which serves as the pathfinder of the calibration efforts of the MethaneSAT instrument, given the close similarity in spectral characteristics between MethaneAIR and MethaneSAT. The structure of this paper is organized as follows. The MethaneAIR instrument and its integration on the GV aircraft is briefly summarized in Section 2. The ISRF and stray light calibration setups are described in Section 3. The stray light correction procedure is described in Section 4. Section 5 presents the construction of the ISRF look-up table, and Section 6 presents the determination of wavelength registration based on the ISRF calibration data set. The spectral calibration is applied in the MethaneAIR spectral fitting algorithm in Section 7, followed by the conclusion in Section 8.

2 MethaneAIR instrument overview

~~MethaneAIR~~ Specifications of the MethaneAIR instrument are listed in Table 1. It consists of two customized imaging spectrometers from Headwall Photonics (part number 1003A-20507 for the O_2 spectrometer and 1003A-20507 for the CH_4 spectrometer), each with a 1.3 megapixel InGaAs camera from Princeton Infrared Technologies. The airborne instrument provides similar spectroscopy to MethaneSAT with higher spatial resolution, although with a significantly smaller swath width

. Instruction specifications are listed in Table 1. (5.05 km at a flight altitude of 12 km for MethaneAIR vs. ∼260 km for MethaneSAT) due to the difference in operating altitude. The MethaneAIR point spread function (PSF) is roughly 2.5 pixels wide across-track, estimated from the spatial stray light data. The swath angles of MethaneAIR and MethaneSAT are similar, at 23.7° and 21.3°, respectively. While MethaneSAT has a larger FPA of 2048×2048 pixels compared to the 1024×1280 pixels of MethaneAIR, the spectral range of the satellite instrument is reduced due to illumination of only 1000 spectral pixels at most. The spectral resolution of MethaneSAT, however, is 20%–30% higher than that of MethaneAIR. One of the most significant differences between the instruments is the detector material; the satellite detector is Mercury-Cadmium-Telluride (MCT), unlike that of MethaneAIR.

Table 1. MethaneAIR specifications.

Optical and Detector		Spectral and Spatial	
Focal length (mm)	25	O_2 passband (nm)	1236–1319
F-number	3.5	O_2 dispersion (nm/pixel)	0.08
Entrance slit width (μm)	34	O_2 spectral FWHM (nm)	0.22
Optical transmittance (%)	≥ 37	CH_4 passband (nm)	1592–1680
Polarization sensitivity (%)	≤ 25	CH_4 dispersion (nm/pixel)	0.1
FPA dimensions (spectral $\times$ spatial pixels)	1024×1280	CH_4 spectral FWHM (nm)	0.3
Pixel pitch (μm)	12	Plate scale (°/pixel)	0.0275
Quantum efficiency below 1650 nm	> 0.7	Field of view (°)	23.7
Frame rate (Hz)	10	Swath width (km) at 12 km altitude	5.05
Readout noise (e-), typical	35	Cross-track pixel (m) at 12 km altitude	5.76
Dark current (e-/s/pixel)	$< 8,500$	Along-track pixel (m)	≈ 25

Figure 1 shows a representation of the light path within each spectrometer. Light entering through the foreoptic is focused onto the entrance slit. The slit is then imaged onto the focal plane through an Offner spectrometer with a convex holographic grating, resulting in a 2D image with spatial information along one dimension and wavelength along the other. In Figure 1, the spectral dimension of the image is up/down, and the spatial dimension is into/out of the page. The optical design provides sub-pixel spectral smile and keystone distortion and relatively uniform focus across wavelength and field angle. Anti-reflection coatings and high grating efficiency provide an optical transmittance of 37–39% in the CH_4 channel and 45–47% in the O_2 channel. The CH_4 channel has a polarization sensitivity of 5–10% and the O_2 channel has a polarization sensitivity of 20–25%.

The infrared camera used in each channel is the 1280SCICAM from Princeton Infrared Technologies. The InGaAs focal plane provides greater than 0.7 quantum efficiency (QE) below 1650 nm. The QE begins to roll off above this wavelength, decreasing to 0.52 at 1660 nm, then 0.26 at 1670 nm before reaching a minimum of about 0.15 at the 1680 nm end of the CH_4 passband. The focal plane operates at $0°C$, which provides a reasonable compromise between dark current and the temperature-sensitive long-wavelength cutoff. The 1024 columns and 1280 rows of the focal plane array (FPA) correspond to spectral and
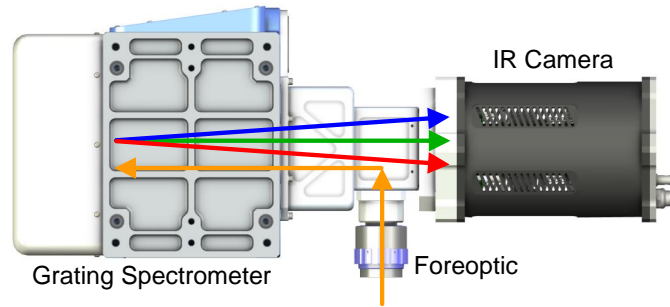
Figure 1. Light path inside each spectrometer.

spatial pixels as shown in Figure 2. Only spatial pixel indices 135–997 and 308–1170 out of 1–1280 are illuminated by the slit for the CH_4 and O_2 bands, respectively.

Initial MethaneAIR research flights were performed aboard the NSF GV aircraft. To simplify aircraft integration, the two MethaneAIR spectrometers are mounted side by side in a single instrument rack (Figure 3), which is isolated from aircraft vibration by wire isolators. Each spectrometer was internally aligned from foreoptic to focal plane by Headwall, and the two spectrometers were co-boresighted to within $1°$ when they were mounted in the rack. For CH_4 and CO_2 measurements, the spectrometers observe out of an 18 inch viewport on the bottom of the GV, using a 25 mm wide angle lens ($23.7°$ field of view). Both panes of glass in the viewport window were anti-reflection coated by L&L Optical Services. The spectral reflectivity of all four surfaces was measured from 400 to 1700 nm by the coating manufacturer. The resulting window transmittance is a smooth function ranging from 99.7% to 98.1% in the MethaneAIR spectral range. A 180 degree rotation of the instrument rack allows the O_2 spectrometer to observe out of the overhead viewport in order to image the airglow, using an 85 mm lens that provides a $7°$ field of view.

3 Calibration measurements

In an effort to reproduce the mechanical and thermal environment experienced during flight, MethaneAIR was mounted during laboratory calibration activities on a rack in its downward viewing orientation and was controlled to just above room temperature by the same thermal housing used aboard the GV (Figure 4a-b). Calibration equipment (including an integrating sphere and a collimator) were placed under the rack pointing upward. Each spectrometer collected measurements for stray light and ISRF calibration, as described in the next two subsections. In addition, flat fields were taken using the integrating sphere coupled with a broadband lamp behind a variable aperture.

The integrating sphere, model #OL 455-8SA-2 from Optronic Laboratories, has an overall diameter of 8 inches and a 2 inch diameter output port (Figure 4c). The spectral radiance at the output port was calibrated by the manufacturer every 10 nm between 350 nm and 2500 nm. During the MethaneAIR flat field measurements, the light level was tuned from zero to just beyond detector saturation in 40 steps by adjusting the ~~aperture area~~variable input aperture between the integrating sphere and
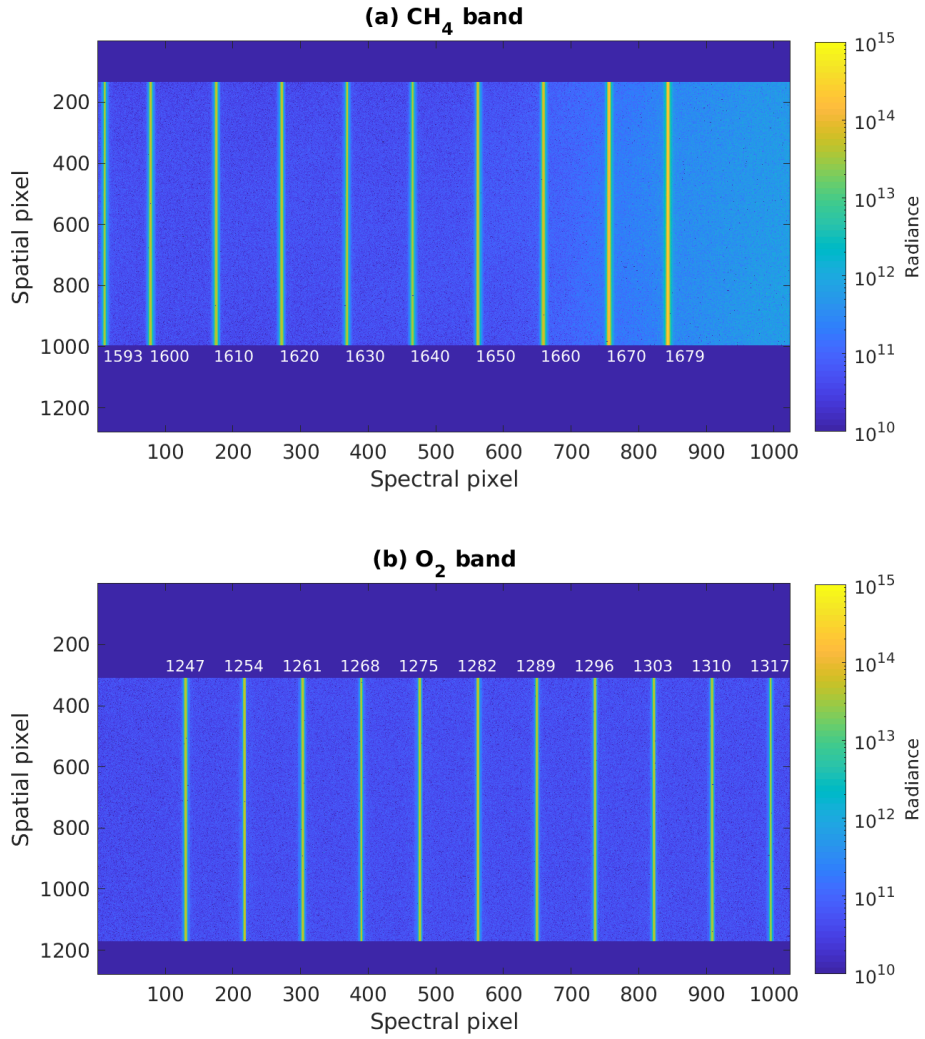
Figure 2. Responses of the focal plane arrays shown as calibrated radiance for the CH$_4$ (a) and O$_2$ band (b) over a range of laser wavelengths. The laser wavelengths in nm are labeled next to the corresponding slit images. The radiance is in photons s^{-1} cm^{-2} nm^{-1} sr^{-1}.
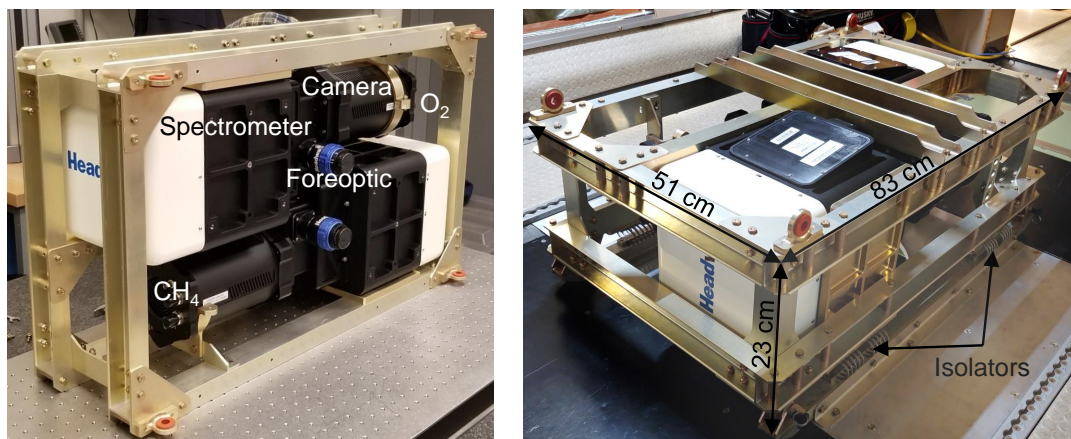
Figure 3. MethaneAIR instrument rack, side view (left) and down-looking configuration in the GV aircraft (right).
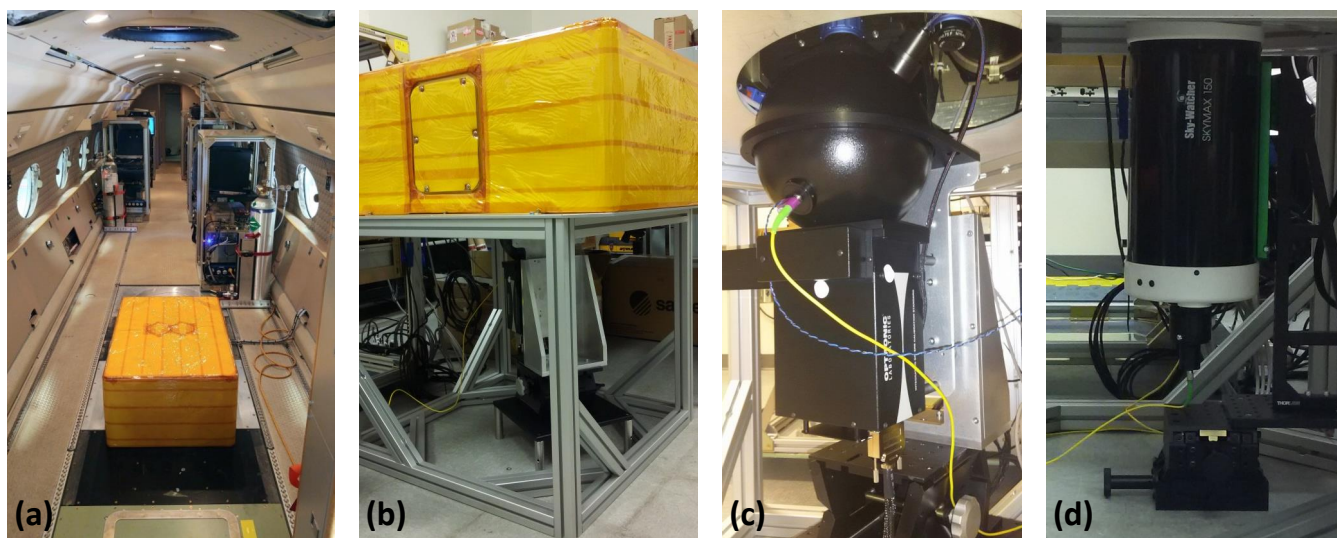

Figure 4. During flight (a) and calibration (b), the instrument is mounted in the same orientation and controlled to the same temperature by the yellow thermal housing. An integrating sphere (c) is used to perform non-uniformity and ISRF calibration, while a collimator (d) is used for stray light measurements.

the lamp. The aperture area was tied to the manufacturer calibration value using a photodetector mounted on the wall of the sphere. Saturated values were identified by plotting signal level as a function of exposure time and finding the "knee" where the response became nonlinear. For almost all pixels, this occurred within a few hundred counts of 10,000 DN. Flat field data were taken at exposure times of 50, 100, and 150 ms, matching the exposure times used in flight and in the ISRF calibration. The resulting , and the dark frames were subtracted. This resulted in curves of spectral radiance (phot s^{-1} cm^{-2} sr^{-1} nm^{-1}) vs. dark-subtracted focal plane intensity (DN s^{-1}) for each exposure time and every active pixel. These radiometric calibration

curves were fitted by fifth-order polynomials with the intercept forced to be zero. The zero intercept is necessary to guarantee zero radiance at zero DN. The resultant coefficients were used to correct pixel-to-pixel non-uniformity in the stray light and ISRF data. A separate linear (gain-only) calibration was used to flag defective pixels. Bad pixels were identified as those with a dark value more than 3-sigma from the mean or a gain value outside thresholds determined by visual inspection of the gain distribution. Bad pixels made up 0.19% and 0.055% of the active area of the O_2 and CH_4 FPAs, respectively.

3.1   Stray light measurements

Stray light measurements were made by systematically illuminating individual points on the focal plane and quantifying the light detected elsewhere on the detector. Preliminary stray light measurements used a 150 mm diameter f/12 Maksutov-Cassegrain telescope (Figure 4d) to collimate the incoming light. A 100 μm pinhole placed at the focus of the telescope was illuminated using fiber-coupled tunable lasers (SANTEC TSL-550s; one for O_2 and one for CH_4). The ~~laser~~ wavelength stability of the CH_4 laser is ±5 pm, and the optical power is +1.2%/-0.9%. For the O_2 laser, the wavelength stability is +5/-6 pm, and the optical power is +1.1%/-0.5%. The laser line width is 40 MHz, three orders of magnitude lower than the instrument spectral resolution, and hence the laser is considered as a delta function in wavelength space. At the slit, the image of the pinhole fit within 12×12 μm (equivalent to one FPA pixel).

At each sampled spatial position the tunable laser was stepped across the passband in increments of 0.5 nm. The collimator was mounted on a goniometer stage and manually repositioned to sample three angles along the slit ($0°$, $-7°$, $+9°$ in CH_4 band; $0°$, $-5°$, $+10°$ in O_2 band). Exposure times of 10 ms, 100 ms, and 1000 ms were combined for high dynamic range, and one additional exposure was made at 1000 ms while increasing the laser power by a factor of 10 (Figure 5a-d). Background measurements were made by temporarily closing a shutter internal to the tunable laser and subtracted from each individual exposure.
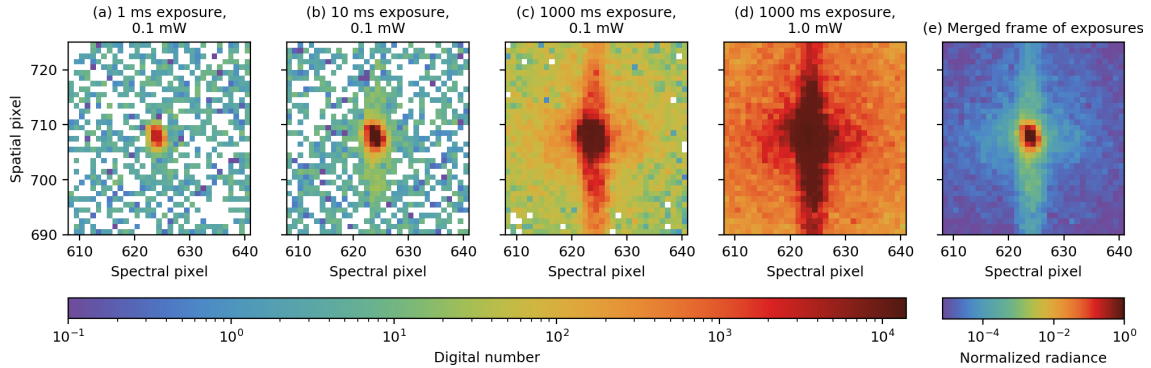

Figure 5. Individual frames with different exposure times in ms and listed laser power in mW (a-d) are combined to create the resulting normalized merged frame (e). At shorter exposure times, the peak is well defined, but the floor is dominated by measurement noise. Longer exposure times allow for characterization of the floor, but the peak and its surrounding area become saturated.

~~Future improvements to the measurement setup will~~ The measurements described above are preliminary and were used primarily to develop the stray light correction algorithm. In the near future, the stray light will be measured with higher precision and an updated correction will be derived. Improvements to the measurement setup are currently underway and include automated tilt and translation stages to address many more field angles and an all-reflective collimator to avoid stray reflections from the refractive corrector plate. ~~The~~ In addition, the pinhole will be replaced with a 100 μm slit oriented perpendicular to the spectrometer entrance slit, in order to fill the width of the spectrometer slit while providing a point source in the across-track dimension.

3.2 ISRF measurements

ISRF measurements used the same tunable lasers as the stray light measurements. Each laser was coupled to the integrating sphere (Figure 4c) in order to uniformly illuminate the slit at a single wavelength. An 8000 RPM vibration motor was attached to the fiber near the integrating sphere to avoid coherence effects in the image. The O_2 laser was stepped from 1247 nm to 1317 nm in increments of 7 nm, and the CH_4 laser was stepped from 1593 nm to 1679 nm in increments of at most 10 nm (see Figure 2). The vicinity of each center wavelength was finely sampled by scanning the laser ±0.1 nm from the central wavelengths in steps of 0.005 nm. The 1247 nm central wavelength step was discarded in following analysis because it is right at the edge of the laser wavelength cut off. In the CH_4 band, the laser power was increased ~~at long wavelengths to compensate for the decrease in QE~~ progressively from -3.0 dBm at wavelengths $\leq$1640 nm, up to +2.5 dBm at 1670 nm, in order to maintain high SNR as the QE decreased at longer wavelengths. Both spectrometers recorded data with a fixed exposure time of 50 ms.

~~Responses of the focal plane arrays shown as calibrated radiance for the CH_4 (a) and O_2 band (b) over a range of laser wavelengths. The laser wavelengths in nm are labeled next to the corresponding slit images. The radiance is in photons s^{-1} cm^{-2} nm^{-1} sr^{-1}.~~

4 Stray light correction

Stray light correction for MethaneAIR follows an approach similar to the method set forth by Tol et al. (2018) for the TROPOMI SWIR spectrometer. This method will also be applied to MethaneSAT, incorporating lessons learned from MethaneAIR. Preliminary processing of the stray light measurement data includes masking bad pixels and subtracting dark current. Radiometric calibration is applied to convert from digital number per second to radiance, and each frame is normalized by its corresponding laser power. Multiple frames at a given position on the FPA can then be combined into a single merged frame, as shown in Figure 5e. Merging different exposures allows for a more complete characterization of stray light structure since the peak is defined but the floor is incomplete at short exposures, and at longer exposures, the floor is defined while the peak area is saturated. A 2D Gaussian function is fitted to each merged frame to identify the central spatial and spectral position of the peak. The identified spectral peak positions were analyzed as a potential supplement to ISRF measurements for wavelength registration, but were ultimately found to be too noisy for this purpose. The partial illumination of the slit resulting from the use of the pinhole in the measurement setup likely contributed to the noise by distorting the spectral response.

All merged frames are interpolated to a common grid of spatial and spectral pixels that are relative to peak position obtained from the 2D Gaussian fitting. The stray light structure observed in the merged frames is generally consistent for different positions on the FPA. The only notable exceptions are spatial stray light features that are up to 10^{-4} of the peak. These features, which appear in the tails of the spatial stray light profile, exhibit no apparent pattern relative to spatial position. That is, spatial stray light features at one spatial pixel were not observed in the profile measured at a nearby spatial pixel. Such inconsistency suggests that these features are not internal to the instrument, but likely originated from the reflections from the refractive corrector plate within the collimator. As such, data displaying what appear to be spatial artifacts of the test setup are removed via replacement with NaN values. Since stray light measurements were taken for three spatial positions, at least one other spatial position that does not exhibit the observed artifact still supplies data at the replaced point. After excluding these spurious spatial stray light data points, all merged frames are stacked together and the median is determined to produce a common kernel function for the entire FPA. This process ideally gives a stray light kernel that is up to four times larger than the FPA. However, due to the limited spatial swath angles, the regions near the spatial dimension edges are often subject to excessive noise. The spectral coverage in the CH_4 band is further limited by the QE drop towards the long wavelength. As such, we limit the stray light kernel to be within ± 400 pixels for both spatial and spectral dimensions.

The median stray light kernels for both the CH_4 and O_2 bands are depicted in Figure 6, where it may be seen that the peaks are separated from the noise floor by over six orders of magnitude. For use in the stray light correction algorithm, the kernel is normalized such that all elements sum to unity. A central area of 11 spatial pixels by 15 spectral pixels is then set equal to zero. This window is determined by the extent of the ISRF in the spectral dimension and the width of the spatial response function in the across-track dimension. The kernel with the central region masked as zeros is now referred to as the far-field kernel ($\mathbf{K}_{\text{far}}$), which defines where stray light correction will be applied. The sum of the far-field kernel is 2.4% for the CH_4 band and 2.1% for the O_2 band. This indicates that the stray light is small relative to the useful signals at each spatial and spectral position.

The correction algorithm is rooted in the idea that a measured frame can be viewed as an ideal frame convolved with $\mathbf{K}_{\text{far}}$. Therefore, to correct the stray light, an iterative deconvolution algorithm is used, based on Van Cittert deconvolution (Tol et al., 2018). The correction is a redistribution rather than a removal of light in a given frame. As given by Tol et al. (2018), the frame ($\mathbf{J}$) after iteration i is

$$\mathbf{J}_i = \frac{\mathbf{J}_0 - \mathbf{K}_{\text{far}} \otimes \mathbf{J}_{i-1}}{1 - \sum_{k,l}(\mathbf{K}_{\text{far}})_{k,l}} \tag{1}$$

where $\mathbf{J}_0$ is the measured input frame and $\otimes$ denotes 2D convolution that is implemented through Fast Fourier Transform (FFT) in the astropy Python library. Three iterations were used after finding that a greater number did not significantly alter the correction results.

The stray light correction was relatively small for both MethaneAIR bands, approximately 2: 2.4% of total detected light for CH_4 and 2.1% for O_2. A comparison of the slit images on the CH_4 and O_2 FPAs before and after applying the stray light correction is shown in Figure 7. The slit images appear in sharper contrast with the noise floor after correction, and the spectral stray light beyond the 15-pixel window is substantially reduced.
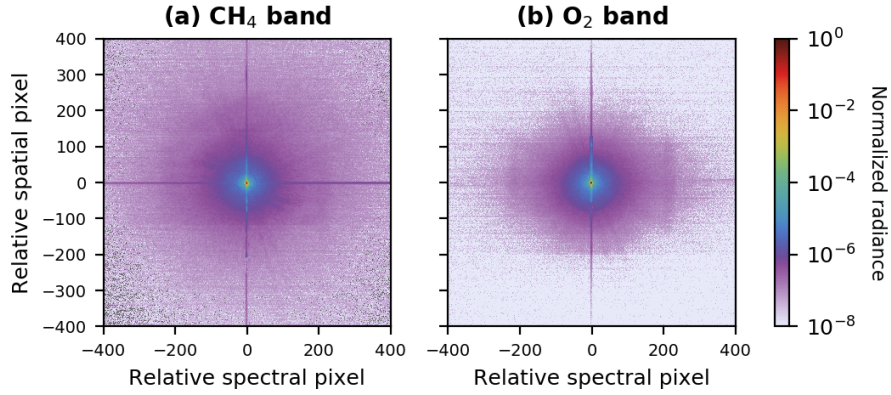
Figure 6. Median stray light kernels for (a) CH_4 and (b) O_2 bands. Multiple merged frames were interpolated to a common spatial/spectral pixel grid before taking the median of all frames to produce the kernels for use in the stray light correction algorithm.
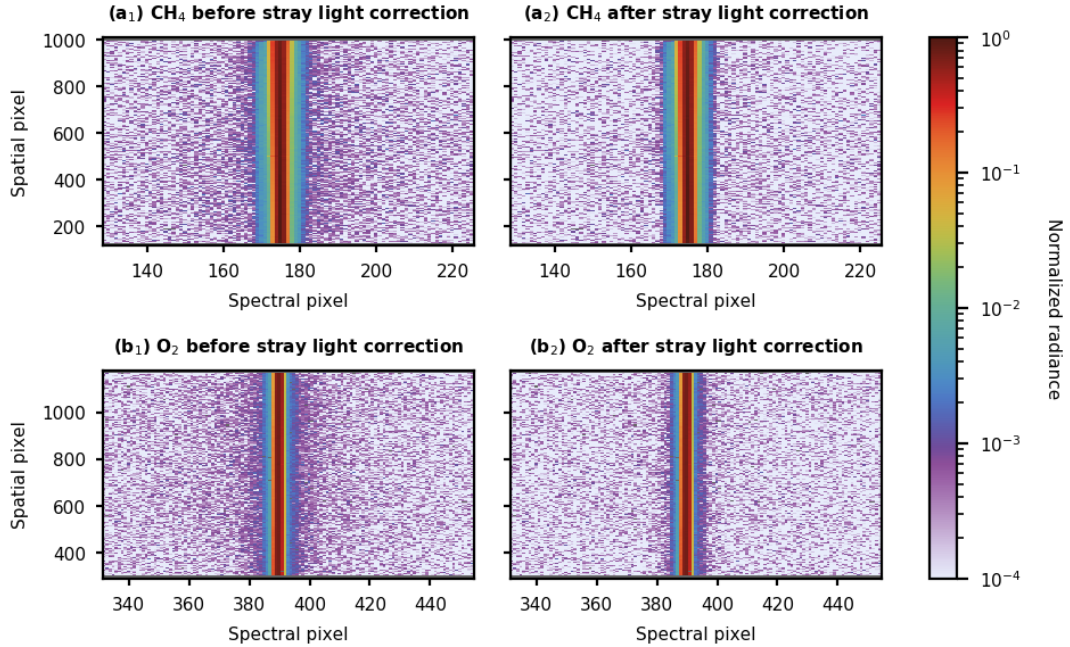

Figure 7. Slit images on the FPA, as given by normalized radiance before (a_1, b_1) and after (a_2, b_2) applying stray light correction. After correction, the slit image at each row (i.e., spectral pixels at a given spatial pixel) is effectively an ISSF as discussed in Section 5.

5 Construction of ISRF

5.1 Oversampling ISSF

The laser wavelength scans shown in Figure 2 yield a series of instrument spectral spread functions (ISSFs) positioned around selected central wavelengths for each spatial pixel in each band. Since each ISSF corresponds to a wavelength, there is theoretically an infinite number of ISSFs. In contrast, there is a single ISRF for each spectral pixel, defining the response of that pixel to light of different wavelengths. The relationship between the ISSF and ISRF is depicted in Figure 8a. Each ISSF extends over multiple spectral pixels and is comprised of samples from the ISRFs of these spectral pixels. ~~It is assumed that the ISRF does not vary significantly over a small sample of spectral pixels~~ The ISRF variation between spectral pixels within a small wavelength window (±0.1 nm) is negligible. Therefore, the ISSF can be viewed as a sparsely sampled version of a representative ISRF (van Hees et al., 2018). By measuring a series of ISSFs with small wavelength steps surrounding a central wavelength and manipulating the frames to align, an oversampled ISSF can be constructed. As shown in Figure 8b for a given central wavelength and spatial pixel, the oversampled ISSF, constructed from rows in Figure 8a, is the mirror image of the oversampled ISRF, constructed from columns in Figure 8a. We determine the ISRF by oversampling the ISSFs because it enables better corrections of laser power and wavelength fluctuation.
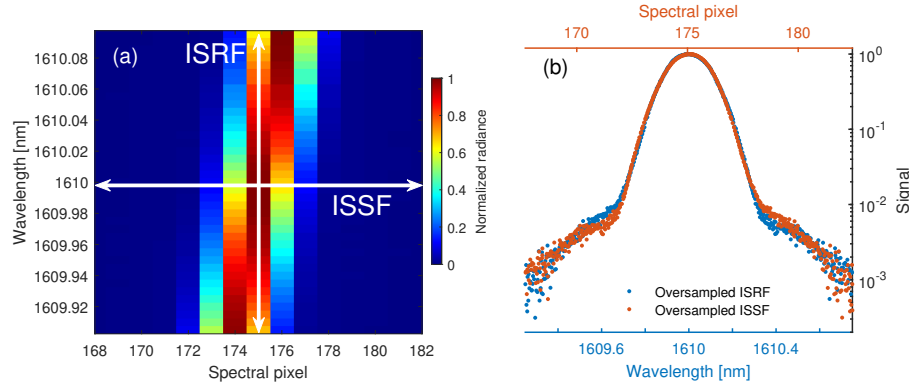

Figure 8. (a) Illustration of ISRFs and ISSFs near 1610 nm through the spectral responses of the row that corresponds to spatial pixel 300 of the CH$_4$ FPA. The laser was scanned from 1609.9 nm to 1610.1 nm with a step size of 0.005 nm. (b) Oversampled ISSF and ISRF. The horizontal coordinate of spectral pixel (for ISSF) is aligned with wavelength (for ISRF). The oversampled ISSF will match the ISRF if the profile shown is flipped (not shown here) and the spectral pixel coordinate is projected to wavelength space.

An iterative approach is used to construct the oversampled ISSF, starting with a series of individual ISSFs obtained by stepping the laser at 0.005 nm increments ±0.1 nm from a given central wavelength. Figures 9a and 10a exemplify a set of measured ISSFs at one central wavelength and spatial pixel in each band. For each laser wavelength step, the center of mass and total mass of the corresponding ISSF are calculated. The centers of mass and laser wavelengths are used in an orthogonal linear regression to obtain a spectral pixel-wavelength registration function. To assemble the first oversampled ISSF, individual

ISSFs are shifted horizontally by first subtracting the calculated centers of mass from the originally defined spectral pixels at each laser step. The spectral pixel center registered at the central wavelength is then added back to all ISSFs to shift the aligned frames to the appropriate spectral pixel position. Each ISSF is also divided by its total mass to normalize the functions vertically and account for the laser power fluctuation. Figures 9b and 10b show the resulting oversampled ISSF for a specified central wavelength and spatial pixel.

The oversampled ISSFs are refined by honing the shifting and scaling constants for the ISSFs at every laser wavelength step. The center of mass and total mass of each ISSF is updated by fitting a horizontal shift and vertical scale with the oversampled ISSF constructed in the previous step. The shift and scale previously calculated are used as the initial values in this nonlinear fitting. The center spectral pixel corresponding to the central wavelength of interest is also adjusted from an updated linear fit between the new centers of mass and the set wavelength. The shifts and scaling are applied as before to assemble the improved oversampled ISSFs seen in Figures 9c and 10c. This process is repeated, though improvements after the second iteration are relatively small. Three iterations are shown for demonstration, but a total of four iterations were conducted. The spectral pixel centers from the final iteration are saved for analysis of wavelength registration (Section 6).

After this iterative process of shifting and scaling, there is an oversampled ISSF at approximately 860 spatial positions for each of the central wavelengths in each band. In order to convert the oversampled ISSF to ISRF, the profile is flipped about its center of mass, and the horizontal coordinate is mapped from spectral pixel space to wavelength space using the wavelength registration curve fitted in the last iteration. The ISRFs are then linearly interpolated to a common wavelength grid defined from relative wavelength -0.75 to 0.75 in 0.005 nm intervals. The spectral calibration of MethaneSAT will follow and build upon the method of ISRF determination presented here for MethaneAIR.

5.2 Smoothed ISRF results

The ISRFs constructed from the oversampled ISSF data are noisy at the tails, as seen in Figure 11. Structures in the tails are inconsistent across spatial pixels and central wavelengths, so it is beneficial to smooth out these random features while preserving the ISRF shape at the core. Various analytical functions were tested to fit the ISRFs, including the TROPOMI ISRF model described in van Hees et al. (2018), but they cannot provide sufficient fitting accuracy across all measurement positions in both MethaneAIR bands. Instead, a Savitzky-Golay filter is implemented, which fits a local polynomial to a subset of data in a moving window (Savitzky and Golay, 1964). A filter of order 3 with a window length of 40 points on either side of the the central point is used, i.e., a 3.40.40 filter. The Savitzky-Golay filter was found to effectively avoid peak flattening and provide superior processing speed compared to other filters (e.g., penalized spline and robust lowess smoothing). Applying the filter once smoothed the tails fairly well, as demonstrated by the red lines in Figure 11. Still, there is room for improvement after the first pass, particularly in the O_2 band. In order to achieve a smoother result, an iterative version of the ~~Savitzy-Golay~~ Savitzky-Golay filter is devised. This filter works by calculating the residuals between the logs of the raw data and the smoothed lines after an initial application of the filter. At locations outside of the core where the residuals are higher than a specified threshold, the ISRF data points are replaced by the filtered result. The same filter is then applied again to the updated set of ISRF data, and residuals are again calculated. With each iteration, the residual threshold for replacement is decreased. The
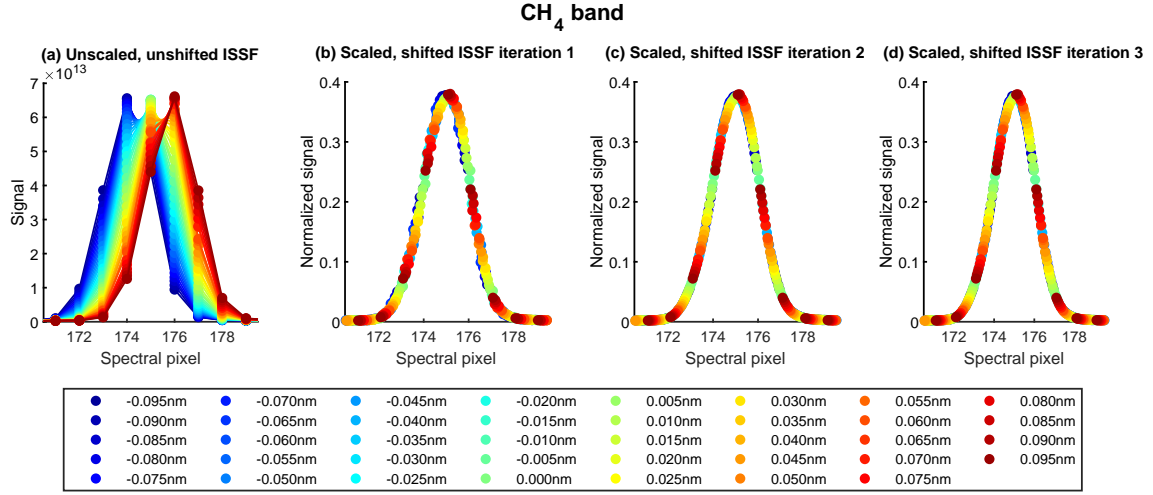
CH$_4$ band

(a) Unscaled, unshifted ISSF

(b) Scaled, shifted ISSF iteration 1

(c) Scaled, shifted ISSF iteration 2

(d) Scaled, shifted ISSF iteration 3

● -0.095nm	● -0.070nm	● -0.045nm	● -0.020nm	● 0.005nm	● 0.030nm	● 0.055nm	● 0.080nm
● -0.090nm	● -0.065nm	● -0.040nm	● -0.015nm	● 0.010nm	● 0.035nm	● 0.060nm	● 0.085nm
● -0.085nm	● -0.060nm	● -0.035nm	● -0.010nm	● 0.015nm	● 0.040nm	● 0.065nm	● 0.090nm
● -0.080nm	● -0.055nm	● -0.030nm	● -0.005nm	● 0.020nm	● 0.045nm	● 0.070nm	● 0.095nm
● -0.075nm	● -0.050nm	● -0.025nm	● 0.000nm	● 0.025nm	● 0.050nm	● 0.075nm	

Figure 9. Demonstration of ISSF oversampling for the CH$_4$ band using a central wavelength of 1610 nm and spatial pixel 500. The laser was scanned in 0.005 nm steps over a range corresponding to the central wavelength $\pm$ 0.095 nm. The resulting series of individual ISSFs (a) are then shifted and scaled to produce a single oversampled ISSF (b). Successive iterations of shifting and scaling (c, d) are performed to construct smoother oversampled ISSFs, which can then be mapped from pixel space to wavelength space for ISRF analysis.
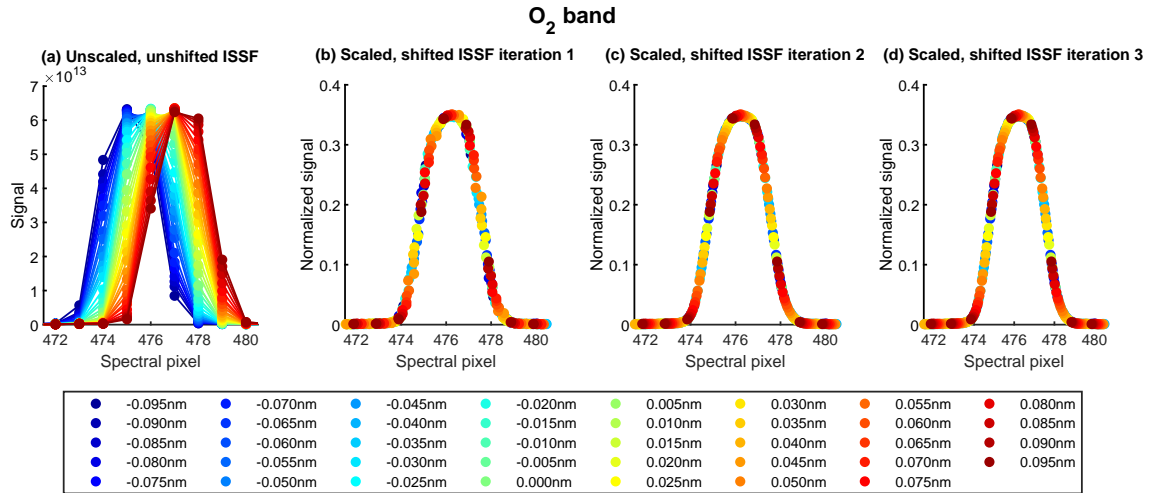
O$_2$ band

(a) Unscaled, unshifted ISSF

(b) Scaled, shifted ISSF iteration 1

(c) Scaled, shifted ISSF iteration 2

(d) Scaled, shifted ISSF iteration 3

● -0.095nm	● -0.070nm	● -0.045nm	● -0.020nm	● 0.005nm	● 0.030nm	● 0.055nm	● 0.080nm
● -0.090nm	● -0.065nm	● -0.040nm	● -0.015nm	● 0.010nm	● 0.035nm	● 0.060nm	● 0.085nm
● -0.085nm	● -0.060nm	● -0.035nm	● -0.010nm	● 0.015nm	● 0.040nm	● 0.065nm	● 0.090nm
● -0.080nm	● -0.055nm	● -0.030nm	● -0.005nm	● 0.020nm	● 0.045nm	● 0.070nm	● 0.095nm
● -0.075nm	● -0.050nm	● -0.025nm	● 0.000nm	● 0.025nm	● 0.050nm	● 0.075nm	

Figure 10. Demonstration of ISSF oversampling for the O$_2$ band at a central wavelength of 1275 nm and spatial pixel 500. ISSF processing is as described in Figure 9.

numbers of iterations used for the CH_4 and O_2 bands are five and six, respectively. The result of the iterative filter shows fewer defined features in the tails, as shown in Figure 11. ~~Values~~ Since values in the smoothed ISRF beyond ± 7.5 pixels from the center ~~are set equal to zero since these values~~ should be taken care of by the spectral stray light correction as described in Section ~~4.~~ 4, these values are set equal to zero. This area corresponds to pixels outside of the central wavelength ± 0.75 nm and ± 0.6 nm in the CH_4 and O_2 bands, respectively. The ISRF is then normalized so that it integrates to unity.

After ~~examining the variation of the filtered~~ applying the Savitzky-Golay filter to the ISRF across all spatial and spectral pixels, ~~it was evident that additional smoothing was required for~~ a small number of ~~pixels~~ ISRFs (74 ~~pixels~~ out of 7767 in the CH_4 band, ~~and~~ 87 ~~pixels~~ out of 8630 in the O_2 band) exhibit anomalous widths by way of sharp contrasts with their neighbors, presumably due to insufficient bad pixel removal. By nature, the ISRF shape should vary smoothly between spatial and spectral pixels. ~~However, some pixels exhibited anomalous behavior by way of sharp contrasts with neighboring pixels.~~ ~~The performance of these atypical pixels was irregular enough to be noticeable in the ISRF results, but not poor enough to be flagged in the bad pixel map~~ Due to the sparse ISRF measurements in the spectral dimension, it is desirable to remove those outliers to avoid inference to a broad wavelength range. To remove the effects of these remaining anomalous pixels, a median filter was first applied to the spatial and spectral dimensions of all ISRFs, which are assembled to a table defined in spatial, spectral, and relative wavelength dimensions. The median filter window sizes are 5 elements in the spatial and 3 elements in the spectral dimension. The root-mean-square error (RMSE) between the original ISRF table and the median filtered ISRF table was calculated to define outliers with RMSE greater than three standard deviations from the mean for each central wavelength. Then, only ISRFs at outlier locations were replaced with the median filtered version. Due to the higher noise levels accompanying the decrease in QE at higher wavelengths in the CH_4 band, pixels at 1670 nm were not included in the replacement. Exceptions were also made at specific spatial pixel indices in both bands where real slit shape characteristics were seen to cause significant irregular features, which is discussed in greater detail with the wavelength registration (Section 6).

Examples of the smoothed ISRF shapes after Savitzky-Golay filtering and outlier smoothing are given in Figures 12 and 13. Non-smooth features at 10^{-3} level remain over some ISRF tails at log scale due to detector noise that cannot be fully suppressed. Figure 14 displays the ISRF full width at 20%, 50%, and 80% of peak height, conveying the variation in ISRF shapes in both bands across the FPA. As shown by the figures, the ISRF is often asymmetric at both the core and the tails. The ISRF is broader and more triangular in the CH_4 band compared to the O_2 band. Additionally, the shape tends to grow wider with increasing spatial and spectral indices in the CH_4 band, as seen in Figure 14a-c. In contrast, the O_2 band exhibits much less variation, indicated by the relatively narrow color ranges in Figure 14d-f. The smoothed ISRFs are saved to produce a three dimensional lookup table defined for each illuminated spatial pixel, each central wavelength, and a relative wavelength grid from -0.75 nm to 0.75 nm with 0.005 nm steps for each ISRF. The ~~use of only~~ spectral variation of the ISRF at ~ 10 central wavelength positions ~~in the table rather than all spectral pixels is enabled by the smooth~~ ~~spectral~~ is smooth, making it possible to interpolate the ISRF along the spectral dimension to all possible wavelengths. However, the spatial variation of the ISRF ~~;~~ ~~all spatial positions are defined due to more irregular spatial variation~~ is significant due to the slit width irregularity.
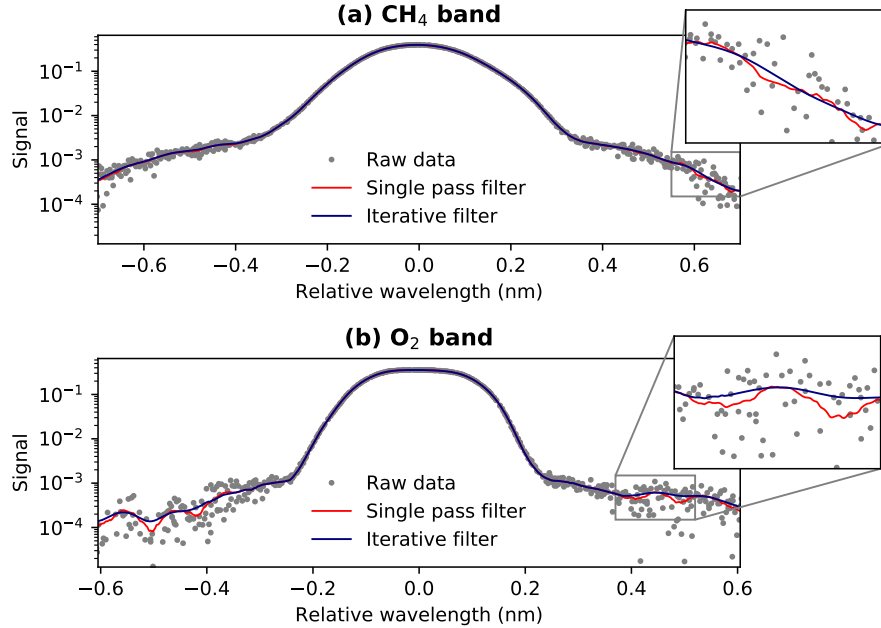
Figure 11. Demonstration of the iterative Savitzky-Golay filter used to smooth ISRF measurement data in the CH_4 (a) and O_2 (b) bands. One application of the filter, shown in red, was fairly effective, especially for the CH_4 band. Successive iterations applied to the residuals at the tails provided additional smoothing while preserving the ISRF shape at the core, as indicated by the blue line.

6 Wavelength registration

The ISRF construction process as previously described resulted in spectral pixel centers that correspond to the laser central wavelengths labeled in Figure 2. Those spectral pixel-wavelength relationships are determined with high accuracy for all illuminated spatial pixels. It is possible to derive the wavelength registration function for each spatial pixel by independently fitting the spectral pixel centers vs. laser central wavelengths. However, we noticed some outliers that are caused by either inadequate filtering of bad pixels or the deficiency in the ISRF after a significant number of pixels are removed as bad pixels, as shown in Figure 15. To prevent the impact of those localized outliers from propagating to the wavelength calibration curves that cover the full spectral range, we apply an additional smoothing to the spectral pixel centers as described in the following. For each central wavelength, the median is removed from the spectral pixel centers of all spatial pixels, and the resultant relative spectral pixel values are highly consistent for all central wavelengths, as shown by the dots in Figure 15. The fine scale structures in the spatial dimension likely originate from irregularities of the slit along its length. Such structures are most easily seen near spatial pixel 505 in the CH_4 band and spatial pixel 780 in the O_2 band. Those structures are also observable in the ISRF widths shown in Figure 14. The medians along the wavelength dimension are then taken from the combined relative spectral pixel values of all wavelengths, represented by the black lines in Figure 15. These series of median values remain largely unaffected by the random noise or outliers at individual wavelengths while preserving the structures that are common
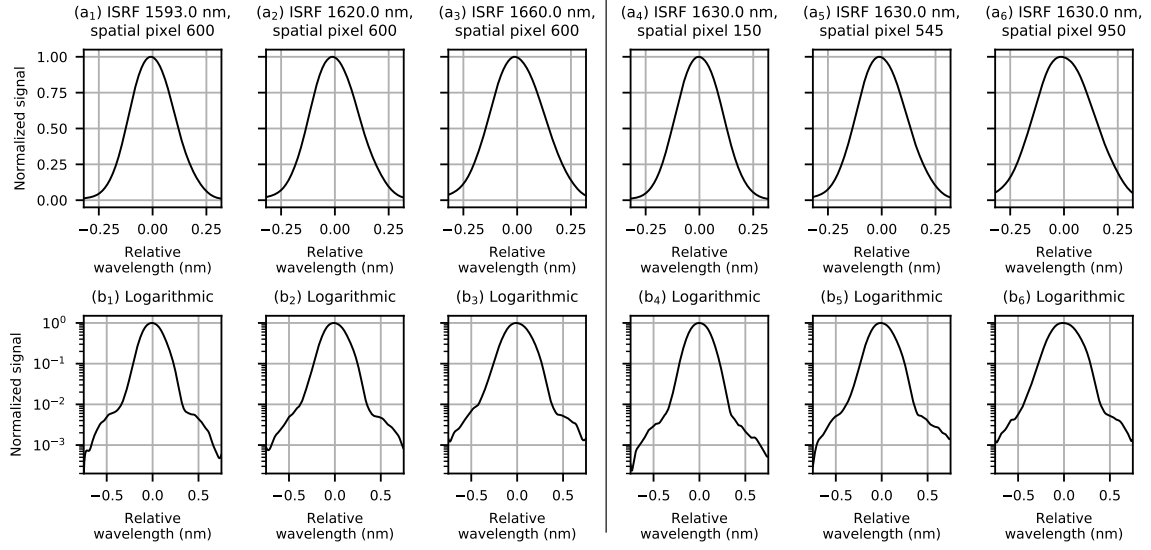
Figure 12. ISRF shapes at various positions for the CH_4 band. The first three panels (a_1-a_3) demonstrate the variation in shape for different central wavelengths at a constant spatial position, while the rightmost three panels (a_4-a_6) hold central wavelength constant to show ISRF changes across spatial pixels. The bottom row of panels (b_1-b_6) displays the same data on a logarithmic scale and wider relative wavelength range. The ISRFs are normalized so the maximum is unity.

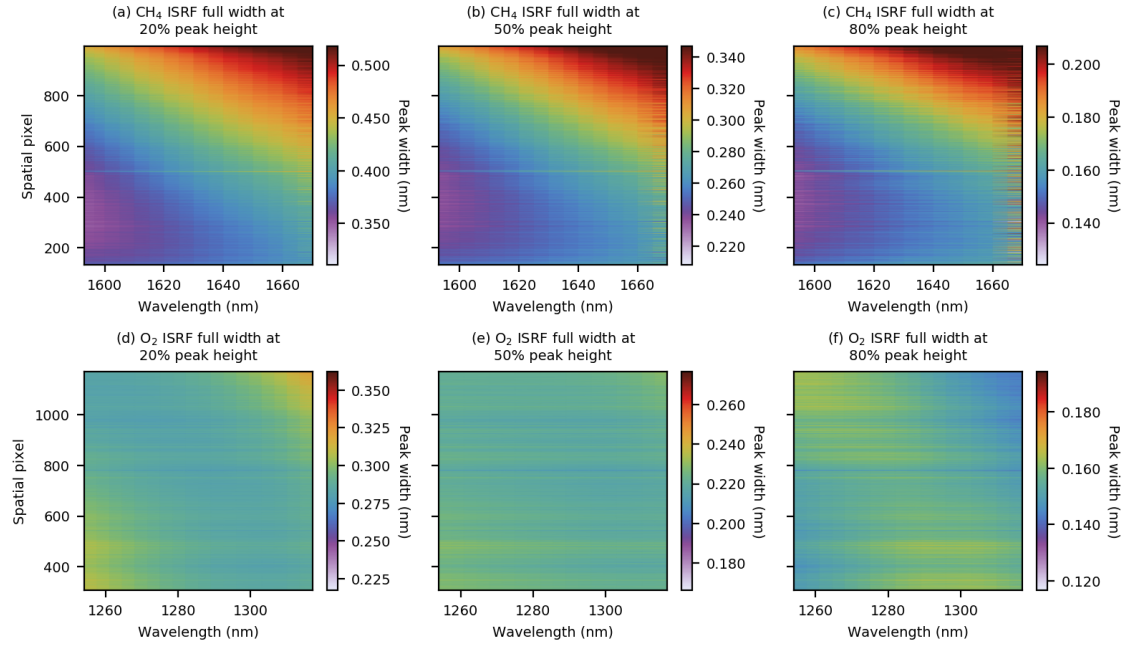**Figure 13.** Similar to Figure 12 but for the O_2 band.

Figure 14. Full width of the smoothed ISRF at 20% (a,d), 50% (b,e), and 80% (c,f) of maximum peak height for all spatial and spectral pixels. Gouraud shading is applied to render smooth ISRF variation across the FPA. Wavelength labels have been projected to the abscissa in order to provide more context compared to the spectral pixel index. The top three panels correspond to the CH_4 band, which shows a general broadening of the ISRF with increasing wavelength and spatial pixel index. In contrast, the O_2 band ISRF is more homogeneous across different spatial and spectral pixels, as reinforced by the relatively narrower scales for the bottom three panels. The color limit in each panel is fixed at $\pm 25\%$ from the FPA-mean value.

to all wavelengths. Finally, a linear fit is made between those median values and the spectral pixel center values for each center wavelength, and the predicted spectral pixel center values, which are smooth and free of outlier points, are used in the final wavelength calibration.

In both bands, a polynomial fit is applied to the smoothed spectral pixel centers as a function of wavelength. This is necessary to map spectral pixel to wavelength at locations between the measured points. As shown by the bottom panels of Figure 16, the residuals for various polynomial degrees are quite similar, and less than approximately 0.02 spectral pixel. For clarity, only first through fourth order polynomial residuals are plotted, but higher orders, up to and including seventh, were tested. A first order polynomial was selected as the optimal model for both bands, in accordance with the Akaike information criterion (AIC) (Akaike, 1974) and Bayesian information criterion (BIC) (Schwarz, 1978). The linear fit between spectral pixel index and wavelength is shown in the top panels of Figure 16.
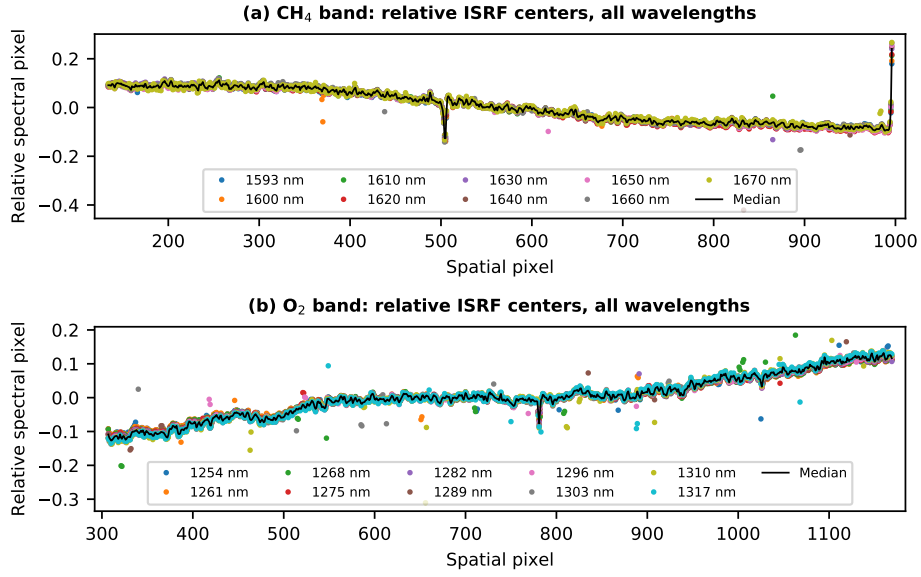
Figure 15. For each wavelength, the spectral pixel center at every spatial pixel is shifted to align all wavelengths for a given band. The median of the combined data is taken (black line), resulting in a smoothed version of the central spectral pixel indices for all spatial pixels. Variations common to all wavelengths, such as the feature near spatial pixel 505 in the CH_4 band (a) are preserved in the smoothing. These are real features, likely due to irregularities in the slit width.
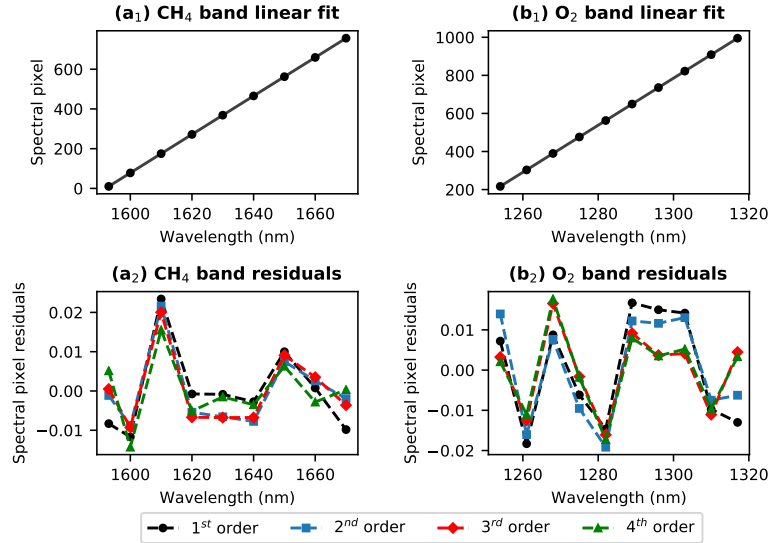

Figure 16. Wavelength registration fitting results for CH_4 (a) and O_2 (b) bands, demonstrated for spatial pixel 600. Top panels show a linear fit to the data, which was determined to be the optimal polynomial order by AIC and BIC. Residuals from first through fourth order polynomial fits are given in the bottom panels.

7 Flight spectra demonstration

335 Here we evaluate the performance of the on-ground MethaneAIR calibration using radiance spectra from the first instrument flight over a clean region of the Colorado Front Range, using the optimal-estimation-based (Rodgers, 2000) retrieval algorithm being developed for MethaneAIR/MethaneSAT (Chan Miller et al., 2018). The flight coverage began at 15:51:29 UTC and ended at 19:40:46 UTC on 11/8/2019. Further detailed description of the algorithm will be provided in future publications on MethaneAIR retrieval. The Level 0 detector signals are converted to Level 1b radiance spectra through dark current subtraction,
340 bad pixel removal, radiometric calibration, and stray light correction in a similar way as the ISRF calibration data. In addition, the wavelength-dependent viewport window transmittance is corrected. Fits for spectra in the O_2 and CH_4 bands are used for cloud filtering and CH_4/CO_2 proxy retrieval, respectively. The algorithm settings are summarized in Table 2. Scattering is neglected in both retrievals; A reasonable assumption since Rayleigh scattering is negligible, and aerosol loadings during the flight were low (observed 1640 nm aerosol optical depths were < 0.01 at the AERONET NEON-CPER site, close to the flight
345 path).

Table 2. MethaneAIR Level 2 algorithm fit settings

State Vector Element	A Priori	Error	O_2 Band[1]	CH_4 Band[2]
CH_4 Profile	TCCON GGG2020[3]	Altitude-correlated covariance[4]	✗	✓
CO_2 Column	TCCON GGG2020	12 ppmv	✗	✓
H_2O Column	GEOS-FP[5]	0.02 v/v	✓	✓
O_2 CIA pseudo absorber	0.21 v/v	15%	✓	✗
Temperature Profile Shift	GEOS-FP	5 K	✓	✓
Surface Pressure	GEOS-FP	4 hPa	✓	✓
Albedo	Derived from observation	100%	5th order	3rd order[6]
Wavelength Offset	0.0 nm	0.01 nm	✓	✓
ISRF squeeze	1.0	0.2	Optional	Optional[6]

[1] Fit window 1249.2–1287.8 nm (O_2)

[2] Two fit windows: 1595–1610 nm. (CO_2), 1629–1654nm (CH_4)

[3] Laughner et al. (2020)

[4] 6-km vertical length scale

[5] Knowland et al. (2020)

[6] Different for CO_2/CH_4 window

Figure 17 shows spectral fits for each band for an across track position at the center of the detector. The spectra constitute a 10 s along-track aggregate of frames, taken when the flight was at cruise altitude (~12 km). Time aggregation was performed to boost signal-to-noise and mitigate the impact of inhomogeneous slit illumination on the ISRF. Applying the nominal calibration derived in this paper is shown by the blue lines, leading to fit residual RMSE of 1.12% and 0.52% in the O_2 and CH_4 bands,
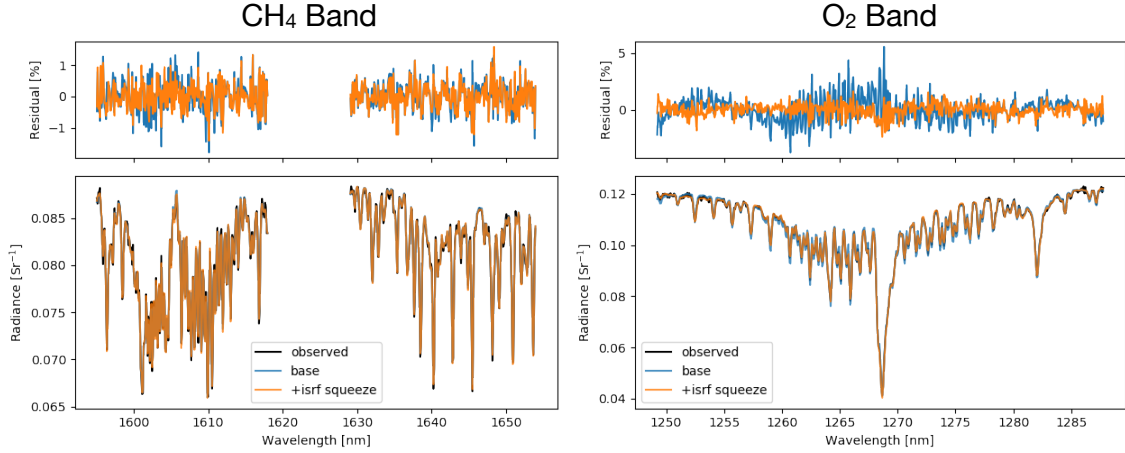350 respectively.

Figure 17. Spectral fits from MethaneAIR Research Flight 1 (11/8/2019, 18:36 UTC) using the MethaneAIR optimal-estimation algorithm. Spectra are 10 second along-track aggregates for spatial pixel 600 (approximate center of detector). Blue color indicates the fit and residual using the laboratory calibrated ISRF look-up tables, and orange color indicates the fit and residual with an ISRF squeeze parameter.

The large difference in the residuals between instruments and simulations could be due to a change in the detector focus from on-ground to in-flight especially for the O_2 spectrometer. The small F-number of both spectrometers makes the focal point sensitive to deformation of the mechanical structure. This may arise from a difference from the lab and flight environments, such as a change in the temperature of the optical bench or mechanical stress of the instrument that responds to cabin temperature and/or aircraft motion. To first order, these changes manifest as a change in ISRF width, which can be modeled by scaling the wavelength grid (λ) of the tabulated ISRF ($\Gamma_{TAB}(\lambda)$) (Sun et al., 2017) via squeeze parameter (x_{sqz}):

$$\Gamma(\lambda) = \Gamma_{TAB}(x_{sqz}\lambda) \tag{2}$$

The orange lines in Figure 17 show the improvement in spectral fits after including x_{sqz} in the retrieval state vector. The fitted x_{sqz} for the O_2/CH_4 bands for those particular across-track positions are 0.865 and 1.055, representing a broadening/narrowing of the ISRF, respectively. Accounting for changes to the ISRF width yields comparable fit RMSE for both channels (0.6% for O_2 and 0.45% for CH_4). ~~Application of the ISRF squeezing improves the fitting quality in~~ Those fitting residuals are consistent with the signal-to-noise ratio predicted by the MethaneAIR specs. The retrieved X_{CH_4} will be presented in the following algorithm paper. The spectral fitting with varying ISRF width is applied to other across-track positions ~~similarly~~throughout the flight and reveals across-track and time dependent ISRF changes. This indicates that the systematic difference between in-flight and on-ground calibration of ISRF needs to be accounted for in the retrieval algorithm. Ideally, in-flight measurements from on-board lasers would be used to update the ISRF in flight, as is done for TROPOMI (van Kempen et al., 2019). MethaneAIR and MethaneSAT are not equipped with this capability, but on-orbit ISRF monitoring is being planned by looking at targets on the earth, the airglow, and the moon for MethaneSAT.

8 Conclusions

This paper focuses on the spectral calibration of MethaneAIR including stray light correction, ISRF characterization, and wavelength calibration. The stray light was stable in both bands, allowing for the use of a position-independent median kernel in the correction algorithm based on Van Cittert deconvolution. The correction was rather minor since stray light accounted for only a small fraction of the total detected light.

The ISRF was determined by first oversampling the ISSF around roughly ten central wavelengths in each band. Each oversampled ISSF was reflected about its center of mass and projected to a fine wavelength grid to transform the profile into an ISRF. This ISSF approach, which allows for more precise correction of laser power/wavelength fluctuation, approximates the true ISRF better than direct ISRF measurements. The ISRFs were further processed by applying an iterative Savitzky-Golay filter to smooth high-frequency noise at the tails. Final ISRFs were saved to a lookup table for use in the retrieval algorithm since the shapes could not be satisfactorily modeled by an analytical function. The observed shape of the ISRF peak was more triangular in the CH_4 band compared to the O_2 band. The ISRF shape in the CH_4 band varied considerably more than in the O_2 band in both spatial and spectral dimensions. This increased variability in the CH_4 band may have been due to optical influences from the internal alignment of the instrument. In contrast, the O_2 ISRF full width at half-maximum (FWHM) was dominated by the slit width, which is essentially constant. Analysis of the wavelength-spectral pixel relationship found that a linear wavelength calibration is sufficient after reducing individual noise contributions.

The performance of the on-ground MethaneAIR spectral calibration was demonstrated using radiance spectra retrieved from an instrument flight over the Colorado Front Range. Fitting the base calibration from the ISRF lookup table to the spectra resulted in larger residual RMSE for the O_2 band than the CH_4 band, which was presumably caused by a change in detector focus in flight. Slight differences in environmental conditions between lab and flight situations could contribute to this change, embodied by an adjustment in the ISRF width. Scaling the wavelength grid of the tabulated ISRF by a constant parameter improves the spectral fit in both bands. This squeeze factor indicated a broadening of the ISRF in the O_2 band and a narrowing in the CH_4 band.

The general calibration framework as well as specific insights gained from MethaneAIR may help to advance the future spectral calibration of MethaneSAT. ~~Stray light measurement data showed that the partial illumination of the slit width distorted the ISRF.~~ In future stray light measurements, the pinhole will be replaced with a thin slit in order to fully illuminate the width of the spectrometer slit <u>and hence avoid distorting the spectral response</u>. Similarly, the MethaneAIR ISRF construction process and results can be used to inform the necessary ISSF measurement extent for MethaneSAT. Measurements at ten or so central wavelengths appears to be adequate, given that the ISRF varies smoothly in the spectral dimension. However, the degree of spatial variation seen in the MethaneAIR ISRF suggests that it is important to assess all pixels in the spatial dimension. Application of the calibration to real flight data demonstrated the possibility that the ISRF width may change between on-ground calibration and in-flight or on-orbit conditions; however, this may be compensated for by including a scaling parameter in the retrieval algorithm.

Author contributions. TEXT

Competing interests. The authors declare that they have no conflict of interest.

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