

## Reply to Reviewer #1 comments

The authors express sincere thanks to Dr. Otto Hasekamp for reviewing this research paper promptly with constructive comments and suggestions. We especially appreciate the suggestion of minimizing the number of GRASP configurations used. We now are down to one representation of land surface reflectance (Ross-Li BRDF) and two aerosol kernels. We primarily use the GRASP/Five mode kernel that allows for 15 free parameters but also use a GRASP/Models kernel with only 6 free parameters for a specific validation exercise when the AOD is low. We introduce a new figure that shows the difference in agreement with AERONET when using the different kernels in that validation exercise. For the ease of cross reading, authors responses are given under the reproduced version of each comment by Dr. Otto Hasekamp. Each of the comments from the reviewer are numbered and the changes made in the manuscript are shown using a red font under the authors response. The line numbers given in parenthesis at the end of author's comments will help the readers to locate the comments on the original manuscript submitted for discussion in AMT.

### Minor Comments

#### 1. Comment on the aerosol volume concentration (Line #21)

Changed aerosol volume concentration to aerosol column concentration.

The retrieved aerosol properties include spherical fraction (SF), aerosol ~~volume~~ column concentration in multiple size distribution modes, and with sufficient aerosol loading, complex aerosol refractive index.

#### 2. Recommended to add the Mean absolute error for the HSRL2 AOD comparison (Line #25)

Added the MAE and discussed the non-agreement caused by the edge of the plume, and the mismatch caused by the spatial sampling near the smoke source.

A good ~~correlation~~agreement with HSRL2 ( $\rho = 0.940$ ,  $-\text{BIAS} = 0.062$ ) ~~and AERONET AOD ( $0.013 \leq$~~  Mean Absolute Error (MAE)  ~~$\leq 0.017$ ,  $= 0.122$ ) and AERONET AOD ( $0.010 \leq \text{MAE} \leq 0.013$~~   $0.002 \leq -\text{BIAS} \leq 0.017$ ) measurements is observed for the collocated points. There was a mismatch between the HSRL2 and AirHARP retrieved AOD for the pixels close to the forest fire smoke source and to the edges of the plume due to spatial mismatch in the sampling. This resulted in a higher BIAS and MAE for the HSRL2 AOD comparison. For the case of AERONET AOD comparison two different approaches are used in the GRASP retrievals, and the simplified aerosol type-based kernel which retrieves fewer number of aerosol parameter performed well compared to a more generous approach in the low aerosol loading cases. Forest fire smoke intercepted during ACEPOL provided a situation with homogenous plume and sufficient aerosol loading to retrieve the real part of the refractive index (RRI) of 1.55 and the imaginary part of the refractive index (IRI) of 0.024.

#### 3. Recommendation on rephrasing (Line #36)

Rephrased the sentence in the introduction.

they directly perturb Earth's radiation budget and indirectly ~~modify~~by modifying cloud properties

4. *Add the additional reference Hasekamp et. al 2011 for the POLDER AOD retrievals (Line #73)*

Added the reference

This capability has been demonstrated by space-borne POLDER I, II and III (POLarization and Directionality of the Earth's Reflectance) (Deuzé et al., 1999, 2001; Dubovik et al., 2019; Goloub et al., 1999; Hasekamp et al., 2011; Leroy et al., 1997),

5. *Recommended to move a sentence into the theory section (Line #93-95)*

The authors prefer to keep this information in appendices and not move them to the theory section. These pages are meant as background information and rigorous completeness. They do not serve the casual reader if they appear in the flow of the main text.

6. *Commented on the unconventional naming of Section 2.1 (Line #97)*

Yes, this is a bit unconventional but conveys the meaning properly.

7. *Recommended using a more common notation for the reflectance calculated using the Stokes vector (Line #109, 113).*

Recommended change has been implemented in the manuscript, in its entirety, to use a more common notation for the reflectance.

8. *Reviewer instructed to provide the uncertainty used in retrievals for the 870 nm channel (Line #144-145)*

The uncertainty/noise level used for the 870 nm band has been added to the manuscript.

The study in this paper uses 3 % radiometric uncertainty for all the bands and 0.5 % *DoLP* uncertainty for 440 nm, 550 nm, and 670 nm and 1.5% for 870 nm as inputs to GRASP. The 870 nm polarimetric data ~~is also used in the GRASP retrievals but has larger uncertainty~~ due to lower signal-to-noise ratio in the field data compared to 440 nm, 550 nm, and 670 nm, therefore, we give these data less relative weight in the retrievals.

9. *Additional references for the standard reference frame used to calculate  $Q$  and  $U$  (Line #155)*

Thanks for pointing out this. This reference frame goes back to Chandrasekhar, Radiative transfer -1950. Additional references have been added.

The reference plane for the definition of  $\mathbf{E}_\perp$  and  $\mathbf{E}_\parallel$  is based on the local ~~meridional~~meridian plane, which is a standard reference frame used for reporting  $Q$  and  $U$  (~~Emde et al., 2015~~);(Chandrasekhar, 1950; Emde et al., 2015; Hansen and Travis, 1974; Hovenier et al., 2004).

10. *Add a hyper-link to the ACEPOL website (Line #163)*

Added a link to the ACEPOL campaign website.

The ACEPOL campaign (<https://www-air.larc.nasa.gov/missions/acepol/index.html>) was a collaborative effort of NASA and SRON (Netherlands Institute of Space Research) based out of Armstrong Flight Research Center (AFRC) in Palmdale, California, USA.

11. Change the name of the instrument from 'airborne SPEX' to 'SPEX airborne' (Line #168)

Corrected the name.

~~SPEX~~ airborne ~~SPEX~~ (Smit et al., 2019),

12. Mention the limitation of HSRL2 during ACEPOL (Line #186-189)

For this study, aerosol extinction and AOD calculated using HSRL technique were only used. Whereas, for low aerosol loading cases these parameters are calculated using an assumption of lidar ratio of 40 sr. However, this limitation of HSRL2 has been added to the manuscript.

In some ACEPOL cases, due to atmospheric turbulence, interference in the HSRL2 measurement resulted in the inability to use the molecular channels at 355 nm and 532 nm to report the AOD, and required assumed lidar ratios of 20 sr and 40 sr over the ocean and land, respectively. However, for all the comparisons shown in this study, those cases were avoided and HSRL2 AOD reported here required no lidar ratio assumptions.

13. Explain in more detail what is a kernel? and what are the parameters calculated for predefined optical and microphysical properties? (Line #219)

According to the recommendation from the reviewer added an explanation on the GRASP kernel. Described the parameters in the kernel, and the range of the size and complex refractive index used for the generation of the single scattering kernel.

Relevant changes in the Section 3.2,

For the case of aerosol measurements, the forward model consists of a polarized Radiative Transfer (RT) code to calculate the radiance measured by the instrument and it ~~also consists of a kernel to calculate the contribution of single scattering by the aerosol particles.~~ uses precalculated spheroidal kernel to calculate the contribution of single scattering by the aerosol particles following the strategy described by Dubovik et al. (2006, 2011). The kernel includes the pre-calculated full phase matrix elements, extinction and absorption for five log-normal size distributions with preselected size parameters for the range of real refractive index 1.33 to 1.7, and 0.0005 to 0.5 for the imaginary part of the refractive index for both spherical and non-spherical aerosol approximated by a mixture of spheroids with a fixed particle shape distribution derived in Dubovik et al., 2006. This approach allows for very fast and accurate calculations aerosol single-scattering properties in the wide range of refractive indices even for non-spherical aerosol. The details of the application of the kernels to satellite polarimetry are discussed in detail by Dubovik et al., 2011 (e.g. see Section 3.1, and Fig.4 in Dubovik et al., 2011).

14. Do you use  $I$ ,  $q$ ,  $u$  or  $I$  and DoLP for the retrievals in this paper? (Line #230)

For the demonstration of fit using individual pixels from the different land surfaces,  $R_i$ ,  $q$ ,  $u$  are used. For the AERONET and smoke case analysis on  $R_i$  and DoLP are used for the GRASP fit.  $q$  and  $u$  calculated using the AirHARP is sensitive to the local meridian plane definition. Any error in the rotation of  $q$  and  $u$  will affect the retrieval and to avoid the extra source of uncertainty,  $R_i$  and DoLP are used for the large scale retrievals. One exception is that for the ocean pixel study using the flight leg on 23-October-2017 T21:30 UTC we have used  $R_i$ ,  $q$ , and  $u$  for the retrieval. This flight leg has been thoroughly quality checked for the error in the rotation of  $q$  and  $u$  from the instrument reference plane to the local meridional

plane. Throughout the manuscript, it has clearly mentioned which variables are used for the GRASP retrievals.

Changes implemented in Section 3.2,

For the AirHARP observations,  $\mathbf{f}^*$  is a vector containing information of  $R_i$ ,  $Q/I$ , (same as  $R_Q/R_I$ ), and  $U/I$  (same as  $R_U/R_I$ ) or  $R_i$  and  $DoLP$  for all the spectral bands and viewing angles. GRASP is able to accept different configurations of the input parameters to make its retrieval. We will use the following sets of input in this work in different situations:  $(R_i, Q/I, U/I)$ , or  $(R_i, DoLP)$ . The text will explicitly state the inputs in each instance.

15. A well-known feature of GRASP is the multi-pixel retrieval capability, but it seems you are not using that. It would be good to mention this explicitly. (Line #240-243)

Added a sentence stating that we haven't used the multi-pixel capability of GRASP in this study.

GRASP can perform retrievals using multi-pixel information in both spatial and temporal dimensions, however, in this study, we are not utilizing this feature due to the limited availability of data over the same place in the temporal dimension.

16. What is the relation between log-normal error distributions and the Levenberg-Marquardt method? (Line #247-249)

Thanks to the reviewer for pointing this out. This sentence was not clear because of the phrasing. There is no relation between the LM method and log-normal error distribution. The sentence has been modified to make the idea clear. LM method is used as a solver for finding the solution of the non-linear minimization problem.

Relevant changes implemented in Section 3.2,

~~Since we assume that all the input variables have log normal error distribution, the solutions to the set of equations in Eq. 3.1 are found by minimizing the term  $\Psi(a)$  in Eq. 3.2 using the Levenberg-Marquardt iterative method. For more detailed information on the theoretical background of the GRASP retrievals, please refer (Dubovik, 2006; Dubovik et al., 2011; Dubovik and King, 2000). In order to take into account, the non-negative character of measured and retrieved physical values in the retrieval optimization, the log-normal error distributions are assumed for all positively defined measured characteristics and the minimization is defined for logarithms of all positively defined retrieved parameters. The solutions to the set of equations in Eq. 3.1 are found by minimizing the term  $\Psi(a)$  in Eq. 3.2. Since the radiative transfer in the atmosphere has pronounced non-linear character, the Levenberg-Marquardt (Levenberg, 1944; Marquardt, 1963) algorithm is harmoniously adapted into the statistically optimized fitting to assure the monotonic convergence of the iterative solution. These and other technical details of numerical inversion are described in Dubovik et al., 2011 and in-depth discussion of the above methodological aspects are also can be found in Dubovik and King, 2000, and Dubovik, 2006.~~

17. Add the information on the SPEX retrieved refractive index for a similar forest fire smoke from the ACEPOL campaign (Line #381)

Added the information on the SPEX airborne retrieved refractive index value.

The values of RRI retrieved from AirHARP and shown in Figure 9(c) can be represented as a Gaussian distribution with a mode value of 1.55 for all wavelengths, while retrievals from the

RSP instrument and SPEX airborne instruments during the ACEPOL campaign produced values of RRI of 1.56 and 1.58 respectively for a similar forest fire smoke (Fu et al., 2020).

18. Suggested to add 'and are close the values retrieved from SPEX airborne and RSP' to the sentence in Line #390

As per the suggestion, the sentence has been modified to make the comparison more consistent.

Retrieved single scattering albedo values are well within the range measured during the FLAME 2 experiment using a photo acoustic spectrometer and a nephelometer and are close to the retrieved values from SPEX airborne and RSP by Fu et al., 2020.

19. Comment on Line #400-401 'Actually, those retrievals are for a smoke plume on 9 November. There, the % sphere seems to agree quite well with the HSRL2 depolarization ratio. Could you compare that here as well?'

A comparison with the HSRL2 aerosol depolarization ratio and the GRASP retrieved spherical fraction (SF) as a function of along-track flight pixels is plotted in Figure AR1.1. It also includes the trend of Angstrom Exponent (AE) along with the  $AOD_{532\text{ nm}}$  measured by HSRL2. From the AE value, it is clear that we have fine mode dominated particle size distribution and, correspondingly, the sensitivity of SF in the aerosol retrieval is low compared to the situation when the coarse mode aerosol, such as dust, dominates. The range of values we see for the aerosol depolarization from HSRL2 suggests that particles are fine but may have some non-spherical shapes. The HSRL2 data also suggest that the depolarization is decreasing when we go closer to the smoke plume. In these regards, HARP retrievals do not show the corresponding decrease of SF, however, the effect of particle non-sphericity on the radiances and polarization observed by passive instruments is rather small for fine mode dominated aerosols (e.g. see analysis by Dubovik et al., 2006) and the retrieval of SF has very limited accuracy. A detailed study on how the aerosol depolarization ratio change for spherical and non-spherical particles for a fine-mode dominated aerosol will help us understand better about this problem.

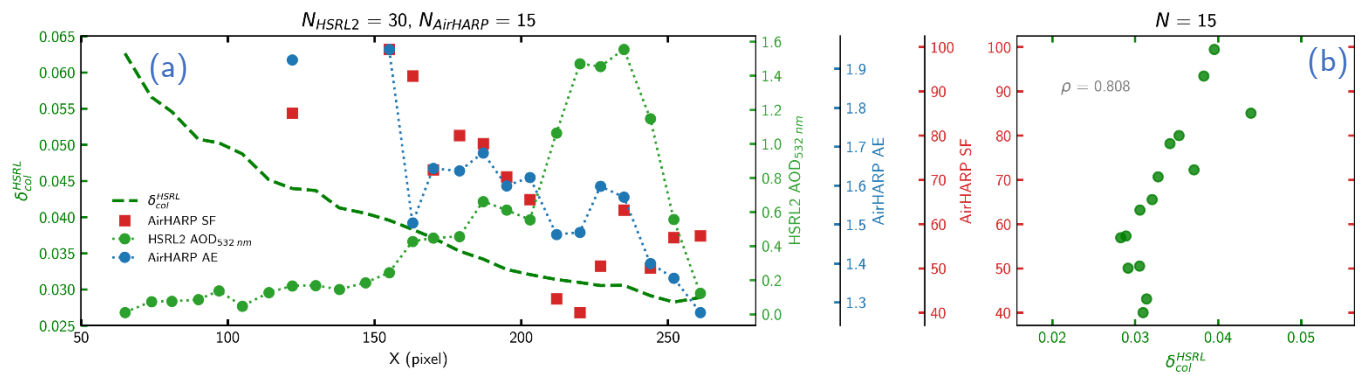


Figure AR1.1 (a) Columnar aerosol depolarization ratio and aerosol optical depth (AOD) at 532 nm from HSRL2 measurement, spherical fraction and angstrom exponent (AE) (using 440 and 870 nm bands) exponent retrieved using GRASP and AirHARP observation for the forest fire smoke plume on 9<sup>th</sup> November 2017 T19:30 UTC as a function of the along-track flight pixels. (b) Scatterplot of collocated columnar aerosol depolarization ratio and mean SF values

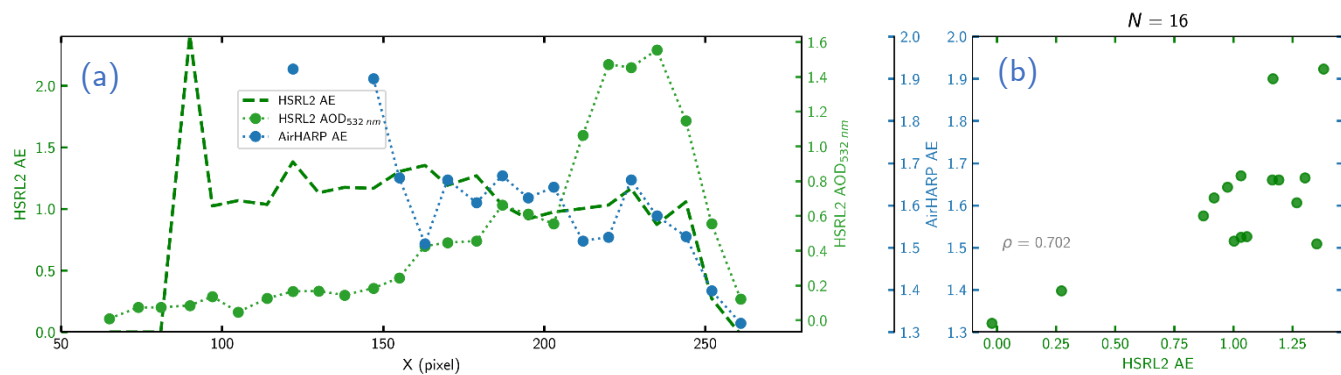


Figure AR1.2 (a) Columnar backscatter weighted angstrom exponent (AE) calculated using 355 and 532 nm observations and aerosol optical depth (AOD) at 532 nm from HSRL2 measurement, spherical fraction and angstrom exponent (AE) (using 440 and 870 nm bands) exponent retrieved using GRASP and AirHARP observation for the forest fire smoke plume on 9<sup>th</sup> November 2017 T19:30 UTC as a function of the along-track flight pixels. (b) Scatterplot of collocated columnar AE from HSRL and AE value from AirHARP.

Figure. AR1.2 shows that there is a clear correlation between the AE measured by HSRL2 and AirHARP at particularly AOD(532 nm) > 0.4. This implies that the particle size distribution changes with the location of the plume. The corresponding author is currently working on a project to analyze the retrieved aerosol and surface product from AirHARP and SPEX airborne polarimeters to understand how the synergy between two polarimeters can benefit the PACE mission. As a part of future study, this concern by the reviewer will be analyzed in detail. Given the results of this analysis and the other paper in process, the authors choose to not compare columnar aerosol depolarization ratio and SF in the current paper.

20. Comment on Line #432-433 'It would be interesting to also show results for the microphysical properties for this case as they can be directly compared to the values of Fu et al (2020) for SPEX airborne and RSP. Also, the sphericity can be checked using the depolarization ratio'

Results of the 9<sup>th</sup> November 2017 T19:31 UTC plume is not added to the manuscript because of the non-homogeneity of the plume compared to 27<sup>th</sup> October 2017 T 18:15 UTC one. The retrievals of aerosol properties show a high variability along the smoke plume source and edges and this can bias the mean calculation of aerosol and microphysical properties reported for this case. Further studies are ongoing based on the flight leg on 9<sup>th</sup> November 2017 T19:31 UTC to improve the retrievals and understand how the optical property of smoke aerosol changes with the age/location from the plume source. We have added a sentence in the text to explain why particle properties will not be shown. A list of the mean aerosol optical properties for the same scene is tabulated in Table AR1.1 for your reference. As mentioned in the reply for comment #19, the corresponding author is working on a project to compare the aerosol and surface products from two polarimeters onboard on ACEPOL.

Table AR1.1: Mean aerosol optical and microphysical properties retrieved for the smoke scene on 9<sup>th</sup> November 2017 T19:31 UTC (for pixels with AOD<sub>440 nm</sub> > 0.4).

Spectral Band	Single Scattering Albedo	Spherical Fraction (%)	Angstrom Exponent <sup>#</sup>	Real Refractive Index (RRI)	Imaginary Refractive Index (RRI)
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440 nm	0.83±0.1				0.034±0.02
550 nm	0.84±0.1				0.028±0.02
670 nm	0.80±0.13	70±34% <sup>®</sup>	1.58±0.36	1.54±0.03	0.035±0.02
870 nm	0.76±0.15				0.039±0.02

#Angstrom Exponent calculated using the AOD at wavelength bands 440 nm and 870 nm of the AirHARP

®Retrieved spherical fraction includes a significant number of pixels with SF ~ 99%

21. Does the agreement improve when using a stricter chi2 filter? (Line #448)

Yes, the agreement improves when stricter  $\chi^2_{norm}$  filtering ( $\chi^2_{norm} > 5$ ) is used to remove bad fits. The comparison is plotted in Figure AR1.3. The bias and MAE improve over the less strict  $\chi^2_{norm}$  filtering. However, several higher AOD points are missing from the analysis.

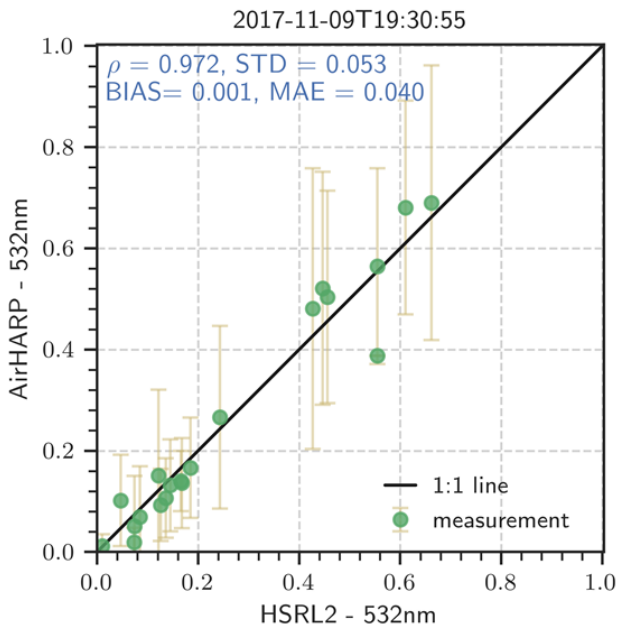


Figure AR1.3 Scatterplot of the collocated observation AOD from HSRL2. The plot is the same as Fig. 13 (b) in the manuscript but a stricter  $\chi^2_{norm} < 5$  filter is used for the removal of pixels. Also, if the box used for the mean AOD doesn't have enough pixels to do the statistics.

22. I think the 3D effect is only important very close to the source but not for the majority of pixels here. In Fu et al (2020) a stricter chi2 criterion for SPEX airborne and RSP was used and still, some high AOD values were in the comparison. Still, the spatial mismatch between airHARP and HSRL2 is probably an important reason for disagreement and I think this is much more relevant than the 3D effects (for most pixels). (Line #457-458)

Thanks for pointing this out. This mismatch is mainly caused by the difference in the spatial resolution of the measurement, which will affect the comparison over the plume edges and boundaries where there is a sharp change in the AOD values. Also, this will affect the pixels near to the plume source, since each viewing angle of the instrument will be looking at



different thickness and this violates the plane parallel assumption. To accommodate this issue, we will have to consider different thickness for different viewing angles in 1D RT code or will have to use 3D RT code completely in the forward model calculations. The sentence has been modified to avoid the confusion.

Matching the HSRL2 AOD in regions of heterogeneity is challenging ~~using 1D plane parallel aerosol assumptions; the aerosol layer must be characterized first, i.e. from the HSRL2 AOD vertical profile, and used as input in a 3D radiative transfer simulation to calculate  $I$ ,  $Q$  and  $U$  for the scene at different viewing angles. Also, the~~ due to spatial mismatch between AirHARP and HSRL2 pixels. This will create issues where there is a sharp variation in the AOD, like close to the source, and in the boundary of the smoke plume. The different cross-track pixel size between the HSRL2 and AirHARP measurement makes the intercomparison difficult to interpret in some cases. For points near the plume source, higher pixel variability may also bias AirHARP AOD retrievals performed at the same general location as the HSRL2 measurement. In a scene with this much complexity there is additional uncertainty in matching multiangle views for the AirHARP retrieval, because each viewing angle of the instrument will be looking at a different plume thickness and this violates the plane parallel assumption.

23. A reference to Stap et al. would fit here: *Atmos. Meas. Tech.*, 8, 1287–1301, 2015  
[www.atmos-meas-tech.net/8/1287/2015/doi:10.5194/amt-8-1287-2015](http://www.atmos-meas-tech.net/8/1287/2015/doi:10.5194/amt-8-1287-2015) (Line #469)

Added the reference in Section 5.2,

To further protect the algorithm from subpixel inhomogeneity and other features inappropriate for retrieval a  $\chi^2_{norm} > 1.5$  filter is used to remove the bad pixels/fits which may be caused by the presence of thin clouds (Stap et al., 2015) or due to the inability of surface reflection models to represent the directional reflectance from a complicated surface.

24. The 2E-3 degree seems to contradict with the 5.5x5.5km<sup>2</sup> area where airHARP AOD is averaged. (Line #470-474)

Actually, 2e-3 degree is used to locate the central AERONET pixel (a single-pixel) and used a 10x10 pixel square around the AERONET station pixel to calculate mean AOD.

Changes in Section 5.2,

To collocate the AERONET ~~station (a single-pixel-in)~~ within the AirHARP image, the latitude and longitude of the AERONET location are matched to the AirHARP latitude and longitude with a tolerance of  $2 \times 10^{-3}$  degree, which is approximately equivalent to 200m on the ground. An area of 5.5 km x 5.5 km (10x10 retrieval pixels) around this collocated pixel is used ~~to calculate~~ for the calculation of the area mean AOD from the AirHARP retrievals, and this is matched to a one-hour temporal mean from AERONET measurements.

25. Question on how the AOD from AERONET measurements is interpolated to AirHARP bands? (Line #492-493)

AOD is interpolated linearly in log-log space using the Angstrom Exponent calculated using the closest bands around the wavelength of interest.

Added a sentence in Section 5.2,

AERONET measured AOD are interpolated linearly in log-log space using the AE to AirHARP spectral bands for 1:1 comparison.



26. If you choose to mention this then for completeness you should also mention that airMSPI and SPEX airborne have smaller biases against AERONET (Line #500-501)

The authors were talking about the negative bias we saw in the AOD range of 0 to 0.1. In the Fu et. al 2020, for the AEROENT AOD comparison, SPEX airborne and AirMSPI were showing a positive bias in this low AOD range mentioned. Whereas RSP shows the negative bias for this AOD range. But this sentence in the manuscript has been removed after the new AERONET comparison using Ross-Li based land model

Removed the sentence in Section 5.2,

~~At low AOD we can see a low bias compared to AERONET AOD measurements, which is similar to what we see for RSP vs AERONET comparison in (Fu et al., 2020)~~

27. Mention in the conclusion also the different retrieval setups used for the different cases. (Line #514)

Findings based on the two approaches have been added to the conclusion.

In situations with low aerosol loading ( $\text{AOD} < 0.17$ ) over land, a simplified retrieval approach based on GRASP/Models kernel approximating aerosol as an external mixture of five aerosol components is also used for the AOD retrievals. One advantage of using this simplified kernel is that it retrieves a significantly smaller number of aerosol parameters compared to the standard GRASP/Five mode kernel and performed well for low aerosol loading cases in an AERONET comparison, despite the simplifying assumption of prescribed complex refractive index for each aerosol component. AOD retrieved from AirHARP using GRASP, matches collocated AERONET observations to within  $+0.005018/-0.02504$  with a minimum MAE of 0.01 in 440 and 550 nm bands and maximum of 0.015 in the 870 nm spectral band.

28. This part should be left out. The performance for 7 AERONET overpasses is in no way representative for global performance and should hence not be compared to the quoted uncertainties for MODIS. Even not with the reservation that you make at the end. (Line #530-534)

We feel that it is good to put the numbers that come out of the collocation with AERONET into some kind of perspective for people who are novices to MAPs can digest. Yes, of course, it is a microscopic data sample compared to global statistics, but the caveat is stated clearly. If the reviewer has a suggestion on how to put the results into context, the authors are open to new wording. Otherwise, the authors prefer to keep the statement, as is.

29. This suggests that you validated these properties. I would weaken it a bit, e.g. "...that we retrieved with GRASP optical and microphysical ..." (Line #537)

The sentence has been modified to avoid confusion.

It is in one of these situations that ~~GRASP was able to retrieve~~ optical and microphysical characteristics of the smoke, in addition to AOD, are retrieved using the GRASP software.

30. See my comments above. I do not believe that the 3D RT effect is the problem for most of the pixels (it only is very close to the source) but rather the spatial mismatch between airHARP and HSRL2. On the other hand, it could even be related to HSRL2 itself. Also, SPEX airborne and airHARP see a similar trend in underestimation while they all have different spatial samplings ... (Line #546-548)

Agree with the reviewer that this is mainly caused by the spatial mismatch between the HSRL2 and AirHARP pixels. But the 3D structure also plays a role in the mismatch near the smoke source. Also, it can be due to the HSRL2 itself. The sentence was modified.

Note that when the plume is highly heterogeneous, the ~~3D~~smaller cross-track footprint of HSRL2 measurements, relative to AirHARP makes collocation extremely difficult. Also, the complex structure of the plume must be accounted for in the polarimeter multi-angle vs. lidar nadir observations. This violates the plane-parallel aerosol layer assumption ~~and will result in an AOD bias depending on of the location of the measurement in the plume. Also, the smaller cross-track footprint of HSRL2 measurements, relative to AirHARP, adds complexity in the intercomparison retrieval, adding uncertainty and bias.~~

31. *This is still to be demonstrated for the microphysical properties and SSA, so please weaken the statement a bit. (Line #553-554)*

The sentence has been modified to make it weaker and clearer.

Thus, the encouraging results demonstrated here show that when combined with GRASP inversion methods, HARP measurements ~~can~~have the potential to be used to retrieve ~~highly~~ accurate measures of AOD. With sufficient aerosol loading and homogeneity, aerosol optical/microphysical characteristics can be retrieved over a broad area.

32. *It would be nice to stress the synergy with SPEXone (<https://www.sciencedirect.com/science/article/pii/S0022407318308653>), the other polarimeter on PACE. (Line #559)*

A description of the synergy between the three instruments onboard on the PACE mission is provided with references.

Furthermore, HARP has the potential to provide new characterization for clouds (~~McBride~~McBride et al., 2020) and surface properties over various surface types, land and ocean. The PACE mission also opens the corridor for a synergetic observation using the Ocean Color Instrument (OCI) along with the two multi-angle polarimeters: HARP2 and SPEXone. OCI is a hyperspectral, wide swath radiometer, HARP2 – a wide swath multi-angle polarimeter and SPEXone – a hyperspectral narrow swath multi-angle polarimeter. The combined spectral and spatial coverage and resolution of these three instruments will provide an unprecedented dataset for the atmospheric, ocean and terrestrial science research communities (Frouin et al., 2019; Hasekamp et al., 2019; Remer et al., 2019).

33. *Please also acknowledge the Dutch funding of ACEPOL flight hours: "The Dutch contribution to the ACEPOL flight campaign hours was funded by SRON Netherlands Institute for SPACE Research and by NSO/NWO under project number ALW-GO/16-09. Same for the NASA flight hours (We acknowledge the former Aerosol, Cloud, Ecosystem (ACE) program at NASA's Earth Science Division as a sponsor for ACEPOL flights.) (Line #635)*

Added a sentence in the acknowledgement,

We acknowledge the former Aerosol, Cloud, Ecosystem (ACE) program at NASA's Earth Science Division as a sponsor for ACEPOL flights. The Dutch contribution to the ACEPOL flight campaign hours was funded by SRON Netherlands Institute for SPACE Research and by NSO/NWO under project number ALW-GO/16-09.

## Other comments

34. *It seems that 3 different GRASP setups are used for 3 different cases:*

- *GRASP for fixed aerosol models, together with the RPV surface model for the AERONET comparison.*
- *Retrievals for 5 aerosol modes with fixed refractive index, together with the Ross-Li surface model for the Rosamond Dry lake.*
- *'Full' retrievals for 5 aerosol modes where also microphysical properties are retrieved for the smoke case. Here also the Ross-Li surface model has been used.*

*These 3 setups should be clearly described in the Theory section and not in the Result sections where they are being used. Also, the choice for a given setup should be better motivated, and perhaps also some numbers for retrievals in other setups should be quoted.*

*If possible, I would even suggest restricting to 2 setups: the ones corresponding to 'full' and models', and using the same surface model for all over land cases.*

Authors would like to thank Otto for suggesting this comment and as per the recommendation of the reviewers, only one land surface model (Ross-Li based BRDF) is now used in the retrievals over the land pixels. The updated manuscript includes a comparison of the two different retrieval methods. Validation plots of AirHARP vs AERONET AOD for the two methods: a) five fixed modal log-normal size distribution GRASP kernel (GRASP/Five mode) and b) aerosol component-based GRASP kernel (GRASP/Models) where complex refractive index, spherical fraction and aerosol distribution are fixed. Only the weight for each aerosol type can change in the retrieval. Case (b) has a significant reduction in the number of retrieved aerosol parameters from 15 to 6, which will reduce the non-linearity of the minimization problem. This simplified method seems to perform well over the five modal log-normal approach for these low aerosol loading cases.

In section 5.2 added a discussion of the two aerosol GRASP kernel approaches and the results,

~~Due to the low loading of aerosol over the AERONET stations, treating the aerosols as a mixture of predefined aerosol components with fixed size and shape distributions, and complex refractive index will benefit the accuracy of AOD retrievals using AirHARP and GRASP. A five-component mixture of the aerosol is used to create the phase matrix kernels, which includes the aerosol types: biomass burning, urban, urban polluted, maritime, and desert dust. Among these, only desert dust is considered as completely nonspherical and uses a shape distribution mentioned in (Dubovik et al., 2006). AERONET measured AOD are interpolated linearly in log-log space using the AE to AirHARP spectral bands for 1:1 comparison. The Ross-Li BRDF All the other types are treated as 100 % spherical particles. The details of the bi-modal size distribution parameters along with the fixed complex refractive index for each of the aerosol types are tabulated in Table 6 and are based on the work of Dubovik et al., 2002. Figure 13 shows the particle size distribution as a function of radii for the different aerosol types. The main differences between the five log-normal mode kernel-based retrievals are, 1.) instead of retrieving the concentration of each log normal mode, weight for each of the aerosol components mentioned in the Table 6 are retrieved. 2) RRI, IRI, and SF are not retrieved since~~

these are fixed for each of the aerosol components. This simplified approach significantly drops the complexity of the aerosol model by reducing the number of parameters retrieved in the joint retrieval. It helps in reducing the nonlinearity of the inverse problem and makes the separation of the surface and aerosol signal much less complicated compared to a five-lognormal mode kernel. The maximum AOD measured by a collocated AERONET station during the ACEPOL campaign is 0.158 at 440 nm and using this simplified aerosol type model will greatly benefit the AOD estimation from AirHARP GRASP retrievals. The Rahman Pinty-Verstraete (RPV) BRDF surface model along with the Maignan-Breon BPDF models are used for representing the directional reflectance from the land surface. RPV BRDF model perform better over the urban and barren land area compared to Ross Li BRDF kernels. AERONET measured AOD are interpolated to AirHARP spectral bands for 1:1 comparison. for all retrievals used in the validation.

AirHARP observations in this validation exercise are retrieved with two versions of the GRASP aerosol kernels, one using the GRASP/Five mode kernel with 15 free parameters (Table 3) that allows for retrieval of particle properties, and the other using the GRASP/Models kernel with only 6 free parameters (Table 4) that restricts the particle properties to focus on the AOD retrieval. When aerosol loading is low, there is insufficient signal to retrieve particle properties. Allowing for additional free parameters without having sufficient signal will degrade the accuracy of the AOD retrieval. The maximum AOD measured by a collocated AERONET station during the ACEPOL campaign is 0.158 at 440 nm suggesting that in this exercise the simplified aerosol component model would be preferred over using the option with a greater number of free parameters. This is evident in the two figures, Fig. 14(a) and Fig. 14(b). Figure 14 shows the scatterplot of these two data sets with  $AOD_{AERONET}$  in the X-axis and  $AOD_{AirHARP}$  on the Y-axis. The spatial standard deviation of AOD within this 5.5 km x 5.5 km box is indicated using the error bars in Fig. 14. Statistical parameters that represent the correlation between these two data sets are tabulated in the table inside Fig. 14. The black dashed lines in Fig. 14 are  $AOD(1:1) \pm 0.04$  lines. Mean absolute error of 0.014, 0.013, 0.013 and 0.017 the plots. In Fig. 14 a, for the case of AOD retrievals based on the GRASP/Five mode kernel with the greater number of free parameters, MAE of 0.041, 0.039, 0.037, 0.035 are obtained for the spectral bands 440, 550, 670, and 870 nm bands, respectively, with. The bias ranges from 0.022 to 0.038, with the 440 nm band having the largest bias and the 870 nm band having with the least. However, in Fig. 14b, for the case using the GRASP/Models kernel with the reduced number of free parameters, mean absolute error of 0.010, 0.010, 0.011, and 0.015 are obtained for the spectral bands 440, 550, 670, and 870 nm, respectively, with 870 nm band having a slightly higher spread than the other bands. Also, a similar trend is seen for 870 nm in the case of BIAS, where the 440, 550, and 670 nm bands have a BIAS of -0.011, -0.013, -0.002, -0.011, -0.003, -0.004, respectively whereas 870 nm has a BIAS of -0.017. At low AOD we can see a low bias compared to AERONET AOD measurements, which is similar to what we see for RSP vs AERONET comparison in (Fu et al., 2020).009. Figure 14 demonstrates the need to match the appropriate kernel to the available information in the scene and to not attempt the retrieval of more free parameters than the aerosol loading permits. Overall, the performance of the AirHARP observations plus the GRASP retrieval algorithm gives a good correlation agreement with the collocated AERONET observations- especially when GRASP/Models kernel is used. The above tendency is well identified in the in-depth analysis of PARASOL data processing using different retrieval setups by Chen et al. 2020 (In preparation).

Updated Fig. 14 that plots the AirHARP AOD comparison with AERONET observations,

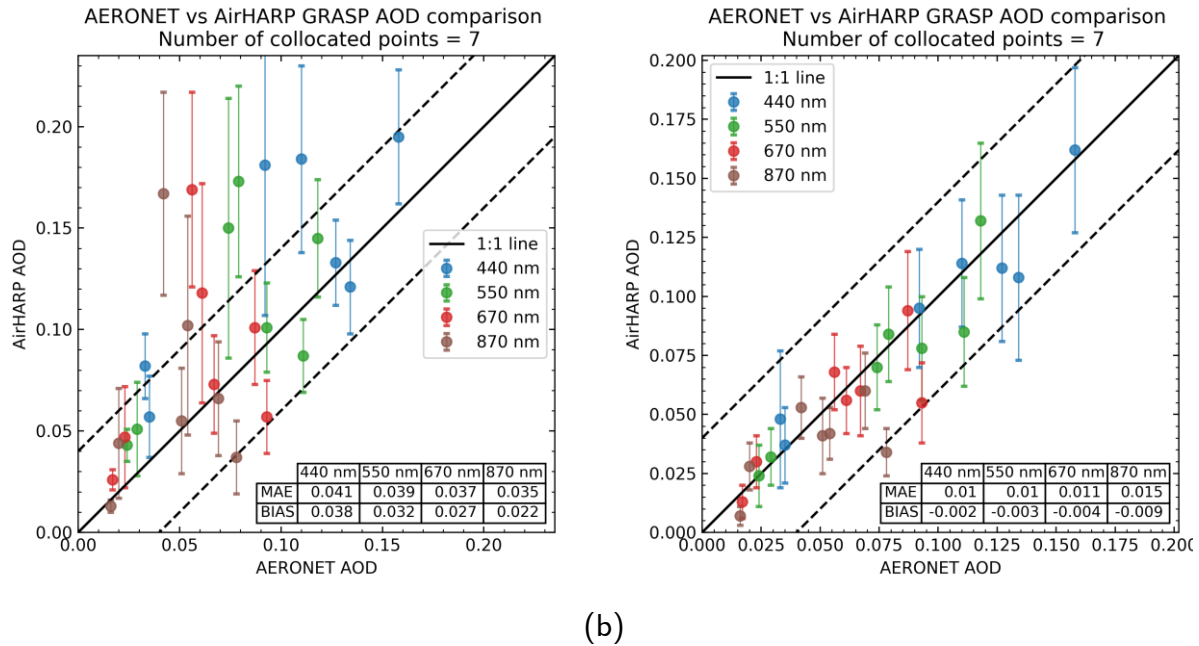


Figure 14. **Scattergrams** of aerosol optical depth (AOD) retrieved using AirHARP observations over collocated AERONET ~~pixels~~**stations** vs AERONET measured AOD interpolated ~~at to~~ AirHARP spectral bands. **Plotted are the areal mean AirHARP AODs calculated from all the qualified retrievals within a box of 5.5km x 5.5km around the AERONET station against the collocated AERONET pixel-is used to calculate the spatial mean AOD (solid colored circles)-over AERONET station using the AirHARP AOD retrievals-temporal mean AOD.** Each colored error ~~bars indicate~~**bar indicates** the standard deviation of AOD within the ~~matching areal~~ box. Mean Absolute Error (MAE) and BIAS for each spectral band are provided in the table inside the scattergram. ~~Black-~~**The black solid lines in the plots are the 1:1 lines and the dashed lines in are  $\pm 0.04$  AOD from the plot are 1:1 line  $\pm 0.04$ .** (a) GRASP retrievals using the GRASP/Five mode kernel (Table 3) that has 15 free parameters and allows for retrieval of particle properties along with AOD; (b) same as (a) except using the GRASP/Models kernel (Table 4) that reduces free parameters to 6 and fixes particle properties based on Table 4 and only retrieves the concentration for each aerosol component.

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## Reply to Reviewer #2 comments

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The authors would like to thank anonymous reviewer #2 for taking the time to review this manuscript and providing valuable comments and recommendations on an open discussion. For the ease of cross reading, authors responses are given under the reproduced version of each comment by reviewer #2. Each of the comments from the reviewer are numbered and the changes made in the manuscript are shown using a red font under the authors response given in blue font.

### Comments

1. *The authors review the airborne polarimeters (SPEX, RSP, AirMSPI). It is also necessary to review aerosol retrieval algorithms used by these sensors and published elsewhere.*

References to the current retrieval algorithms used by different sensors have been added to the revised manuscript. Also redirecting the readers to more comprehensive review papers on polarimetric aerosol sensing and retrieval algorithms.

Changes implemented in Section 1,

~~For~~ There are several aerosol retrieval algorithms specifically optimized for MAPs which includes: SRON multi-mode inversion algorithm for SPEX airborne (Fu et al., 2020; Fu and Hasekamp, 2018); Microphysical Aerosol Property from Polarimeters (MAPP) (Stamnes et al., 2018) and GISS/RSP algorithm (Knobelspiesse et al., 2011; Waquet et al., 2009) for RSP; correlated multi-pixel and joint retrieval algorithm for AirMSPI developed at Jet Propulsion Laboratory (JPL) (Xu et al., 2017, 2019). This list is not complete, for a comprehensive review of the polarimetric remote sensing of atmospheric aerosols based on MAPs, we encourage the readers to refer to several reviews in the literature (Dubovik et al., 2019; Kokhanovsky et al., 2015; Remer et al., 2019).

2. *Associated with the comparison of AirHARP AOD results against AERONET reference data in Figure 14, how do the comparison of single scattering albedo and non-spherical particle fraction look like? Though the AOD loading is low, are we still able to see a trend of improved agreement of these properties as AOD increases?*

Since the aerosol loading is very low, most of the AERONET stations do not have SSA retrievals for many of the collocated observations. For those AERONET stations that do have a retrieval for SSA are only at Level 1.5, which are not quality assured. There are 6 collocated observations for the SSA. A comparison plot for the GRASP retrieved SSA using AirHARP observation and L1.5 SSA retrieved using AERONET almucantar measurements is given in Fig. AR2.1. The figure also includes the plot which shows the trend of difference in SSA with an increase in the AOD measured by the AERONET. The same plots are given for two cases: a) five modal log-normal size distribution based GRASP/Five mode kernel and b) aerosol component-based GRASP/Models kernel where complex refractive index, spherical fraction and aerosol distribution are fixed. Only the weight for each aerosol components can change in the retrieval. There is a significant reduction in the number of retrieved aerosol parameters from 15 to 6 in case (b), which will reduce the non-linearity of the minimization problem. In the Reply to Reviewer #1, we show an analysis that demonstrates that the

sensitivity to the spherical fraction is small for fine mode dominated particle size distribution and we can't expect a good agreement with the AERONET retrieved SF.

The point is that there is insufficient aerosol loading with the AERONET match-ups to expect a good retrievals of particle properties from any inversion. This is why AERONET has no Level 2 Quality Assured retrievals, and why we do not want to include any comparisons in the paper.

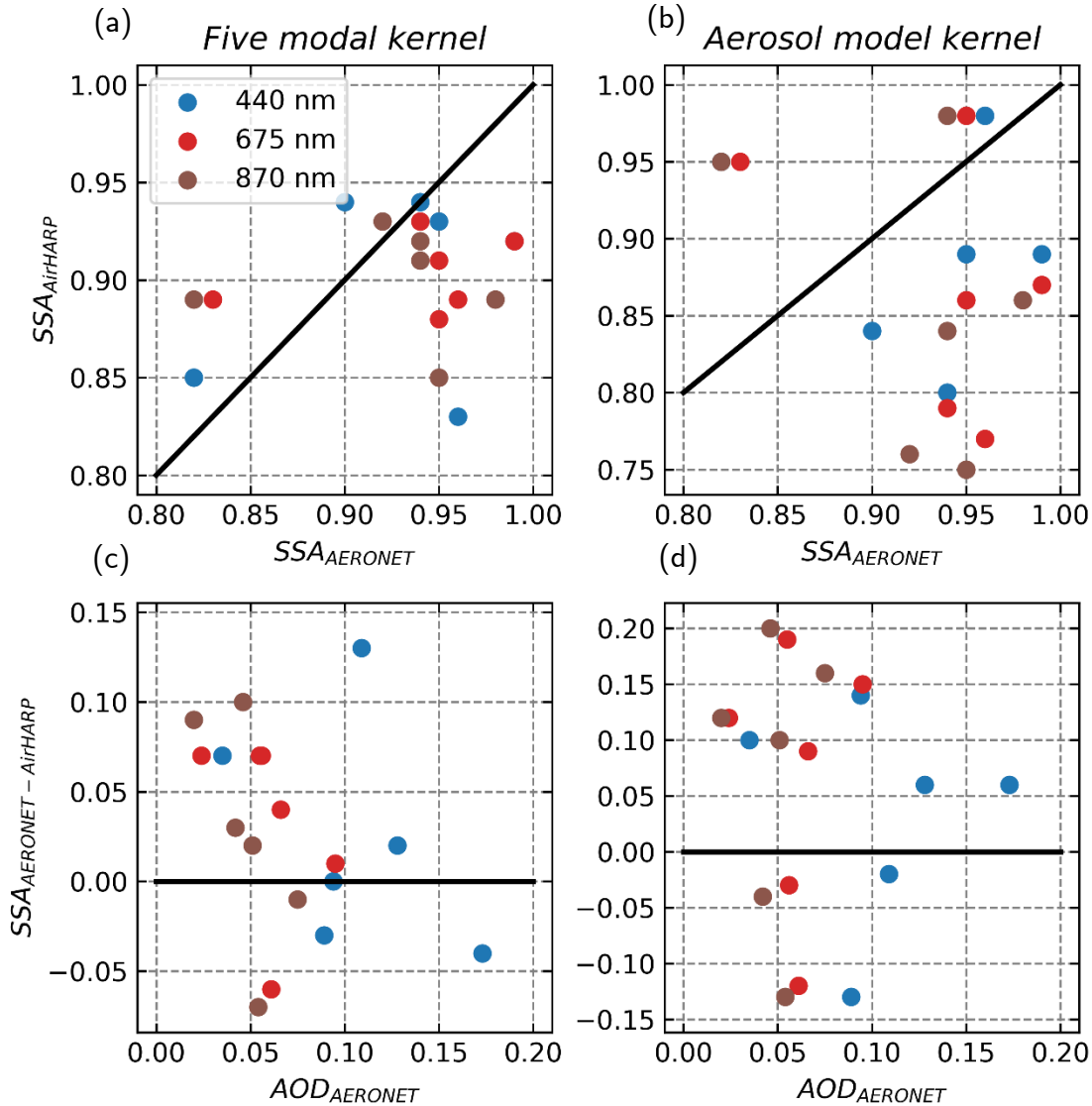


Figure AR2.1: (a) and (b) are the scatter plots of retrieved SSA from AERONET and AirHARP observations. For the case of (a), AirHARP retrievals use a GRASP five modal log-normal kernel, where the complex refractive index and spherical fraction are retrieved along with the weight for each lognormal mode in the PSD (See Table. 3 in the manuscript for more details on the fixed size modes). On the other hand, case (b) uses an aerosol type-based GRASP kernel where optical properties are precomputed using different aerosol types mentioned in Table. 6. Subplots (c) and (d) show the trend of difference in SSA retrieved from AERONET and AirHARP observations with an increase in AOD measured by AERONET stations. Plots (c) and (d) are based on the kernels mentioned in (a) and (b) respectively.

3. The authors need to be clearer on the adoption of size components in AirHARP retrieval. Table 3 and Table 6 give two different size components in retrieval. If I

*understand well, size components in Table 3 are the default option in GRASP while size components in Table 6 were created for AirHARP retrieval. What is the difference in retrieval based on these two different assumptions? Which one gives a better fit to AERONET AOD and SSA? As the authors pointed out “This simplified approach significantly drops the complexity of the aerosol model by reducing the number of parameters retrieved in the joint retrieval. It helps in reducing the nonlinearity of the inverse problem and makes the separation of the surface and aerosol signal much less complicated compared to a five-lognormal mode kernel.” However, would it also possible that the size components in Table 6 (with a fixed refractive index for each mode) also increase the risk of getting more subsection to pre-determined aerosol modeling errors? If so, how large is the modeling error?*

Table 3 is the default option used for the retrieval in this paper. It is not the default option in GRASP. GRASP offers many options. Its most generalized version of a kernel has 22 bins for the particle size distribution plus all of the other particle properties. But to reduce the complexity for the AirHARP retrievals, based on the experience of PARASOL/GRASP retrievals, we are using a different option with the predefined five modal log-normal distribution mentioned in Table 3. This one has 15 free parameters including spectrally dependent complex refractive index, spherical fraction, etc. For the AERONET comparison, we invoke yet a different GRASP option. We used the GRASP/Models approach representing aerosol as an external mixture of predetermined aerosol components, where the number of free parameters is further reduced to 6 and the complex refractive index and the spherical fraction are fixed for each aerosol type. Only the concentration (weight) of each aerosol component in Table 4 (old Table 6) are retrieved during the inversion. Since the aerosol loading for the AERONET comparison cases is below 0.17, this approach seems to be working well compared to the one mentioned in Table 3 (complex refractive index and spherical fraction are retrieved parameters).

We have worked hard to try and clarify the text in this matter, and have added a plot (Figure 14 in the revised manuscript) that compares the 15 and 6 free parameter options.

Figure AR2.1 gives us an insight into modeling error because of the assumption of the aerosol components. For this range of aerosol loading, the assumption of aerosol type will not significantly affect the  $R_i$  and  $DoLP$  calculations. However, this assumption may not hold for higher aerosol loading where a predetermined aerosol model will create modeling error in  $R_i$  and  $DoLP$  calculated using the forward model.

Changes implemented in the manuscript relevant to this comment:

In section 3.2 describing the different GRASP kernels and surface models used in the retrievals,

The particle single-scattering kernel calculations that we employ for the AirHARP retrieval ~~use~~ use one of two possible retrieval set-ups: 1) five fixed-log-normal distribution modes as described in Table 3, or 2) the aerosol is assumed as an external mixture of five aerosol components as described in Table 4. Both approaches were extensively used in PARASOL/GRASP processing and, therefore, considered here. For the first kernel possibility, the retrieval has 15 aerosol parameters to retrieve and is called as “GRASP/Five mode” kernel. Each of the log-normal modes has a fixed mode radius and width. The only free parameter in the retrieval for particle size distribution is the concentration of particles in each bin. There are three lognormal modes in the fine mode and two in the coarse mode. (log-normal modes 1 to 3 in

Table 3) and two in the coarse mode (log-normal modes 4 and 5 in Table 3). Other retrieved parameters related to aerosol properties include a complex refractive index, aerosol layer height, and the fraction of spherical particles (SF). The same kernel is used for all the retrievals in this paper with an exception for the AERONET comparison mentioned in Section 5.2. For the AERONET comparison, we make use of the second GRASP kernel that has reduced the number of aerosol parameters from 15 to 6. This reduced parameter option is the “GRASP/Models” kernel, where particle properties are assumed for each aerosol components given in Table 4. Complex refractive index, SF, and particle size distribution of each aerosol components are fixed for this kernel. Only the concentration (weight) for each aerosol component is retrieved.

Another change in the same section,

The state vector  $a$  includes the information on particle size distribution which is the concentration for five log-normal modes of Table 3, the complex refractive index in the four spectral bands that are independent of particle size, the fraction of spherical particles (SF), aerosol layer height, and parameters characterizing the directional reflectance of the surface. AOD is derived from retrieved aerosol properties using the method mentioned in appendix B.1. Additionally, fine mode AOD is calculated using modes 1-3 mentioned in Table 3 and coarse mode AOD using modes 4 and 5. Single Scattering Albedo (SSA), Angstrom Exponent (AE) are also derived from the retrieved aerosol properties. For the GRASP/Models approach, the state vector  $a$  includes the concentration for each aerosol component mentioned in Table 4. State vector  $a$  does not contain information on the particle size distribution, SF, and complex refractive index. All this is embedded in the aerosol components which includes the aerosol types: are close (with some modifications) to biomass burning, urban, urban polluted, maritime, and desert dust observed in AERONET climatology by {Dubovik et al., 2002}. Among these, only desert dust is considered as completely non-spherical, and similarly to AERONET retrievals, uses a shape distribution mentioned in {Dubovik et al., 2006}. All the other types are treated as 100 % spherical particles. The details of the bi-modal size distribution parameters along with the fixed complex refractive index for each of the aerosol component types are tabulated in Table 4 and are based on the work of Dubovik et al., 2002. Figure 13 shows the particle size distribution as a function of radii for the different aerosol component types. The main differences between the five log-normal mode kernel-GRASP/Five mode and GRASP/Models approach based retrievals are, 1.) instead of retrieving the concentration of each log-normal mode, concentration (weight) for each of the aerosol components mentioned in the Table 4 are retrieved. 2) RRI, IRI, and SF are not retrieved since these are fixed for each of the aerosol components. This simplified approach significantly drops the complexity of the aerosol model by reducing the number of parameters retrieved directly in the joint retrieval. It helps in reducing the nonlinearity of the inverse problem and makes the separation of the surface and aerosol signal much less complicated compared to the GRASP/Five mode approach a five-lognormal mode kernel. At the same time, all aerosol total properties as SSA, effective size distribution, complex refractive index can be obtained using external aerosol mixture concept. The reduction of sought unknowns helps situations in lower information content (e.g., for low AOD) and makes the separation of the surface and aerosol signal much less complicated compared to a GRASP/Five mode kernel. This tendency is well identified in the in-depth analysis of PARASOL data processing using different retrieval setups by Chen et al. 2020 (In preparation). Like the GRASP/Five mode kernel, the state vector  $a$  includes the information on aerosol layer height. Even though aerosol layer height is retrieved during the retrieval process, the sensitivity

to aerosol height for the AirHARP wavelengths is negligible for most of the low loading cases. Retrieved aerosol layer height is thus not discussed in this work.

Retrieval of aerosol properties from MAPs is highly sensitive to the accurate representation of the directional reflectance from the surface. For the ocean pixels, the ocean surface model used is the NASA GISS model (Mishchenko and Travis, 1997) based on Cox and Munk (1954), in which the ocean surface reflectance is represented by three parameters: ocean surface albedo, the fraction of Fresnel reflection surface, and wind speed denoted by  $a_0$ ,  $a_1$ , and  $a_2$  respectively, with details given in Appendix A.2. These three parameters are the surface components in the state vector  $\mathbf{a}$  for the case of ocean pixels. For the case of land pixel, Ross-Thick Li-Sparse linear BRDF model is used to represent the directional reflectance from the surface (see Appendix A.1.1), which uses three parameters  $K_0$ ,  $K_1$ ,  $K_2$ .  $K_0$  is a spectrally dependent parameter that represents the isotropic reflectance,  $K_1$  and  $K_2$  normalized to  $K_0$  are the spectrally independent parameters which are the coefficient of geometric and volumetric scattering kernels respectively (Maignan et al., 2004; Wanner et al., 1995). Polarized reflectance from the surface is modeled using the Maignan-Breon one-parameter  $\alpha$  model and the retrieved parameter is a scaling factor ( $\alpha$ ) that is spectrally dependent (Maignan et al., 2009). Refer to Appendix A.1.2 for detailed information on the surface models. The four parameters  $K_0$ ,  $K_1/K_0$ ,  $K_2/K_0$ , and  $\alpha$  are the surface components in the state vector  $\mathbf{a}$  for the case of land pixels. In the next section, we discuss the results of applying GRASP to AirHARP measurements of  $R_i$ ,  $Q/I$  and  $U/I$  for selected cases from the ACEPOL campaign.

In section 5.2 discussing the two aerosol GRASP kernel approaches and the results,

AirHARP observations in this validation exercise are retrieved with two versions of the GRASP aerosol kernels, one using the GRASP/Five mode kernel with 15 free parameters (Table 3) that allows for retrieval of particle properties, and the other using the GRASP/Models kernel with only 6 free parameters (Table 4) that restricts the particle properties to focus on the AOD retrieval. When aerosol loading is low, there is insufficient signal to retrieve particle properties. Allowing for additional free parameters without having sufficient signal will degrade the accuracy of the AOD retrieval. The maximum AOD measured by a collocated AERONET station during the ACEPOL campaign is 0.158 at 440 nm suggesting that in this exercise the simplified aerosol component model would be preferred over using the option with a greater number of free parameters. This is evident in the two figures, Fig. 14(a) and Fig. 14(b). Figure 14 shows the scatterplot of these two data sets with  $AOD_{AERONET}$  in the X-axis and  $AOD_{AirHARP}$  on the Y-axis. The spatial standard deviation of AOD within this 5.5 km x 5.5 km box is indicated using the error bars in Fig. 14. Statistical parameters that represent the correlation between these two data sets are tabulated in the table inside Fig. 14. The black dashed lines in Fig. 14 are  $AOD(1:1) \pm 0.04$  lines. Mean absolute error of 0.014, 0.013, 0.013 and 0.017 are obtained for the plots. In Fig. 14 a, for the case of AOD retrievals based on the GRASP/Five mode kernel with the greater number of free parameters, MAE of 0.041, 0.039, 0.037, 0.035 are obtained for the spectral bands 440, 550, 670, and 870 nm bands, respectively, with the bias ranges from 0.022 to 0.038, with the 440 nm band having the largest bias and the 870 nm band having the least. However, in Fig. 14b, for the case using the GRASP/Models kernel with the reduced number of free parameters, mean absolute error of 0.010, 0.010, 0.011, and 0.015 are obtained for the spectral bands 440, 550, 670, and 870 nm, respectively, with 870 nm band having a slightly higher spread than the other bands. Also, a similar trend is seen for 870 nm in the case of BIAS, where the 440, 550, and 670 nm bands have a BIAS of -0.011, -0.013, 0.002, -0.011, -0.003, -0.004, respectively whereas 870 nm has a BIAS of -0.017. At low AOD we

can see a low bias compared to AERONET AOD measurements, which is similar to what we see for RSP vs AERONET comparison in (Fu et al., 2020).009. Figure 14 demonstrates the need to match the appropriate kernel to the available information in the scene and to not attempt the retrieval of more free parameters than the aerosol loading permits. Overall, the performance of the AirHARP observations plus the GRASP retrieval algorithm gives a good ~~correlation agreement~~ with the collocated AERONET observations— especially when GRASP/Models kernel is used. The above tendency is well identified in the in-depth analysis of PARASOL data processing using different retrieval setups by Chen et al. 2020 (In preparation).

Updated Fig. 14 that plots the AirHARP AOD comparison with AERONET observations,

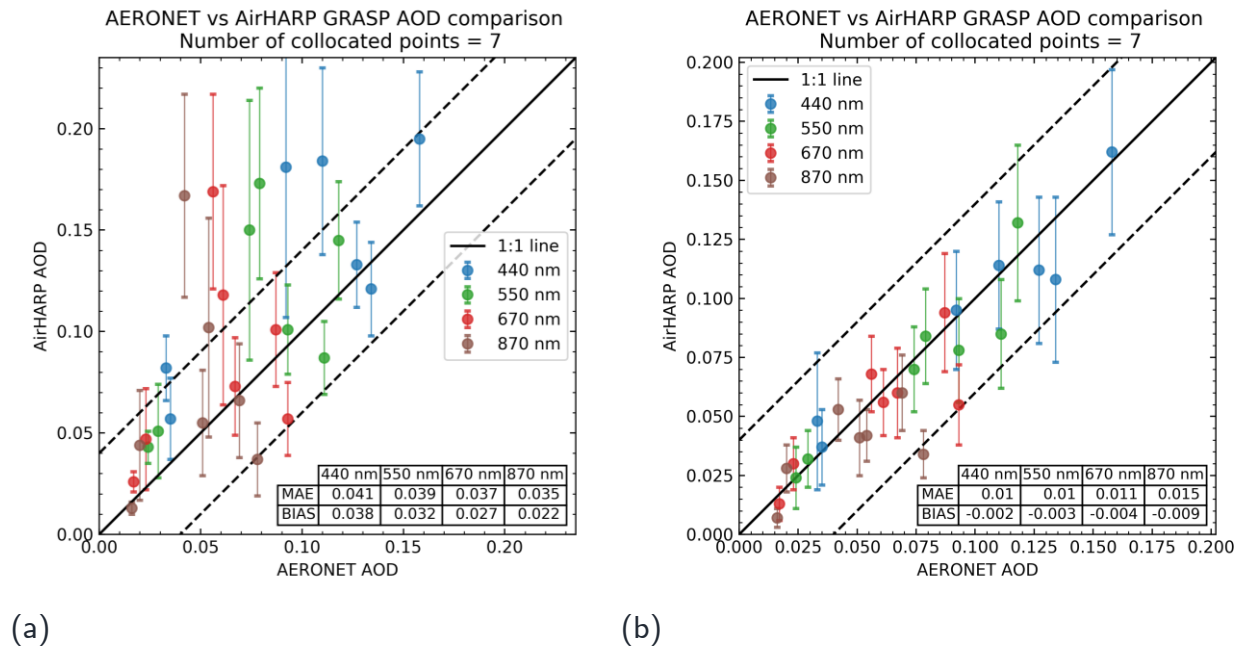


Figure 14. ~~Scattergram~~Scattergrams of aerosol optical depth (AOD) retrieved using AirHARP observations over collocated AERONET ~~pixels~~stations vs AERONET measured AOD interpolated ~~at to~~ AirHARP spectral bands. ~~Plotted are the areal mean AirHARP AODs calculated from all the qualified retrievals within a box of 5.5km x 5.5km around the AERONET station against the collocated AERONET pixel is used to calculate the spatial mean AOD (solid colored circles) over AERONET station using the AirHARP AOD retrievals.~~temporal mean AOD. Each colored error ~~bars indicate~~bar indicates the standard deviation of AOD within the ~~matching areal~~ box. Mean Absolute Error (MAE) and BIAS for each spectral band are provided in the table inside the scattergram. ~~Black~~The black solid lines in the plots are the 1:1 lines and the dashed lines ~~in are~~  $\pm 0.04$  AOD from the ~~plot are~~ 1:1 line  $\pm 0.04$ . (a) GRASP retrievals using the fixed five modal log-normal GRASP kernel (Table 3) that has 15 free parameters and allows for retrieval of particle properties along with AOD (b) same as (a) except using the GRASP/Models approach (Table 4) that reduces free parameters to 6 and fixes particle properties based on the Table 4 and only retrieves the weight for each aerosol type.



Change implemented in the conclusion based on the new results,

In situations with low aerosol loading ( $AOD \leq 0.17$ ) over land, a simplified retrieval approach based on GRASP/Models kernel approximating aerosol as an external mixture of five aerosol components is also used for the AOD retrievals. One advantage of using this simplified kernel is that it retrieves a significantly smaller number of aerosol parameters compared to the standard GRASP/Five mode kernel and performed well for low aerosol loading cases in an AERONET comparison, despite the simplifying assumption of prescribed complex refractive index for each aerosol component. AOD retrieved from AirHARP using GRASP, matches collocated AERONET observations to within  $+0.005018/-0.02504$  with a minimum MAE of 0.01 in 440 and 550 nm bands and maximum of 0.015 in the 870 nm spectral band. Thus, we note an overall low bias of  $-0.011002$  to  $-0.017009$ , depending on wavelength..

4. *As the AOD loading during the ACEPOL field campaign is low, it provides a very good testbed for surface retrieval. Is there any comparison of surface BRDF and pBRDF as retrieved from AirHARP and other sensors such as SPEX, RSP, and AirMSPI?*

The authors agree with the reviewer that this dataset/campaign is a good testbed for surface retrieval. This is an ongoing project and will be part of a publication expected from that project. For now, the authors believe that it is beyond the scope of this paper.

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# Retrieval of aerosol properties from Airborne Hyper Angular Rainbow Polarimeter (AirHARP) observations during ACEPOL 2017

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**Abstract.** Multi-angle polarimetric (MAP) imaging of Earth scenes can be used for the retrieval of microphysical and optical parameters of aerosols and clouds. The Airborne Hyper-Angular Rainbow Polarimeter (AirHARP) is an aircraft MAP instrument with the hyper-angular imaging capability of 60 along-track viewing angles at 670 nm, and 20 along-track viewing angles at other wavelengths 440, 550, 870 nm across the full 114° (94°) along-track (cross-track) field-of-view. Here we report the retrieval of aerosol properties using the Generalized Retrieval of Aerosols and Surface Properties (GRASP) algorithm applied to AirHARP observations collected during the NASA Aerosol Characterization from Polarimeter and Lidar (ACEPOL) campaign in October – November 2017. The retrieved aerosol properties include spherical fraction (SF), aerosol ~~volumecolumn~~ concentration in multiple size distribution modes, and with sufficient aerosol loading, complex aerosol refractive index. From these primary retrievals, we derive aerosol optical depth (AOD), Angstrom exponent (AE), and single scattering albedo (SSA). AOD retrieved from AirHARP measurements are compared with the High Spectral Resolution LiDAR-2 (HSRL2) AOD measurements at 532 nm and validated with measurements from collocated Aerosol Robotic NETwork (AERONET) stations. A good ~~correlationagreement~~ with HSRL2 ( $\rho = 0.940$ ,  $|BIAS| = 0.062$ ) ~~and AERONET AOD~~ ~~( $0.013 \leq$~~  Mean Absolute Error ( $MAE \leq 0.017$ ,  $= 0.122$ ) and AERONET AOD ( $0.010 \leq MAE \leq 0.013$ ,  $0.002 \leq |BIAS| \leq 0.017$ ) measurements is observed for the collocated points. There was a mismatch between the HSRL2 and AirHARP retrieved AOD for the pixels close to the forest fire smoke source and to the edges of the plume due to spatial mismatch in the sampling. This resulted in a higher BIAS and MAE for the HSRL2 AOD comparison. For the case of AERONET AOD comparison, two different approaches are used in the GRASP retrievals, and the simplified aerosol component-based GRASP/Models kernel which retrieves fewer number of aerosol parameter performed well compared to a more generous GRASP/Five mode approach in the low aerosol loading cases. Forest fire smoke intercepted during ACEPOL provided a situation with homogenous plume and sufficient aerosol loading to retrieve the real part of the refractive index (RRI) of 1.55

and the imaginary part of the refractive index (IRI) of 0.024. The derived SSAs for this case are 0.87, 0.86, 0.84, 0.81 at wavelengths of 440 nm, 550 nm, 670 nm, and 870 nm, respectively. Finer particles with an average AE of 1.53, volume median radius of 0.157  $\mu\text{m}$ , and a standard deviation of 0.55  $\mu\text{m}$  for fine mode is observed for the same smoke plume. These results serve as a proxy for the scale and detail of aerosol retrievals that are anticipated from future space mission data, as HARP CubeSat (mission begins 2020) and HARP2 (aboard the NASA PACE mission with launch in 2023) are near duplicates of AirHARP and are expected to provide the same level of aerosol characterization.

## 1 Introduction

Aerosols play an important role in Earth's climate (Boucher et al., 2013; Hobbs, 1993; Kaufman et al., 2002; Koren et al., 2004): they directly perturb Earth's radiation budget and indirectly ~~modify~~by modifying cloud properties, which in turn influence the planet's energy and hydrological budgets (Lenoble et al., 2013; Penner et al., 2001). The *direct radiative effects* of aerosols, the absorption and scattering of light, depend on the intrinsic optical properties of the particles, the total aerosol loading and the radiative properties of the surface beneath the aerosol layer. Aerosols are highly variable, both in their spatial and temporal distributions, but also in their optical and microphysical properties; it is especially challenging to represent their radiative effect realistically in climate models (Dubovik et al., 2002; Masmoudi et al., 2003). Therefore, aerosol radiative forcing remains one of the main uncertainties in global climate change estimation (Boucher et al., 2013; Chen and Penner, 2005; Hansen et al., 2011; Penner et al., 2011). Furthermore, aerosols are a mixture of sub-millimeter, suspended particles with different sizes, morphology, and composition that result in complex physical, chemical and optical properties (Kahnert, 2010; Kokhanovsky et al., 2015; Tanré et al., 2011). To better characterize the aerosol role in the global radiation budget and narrow uncertainties in predicting climate change, we need to better understand and constrain the temporal and spatial distributions of these properties. In addition, a careful understanding of aerosol properties is essential for air quality monitoring/mitigation, characterizing fertilization of ecosystems, hydrological forecasting, etc. (Shiraiwa et al., 2017; Westberry et al., 2019).

The last few decades have seen unprecedented efforts to better characterize aerosol particle properties and aerosol radiative effects with in situ and remote sensing observations. For example, in situ measurements based on a wide variety of techniques, such as photoacoustic and cavity ring-down spectrometers, filter-based photometers, and polarized imaging nephelometers have provided detailed information on size, shape, and absorption for many different regions across the world, and continue to do so (Bergstrom et al., 2007; Bond et al., 1999; Dubovik et al., 2000; Espinosa et al., 2017, 2018; Moosmüller et al., 2005; Petzold et al., 2005; Rocha-Lima et al., 2014; Snider et al., 2015). However, in situ measurements have limitations due to the small sampling volumes that they represent and very limited in number and spatial coverage. In addition to in situ instruments, ground-based remote sensing networks, primarily the AErosol RObotic NETwork (AERONET), provide much larger coverage over the continental Earth (Holben et al., 1998, 2001). These AERONET observations measure downwelling direct sunlight, and from these measurements, it is possible to obtain highly accurate spectral aerosol optical depth (AOD), defined as the

integration of the aerosol extinction over the entire atmospheric column. In addition, AERONET instruments measure diffused and polarized sky radiance, from which columnar particle optical and microphysical properties are retrieved (Dubovik et al., 2006; Dubovik and King, 2000; Xu and Wang, 2015). AERONET instruments are widespread but are not truly global.

In order to achieve seamless global coverage, we need to rely on satellite remote sensing to characterize the global aerosol system, including particle properties. Most aerosol products retrieved from satellite instrument data are limited to AOD or qualitative aerosol type (Diner et al., 2008; Kahn et al., 2009; Lenoble et al., 2013; Levy et al., 2013; Limbacher and Kahn, 2019; Martonchik et al., 2002). Whereas, a Multi-Angle Polarimeter (MAP) have enough information content to retrieve particle properties with a greater degree of accuracy (Dubovik et al., 2011; Hasekamp and Landgraf, 2007; Knobelspiesse et al., 2012; Mishchenko et al., 2002; Mishchenko and Travis, 1997). A MAP instrument looks at Earth scenes at different viewing angles and measures the angular scattering and polarization of reflected light after interacting with Earth's surface, atmospheric molecules, clouds, and aerosols. Using multiple polarization angles and multiple wavelengths (if available), the aerosol signal can be isolated from the signals coming from the atmosphere and the surface beneath. Furthermore, these algorithms can invert MAP measurements to obtain optical properties of the aerosol within a significant level of certainty. This capability has been demonstrated by space-borne POLDER I, II and III (POLarization and Directionality of the Earth's Reflectance) (Deuzé et al., 1999, 2001; Dubovik et al., 2019; Goloub et al., 1999; Hasekamp et al., 2011; Leroy et al., 1997), and will be continued by the Multi-viewing multi-channel multi-polarisation imager (3MI): a future MAP instrument from the POLDER heritage scheduled to launch in 2021 (Fougnie et al., 2018). Currently, there are several modern MAP concepts that demonstrate technological advancements relative to the original POLDER, designed specifically as proxies for future spaceborne missions. These include, in addition to 3MI, Research Scanning Polarimeter (RSP) (Cairns et al., 1999, 2003), Airborne Multiangle Spectro Polarimetric Imager (AirMSPI) (Diner et al., 2013), SPEX Airborne (Smit et al., 2019), Observing System Including PolaRisation in the Solar Infrared Spectrum (OSIRIS) which is a 3MI airborne simulator, and Hyper-Angular Rainbow Polarimeter (HARP) (Martins et al., 2018; McBride et al., 2020). ~~For~~ There are several aerosol retrieval algorithms specifically optimized for MAPs which includes: SRON multi-mode inversion algorithm for SPEX airborne (Fu et al., 2020; Fu and Hasekamp, 2018); Microphysical Aerosol Property from Polarimeters (MAPP) (Stamnes et al., 2018) and GISS/RSP algorithm (Knobelspiesse et al., 2011; Waquet et al., 2009) for RSP; correlated multi-pixel and joint retrieval algorithm for AirMSPI developed at Jet Propulsion Laboratory (JPL) (Xu et al., 2017, 2019). This list is not complete, for a comprehensive review of the polarimetric remote sensing of atmospheric aerosols based on MAPs, we encourage the readers to refer to several reviews in the literature (Dubovik et al., 2019; Kokhanovsky et al., 2010, 2015; Remer et al., 2019). In this work, we focus on retrieval of aerosol properties using AirHARP data, the airborne version of HARP, from the NASA aircraft campaign, Aerosol Characterization from Polarimeter and Lidar (ACEPOL). We apply an inversion algorithm to AirHARP polarized measurements of the same target at different viewing angles and wavelengths. The specific inversion algorithm is Generalized Retrieval of Aerosols and Surface Properties (GRASP) (Dubovik et al., 2011, 2014).

In Section 2, we provide a theoretical background for the measurements of multi-angle polarimetry and the inversion of those measurements to retrieve aerosol properties, and then describe the AirHARP instrument specifically, define the measuring

100 geometry, and introduce the specific campaign when the measurements were made. Section 3 describes the GRASP retrieval after covering the preliminary work preparing measurements for retrieval, including gas corrections. The results of applying GRASP to AirHARP measurements, including comparisons to collocated High Spectral Resolution LiDAR - 2 (HSRL2) and AERONET, are shown and discussed in Section 4 and 5. Section 6 discusses future research directions. Finally, Section 7 offers a conclusion. In addition, we provide two appendices. One details the land and ocean surface models that are essential  
 105 to the GRASP inversion of aerosol, and the second one describes the calculation of aerosol optical depth from retrieved aerosol particles.

## 2 Background

### 2.1 Theoretical basis of the measurements and retrieval

MAP instruments measure radiances at different viewing angles, polarization angles, and spectral bands. The state of  
 110 polarization of measured light can be represented by the Stokes vector,  $\mathbf{S}$ , where the transpose of the vector is given as  $\mathbf{S}^T = [S_0 \ S_1 \ S_2 \ S_3 \ I \ Q \ U \ V]$  (Schott, 2009). The elements in the Stokes vector are,

$$\begin{bmatrix} S_0 \\ S_1 \\ S_2 \\ S_3 \end{bmatrix} = \begin{bmatrix} E_{\parallel}E_{\parallel} + E_{\perp}E_{\perp} \\ E_{\parallel}E_{\perp}^* + E_{\perp}E_{\parallel}^* \\ E_{\parallel}E_{\perp}^* - E_{\perp}E_{\parallel}^* \\ i(E_{\parallel}E_{\perp}^* - E_{\perp}E_{\parallel}^*) \end{bmatrix} \begin{bmatrix} I \\ Q \\ U \\ V \end{bmatrix} = \begin{bmatrix} E_{\parallel}E_{\parallel} + E_{\perp}E_{\perp} \\ E_{\parallel}E_{\perp}^* - E_{\perp}E_{\parallel}^* \\ E_{\parallel}E_{\perp}^* + E_{\perp}E_{\parallel}^* \\ i(E_{\parallel}E_{\perp}^* - E_{\perp}E_{\parallel}^*) \end{bmatrix} \quad (1.1)$$

Where  $E_{\perp}$  and  $E_{\parallel}$  are the perpendicular and parallel components of the electric field  $\vec{\mathbf{E}}$  respectively. The first element ( $S_0 I$ ) represents the total radiance. The second and third elements ( $S_1, S_2 Q, U$ ) represent the linear polarization of the radiance, and the fourth element ( $S_3 U$ ) represents circular polarization. Passive remote sensors, like AirHARP, use the sun as their light  
 115 source. Therefore, sunlight incident on the atmosphere is defined as:

$$\mathbf{S}_{\text{Inc}}^T = [S_0 \ 0 \ 0 \ 0] \cdot \mathbf{S}_{\text{Inc}}^T = [I \ 0 \ 0 \ 0] \quad (1.2)$$

Since the light from the sun is unpolarized,  $S_1, S_2 Q, U$ , and  $S_3 V$  of the Stokes vector are zero. The Stokes vector of the scattered light back into the instrument sensor is given by,

$$\mathbf{S}_{\text{sca}}^T = [S_{0\text{sca}} \ S_{1\text{sca}} \ S_{2\text{sca}} \ 0] [I_{\text{sca}} \ Q_{\text{sca}} \ U_{\text{sca}} \ 0] \quad (1.3)$$

where the light reaching the instrument sensor has now acquired some polarization but is assumed to be only linearly polarized, an assumption that holds well for the Earth's atmosphere and surface (Dubovik et al., 2011; Kokhanovsky et al., 2015). In this  
 120 paper, we use reduced radiances  $I R_1 = \frac{\pi S_{0\text{sca}}}{F_0} \frac{\pi I_{\text{sca}}}{F_0}$ ,  $Q = \frac{\pi S_{1\text{sca}}}{F_0} R_Q = \frac{\pi Q_{\text{sca}}}{F_0}$ , and  $U = \frac{\pi S_{2\text{sca}}}{F_0} R_U = \frac{\pi U_{\text{sca}}}{F_0}$  to define the Stokes vector of the scattered light measured by the MAP with  $I, Q, U, R_1, R_Q, R_U$  notation.  $F_0$  is the solar radiance ( $\text{Wm}^{-2}\mu\text{m}^{-1}$ ) and hence  $I, Q, R_1, R_Q$ , and  $U, R_U$  are dimensionless variables.  $I R_1$  is the total radiation measured by MAP, the same that would be measured by a radiometer normalized by  $F_0/\pi$ .  $Q, R_Q$  and  $U, R_U$  define orthogonal states of linear polarization and together, they form the *polarized intensity*, defined as (Schott, 2009),

$$P = \sqrt{Q^2 + U^2} R_P = \sqrt{R_Q^2 + R_U^2} \quad (1.4)$$

125 and the degree of linear polarization (*DoLP*) is

$$DoLP = P/R_I \quad (1.5)$$

## 2.2 AirHARP (Airborne Hyper Angular Rainbow Polarimeter)

The Hyper Angular Rainbow Polarimeter (HARP) is a modern MAP concept capable of wide Field-of-View (FOV), multi-angle, multi-wavelength polarimetric imagery of a ground scene even from a low-cost, CubeSat-size platform. The HARP program was initially funded by the NASA Earth Science and Technology Office (ESTO) InVEST program as a joint collaboration between the University of Maryland, Baltimore County (UMBC) in Baltimore, MD and the Space Dynamics Laboratory at Utah State University in Logan, Utah. There are currently three instruments based on the original HARP concept: HARP CubeSat, a self-contained space technology demonstration mission launched to the International Space Station in November 2019 for a year-long mission beginning in February 2020; HARP2, a payload instrument for NASA's Plankton, Aerosols, Clouds, ocean Ecosystem (PACE) mission set to launch in the early 2023s (Werdell et al., 2019); and AirHARP, an airborne version of the HARP concept. In this paper, we focus on aerosol retrievals derived from measurements made from AirHARP as a proxy for these future space missions.

AirHARP's swath spans an angle of 114° along-track and 94° in cross-track; a simulated cross-section image of the AirHARP instrument is shown in Fig. 1(a). It uses a Phillips prism system that splits the incoming beam of light into three components so that the radiation can be measured at three polarization angles simultaneously, with no moving parts. These polarization states are imaged on three CCD imaging sensors, denoted by A, B, and C, which measure the light at angles of linear polarization (AoLP) = 0°, 45°, and 90°, respectively, which are hereby denoted as  $I_A$ ,  $I_B$  and  $I_C$  radiances. AirHARP has three wavelengths (440 nm, 550 nm, and 870 nm) that measure at 20 along-track view angles plus a hyper-angle measurement at the 670 nm wavelength that measures at 60 along-track view angles (See Table 1). This capability allows AirHARP to view a single ground target from up to 60 different perspectives, and measure the angular scattering response emanating from that location in both total and polarized radiances. These radiances are measured in all four channels, and each collocated detector pixel, which corresponds to a single channel and view angle, is calibrated independently for the radiometric and polarimetric measurements.

Using the calibration matrix  $C$  and measured  $I_A$ ,  $I_B$  and  $I_C$ ; the  $S_0, S_1, S_2, S_3, Q_{sca}, U_{sca}$  elements of the Stokes vector are calculated using Eq. 2.1 (Fernandez-Borda et al., 2009) and subsequently reduced radiances  $I, Q, R, U$  for each collocated detector pixel.

$$\begin{bmatrix} S_0 \\ S_1 \\ S_2 \\ S_3 \end{bmatrix} \begin{bmatrix} I_{sca} \\ Q_{sca} \\ U_{sca} \end{bmatrix} = \begin{bmatrix} C_{11} & C_{12} & C_{13} \\ C_{21} & C_{22} & C_{23} \\ C_{31} & C_{32} & C_{33} \end{bmatrix} \begin{bmatrix} I_A \\ I_B \\ I_C \end{bmatrix} \quad (2.1)$$



The calibration matrix,  $\mathbf{C}$ , is derived from a laboratory calibration scheme described in Fernandez-Borda et al., 2009. The AirHARP instrument was validated in the lab to perform at a 3-5 % radiometric and 0.5 % *DoLP* uncertainty across all spectral bands, though the ~~HARP-CubeSat and~~ HARP2 may further reduce this uncertainty with improvements to on-board calibration and optical design (McBride et al. 2020, in prep). The study in this paper uses 3 % radiometric uncertainty for all the bands and 0.5 % *DoLP* uncertainty for 440 nm, 550 nm, and 670 nm and 1.5% for 870 nm as inputs to GRASP. The 870 nm polarimetric data ~~is also used in the GRASP retrievals but~~ has larger uncertainty due to lower signal-to-noise ratio in the field data compared to 440 nm, 550 nm, and 670 nm, therefore, we give these data less relative weight in the retrievals. The total radiance ( $I$ ) and *DoLP* are both useful for accuracy assessments and retrievals: they are not sensitive to reference plane that defines electric field  $\vec{\mathbf{E}}$ .  $Q$  and  $U$  as measured by AirHARP, on the other hand, are defined based on a reference plane and their absolute values depend directly on this chosen frame of reference. The details of this reference plane, including instrument scattering geometry, are described in the next section.

### 2.3 Definition of scattering geometry

Figure 2 defines the scattering geometry. Scattering angle ( $\theta_{\text{sca}}$ ) is defined as the angle between the sun vector and the viewing direction.  $\theta_s$  is the solar zenith angle,  $\theta_v$  is the instrument viewing zenith angle,  $\phi_{\text{sat}}$  is the satellite azimuthal angle and  $\phi_{\text{sun}}$  is the solar azimuthal angle. The relative azimuthal angle is  $\phi = \phi_{\text{sun}} - \phi_{\text{sat}}$ . For the calculation of  $\theta_{\text{sca}}$ , we need to know  $\theta_s$ ,  $\theta_v$  and  $\phi$ .

The reference plane for the definition of  $\mathbf{E}_{\perp}$  and  $\mathbf{E}_{\parallel}$  is based on the local ~~meridional~~meridian plane, which is a standard reference frame used for reporting  $Q$  and  $U$  (~~Emde et al., 2015~~)(~~Chandrasekhar, 1950~~; ~~Emde et al., 2015~~; ~~Hansen and Travis, 1974~~; ~~Hovenier et al., 2004~~). For detailed information please refer to the coordinate system as defined in the book by Hovenier et al. (2004).  $Q$  and  $U$  measured by AirHARP are based on the instrument reference frame and these are rotated to the local meridian plane that is formed of the local nadir vector plus the viewing zenith vector (see Fig. 2). The electric field parallel to the local meridian plane is called  $\mathbf{E}_{\parallel}$  and the electric field perpendicular to the local meridian plane is  $\mathbf{E}_{\perp}$ . Using the information from aircraft Inertial Measurement Unit (IMU), the  $Q$  and  $U$  are rotated to the local ~~meridional~~meridian plane from the instrument reference frame.

### 2.4 Aerosol Characterization from Polarimeter and LiDAR (ACEPOL)

The ACEPOL campaign (<https://www-air.larc.nasa.gov/missions/acepol/index.html>) was a collaborative effort of NASA and SRON (Netherlands Institute of Space Research) based out of Armstrong Flight Research Center (AFRC) in Palmdale, California, USA. One primary aim of the campaign was to acquire data using airborne advanced passive and active remote sensing instruments, and then use the expanded information content available from the new sensors, both individually and in synergy, to better characterize aerosol (Knobelspiesse et al., 2020). Multiple polarimeters and lidars were mounted on the NASA ER-2 aircraft. These included AirHARP, as well as AirMSPI (Diner et al., 2013), RSP (Cairns et al., 1999, 2003),

~~SPEX~~ airborne-~~SPEX~~ (Smit et al., 2019), HSRL2 (Burton et al., 2018; Hair et al., 2008) and Cloud Physics Lidar (CPL) (McGill et al., 2002). ACEPOL also made use of ground-based instruments such as AERONET and Micro-Pulse Lidar Network (MPLNET) for validation of aircraft measurements (Holben et al., 2001; Welton et al., 2001). The measurements and inversion algorithms used to analyze the ACEPOL data will be helpful in understanding the potential use of polarimeters in future satellite missions like the NASA PACE mission, the Aerosols, Clouds, Convection and Precipitation (A-CCP) Decadal Survey mission, and the European EarthCare mission. The ACEPOL campaign had nine flights over the period of October 19, 2017, to November 9, 2017, with a combined flight time of approximately 41.3 hours. The main objectives of ACEPOL include the calibration of instruments over ocean and land with no clouds or aerosol, geolocation of image using coastlines, coordinated Cloud-Aerosol Lidar and Infrared Pathfinder Satellite Observation (CALIPSO) or Cloud-Aerosol Transport System (CATS) under flights, validation with AERONET in low, medium and high aerosol loading, satellite intercomparison for aerosol and cloud retrievals, and calibration over a spatially uniform ~~surfaecessurface~~ amongst other lower priority goals, such as cirrus cloud observations- (Knobelspiesse et al., 2020).

For the ACEPOL 2017 campaign, the AirHARP instrument was mounted on an ER-2 aircraft left wing pod. It collected data over 8 flights consisting of a total of 45 flight leg images. For this study, we have analyzed only eleven of these flight legs, listed in Table 2, including scenes over the ocean, dry lakes, forest fire smoke, and AERONET sites. Along with the airborne polarimeters, the HSRL2 also flew aboard on the ER-2 aircraft during ACEPOL. ~~HSRL-2~~HSRL2 is a NASA high spectral lidar that has been used to measure clouds and aerosols (Burton et al., 2012; Hair et al., 2008). HSRL2 measures extinction coefficients at two wavelengths ( $2\alpha$  at 355 and 532 nm) and backscattering coefficients at three wavelengths ( $3\beta$  at 355, 532, and 1064 nm) (Burton et al., 2018). These measurements allow the detection of the vertical distribution of aerosol extinction with a precision of about  $0.02 \text{ km}^{-1}$ . The HSRL2 instrument points at nadir and measures the vertical profile of the aerosol backscatter coefficient at 0.1Hz frequency with a vertical resolution of 15m and aerosol extinction coefficient at 1 minute temporal resolution and 150 m vertical resolution. In some ACEPOL cases, due to atmospheric turbulence, interference in the HSRL2 measurement resulted in the inability to use the molecular channels at 355 nm and 532 nm to report the AOD and required assumed lidar ratios of 20 sr and 40 sr over the ocean and land, respectively. However, for all the comparisons shown in this study, those cases were avoided and HSRL2 AOD reported here required no lidar ratio assumptions.

### 3 Aerosol retrievals from AirHARP using GRASP

#### 3.1 Atmospheric gas absorption correction for aerosol retrieval

Before the inversion of the AirHARP measured  $I$ ,  $Q$  and  $U$  components, each measured pixel must be prepared for aerosol retrievals. This involves first avoiding groups of pixels that are inappropriate for an aerosol retrieval, such as clouds, and correcting for gaseous absorption in the remaining signal. Automatic algorithm-level cloud masking can be challenging. In the work presented here, scenes were selected by eye, so that there was no need to develop an automatic cloud mask for AirHARP at this time. However, correction for gaseous absorption was necessary.  $I$ ,  $Q$ , and  $U$  are corrected for the atmospheric gas

absorption using the technique mentioned in Patadia et al. (2018). For AirHARP spectral bands, gas absorption is most significant at the 550 nm and 670 nm bands and is mainly due to the four atmospheric gasses O<sub>2</sub>, H<sub>2</sub>O, O<sub>3</sub>, and NO<sub>2</sub>. Columnar optical depth of 0.004, 0.032, 0.014, and 0.003 due to atmospheric gases are observed at 440 nm, 550 nm, 670 nm, and 870 nm spectral bands respectively. The radiative transfer model: Unified Linearized Vector Radiative Transfer Model (UNL-VRM) (Wang et al., 2014; Xu and Wang, 2019) is used to calculate transmission due to the total effect of all atmospheric gas absorption, which is translated to a multiplicative correction factor for each of the four AirHARP bands. These correction factors are a function of the path length through the atmosphere, which is a combination of solar and instrument viewing zenith. All the calculations are done for a mid-latitude summer US atmosphere assuming no variation in the four gases and for an AirHARP observation height of 20 km above sea level. This correction is applied to each band, for each pixel, prior to the inversion.

### 3.2 Generalized Retrieval of Aerosol and Surface Properties (GRASP)

GRASP is a versatile retrieval algorithm that can be used for a variety of remote sensing and in-situ measurements to retrieve aerosol and surface properties (Dubovik et al., 2014). It is open-source software and is available free to non-commercial users for downloading from the website <https://www.grasp-open.com/>. GRASP first demonstrated its overall capability in an aerosol retrieval test study (Kokhanovsky et al., 2015). It has gone on to prove itself in a variety of real-world applications (Chen et al., 2018, 2019; Frouin et al., 2019; Li et al., 2019; Schuster et al., 2019; Torres et al., 2017). GRASP has been successfully applied to measurements from many different types of instruments (Benavent-Oltra et al., 2019; Espinosa et al., 2017, 2018; Román et al., 2018; Titos et al., 2019; Torres et al., 2017), but the most pertinent to AirHARP are the previous applications of GRASP to POLDER-3 on PARASOL (Chen et al., 2018, 2019; Dubovik et al., 2011; Frouin et al., 2019; Li et al., 2019) because of its familiar polarization, multi-wavelength, and multi-angle sampling characteristics.

GRASP consists of two modules: a forward model and an inversion module. For the case of aerosol measurements, the forward model consists of a polarized Radiative Transfer (RT) code to calculate the radiance measured by the instrument and it ~~also consists of a kernel to calculate the contribution of single scattering by the aerosol particles.~~ uses precalculated spheroidal kernel to calculate the contribution of single scattering by the aerosol particles following the strategy described by Dubovik et al. (2006, 2011). The kernel includes the pre-calculated full phase matrix elements, extinction and absorption for five log-normal size distributions with preselected size parameters for the range of real refractive index 1.33 to 1.7, and 0.0005 to 0.5 for the imaginary part of the refractive index for both spherical and non-spherical aerosol approximated by a mixture of spheroids with a fixed particle shape distribution derived in Dubovik et al., 2006. This approach allows for very fast and accurate calculations aerosol single-scattering properties in the wide range of refractive indices even for non-spherical aerosol. The details of the application of the kernels to satellite polarimetry are discussed in detail by Dubovik et al., 2011 (e.g. see Section 3.1, and Fig.4 in Dubovik et al., 2011).

For the RT calculations, GRASP uses a Successive Order of Scattering (SOS) scheme. The RT module consists of different surface Bi-Directional Reflectance Distribution Function (BRDF) and Bi-Directional Polarized Distribution Function (BPDF)

models for land and ocean. These models are briefly discussed in Appendix A, and further information about the RT code and single scattering database that are beyond the scope of this paper can be found in (Dubovik et al., 2011; Lenoble et al., 2007). The particle single-scattering ~~kernel~~ calculations that we employ for the AirHARP retrieval ~~uses~~ use one of two possible retrieval set-ups: 1) five fixed-log-normal distribution modes as described in Table 3, or 2) the aerosol is assumed as an external mixture of five aerosol components as described in Table 4. Both approaches were extensively used in PARASOL/GRASP processing and, therefore, considered here. For the first kernel possibility, the retrieval has 15 aerosol parameters to retrieve and is called as “GRASP/Five mode” kernel. Each of ~~those~~ the log-normal modes has a fixed mode radius and width. The ~~only~~ free parameter in the retrieval for particle size distribution is the concentration of particles in each bin. There are three lognormal modes in the fine mode ~~and two in the coarse mode~~ (log-normal modes 1 to 3 in Table 3) and two in the coarse mode (log-normal modes 4 and 5 in Table 3). Other retrieved parameters related to aerosol properties include a complex refractive index, aerosol layer height, and the fraction of spherical particles (SF). The same kernel is used for all the retrievals in this paper with an exception for the AERONET comparison mentioned in Section 5.2. For the AERONET comparison, we make use of the second GRASP kernel that has reduced the number of aerosol parameters from 15 to 6. This reduced parameter option is the “GRASP/Models” kernel, where particle properties are assumed for each aerosol components given in Table 4. Complex refractive index, SF, and particle size distribution of each aerosol components are fixed for this kernel. Only the concentration (weight) for each aerosol component is retrieved.

The inversion module in GRASP uses the multi-term least square method (LSM) to solve the following system of equations,

$$\begin{aligned} \mathbf{f}^* &= \mathbf{f}(\mathbf{a}) + \Delta_f \\ \mathbf{0}^* &= \mathbf{G}\mathbf{a} + \Delta_g \\ \mathbf{a}^* &= \mathbf{a} + \Delta_a \end{aligned} \tag{3.1}$$

where  $\mathbf{a}$  is a vector of unknowns and is called a *state vector*.  $\mathbf{f}^*$  is the vector which contains the instrument observations,  $\Delta_f$  is the uncertainty in the observations, and  $\mathbf{f}(\mathbf{a})$  is the forward model simulated observations. For the AirHARP observations,  $\mathbf{f}^*$  is a vector containing information of  $IR_1$ ,  $Q/I$ , (same as  $R_0/R_1$ ), and  $U/I$  (same as  $R_U/R_1$ ) or  $IR_1$  and  $DoLP$  for all the spectral bands and viewing angles. GRASP is able to accept different configurations of the input parameters to make its retrieval. We will use the following sets of input in this work in different situations:  $(R_1, Q/I, U/I)$ , or  $(R_1, DoLP)$ . The text will explicitly state the inputs in each instance. Given an ideal pixel, AirHARP measures 120 data points for each aforementioned variable. A priori smoothness constraints are imposed on the retrieved solution in order to suppress unrealistic oscillations in the retrieved characteristics. The second equation in Eq. 3.1 represents such smoothness constraint on the retrieved characteristics,  $\mathbf{0}^*$  is the zero vector and it imposes the forced constraint that the derivatives of retrieved parameters to be zero. The matrix  $\mathbf{G}$  includes the coefficients for calculating derivatives of state vectors approximated by finite differences. For example, unrealistic oscillations in particle size distribution are eliminated using coefficients calculated from derivatives with respect to radius. Similarly, spectral dependencies of the refractive index are imposed using the coefficients calculated using wavelength. Uncertainties in the smoothness constraints are represented by the  $\Delta_g$  term. ~~For the AirHARP retrievals, we use the predetermined five modal log-normal distribution mentioned in Table 3, unless otherwise stated. The volume median radius~~

280 ~~and standard deviation for each mode are fixed and only the particle volume concentration is allowed to vary. Also, we~~GRASP  
~~can perform retrievals using multi-pixel information in both spatial and temporal dimensions, however, in this study, we are~~  
~~not utilizing this feature due to the limited availability of data over the same place in the temporal dimension. We~~ use a priori  
constraints on the particle size distribution and these constraints are represented by third and last term in Eq. 3.2. A priori  
estimates of state vector parameters are given by  $\mathbf{a}^*$  and  $\Delta_{\mathbf{a}}$  is the ~~uncertainty~~uncertainty in the a priori constraints of  $\mathbf{a}^*$ . The  
285 multi-term LSM in GRASP finds the statistically optimized solution of the set of equations mentioned in Eq. 3.1 by minimizing  
the term,

$$2\Psi(\mathbf{a}) = (\mathbf{f}(\mathbf{a}) - \mathbf{f}^*)^T \mathbf{W}_{\mathbf{f}}^{-1} (\mathbf{f}(\mathbf{a}) - \mathbf{f}^*) + \gamma_g \mathbf{a}^T \mathbf{W}_g^{-1} \mathbf{G} \mathbf{a} + \gamma_a (\mathbf{a} - \mathbf{a}^*)^T \mathbf{W}_a^{-1} (\mathbf{a} - \mathbf{a}^*) \quad 3.2$$

where,  $\mathbf{W}_{\mathbf{f}} = \frac{1}{\epsilon_f^2} \mathbf{C}_{\mathbf{f}}$  is the weighting matrix calculated using the measurement covariance matrix  $\mathbf{C}_{\mathbf{f}}$  and the first diagonal  
element  $\epsilon_f$ , in the  $\mathbf{C}_{\mathbf{f}}$ . Similarly,  $\mathbf{W}_g = \frac{1}{\epsilon_g^2} \mathbf{C}_g$ ,  $\mathbf{W}_a = \frac{1}{\epsilon_a^2} \mathbf{C}_a$ , are calculated using the covariance matrices of a priori smoothness  
constraints and a priori constraints on the of the retrieved parameters.  $\gamma_g = \frac{\epsilon_f^2}{\epsilon_g^2}$ , and  $\gamma_a = \frac{\epsilon_f^2}{\epsilon_a^2}$  are the *Lagrange multipliers*  
290 (Phillips, 1962; Tikhonov, 1963) calculated using the information from the covariance matrices. ~~Since we assume that all the~~  
~~input variables have log-normal error distribution, the solutions to the set of equations in Eq. 3.1 are found by minimizing the~~  
~~term  $\Psi(\mathbf{a})$  in Eq. 3.2 using the Levenberg-Marquardt iterative method. For more detailed information on the theoretical~~  
~~background of the GRASP retrievals, please refer (Dubovik, 2006; Dubovik et al., 2011; Dubovik and King, 2000). In order to~~  
~~take into account, the non-negative character of measured and retrieved physical values in the retrieval optimization, the log-~~  
295 ~~normal error distributions are assumed for all positively defined measured characteristics and the minimization is defined for~~  
~~logarithms of all positively defined retrieved parameters. The solutions to the set of equations in Eq. 3.1 are found by~~  
~~minimizing the term  $\Psi(\mathbf{a})$  in Eq. 3.2. Since the radiative transfer in the atmosphere has pronounced non-linear character, the~~  
~~Levenberg-Marquardt (Levenberg, 1944; Marquardt, 1963) algorithm is harmoniously adapted into the statistically optimized~~  
~~fitting to assure the monotonic convergence of the iterative solution. These and other technical details of numerical inversion~~  
300 ~~are described in Dubovik et al., 2011 and in-depth discussion of the above methodological aspects are also can be found in~~  
~~Dubovik and King, 2000, and Dubovik, 2006.~~

The state vector  $\mathbf{a}$  includes the information on particle size distribution which is the concentration for five log-normal modes  
of Table 3, the complex refractive index in the four spectral bands that are independent of particle size, the fraction of spherical  
particles (SF), aerosol layer height, and parameters characterizing the directional reflectance of the surface. AOD is derived  
305 from retrieved aerosol properties using the method mentioned in appendix B.1. Additionally, fine mode AOD is calculated  
using modes 1-3 mentioned in Table 3 and coarse mode AOD using modes 4 and 5. Single Scattering Albedo (SSA), Angstrom  
Exponent (AE) are also derived from the retrieved aerosol properties. For the GRASP/Models approach, the state vector  $\mathbf{a}$   
includes the concentration for each aerosol component mentioned in Table 4. State vector  $\mathbf{a}$  does not contain information on  
the particle size distribution, SF, and complex refractive index. All this is embedded in the aerosol components which are close  
310 (with some modifications) to biomass burning, urban, urban polluted, maritime, and desert dust observed in AERONET

climatology by Dubovik et al., 2002. Among these, only desert dust is considered as completely non-spherical, and similarly to AERONET retrievals, uses a shape distribution mentioned in Dubovik et al., 2006. All the other types are treated as 100 % spherical particles. The details of the bi-modal size distribution parameters along with the fixed complex refractive index for each of the aerosol components are tabulated in Table 4 and are based on the work of Dubovik et al., 2002. Figure 3 shows the particle size distribution as a function of radii for the different aerosol components. The main differences between GRASP/Five mode and GRASP/Models approach are, 1.) instead of retrieving the concentration of each log-normal mode, concentration(weight) for each of the aerosol components mentioned in Table 4 are retrieved. 2) RRI, IRI, and SF are not retrieved since these are fixed for each of the aerosol components. This simplified approach significantly drops the complexity of the aerosol model by reducing the number of parameters retrieved directly in the joint retrieval. It helps in reducing the nonlinearity of the inverse problem and makes the separation of the surface and aerosol signal much less complicated compared to the GRASP/Five mode approach. At the same time, all aerosol total properties as SSA, effective size distribution, complex refractive index can be obtained using external aerosol mixture concept. The reduction of sought unknowns helps situations in lower information content (e.g., for low AOD) and makes the separation of the surface and aerosol signal much less complicated compared to a GRASP/Five mode kernel. This tendency is well identified in the in-depth analysis of PARASOL data processing using different retrieval setups by Chen et al. 2020 (In preparation). Like the GRASP/Five mode kernel, the state vector  $a$  includes the information on aerosol layer height. ~~The state vector  $a$  includes the information on particle size distribution which is the concentration for five log-normal modes of Table 3, the complex refractive index in the four spectral bands that are independent of particle size, the fraction of spherical particles (SF), aerosol layer height, and parameters characterizing the directional reflectance of the surface. AOD is derived from retrieved aerosol properties using the method mentioned in appendix B.1. Additionally, fine mode AOD is calculated using modes 1-3 mentioned in Table 3 and coarse mode AOD using modes 4 and 5. Single Scattering Albedo (SSA), Angstrom Exponent (AE) are also derived from the retrieved aerosol properties. Even though aerosol layer height is retrieved during the retrieval process, the sensitivity to aerosol height for the AirHARP wavelengths is negligible for most of the low loading cases. Retrieved aerosol layer height is thus not discussed in this work.~~

Retrieval of aerosol properties from MAPs is highly sensitive to the accurate representation of the directional reflectance from the surface. For the ocean pixels, the ~~Even though aerosol layer height is retrieved during the retrieval process, the sensitivity to aerosol height for the AirHARP wavelengths is negligible for most of the low loading cases. Retrieved aerosol layer height is thus not discussed in this work.~~ In the next section, we discuss the results of applying GRASP to AirHARP measurements of  $I$ ,  $Q$  and  $U$  for selected cases from the ACEPOL campaign.

## 340 ~~4 Aerosol properties from AirHARP measurements~~

### ~~4.1 Selected cases from ACEPOL 2017~~

~~We will focus on four specific cases from ACEPOL 2017 to illustrate the measurement characteristics of AirHARP and demonstrate the GRASP retrieval. Figure 3 shows color composite imagery of the intensity and DoLP of each case, using the 440, 550 and 670 nm bands. Cases include a scene over the ocean with little aerosol loading (23 October 2017; T21:30 UTC),~~  
345 ~~a scene over Rosamond Dry Lake (25 October 2017; T18:26 UTC), and two scenes of forest fire smoke (27 October 2017; 18:16 UTC and 9 November 2017; 19:30 UTC).~~

### ~~4.2 Scene over the ocean (23 October 2017 T21:30 UTC)~~

~~The first of our analysis scenes is a cloud-free segment where the ER-2 flew over the USC SeaPRISM AERONET station located at 33.564N, 118.118W, on a platform off the coast of southern California. The AERONET station measured a low aerosol loading of  $AOD = 0.04$  at 440 nm at the time of ER-2 overpass. The segment includes sun glint, and because of the~~  
350 ~~low AOD, the sun glint and non sun glint pattern are ideal for the intercomparison of different polarimeter measurements of  $I$ ,  $Q$ ,  $U$ , and  $DoLP$ . This flight track aligned with the solar principal plane so that the longer wavelength bands will be highly polarized for the sunglint viewing angles. For a scene with low aerosol loading above the ocean with no sun glint, the polarization follows the Rayleigh pattern and will peak at the 90 degree scattering angle. For the sunglint case, we expect the~~  
355 ~~peak to be at scattering angles where the sunglint is observed. In this case, the maximum sun glint occurs for scattering angles  $70^\circ$  to  $90^\circ$ . Figure 4 shows the measured  $I$ ,  $Q/I$ ,  $U/I$  and  $DoLP$  for one pixel (footprint of 55 m x 55 m) along the nadir track as a function of scattering and plotted as colored circles, for each of the four wavelengths. The measurements show that the maximum intensity occurs in the glint region (scattering angles  $70^\circ$  to  $90^\circ$ ) and confirms that the  $DoLP$  peak also occurs at the sunglint scattering angles. However, while the intensity falls to minimum levels outside of the glint region, the  $DoLP$  has a~~  
360 ~~more gradual fall off, as the Rayleigh pattern with maximum  $DoLP$  at  $90^\circ$  is superimposed on the dark ocean scene.~~

~~GRASP is applied to invert the measured  $I$ ,  $Q/I$  and  $U/I$  for the pixel represented in Fig. 4 for aerosol retrievals. The ocean surface model used is the NASA GISS model (Mishchenko and Travis, 1997) based on Cox and Munk (1954), in which the ocean surface reflectance is represented by three parameters: ocean surface albedo, the fraction of Fresnel reflection surface, and wind speed denoted by  $a_0$ ,  $a_1$ , and  $a_2$  respectively, with details given in Appendix A.2. Because the aerosol loading is very low for this scene, there is insufficient aerosol loading to retrieve the real (RRI) and the imaginary (IRI) part of the complex refractive index, and instead are constrained ( $RRI = 1.4$  and  $IRI = 0.0001$ ) in GRASP using an oceanic aerosol model mentioned in Hasekamp et al. (2008). The five mode particle size distribution (Table 3) These three parameters are the surface components in the state vector  $a$  for the case of ocean pixels. For the case of land pixel, Ross-Thick Li-Sparse linear BRDF model is used to represent the directional reflectance from the surface (see Appendix A.1.1), which uses three parameters  $K_0$ ,  $K_1$ ,  $K_2$ , is used in the retrieval, with the concentrations of each of the five modes unconstrained. Therefore, the retrieved~~

365  
370



parameters include the five concentrations for the five lognormal modes shown in Table 3, aerosol spherical fraction, aerosol layer height, and the ocean model parameters  $a_0$ ,  $a_1$ , and  $a_2$ . AOD is derived from the retrieved and modeled parameters. The solid black lines plotted in all panels of Fig. 4 are the GRASP fits using the AirHARP measured  $I$ ,  $Q/I$ , and  $U/I$  as input. The  $DoLP$  is also calculated from the fitted variables and plotted in the same figure. The sunglint registers in  $I$  as a sharp peak with the width of that peak dependent on surface roughness primarily caused by surface wind. The retrieval of aerosol properties is highly sensitive to wind speed. An inappropriate wind speed estimate can result in high uncertainty in the aerosol properties retrieved. The goodness of the fit in Fig. 4 suggests that retrieval of the ocean parameters, including wind speed is very good for this sampled pixel.

To achieve a better understanding of how well the GRASP retrieval can fit the measurements, we apply the retrieval to 3600 pixels (60 x 60) of this ocean scene. Here, a pixel footprint of 55 m x 55 m is used, since the variability due to the geolocation is negligible for an open ocean pixel as compared to a land pixel. Figure 5 shows two dimensional density scatter plots of the AirHARP measured variables,  $I$ ,  $Q/I$ , and  $U/I$  for the four spectral bands, versus the GRASP fit, and the histogram of the number of points used for each bin is plotted on the respective axes. A dashed magenta line represents the Ordinary Least Square (OLS) fit between retrieved and measured parameters, a black solid line denotes the 1:1 line. The goodness of fit,  $\chi_{norm}^2$  for each pixel, is calculated using the mathematical expression mentioned in Table 4. A list of the statistical parameters used in this study are formulated in Table 4, where  $x_i$  is the measured value, and  $y_i$  is the GRASP fit.  $N$  is the total number of observations for the pixel,  $S_y$  is the error covariance matrix for the observations.  $S_y$  includes only diagonal elements and off-diagonal are assumed to be zero since we do not consider the cross correlation between the different viewing angles for the same spectral band. For the reduced radiance  $I$ , all spectral bands show a good comparison at lower  $I$  values, within the  $\chi_{norm}^2$  confidence interval, and show a slight deviation from the 1:1 line for the sunglint angle data points. The GRASP fit in blue band yields an underestimated  $I$  when its values are greater than 0.2, giving an overall OLS slope of 0.967. However, the range where the underestimation occurs represents only a small fraction of the total analyzed samples. This underestimation is also observed for the 550 nm band with a slightly better  $R^2$  value of 0.995 compared to 0.986 for the 440 nm band. For the case of 670 and 870 nm bands, we observed a slight overestimation with the GRASP fitting having  $R^2$  values 0.997 and 0.996 for red and NIR bands respectively. Some of this under and overestimation is because the isotropic wind model has trouble simulating the multi angle views in the sun glint region. In terms of the spread of points around the regression line, we expected much higher noise for the 870 nm band due to the lower signal to noise ratio (SNR) in this band. Surprisingly, in terms of fitting the  $I$  component, the 870 nm band does not display any repercussion of the lower SNR. For the polarization components  $Q/I$  and  $U/I$ , all the spectral bands demonstrate a good correlation between the GRASP fit and AirHARP measurements. This clearly demonstrates that the polarization variables are less affected by the discrepancies in sunglint pixels for the extreme viewing angles. The average AOD retrieved for these 60 pixels by 60 pixels region are  $0.07 \pm 0.03$ ,  $0.04 \pm 0.02$ ,  $0.03 \pm 0.01$ , and  $0.02 \pm 0.01$  at 440 nm, 550 nm, 670 nm, and 870 nm respectively. In the following section, we detail several case studies of AirHARP land surface, and aerosol plume data applied to GRASP for retrieval of aerosol microphysical and optical properties.

### 4.3 GRASP retrieval over land

For the GRASP retrieval applied to measurements over land, the Ross Thick Li Sparse BRDF model is used to represent the directional reflectance from the surface, which uses three parameters  $K_0, K_1, K_2$ .  $K_0$  is a spectrally dependent parameter that represents the isotropic reflectance,  $K_1$  and  $K_2$  normalized to  $K_0$  are the spectrally independent parameters which are the coefficient of geometric and volumetric scattering kernels respectively (Maignan et al., 2004; Wanner et al., 1995). Polarized reflectance from the surface is modeled using the Maignan-Breon one-parameter model and the retrieved parameter is a scaling factor ( $\alpha$ ) that is spectrally dependent (Maignan et al., 2009). Refer to Appendix A.1.32 for detailed information on the surface models. The four parameters  $K_0, K_1/K_0, K_2/K_0$ , and  $\alpha$  are the surface components in the state vector  $a$  for the case of land pixels. In the next section, we discuss the results of applying GRASP to AirHARP measurements of  $R_i, Q/I$  and  $U/I$  for selected cases from the ACEPOL campaign.

## 4 Aerosol properties from AirHARP measurements

### 4.1 Selected cases from ACEPOL 2017

We will focus on four specific cases from ACEPOL 2017 to illustrate the measurement characteristics of AirHARP and demonstrate GRASP retrieval. Figure 4 shows color composite imagery of the intensity and DoLP of each case, using the 440, 550, and 670 nm bands. Cases include a scene over the ocean with little aerosol loading (23 October 2017; T21:30 UTC), a scene over Rosamond Dry Lake (25 October 2017; T18:26 UTC), and two scenes of forest fire smoke (27 October 2017; T18:16 UTC and 9 November 2017; T19:30 UTC).

### 4.2 Scene over the ocean (23 October 2017 T21:30 UTC)

The first of our analysis scenes is a cloud-free segment where the ER-2 flew over the USC SeaPRISM AERONET station located at 33.564N, 118.118W, on a platform off the coast of southern California. The AERONET station measured a low aerosol loading of  $AOD = 0.04$  at 440 nm at the time of ER-2 overpass. The segment includes sun glint, and because of the low AOD, the sun glint and non-sun glint pattern are ideal for the intercomparison of different polarimeter measurements of  $I, Q, U$ , and  $DoLP$ . This flight track aligned with the solar principal plane so that the longer wavelength bands will be highly polarized for the sunglint viewing angles. For a scene with low aerosol loading above the ocean with no sun glint, the polarization follows the Rayleigh pattern and will peak at the 90-degree scattering angle. For the sunglint case, we expect the peak to be at scattering angles where the sunglint is observed. In this case, the maximum sun glint occurs for scattering angles  $70^\circ$  to  $90^\circ$ . Figure 5 shows the measured  $R_i, Q/I, U/I$ , and  $DoLP$  for one pixel (footprint of 55 m x 55 m) along the nadir track as a function of scattering and plotted as colored circles, for each of the four wavelengths. The measurements show that the maximum intensity occurs in the glint region (scattering angles  $70^\circ$  to  $90^\circ$ ) and confirms that the  $DoLP$  peak also occurs at the

435 sunglint scattering angles. However, while the intensity falls to minimum levels outside of the glint region, the *DoLP* has a more gradual fall off, as the Rayleigh pattern with maximum *DoLP* at 90° is superimposed on the dark ocean scene.

GRASP is applied to invert the measured  $R_i$ ,  $Q/I$  and  $U/I$  for the pixel represented in Fig. 5 for aerosol retrievals. Because the aerosol loading is very low for this scene, there is insufficient aerosol loading to retrieve the real (RRI) and the imaginary (IRI) part of the complex refractive index, and instead are constrained ( $RRI = 1.4$  and  $IRI = 0.0001$ ) in GRASP using the values of the oceanic aerosol model mentioned in Hasekamp et al. (2008). This will reduce the number of retrieved parameters and thus reducing the complexity of the inversion problem by reducing the non-linearity of the forward model. GRASP/Five mode kernel is used in the retrieval, with the concentrations of each of the five modes unconstrained. Therefore, the retrieved parameters include the five concentrations for the five lognormal modes shown in Table 3, aerosol spherical fraction, aerosol layer height, and the ocean model parameters  $a_0$ ,  $a_1$ , and  $a_2$ . AOD is derived from the retrieved and modeled parameters. The solid black lines plotted in all panels of Fig. 5 are the GRASP fits using the AirHARP measured  $R_i$ ,  $Q/I$ , and  $U/I$  as input. The *DoLP* is also calculated from the fitted variables and plotted in the same figure. The sunglint registers in  $R_i$  as a sharp peak with the width of that peak dependent on surface roughness primarily caused by surface wind. The retrieval of aerosol properties is highly sensitive to wind speed. An inappropriate wind speed estimate can result in high uncertainty in the aerosol properties retrieved. The goodness of the fit in Fig. 5 suggests that retrieval of the ocean parameters, including wind speed is very good for this sampled pixel.

To achieve a better understanding of how well the GRASP retrieval can fit the measurements, we apply the retrieval to 3600 pixels (60 x 60) of this ocean scene. Here, a pixel footprint of 55 m x 55 m is used, since the variability due to the geolocation is negligible for an open ocean pixel as compared to a land pixel. Figure 6 shows two-dimensional density scatter plots of the AirHARP measured variables,  $R_i$ ,  $Q/I$ , and  $U/I$  for the four spectral bands, versus the GRASP fit, and the histogram of the number of points used for each bin is plotted on the respective axes. A dashed magenta line represents the Ordinary Least Square (OLS) fit between retrieved and measured parameters, a black solid line denotes the 1:1 line. The goodness of fit,  $\chi^2_{norm}$  for each pixel, is calculated using the mathematical expression mentioned in Table 5. A list of the statistical parameters used in this study are formulated in Table 5, where  $x_i$  is the measured value, and  $y_i$  is the GRASP fit.  $N$  is the total number of observations for the pixel,  $S_y$  is the error covariance matrix for the observations.  $S_y$  includes only diagonal elements and off-diagonal are assumed to be zero since we do not consider the cross-correlation between the different viewing angles for the same spectral band. For the reduced radiance  $R_i$ , all spectral bands show a good comparison at lower  $R_i$  values, within the  $\chi^2_{norm}$  confidence interval, and show a slight deviation from the 1:1 line for the sunglint angle data points. The GRASP fit in blue band yields an underestimated  $R_i$  when its values are greater than 0.2, giving an overall OLS slope of 0.967. However, the range where the underestimation occurs represents only a small fraction of the total analyzed samples. This underestimation is also observed for the 550 nm band with a slightly better  $R^2$  value of 0.995 compared to 0.986 for the 440 nm band. For the case of 670 and 870 nm bands, we observed a slight overestimation with the GRASP fitting having  $R^2$  values 0.997 and 0.996

for red and NIR bands respectively. Some of this under and overestimation is because the isotropic wind model has trouble  
 470 simulating the multi-angle views in the sunglint region. In terms of the spread of points around the regression line, we expected  
much higher noise for the 870 nm band due to the lower signal to noise ratio (SNR) in this band. Surprisingly, in terms of  
fitting the  $R_i$  component, the 870 nm band does not display any repercussion of the lower SNR. For the polarization components  
 $Q/I$  and  $U/I$ , all the spectral bands demonstrate a good correlation between the GRASP fit and AirHARP measurements. This  
demonstrates that the polarization variables are less affected by the discrepancies in sunglint pixels for the extreme viewing  
 475 angles. The average AOD retrieved for these 60 pixels by 60 pixels region are  $0.07 \pm 0.03$ ,  $0.04 \pm 0.02$ ,  $0.03 \pm 0.01$ , and  $0.02 \pm 0.01$   
at 440 nm, 550 nm, 670 nm, and 870 nm respectively. In the following section, we detail several case studies of AirHARP  
land surface, and aerosol plume data applied to GRASP for retrieval of aerosol microphysical and optical properties.

### 4.3 GRASP retrieval over land

Equally important over the land for a multi-angle instrument is the need to co-register each along-track view angle of the same  
 480 target. Over the flat ocean, co-registration is straightforward and is based on a projection of the measurements onto a  
 representation of a smooth geoid Earth. Over the land, topography introduces a challenging situation in which forward and aft  
 views of the same target might image different slopes of a ridge. Topographically corrected projections need to be made either  
 to a digital elevation model at a resolution comparable to the measurements (this is operational for AirHARP Level 1B data),  
 or the measurements need to be projected to a specific altitude in the atmosphere, perhaps cloud top height or to an aerosol  
 485 layer. Figure 67 shows the measured  $R_i$ ,  $Q/I$ ,  $U/I$ , and  $DoLP$  from the 550 nm wavelength for selected pixels in each of the  
 following three flight legs under analysis. In this figure, unlike Fig. 34, the ocean scene is from an offglint pixel. The other  
 pixels represent a dry lake surface, vegetation, and smoke, respectively. Also plotted as the black curves are the GRASP fit to  
 each of these targets. The ocean pixel appears the easiest to fit, and then the smooth dry lake pixels. The other land surface  
 types, with their variable topography, present a greater challenge for GRASP. In the next section, we detail these three flight  
 490 segments over land that include, one on 25<sup>th</sup> October 2017 over Rosamond dry lake at 18:16 UTC, a second one that is a  
 forest fire smoke scene near the Kaibab National Forest and Grand Canyon National Park in Arizona, USA on 27<sup>th</sup> October  
 2017 at 18:16 UTC, and a third scene of fresh smoke on 9<sup>th</sup> November 2017 at 19:30 UTC.

#### **4.3.1 Rosamond dry lake and surrounding vegetation (25 October 2017 T18:26 UTC)**

The flight leg with Rosamond dry lake on 25 October 2017 T18:26 UTC, is a scene with very low aerosol loading according  
 495 to the Moderate Resolution Imaging Spectroradiometer (MODIS) retrieval of AOD at 550 nm = 0.03. The minimal AOD  
 allows for the measured signal to be dominated by surface reflectance features. The retrieved AOD of the pixel of the dry lake  
 whose measurements and GRASP fit are shown in Fig. 67(b) were 0.05, 0.04, 0.04, 0.04 for the 440 nm, 550 nm, 670 nm, and  
 870 nm bands, respectively. Measurement and GRASP fit for another pixel from the same scene but over nearby vegetation  
 (farm field) is plotted in Fig. 67(c) and the retrieved AOD are 0.04, 0.03, 0.03, 0.02 for 440 nm, 550 nm, 670 nm, and 870 nm  
 500 bands respectively. Note that GRASP retrieves a very similar atmosphere over both surfaces. Yet, in Fig. 67(b) the

homogenous surface of the dry lake provides a simpler retrieval and the result is a better fit to the measurements than does the more complex surface presented by the vegetation. The RGB image of the flight leg on 25 October 2017 at 18:26 UTC is plotted in Fig. 34(b).

#### 4.3.2 Forest fire smoke (27 October 2017 T18:16 UTC)

Up to now, all our examples have demonstrated AirHARP measurements and GRASP retrievals in very low aerosol loading. These situations can demonstrate ~~GRASP~~GRASP's ability to fit the measurements and to return values for spectral AOD. The low aerosol loading does not supply enough signal to fully characterize the aerosol using GRASP. The final example that we show, the flight leg on 27 October 2017 at 18:16 UTC, captures a fire and smoke plume with significant aerosol loading. This will demonstrate the potency of AirHARP/GRASP to characterize aerosol particle properties, along with loading. This case has complicated terrain and due to the higher resolution of the pixels, the aerosol retrievals from this scene will be complicated. As a quick check, we show the GRASP retrieval fit to the input measurements in Fig. 67(d) for a single pixel in the smoke plume where the terrain is not that complicated and homogenous smoke is observed. The retrieval is fitting to the measurements well. AOD retrieved at this pixel is 1.62, 1.2, 0.85, and 0.51 for the 440 nm, 550 nm, 670 nm, and 870 nm bands, respectively. An RGB image of the smoke scene on 27 October 2017 at 18:16 UTC is plotted in Fig. 78 with X and Y axis as pixel locations. The GRASP algorithm is applied to 7150 pixels in a large area marked by the red rectangle as shown in Fig. 7, ~~and retrievals for the whole segment are plotted in Fig. 8, 8, and retrievals for the whole segment are plotted in Fig. 9. Measured  $R_I$  and  $DoLP$  are used for fitting in the GRASP algorithm since these two variables are not sensitive to the definition of the local meridian plane. Whereas,  $O/I$  and  $U/I$  are sensitive to the plane of reference for polarization and this can introduce retrieval error due to the error in the rotation of  $O$  and  $U$  from the instrument reference plane to the local meridian plane. To avoid an extra source of uncertainty,  $R_I$  and  $DoLP$  are used as the input in GRASP for large scale retrievals. One exception is that for the ocean pixel study using the flight leg on 23-October-2017 T21:30 UTC we have used  $R_I$ ,  $O/I$  and  $U/I$  for the retrieval. This leg has been thoroughly quality checked for the error in the rotation of  $O$  and  $U$  from the instrument reference plane to the local meridian plane.~~ Retrievals include AOD, RRI, IRI, and SSA at the four spectral bands of AirHARP. AOD is plotted across the image, but the intrinsic particle properties are only shown where GRASP recognizes enough aerosol loading to be sensitive to particle properties. Thus, the plots follow the smoke plume. For the retrievals, a combination of Ross-Li and Maignan-Breon land surface BRDF and BPDF models are used to represent the directional reflectance from the land surface. The pixels are spatially averaged to a resolution of 550 m x 550 m to avoid the micro pixel movement effects which will affect the aerosol retrievals. High non-homogenous smoke near the source makes accurate aerosol retrieval difficult. This is because the GRASP assumes a plane parallel aerosol layer in the radiative transfer multi-angle calculations, whereas in reality at different viewing angles we are seeing different locations in the plume, which introduces complications in the radiative transfer calculations.

Figure 89 (a) shows the retrieved AOD for the 440 nm, 550 nm, 670 nm, and 870 nm spectral bands. The AOD at 440 nm band is much higher than the one at 870 nm band as we expect for the fine forest fire particles. For the higher confidence in the retrieved results, pixels with  $\chi^2_{norm} > 5$  and  $AOD_{440\text{ nm}} < 0.4$  are removed from the analysis of SSA, RRI, IRI, AE, aerosol

volume concentration, and SF. Retrieved forest fire smoke optical properties from the flight leg on 27 October 2017 at 18:16  
 UTC using AirHARP observations are close to values seen previously in the literature. The values of RRI retrieved from  
 AirHARP and shown in Figure 89(c) can be represented as a Gaussian distribution with a mode value of 1.55 for all  
 wavelengths, while retrievals from the RSP ~~instrument and SPEX airborne instruments~~ during the ACEPOL campaign  
 produced values of RRI of 1.56 ~~and 1.58 respectively for a similar forest fire smoke~~ (Fu et al., 2020). Fire Laboratory at  
 Missoula Experiments (FLAME) records the real part of the refractive index in a range from 1.55 to 1.8, depending on the  
 composition of the smoke particles (Poudel et al., 2017). FLAME 2 laboratory experiments reported RRI values in the range  
 of 1.54 to 1.67 depending on the fuel source (Mack et al., 2010). The AirHARP retrievals of IRI range from 0.01 to 0.1 with a  
 mean value of 0.024 (Figure 89(d)), which compares well with the FLAME database range of 0.01 to 0.5 and FLAME 2  
 database range of 0.011 to 0.217 (Mack et al., 2010). Another smoke optical property study reports SSA in the range of 0.78  
 to 0.94 at 532nm, depending on the age of the smoke (Nicolae et al., 2013). Our retrieved SSA from AirHARP in this work  
 (see Fig. 89(b)) ranges from 0.6 to 0.99 with a mean value of  $0.87 \pm 0.06$ ,  $0.86 \pm 0.07$ ,  $0.84 \pm 0.08$ , and  $0.81 \pm 0.09$  for 440nm,  
 550nm, 670nm, and 870nm, respectively. Retrieved single scattering albedo values are well within the range measured during  
 the FLAME 2 experiment using a ~~photo-acoustic spectrometer and a nephelometer. Fine and coarse mode AOD calculated  
 using the log-normal modes listed in the Table 3 are plotted in Fig. 9~~ ~~photoacoustic spectrometer and a nephelometer and are  
 close to the retrieved values from SPEX airborne and RSP by Fu et al., 2020. Fine and coarse mode AOD calculated using the  
 log-normal modes listed in Table 3 are plotted in Fig. 10(a) and 109(b).~~ The main contribution to AOD is from the fine particles  
 (log-normal modes 1 to 3 in Table 3) with almost no contribution from coarse mode (log-normal modes 4 and 5 in Table 3).  
 The retrieved volume median radius for the fine mode ( $r_{v, \text{fine}}$  (see Eq. B.1.6)) is  $0.157 \pm 0.024 \mu\text{m}$  with  $\sigma_{v, \text{fine}} = 0.550 \pm 0.026$   
 $\mu\text{m}$ . Figure 4011(a) shows the AE derived for each pixel calculated using 440nm and 870nm spectral bands. Figure 4011(b)  
 and 4011(c) are aerosol volume concentration ( $\mu\text{m}^3 \mu\text{m}^{-2}$ ) and SF retrieved respectively for each pixel inside the red box in  
 Fig. 78. The Angstrom exponent retrieved from our measurement has a mean value of 1.53 with a standard deviation of 0.336.  
 Also, we see a significant number of pixels with AE >2 which is considered to be fresh smoke (Nicolae et al., 2013). In the  
 smoke scene retrieved from AirHARP measurements the mean value of the percentage of spherical particles is 50 % with a  
 standard deviation of 36 %. It essentially means that the retrieved particle shape of the smoke particles have been retrieved as  
 highly non-spherical for much of the smoke plume, while reports from SPEX and RSP for the same smoke scene indicate the  
 opposite with 99 % and 85 % spherical for SPEX ~~airborne~~ and RSP, respectively (Fu et al., 2020). However, we see that in  
 our retrievals for the scene in Fig. 78 there are ~~a~~ significant number of smoke pixels with spherical fraction close to 100 %  
 (see Fig. 4011(c)). While smoke properties are often spherical (Manfred et al., 2018; Martins et al., 1998), non-spherical fractal  
 shapes can be seen in scanning electron microscopy (Chakrabarty et al., 2006). There is no definite answer whether the results  
 shown in Fig. 4011(c) are a retrieval ~~artefact~~ ~~artifact~~ or are physically true. We do know from experimentation that the GRASP  
 retrievals in this situation ~~was~~ ~~were~~ not particularly sensitive to particle shape, returning the same values for AOD and SSA,  
 within ~~uncertainty~~ ~~uncertainty~~ bounds, whether SF was held constant at 80-99 % or whether it was a free parameter and  
 retrieved as in Fig. 4011(c). A table of retrieved and derived parameters is listed in Table 56. In order to check the quality of



the data fitting for the smoke scene of Fig. 7, 8, 9, 10, and 11, 2D density plots of measured and fitted variables,  $\overline{R}_i$  and  $DoLP$ , for all spectral bands are plotted in Fig. 12. Figures 12 (a), (c), (e), and (g) show the 2D density plot for the reduced radiance  $\overline{R}_i$  measured at four spectral bands 440 nm, 550 nm, 670 nm, and 870 nm respectively. 2D density plot of the measured and GRASP fitted  $DoLP$  at 440 nm, 550 nm, 670 nm, and 870 nm are plotted in Fig. 12(b), (d), (f), and (h) respectively. The fit for  $DoLP$  in 870 nm band has a higher spread in the density plot compared to the other spectral bands because the Silicon-based detector used for imaging in AirHARP has a lower quantum efficiency at 870 nm compared to the three other wavelengths. 550 nm and 670 nm bands data shows the best correlation to GRASP fit with  $R^2 = 0.991$  and  $0.993$  for  $\overline{R}_i$ , whereas, 440 nm and 870 nm have  $R^2 = 0.986$  and  $0.990$  respectively. Ordinary Least Square (OLS) regression for the 440 nm yields a slope of 0.984, which is the least performing band for the variable  $\overline{R}_i$ , followed by 870 nm, 550 nm, and 670 nm spectral bands. For the case of  $DoLP$ , 870 nm has the lowest  $R^2$  value of 0.960, followed by 670 nm ( $R^2 = 0.991$ ). Both 440 nm and 550 nm bands have an  $R^2$  value of 0.995. Unlike the variable  $\overline{R}_i$ , the  $DoLP$  in the 550 nm band shows more deviation from the 1:1 line with a slope of 0.964 for OLS regression fit. Overall, the 2D density plots reveal that the fitting for each variable  $\overline{R}_i$  and  $DoLP$  generated using the GRASP and AirHARP measurements performs well for the smoke scene in Fig. 7. Since the retrieval is an ill-posed mathematical problem, we need to make sure that the retrieved values are reasonable and compatible with co-incident instruments. For the case of the ACEPOL campaign, AOD from the AirHARP-GRASP retrievals are verified by comparing it with HSRL2 and AERONET observations. In the next subsection, we use the flight leg on 9<sup>th</sup> November 2017 at 19:30 UTC to compare the AOD retrievals from AirHARP with the collocated HSRL2 measurements.

## 5 Comparison of AirHARP GRASP retrievals with collocated data sets

### 5.1 High Spectral Resolution LIDAR-2 (HSRL2) vs AirHARP AOD comparison

HSRL2, flying on the same aircraft with AirHARP during ACEPOL provides the opportunity to compare the GRASP retrievals of AOD with an independent and collocated measurement. AirHARP lacks a wavelength channel identical to the wavelengths measured by HSRL2; therefore, for this study, we make use of the 440 nm and 550 nm channels on AirHARP to calculate the Angstrom exponent and then use that information to interpolate the AOD to HSRL2's wavelength of 532 nm. We collocate HSRL2 and AirHARP measures of AOD for the smoke plume shown in Fig. 34(d), (9 November 2017; 19:30 UTC). The smoke plume in this image is a controlled fire started in the Kaibab National Forest, Arizona, USA and is highly non-homogenous near the source fire. The extreme non-homogeneity of the smoke in this scene introduce additional uncertainty to the particle property retrievals and only AOD will be shown here. To match the HSRL2 ground pixel in the AirHARP image, the latitude and the longitude are matched to a tolerance level of about 200m on the ground. For this flight leg, HSRL2 reports the aerosol extinction at 10 s intervals, which translates to 2 km in the ground distance for an ER-2 aircraft flying at 20 km altitude with a speed of ~200 m/s, but with a narrow cross-track footprint of only 15 m. Thus the 2000 m x 15 m footprint of the HSRL2 measurements are inherently mismatched with AirHARP's 275 m x 275 m pixels. Given the inhomogeneity of this



aerosol, we do not expect perfect agreement between the two sensors' retrieved AODs, simply because of the mismatch in spatial sampling.

For this study, we make use of the HSRL2 AOD at 532 nm, where an assumption of the lidar ratio is not required. All the GRASP retrievals for this comparison are done using the  $R_L$  and  $DoLP$  measurements from AirHARP. Aerosol optical depth at 532 nm as a function of the collocated along-track pixels is plotted in Fig. 4213(a), and the scatter plot of the comparison is shown in Fig. 4213(b). In Fig. 4213(a) HSRL2 measured AOD is denoted by the green diamond markers, and AirHARP AOD the grey squares. Each square represents the mean of 28 pixels around the collocated HSRL2 ground pixel in the AirHARP image. We used 7 pixels along-track (~1.93km) and 4 pixels cross-track (~1.1km) to find those mean values. The error bar in the AirHARP data points is the standard deviation of AOD of all pixels within the ~1.93 km x 1.1 km region around the HSRL2 ground pixel, representing the spatial variability of the smoke plume within the averaging rectangular box. For this heterogeneous smoke plume case, we had to apply  $\chi^2_{norm} < 20$ , to filter out bad pixels/fits. Non-homogeneity of the smoke makes the retrieval complicated since we see different parts of the smoke plume when we scan through the different viewing angles of AirHARP data. So, using a higher  $\chi^2_{norm}$  value for filtration helps to catch the higher AOD values. A scatterplot of these two data sets is shown in Fig. 4213(b) and the solid black line is the 1:1 line whereas, the yellow error bar represents the spatial variability of AirHARP AOD similar to that in Fig. 4213(a). A comparison of HSRL2 measured AOD at 532 nm with the AirHARP AOD retrievals at 532 nm shows a strong, positive correlation and only deviates when the plume is thick and heterogeneous. A Pearson correlation coefficient ( $\rho$ ) of 0.940,  $BIAS = -0.062$ , and Mean Absolute Error ( $MAE$ ) = 0.122 is obtained for this comparison. Matching the HSRL2 AOD in regions of heterogeneity is challenging ~~using 1D plane parallel aerosol assumptions; the aerosol layer must be characterized first, i.e. from the HSRL2 AOD vertical profile, and used as input in a 3D radiative transfer simulation to calculate  $I$ ,  $Q$  and  $U$  for the scene at different viewing angles. Also, the~~ due to spatial mismatch between AirHARP and HSRL2 pixels. This will create issues where there is a sharp variation in the AOD, like close to the source, and in the boundary of the smoke plume. The different cross-track pixel size between the HSRL2 and AirHARP measurement makes the intercomparison difficult to interpret in some cases. For points near the plume source, higher pixel variability may also bias AirHARP AOD retrievals performed at the same general location as the HSRL2 measurement. In a scene with this much complexity, there is additional uncertainty in matching multiangle views for the AirHARP retrieval, because each viewing angle of the instrument will be looking at a different plume thickness and this violates the plane parallel assumption.

## 5.2 AERONET vs AirHARP AOD comparison

Validation of AirHARP-GRASP retrievals using AERONET measured aerosol optical depth for the collocated AirHARP pixels during the ACEPOL campaign are discussed in this section. A list of the collocated AERONET stations and measurements used for this analysis are listed in Table 2. Only AERONET stations with data quality of Level 2.0 are used for the comparison. For the AERONET validation, AirHARP pixels with a resolution of 550m x 550m are used for the GRASP

retrievals to avoid the issues due to the small pixel shifting during the reprojection to a common latitude-longitude grid as well as to avoid strong fine resolution surface features that appear over the urban area. To further protect the algorithm from subpixel inhomogeneity and other features inappropriate for retrieval a  $\chi^2_{norm} < 1.5$  filter is used to remove the bad pixels/fits which may be caused by the presence of thin clouds (Stap et al., 2015) or due to the inability of surface reflection models to represent the directional reflectance from a complicated surface. To collocate the AERONET station (a single-pixel-in) within the AirHARP image, the latitude and longitude of the AERONET location are matched to the AirHARP latitude and longitude with a tolerance of  $2 \times 10^{-3}$  degree, which is approximately equivalent to 200m on the ground. An area of 5.5 km x 5.5 km (10x10 retrieval pixels) around this collocated pixel is used to calculate for the calculation of the area mean AOD from the AirHARP retrievals, and this is matched to a one-hour temporal mean from AERONET measurements. Each of the 5.5 km x 5.5 km averaging boxes includes 100 pixels, however many of them are removed after the  $\chi^2_{norm}$  filtering. Due to the low loading of aerosol over the AERONET stations, treating the aerosols as a mixture of predefined aerosol components with fixed size and shape distributions, and complex refractive index will benefit the accuracy of AOD retrievals using AirHARP and GRASP. A five component mixture of the aerosol is used to create the phase matrix kernels, which includes the aerosol types: biomass burning, urban, urban polluted, maritime, and desert dust. Among these, only desert dust is considered as completely nonspherical and uses a shape distribution mentioned in (Dubovik et al., 2006). AERONET measured AOD are interpolated linearly in log-log space using the AE to AirHARP spectral bands for 1:1 comparison. The Ross-Li BRDF. All the other types are treated as 100 % spherical particles. The details of the bi-modal size distribution parameters along with the fixed complex refractive index for each of the aerosol types are tabulated in Table 6 and are based on the work of Dubovik et al., 2002. Figure 13 shows the particle size distribution as a function of radii for the different aerosol types. The main differences between the five log-normal mode kernel based retrievals are, 1.) instead of retrieving the concentration of each log-normal mode, weight for each of the aerosol components mentioned in the Table 6 are retrieved. 2) RRI, IRI, and SF are not retrieved since these are fixed for each of the aerosol components. This simplified approach significantly drops the complexity of the aerosol model by reducing the number of parameters retrieved in the joint retrieval. It helps in reducing the nonlinearity of the inverse problem and makes the separation of the surface and aerosol signal much less complicated compared to a five lognormal mode kernel. The maximum AOD measured by a collocated AERONET station during the ACEPOL campaign is 0.158 at 440 nm and using this simplified aerosol type model will greatly benefit the AOD estimation from AirHARP GRASP retrievals. The Rahman-Pinty-Verstraete (RPV) BRDF surface model along with the Maignan-Breon BPDF models are used for representing the directional reflectance from the land surface. RPV BRDF model perform better over the urban and barren land area compared to Ross-Li BRDF kernels. AERONET measured AOD are interpolated to AirHARP spectral bands for 1:1 comparison. for all retrievals used in the validation.

AirHARP observations in this validation exercise are retrieved with two versions of the GRASP aerosol kernels, one using the GRASP/Five mode kernel with 15 free parameters (Table 3) that allows for retrieval of particle properties, and the other using the GRASP/Models kernel with only 6 free parameters (Table 4) that restricts the particle properties to focus on the AOD retrieval. When aerosol loading is low, there is insufficient signal to retrieve particle properties. Allowing for additional free

parameters without having sufficient signal will degrade the accuracy of the AOD retrieval. The maximum AOD measured by a collocated AERONET station during the ACEPOL campaign is 0.158 at 440 nm suggesting that in this exercise the simplified aerosol component model would be preferred over using the option with a greater number of free parameters. This is evident in the two figures, Fig. 14(a) and Fig. 14(b). Figure 14 shows the scatterplot of these two data sets with AOD<sub>AERONET</sub> in the X-axis and AOD<sub>AirHARP</sub> on the Y-axis. The spatial standard deviation of AOD within this 5.5 km x 5.5 km box is indicated using the error ~~bars~~ in Fig. 14. Statistical parameters that represent the correlation between these two data sets are tabulated in the table inside Fig. 14. ~~The black dashed lines in Fig. 14 are AOD(1:1) ± 0.04 lines. Mean absolute error of 0.014, 0.013, 0.013 and 0.017 the plots. In Fig. 14 a, for the case of AOD retrievals based on the GRASP/Five mode kernel with the greater number of free parameters, MAE of 0.041, 0.039, 0.037, 0.035 are obtained for the spectral bands 440, 550, 670, and 870 nm bands, respectively, with. The bias ranges from 0.022 to 0.038, with the 440 nm band having the largest bias and the 870 nm band having with the least. However, in Fig. 14b, for the case using the GRASP/Models kernel with the reduced number of free parameters, mean absolute error of 0.010, 0.010, 0.011, and 0.015 are obtained for the spectral bands 440, 550, 670, and 870 nm, respectively, with 870 nm band having a slightly higher spread than the other bands. Also, a similar trend is seen for 870 nm in the case of BIAS, where the 440, 550, and 670 nm bandbands have a BIAS of -0.011, -0.013, -0.011, -0.011, -0.004, respectively whereas 870 nm has a BIAS of -0.017. At low AOD we can see a low bias compared to AERONET AOD measurements, which is similar to what we see for RSP vs AERONET comparison in (Fu et al., 2020)-009. Figure 14 demonstrates the need to match the appropriate kernel to the available information in the scene and to not attempt the retrieval of more free parameters than the aerosol loading permits. Overall, the performance of the AirHARP observations plus the GRASP retrieval algorithm gives a good correlation agreement with the collocated AERONET observations, especially when GRASP/Models kernel is used. The above tendency is well identified in the in-depth analysis of PARASOL data processing using different retrieval setups by Chen et al. 2020 (In preparation).~~

## 6 Future research

We note the abundance of very low aerosol loading in the majority of the ACEPOL flight legs. Future work should make use of these data to focus on surface characterization using the AirHARP/GRASP combination. There are several flight segments over the Rosamond Dry Lake, in California, USA in different flight directions and because the dry lake is relatively flat and uniform, it becomes an ideal target for testing GRASP retrievals of surface BRDF and BPDF parameters. Furthermore, on this day, at AirHARP overpass, ground measurements of radiance and polarized radiance were made using the Ground Multiangle Spectro-Polarimetric Imager. This will be a perfect case for a case study on the performance of different BRDF + BPDF kernel combinations to represent the directional reflectance from a bright surface. This data set can be used to improve the BRDF/BPDF model at an unprecedented higher resolution compared to previous studies (Maignan et al., 2004, 2009). This will help in better characterization of directional reflectance from the urban surface and will benefit the overall accuracy of AOD retrievals over the land.

## 7 Conclusions

In this study, AirHARP polarimetric measurements, taken at the high angular and spatial resolution over a wide swath, combined with the GRASP algorithm allow for unprecedented spatial mapping of aerosol properties that are consistent with co-incident instrument retrievals. These properties always include AOD, but can also deliver real and imaginary parts of the refractive index, particle size information, spherical fraction, and single scattering albedo when the aerosol is suitably homogeneous and loading is sufficiently high. We demonstrated that the measurements match the forward model calculations in a variety of environments: the retrieval performs well over barren land surface and vegetation, though retrievals over sunglint still show biases in the AOD. The wide swath of the AirHARP enables the aerosol retrievals over a large scene of interest, which makes the AirHARP instrument unique from many of the other airborne polarimeters available as of today. Also, this wide swath will help in capturing more aerosol events globally compared to a narrow swath multi-angle polarimeter, when the HARP concept is applied to space sensors.

In situations with low aerosol loading ( $\text{AOD} < 0.17$ ) over land, a simplified retrieval approach based on GRASP/Models kernel approximating aerosol as an external mixture of five aerosol components is also used for the AOD retrievals. One advantage of using this simplified kernel is that it retrieves a significantly smaller number of aerosol parameters compared to the standard GRASP/Five mode kernel and performed well for low aerosol loading cases in an AERONET comparison, despite the simplifying assumption of prescribed complex refractive index for each aerosol component. AOD retrieved from AirHARP using GRASP, matches collocated AERONET observations to within  $+0.005018/-0.02504$  with a minimum MAE of 0.01 in 440 and 550 nm bands and maximum of 0.015 in the 870 nm spectral band. Thus, we note an overall low bias of  $-0.044002$  to  $-0.047009$ , depending on wavelength. Traditionally, low AOD conditions over land were some of the most difficult situations for standard operational aerosol retrieval algorithms applied to orbiting radiometers. - For example, the MODIS Dark Target algorithm reports an accuracy at a low loading of  $\pm 0.05$  (Levy et al., 2013), MODIS Deep Blue  $\pm 0.03$  (Sayer et al., 2013), MISR  $\pm 0.03$  to  $\pm 0.05$  (Kahn et al., 2010). -TheAll of these radiometer products all expect twice the uncertainty at the low loading end than what was obtained from AirHARP/GRASP in these circumstances. -Granted that these results were achieved for only seven AirHARP overpasses of AERONET sites and will need to be reproduced in a variety of settings and situations, but for now, the match-ups with AERONET are very promising for AOD retrievals over complex land surfaces.

GRASP was applied to AirHARP observations of two heavy aerosol loading situations, both of smoke plumes near fire sources. It is in one of these situations that ~~GRASP was able to retrieve~~ optical and microphysical characteristics of the smoke, in addition to AOD, are retrieved using the GRASP software. Retrievals of smoke properties on the 27<sup>th</sup> October 2017 T18:16 UTC show that particles are fine with the real and imaginary refractive index of 1.55 and 0.024 respectively. Single scattering albedo of 0.87, 0.86, 0.84, and 0.81 are retrieved for the smoke at 440 nm, 550 nm, 670 nm, and 870 nm respectively with fine mode volume median radius of 0.157  $\mu\text{m}$  and standard deviation of 0.55  $\mu\text{m}$  with a mixture of spherical and non-spherical

particles. The isolated location of these local smoke plumes prevents any validation with AERONET observations. However, the retrieved optical and microphysical properties fall within expectations of fire smoke from previous publications, including a report for a similar smoke from ~~another two other~~ ACEPOL polarimeter (RSP and SPEX airborne) flying on the same aircraft as AirHARP. See the discussion in Section 5. Furthermore, the AirHARP/GRASP-retrieved AOD agrees well with collocated HSRL2 observations of the smoke plume to the degree to which the two sensors with very different observation geometries and cross-track pixel sizes can be matched. Note that when the plume is highly heterogeneous, the 3D smaller cross-track footprint of HSRL2 measurements, relative to AirHARP makes collocation extremely difficult. Also, the complex structure of the plume ~~must be accounted for in the polarimeter multi-angle vs. lidar nadir observations. This~~ violates the plane-parallel aerosol layer assumption ~~and will result in an AOD bias depending on~~ the ~~location of the measurement in the plume. Also,~~  
740 ~~the smaller cross track footprint of HSRL2 measurements, relative to AirHARP, adds complexity in the intercomparison~~ retrieval, adding uncertainty and bias.

AirHARP is the first manifestation of the HARP concept that makes multi-wavelength, hyper-angle, polarization measurements across a wide swath. Thus, the encouraging results demonstrated here show that when combined with GRASP  
745 inversion methods, HARP measurements can be used to retrieve highly accurate measures of AOD and aerosol optical/microphysical characteristics over a broad area. HARP Cubesat that will fly at the International Space Station orbit of ~410 km in 2020 will cover ~1348 km in its across-track image, while HARP2 that will part of the Plankton, Aerosol, Clouds, ocean Ecosystem (PACE) mission at ~676 km orbit will image ~1550 km across its swath. This AirHARP/GRASP demonstration reinforces high expectations for these future HARP space missions. Furthermore, HARP has the potential to  
750 provide new characterization for clouds (McBride et al., 2020) and surface properties over various surface types, land and ocean. The PACE mission also opens the corridor for a synergetic observation using the Ocean Color Instrument (OCI) along with the two multi-angle polarimeters: HARP2 and SPEXone. OCI is a hyperspectral, wide swath radiometer, HARP2 – a wide swath multi-angle polarimeter and SPEXone – a hyperspectral narrow swath multi-angle polarimeter. The combined spectral and spatial coverage and resolution of these three instruments will provide an unprecedented dataset for the  
755 atmospheric, ocean, and terrestrial science research communities (Frouin et al., 2019; Hasekamp et al., 2019; Remer et al., 2019). These new capabilities for aerosol, cloud, and surface characterization will offer the community new insight into important climate processes, public health issues, and other societal concerns.

## Appendix A

### A.1 Land surface models

760 GRASP includes multiple land and ocean surface reflectance models. Here we will be discussing only the one we have used for the retrievals in this paper. Land reflectance BRDF and BPDF models are derived using analytical (Cook et al., 2004; Rahman et al., 1993; Roujean et al., 1992; Wanner et al., 1995) and semi-empirical concept (Breon and Maignan, 2017), which used the heritage data from MODIS, POLDER to characterize the BRDF and BPDF models with higher accuracy. Currently, we use ~~three~~two land models for the retrievals.

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#### A.1.1. ~~Rahman-Pinty-Verstraete (RPV)~~Ross-Li BRDF model

This model ~~uses only three parameters to express~~ characterizes the directional reflectance from the surface which is illuminated from a direction  $(\vartheta_1, \phi_1)$  and observed from a direction  $(\vartheta_2, \phi_2)$  ~~is given by,~~

$$\rho_{\text{RPV}}(\lambda, \vartheta_1, \phi_1, \vartheta_2, \phi_2) = \rho_0(\lambda) \frac{(\cos \vartheta_1 \cos \vartheta_2)^{k-1}}{(\cos \vartheta_1 + \cos \vartheta_2)^{1-k}} F(g) \left(1 + \frac{1 - \rho_0}{1 + G}\right) \quad (\text{A.1.1})$$

Where  $\rho_0$  and  $k$  are two empirical surface parameters.  $\left(1 + \frac{1 - \rho_0}{1 + G}\right)$  is an approximation of the hot spot effect.

$$F(g) = \frac{1 - \Theta^2}{[1 + \Theta^2 - 2\Theta \cos(\pi - g)]^{1.5}} \quad (\text{A.1.2})$$

770  ~~$F(g)$  is the Henyey Greenstein phase function, where  $\Theta$ , the function parameter which controls the relative amount of forward and backward scattering. The phase angle  $g$  in Eq A.1.2 is given by~~

$$\cos(g) = \cos \vartheta_1 \cos \vartheta_2 + \sin \vartheta_1 \sin \vartheta_2 \cos(\phi_1 - \phi_2) \quad (\text{A.1.3})$$

~~When  $\vartheta_1 = \vartheta_2$  and  $\phi_1 = \phi_2$ , i.e., in the hot spot,  $G = 0$  and  $\frac{1 - \rho_0}{1 + G}$  becomes maximum and total reflectance is increased. The equations Eq A.1.1 to Eq A.1.3 describe the anisotropy of the reflectance surface and can be represented by using three parameters  $\rho_0$ ,  $k$  and  $\Theta$~~

#### 775 A.1.2. Ross-Li BRDF model

~~This model characterizes the directional surface reflectance~~ by the linear combination of three types of scattering kernels and is given by,

$$\rho_{\text{Ross-Li}}(\vartheta_1, \phi_1, \vartheta_2, \phi_2) = f_{\text{iso}}(\lambda) + K_{\text{vol}}(\lambda) f_{\text{vol}}(\vartheta_1, \phi_1, \vartheta_2, \phi_2) + K_{\text{geo}}(\lambda) f_{\text{geo}}(\vartheta_1, \phi_1, \vartheta_2, \phi_2) \quad (\text{A.1.4})$$

$f_{\text{iso}}$ ,  $f_{\text{vol}}$  and  $f_{\text{geo}}$  are the three kernels which represent isotropic, volumetric, and geometric-optical surface scattering respectively. Litvinov et al., 2011 show that ~~the~~ surface reflectance can be represented as a product of geometrical and wavelength-dependent terms.

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$$R_l(\vartheta_1, \phi_1, \vartheta_2, \phi_2, \lambda) \approx k(\lambda) f_l(\vartheta_1, \phi_1, \vartheta_2, \phi_2) \quad (\text{A.1.5})$$

From Eq A.1.4, Eq A.1.5 we can derive R as,

$$R_I(\vartheta_1, \phi_1, \vartheta_2, \phi_2, \lambda) = k(\lambda)[1 + k_1 f_{geo}(\vartheta_1, \phi_1, \vartheta_2, \phi_2) + k_2 f_{vol}(\vartheta_1, \phi_1, \vartheta_2, \phi_2)] \quad (\text{A.1.6})$$

~~Where  $k_1$  and  $k_2$  are wavelength-independent linear model parameters for geometrical-optical and volumetric surface scattering kernels respectively. The  $k(\lambda)$  is a wavelength-dependent model parameter.~~

~~A.1.3 Where  $k_1$  and  $k_2$  are wavelength-independent linear model parameters for geometrical-optical and volumetric surface scattering kernels respectively. The  $k(\lambda)$  is a wavelength-dependent model parameter. The volumetric kernel is defined as (Ross, 1981; Roujean et al., 1992; Wanner et al., 1995).~~

$$f_{vol}(\vartheta_1, \phi_1, \vartheta_2, \phi_2) = \frac{\left(\frac{\pi}{2} - \gamma\right) \cos \gamma + \sin \gamma}{\cos \vartheta_1 + \cos \vartheta_2} - \frac{\pi}{4} \quad (\text{A.1.4})$$

~~where  $\gamma$  is the scattering defined in the scattering plane and is given by the equation,~~

$$\gamma = \cos^{-1}(-\cos \vartheta_1 \cos \vartheta_2 - \sin |\vartheta_2| \sin \vartheta_1 \cos \phi) \quad (\text{A.1.5})$$

~~Here,  $\phi = \phi_2 - \phi_1$ , is the relative azimuthal angle. The Li-Sparse geometric kernel is defined as,~~

$$f_{geo}(\vartheta_1, \phi_1, \vartheta_2, \phi_2) = O(\vartheta_1, \phi_1, \vartheta_2, \phi_2) - \sec \vartheta'_1 - \sec \vartheta'_2 + \frac{1}{2}(1 - \cos \vartheta') \sec \vartheta'_1 \sec \vartheta'_2 \quad (\text{A.1.6})$$

$$O = \frac{1}{\pi}(t - \sin t \cos t)(\sec \vartheta'_1 + \sec \vartheta'_2) \quad (\text{A.1.7})$$

$$\cos t = \frac{h \sqrt{D^2 + (\tan \vartheta'_1 \tan \vartheta'_2 \sin \phi)^2}}{b \sec \vartheta'_1 + \sec \vartheta'_2} \quad (\text{A.1.8})$$

$$D = \sqrt{\tan^2 \vartheta'_1 + \tan^2 \vartheta'_2 + 2 \tan \vartheta'_1 \tan \vartheta'_2 \cos \phi} \quad (\text{A.1.9})$$

$$\cos \vartheta' = \cos \vartheta'_1 \cos \vartheta'_2 - \sin \vartheta'_1 \sin \vartheta'_2 \cos \phi \quad (\text{A.1.10})$$

$$\vartheta'_1 = \tan^{-1}\left(\frac{b}{r} \tan \vartheta_1\right), \vartheta'_2 = \tan^{-1}\left(\frac{b}{r} \tan |\vartheta_2|\right) \quad (\text{A.1.11})$$

~~To reduce the number of surface parameters retrieved, in linear model's  $h/b$  and  $b/r$  are fixed. Like the MODIS BRDF retrieval algorithm (Schaaf et al., 2002), we predefine the values  $h/b = 2$  and  $b/r = 1$  in the BRDF kernel.~~

### **A.1.2. Maignan-Breon BPDF model**

Most of the theoretical models developed for the BPDF are based on the Fresnel equation of light reflection from a surface. Nadal-Breon model uses two parameters non-linear Fresnel function to characterize the aerosol over land polarized reflectance. The polarized reflectance can be given by,



$$R_p(\vartheta_1, \phi_1, \vartheta_2, \phi_2) = \alpha \left( 1 - \exp \left( -\beta \frac{F_p(m, \gamma)}{\cos \vartheta_1 + \cos \vartheta_2} \right) \right) \quad (\text{A.1.712})$$

where  $F_p$  is the polarized Fresnel reflection coefficient and is given by,

$$F_p = \frac{1}{2} (r_{\perp}^2 + r_{\parallel}^2) \quad (\text{A.1.813})$$

800 where  $r_{\perp}$  and  $r_{\parallel}$  are perpendicular and parallel components of Fresnel reflection coefficients respectively. Maignan et al., 2009 implemented a simple one-parameter model compared to the complicated two-parameter Nadal-Breon model to represent the polarized reflectance from aerosol over the land surface. It has been used in the POLDER/PARASOL retrieval algorithm as a primary model for the BPDF over land. The one parameter BPDF model is given by,

$$R_p(\vartheta_1, \phi_1, \vartheta_2, \phi_2) = \frac{\alpha \exp(-\tan \vartheta_r) F_p(m, \gamma)}{4(\cos \vartheta_1 + \cos \vartheta_2)} \quad (\text{A.1.914})$$

Here  $\alpha$  is the only free linear parameter.  $\vartheta_r$  is the angle of specular reflection.

## 805 A.2 Ocean surface models

For the surface model in the RT calculation, we used a modified Cox-Munk isotropic model. A detailed description of this can be found in references (Kawata et al., 1995; Mishchenko and Travis, 1997; Sun and Lukashin, 2013). The modified Cox-Munk model calculates the BRDF and BPDF based on three parameters,  $a_0$  is the albedo of the ocean surface, which is spectrally dependent and smooth.  $a_1$  is the fraction of Fresnel's reflection surface and  $a_2$  is the variance of wind speed distribution. Wind speed distribution is given by the equation,

$$p(Z_x, Z_y) = \frac{1}{\pi a_2} (Z_x, Z_y) = \frac{1}{\pi a_2} \exp \left( -\frac{Z_x^2 + Z_y^2}{a_2^2} \right) \quad (\text{A.2.1})$$

Where,

$$a_2^2 = 0.003 + 0.00512V \quad (\text{A.2.2})$$

$Z_x, Z_y$  are X and Y slope components.  $V$  is the surface wind speed in m/s.

## Appendix B

### B.1 Aerosol Optical Depth (AOD) calculation

815 In GRASP, atmospheric aerosol particles are considered as a mixture of spherical and randomly oriented spheroid particles, and the aerosol optical depth is modeled as follows:

$$\tau_{aero}(\lambda) = \tau_{spherical}(\lambda) + \tau_{spheroid}(\lambda) \quad (\text{B.1.1})$$

$$\tau_{spherical}(\lambda) = \int_{\ln r_{min}}^{\ln r_{max}} \frac{C_{ext}^{sphere}(\lambda, n, k, r)}{v(r)} \frac{dV(r)}{d \ln(r)} d(\ln(r)) \quad (\text{B.1.2})$$

And,

$$\tau_{spheroid}(\lambda) = \int_{\ln \epsilon_{min}}^{\ln \epsilon_{max}} \int_{\ln r_{min}}^{\ln r_{max}} \frac{C_{ext}^{\epsilon}(\lambda, n, k, r)}{v(r)} \frac{dn(\epsilon)}{d\ln(\epsilon)} \frac{dV(r)}{d\ln(r)} d(\ln(r)) d(\ln(\epsilon)) \quad (B.1.3)$$

where  $\lambda$  is the wavelength,  $n$  is the real part of the refractive index,  $k$  is the imaginary part of refractive index,  $v(r)$  is the volume of particle,  $C_{ext}^{sphere}$  and  $C_{ext}^{spheroid}$  are extinction cross-section of spherical and spheroid particles with aspect ratio  $\epsilon$  ( $\epsilon = \frac{a}{b}$ ,  $a$  is the axis of spheroid rotational symmetry,  $b$  is the axis perpendicular to the axis of spheroid rotational symmetry) respectively.  $\frac{dn(\epsilon)}{d\ln(\epsilon)}$  used in GRASP is a fixed shape distribution as mentioned in Dubovik et al., 2006. Integrals in the Equation B.1.2, Equation B.1.3 are changed to sum in order to do the computation fast and accurate and thus it becomes,

$$\tau_{spherical}(\lambda) = \sum_{i=1}^{N_r} \left( SF \times K_{\tau}^{spherical}(\lambda, n, k, r) \right) \frac{dV(r_i)}{d\ln(r)} \quad (B.1.4)$$

Where SF is the spherical fraction, K is the quadrature coefficient of extinction and is pre-computed kernels. Precomputed K has been calculated for a wide range of  $n$  ( $1.33 \leq n \leq 1.7$ ) and  $k$  ( $0.00010005 \leq k \leq 0.5$ ). The calculations were done for a fixed aspect ratio from 0.3 to 3.0 and narrow size bins cover the size parameter range from  $\sim 0.0012$  to  $\sim 625$ .

$$\tau_{spheroid}(\lambda) = \sum_{i=1}^{N_r} (1 - SF) K_{\tau}^{spheroid} \frac{dV(r_i)}{d\ln(r)} \quad (B.1.5)$$

Also,

$$\frac{dV_i(r)}{d\ln(r)} = \sum_{i=1, \dots, N} \frac{C_{v,i}}{\sqrt{2\pi}\sigma_i} \exp\left(\frac{-(\ln r - \ln r_{v,i})^2}{2\sigma_i^2}\right) \quad (B.1.6)$$

$C_{v,i}$  is the concentration of different modes,  $r_{v,i}$  is the volume median radius of each ~~modes~~mode, and  $\sigma_i$  is the standard deviation.

## Data availability

The AirHARP L1B and HSRL2 data for the ACEPOL campaign can be accessed from the website <https://www-air.larc.nasa.gov/cgi-bin/ArcView/acepol>. Quick look images for each of the AirHARP ~~flights~~flight legs can be accessed through the website <https://sites.google.com/view/airharp-acepol/home>. AERONET data used for this study can be download from <https://aeronet.gsfc.nasa.gov/>.

## Author contribution

AP designed and implemented the study and analysis. AP wrote the manuscript with significant contributions from LR. BM, HM, and VM managed the operation of the AirHARP instrument during the ACEPOL campaign. VM, BM, XX, and HB

calibrated and developed a scheme to generate the LIB data, which is the input for this data analysis. OD and PL helped with the retrievals by providing the GRASP software and support. SB has provided input for the HSRL2 – AirHARP AOD comparison. All the authors contributed ~~towards~~to the improvement of the manuscript with valuable comments and suggestions.

## Competing interests

The authors declare that they have no conflict of interest.

## Acknowledgement

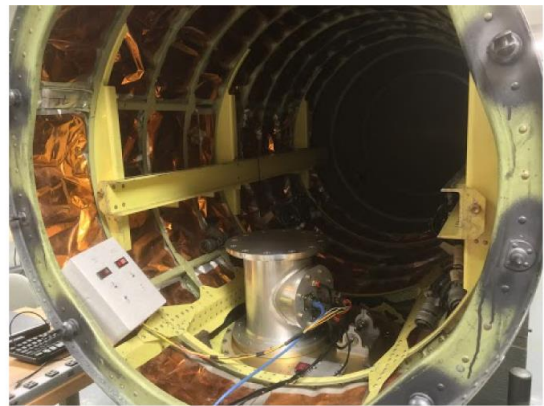
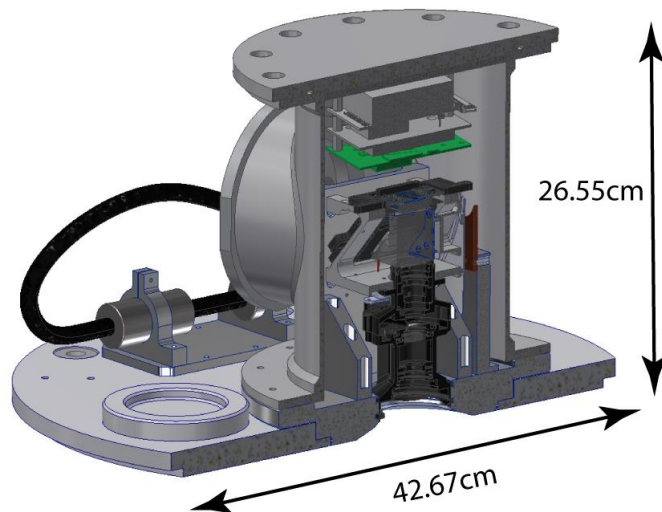
We thank the ACEPOL organizing team for supporting the involvement of the AirHARP instrument in the project. We thank the PIs of the AERONET stations used in this study for maintaining and providing ~~the~~ easy access ~~of~~to data. We also acknowledge the engineering contributions from Dr. Fernandez-Borda (ESI, UMBC), and Mr. D. Cieslak (ESI, UMBC) in designing and manufacturing of AirHARP instrument. ~~The authors acknowledge the support Dr.~~We acknowledge the former Aerosol, Cloud, Ecosystem (ACE) program at NASA’s Earth Science Division as a sponsor for ACEPOL flights. The Dutch contribution to the ACEPOL flight campaign hours was funded by SRON Netherlands Institute for SPACE Research and by NSO/NWO under project number ALW-GO/16-09. The authors acknowledge the support of Dr. Lopatin (GRASP -SAS) and Dr. Lapienak (LOA Université Lille) in providing the GRASP kernels for this study. The authors acknowledge the work by Python Software Foundation (<http://www.python.org>) and Anaconda Inc. (<https://www.anaconda.com/>) for developing and maintaining the python programming language and packages used for ~~analysing~~analyzing and visualizing the data used in this study.

## Financial support

This research is primarily supported through the NASA projects: HARP Cubesat (NNX13AN11G), AirHARP (NNX16AK36G), and JCET cooperative agreement (NNX15AT34A). This research is also supported by the National Key R&D Program of China (Grant 2016YFE0201400). O. Dubovik appreciates the support from the Chemical and Physical Properties of the Atmosphere Project funded by the French National Research Agency through the Programme d’Investissement d’Avenir under contract ANR-11-LABX-0 0 05-01, the Regional Council “Hauts-de-France”, and the “European Funds for Regional Economic Development”. Barbosa acknowledges the support of processo nº 2016/18866-2, Fundação de Amparo à Pesquisa do Estado de São Paulo (FAPESP); and of project 308682/2017-3, Conselho Nacional de Desenvolvimento Científico e Tecnológico (CNPq).

Figures

(a)



(b)

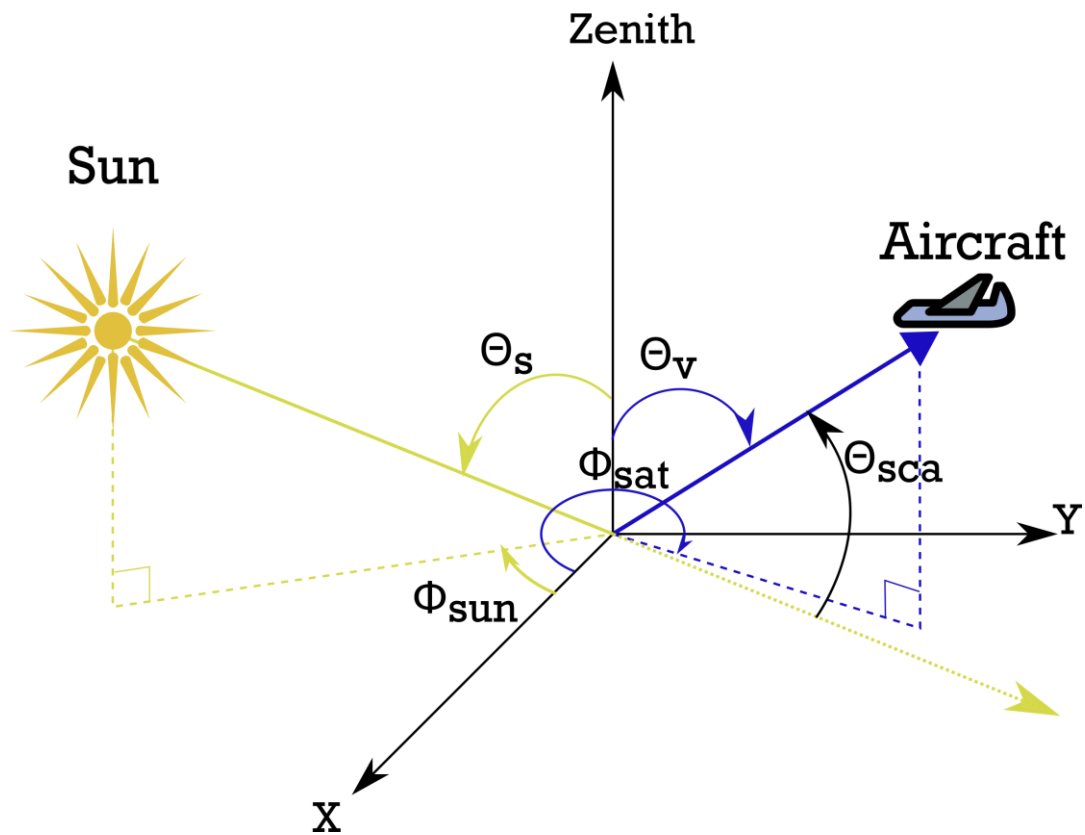


(c)

AirHARP instrument mounted on the front pod of the ER-2 aircraft's left-wing

865

**Figure 1.** (a) Cross-section image of AirHARP instrument rendered using CAD software; (b) AirHARP instrument mounted on ER-2 aircraft left-wing front pod (Image courtesy: Brent McBride); (c) Image captured by NASA Science Pilot D. Stuart Broce, during the ACEPOL flight on Oct-26 2017. The red arrow in the figure points to the AirHARP's exposed part when mounted on the wing pod.



870

**Figure 2.** AirHARP viewing geometry and definition of angles.  $\Theta_s$  is the solar zenith angle,  $\Theta_v$  is the viewing zenith angle,  $\Phi_{sun}$  is the solar azimuthal angle,  $\Phi_{sat}$  is the viewing azimuthal angle, and  $\Theta_{sca}$  is the scattering angle. The point where X and Y coordinates meet is the local ground point.

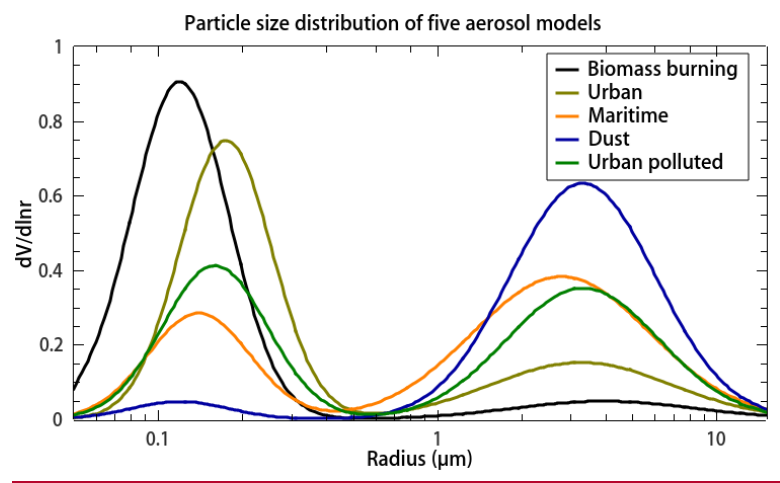
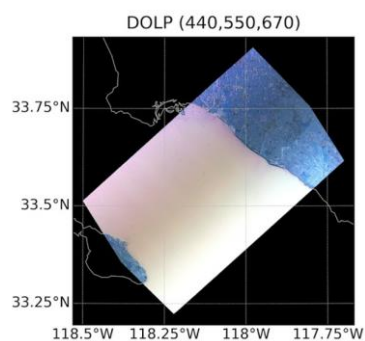
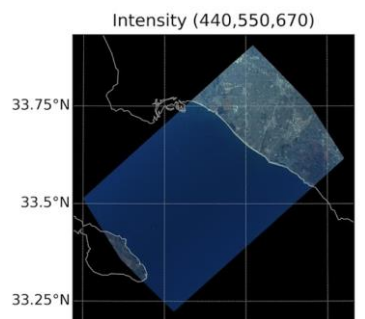
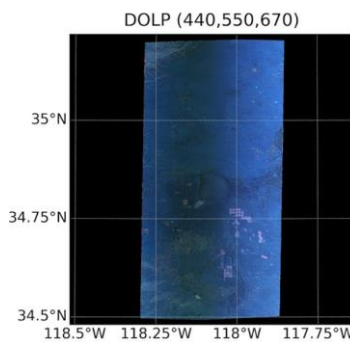
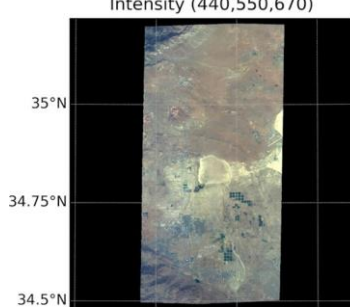
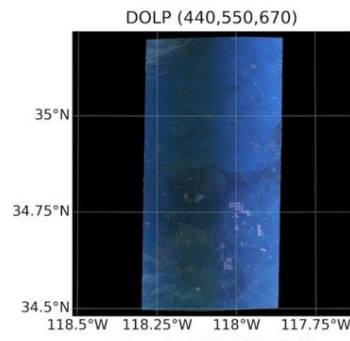
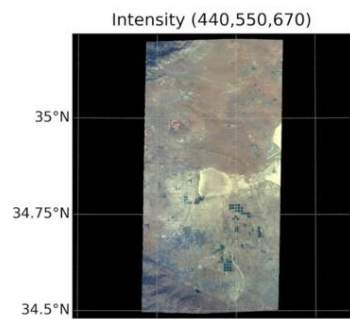


Figure 3. The particle size distribution of five aerosol components listed in Table 4. This simplified aerosol component-based GRASP/Models kernel is used for the AirHARP AOD inversion over the collocated AERONET pixels during ACEPOL 2017 campaign.

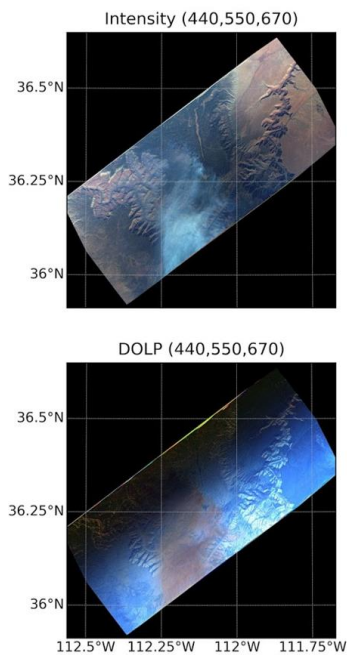


(a)

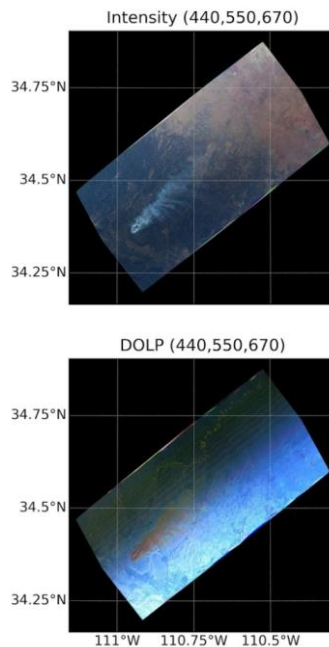


(b)



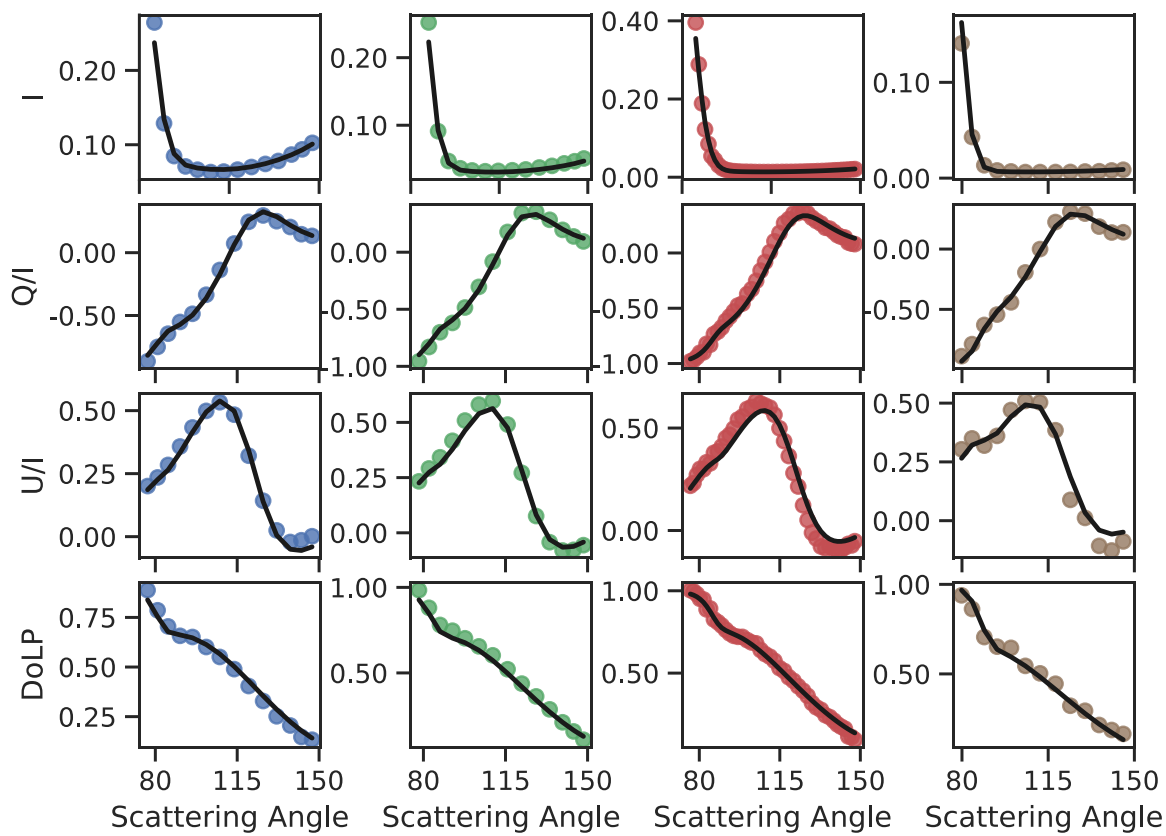


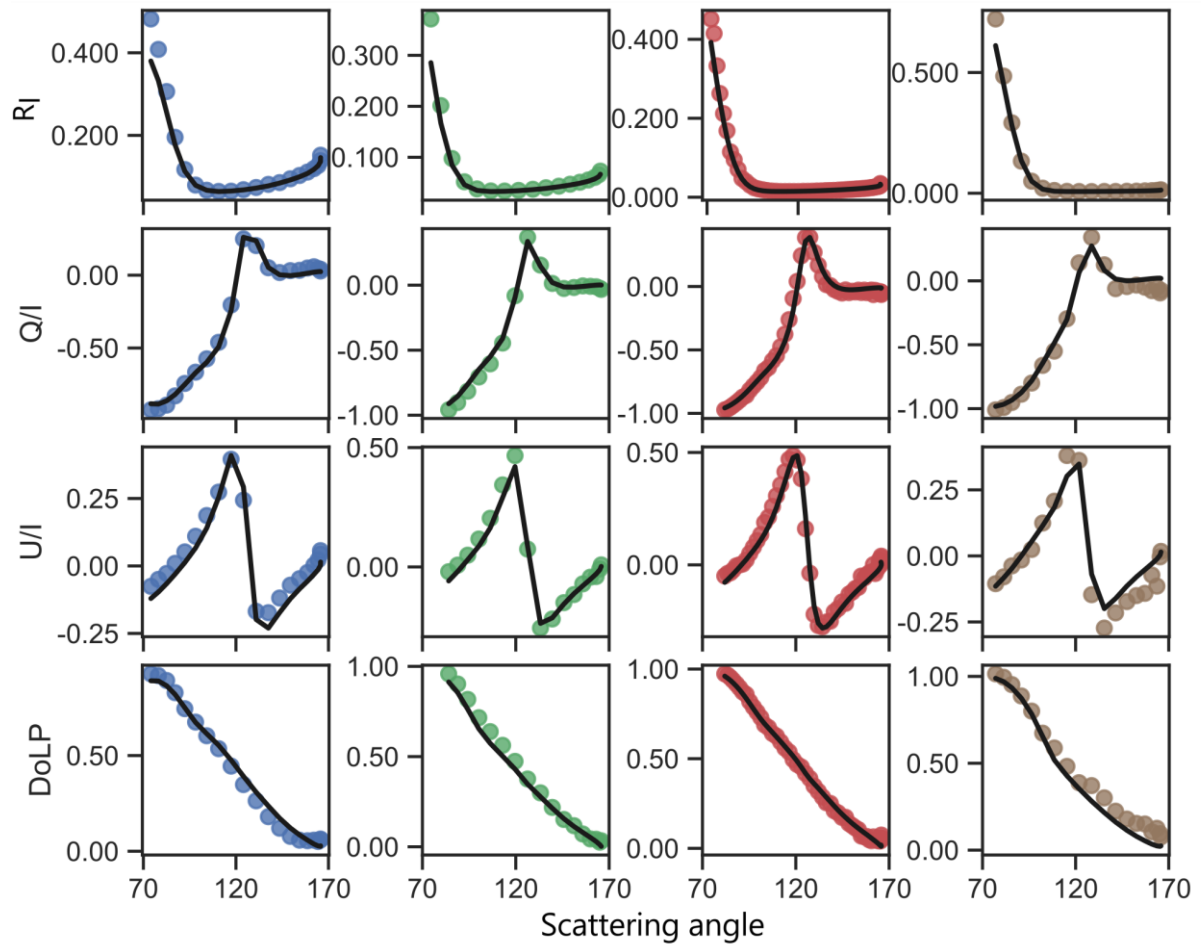
(c)



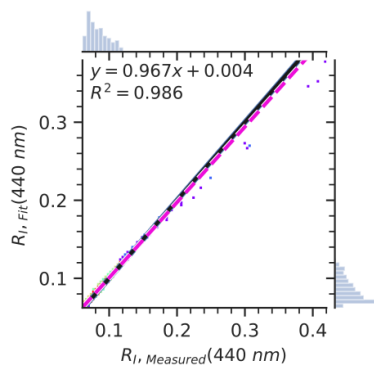
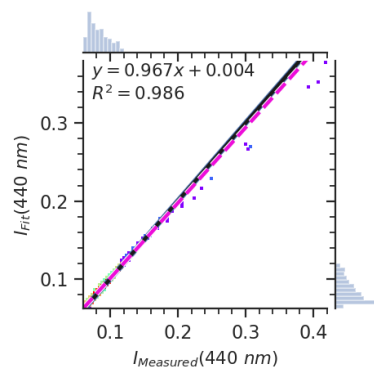
(d)

Figure 34. Nadir RGB (670 nm, 550 nm, and 440 nm) images of radiance and DoLP for the selected cases from AirHARP flight legs listed in Table 2. The X-axis is the longitude and the Y-axis the latitude. The scenes include (a) sun glint scene over the Pacific Ocean near Los Angeles, California, USA (23<sup>rd</sup> October 2017 T21:30 UTC); (b) Rosamond dry lake in California, USA, (25<sup>th</sup> October 2017 T18:26 UTC); (c) biomass burning scene near the Kaibab national forest and Grand Canyon national park, (27<sup>th</sup> October 2017 T18:16 UTC); (d) biomass burning scene near the Kaibab national forest(9<sup>th</sup> November 2017 T19:30 UTC).

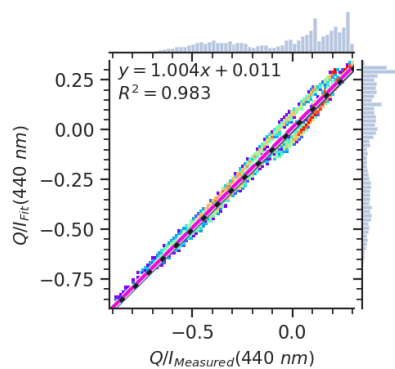




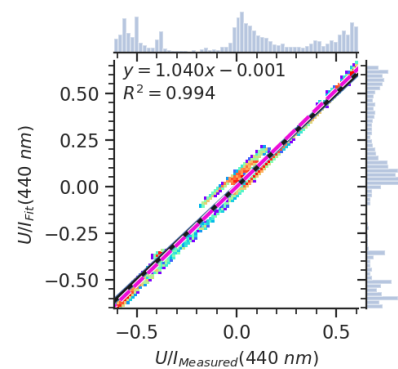
**Figure 45.** AirHARP measured  $I$ ,  $Q/I$ ,  $U/I$ , and  $DoLP$  (solid colored circles) for a single sun glint pixel from the scene in Fig. 34(a) and the GRASP fit to the measurements (black solid line) for all bands (Blue – 440 nm, Green -550 nm, Red – 670 nm and Brown-870 nm)



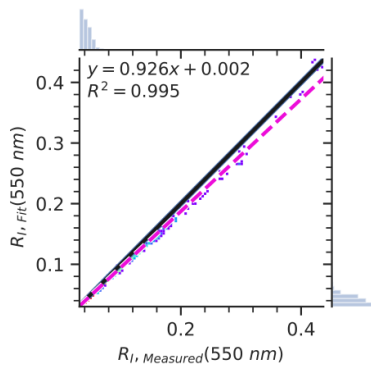
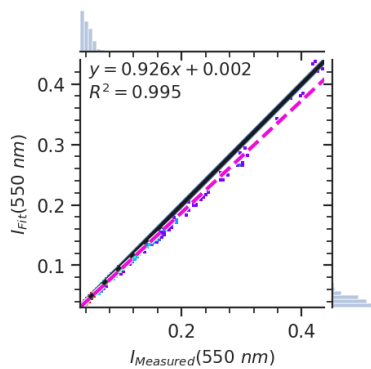
(a)



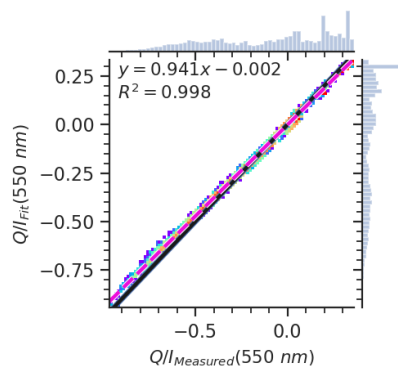
(b)



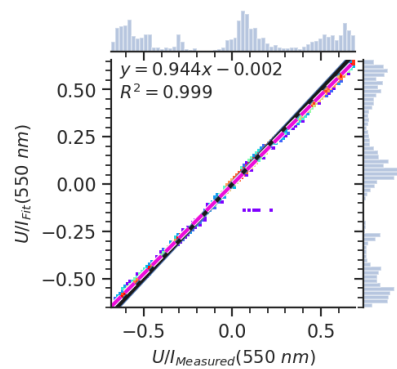
(c)



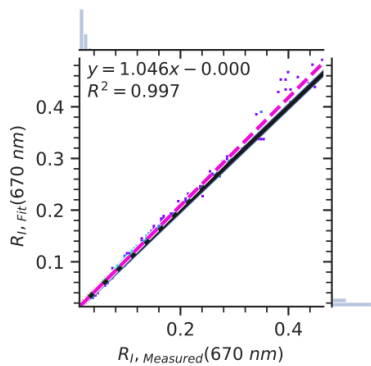
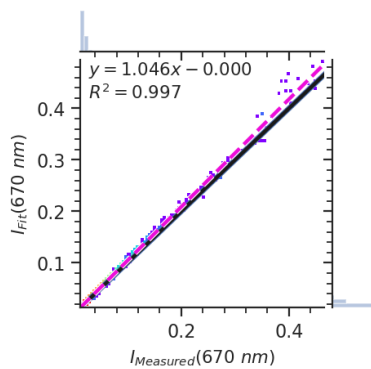
(d)



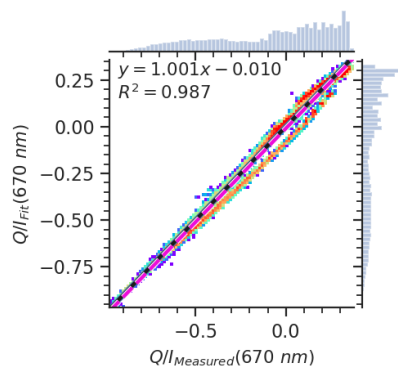
(e)



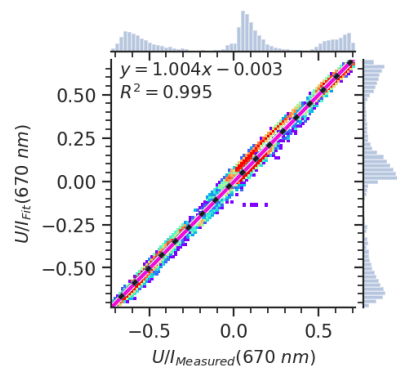
(f)



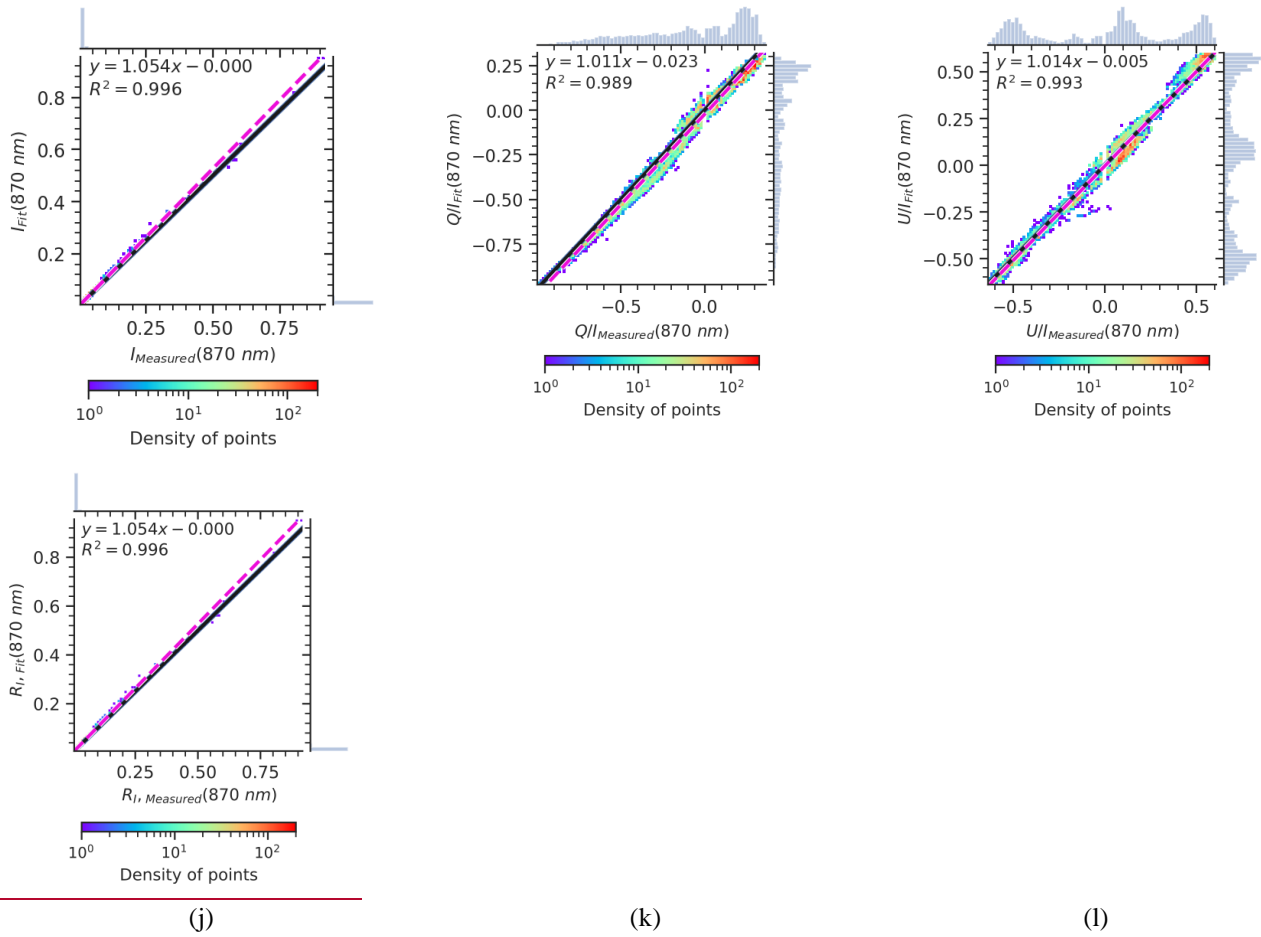
(g)



(h)



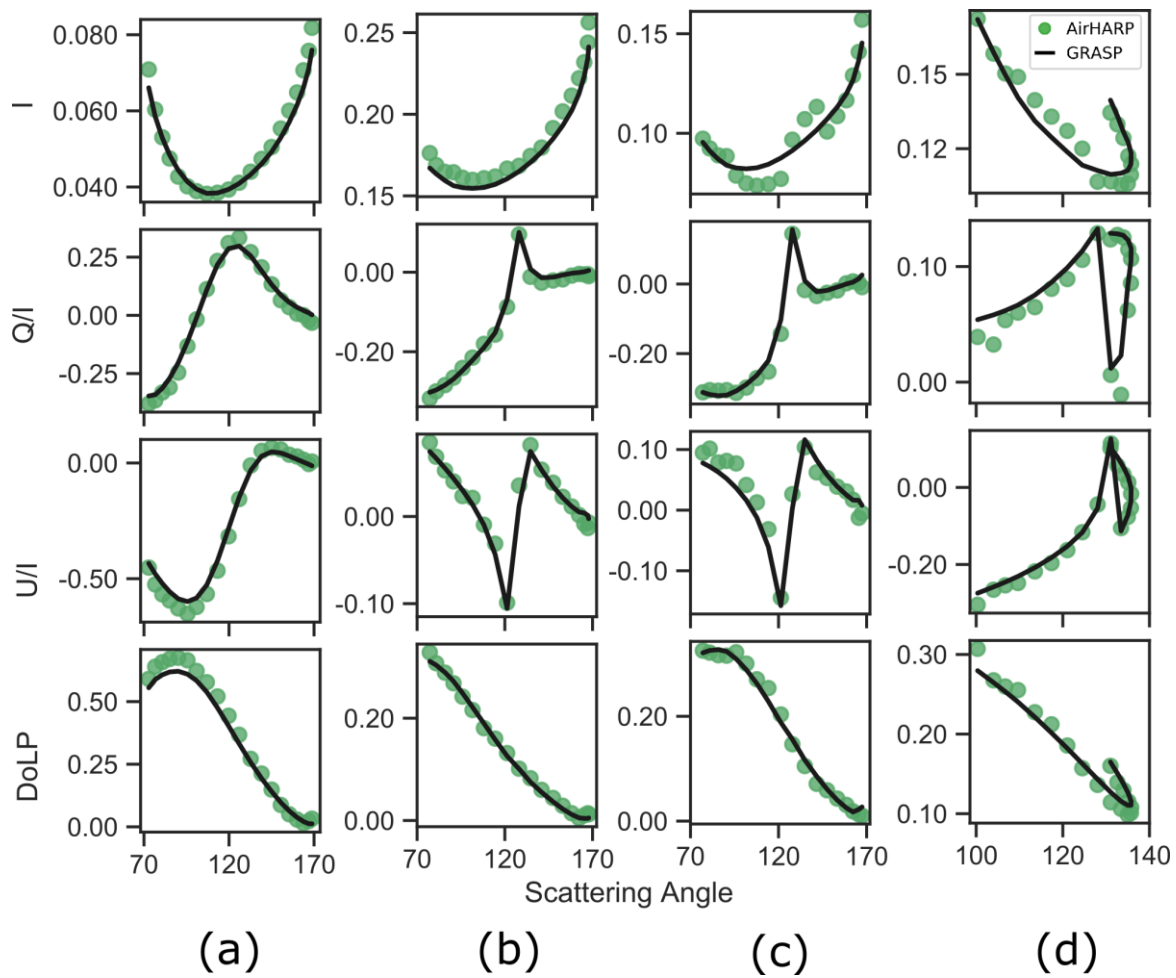
(i)

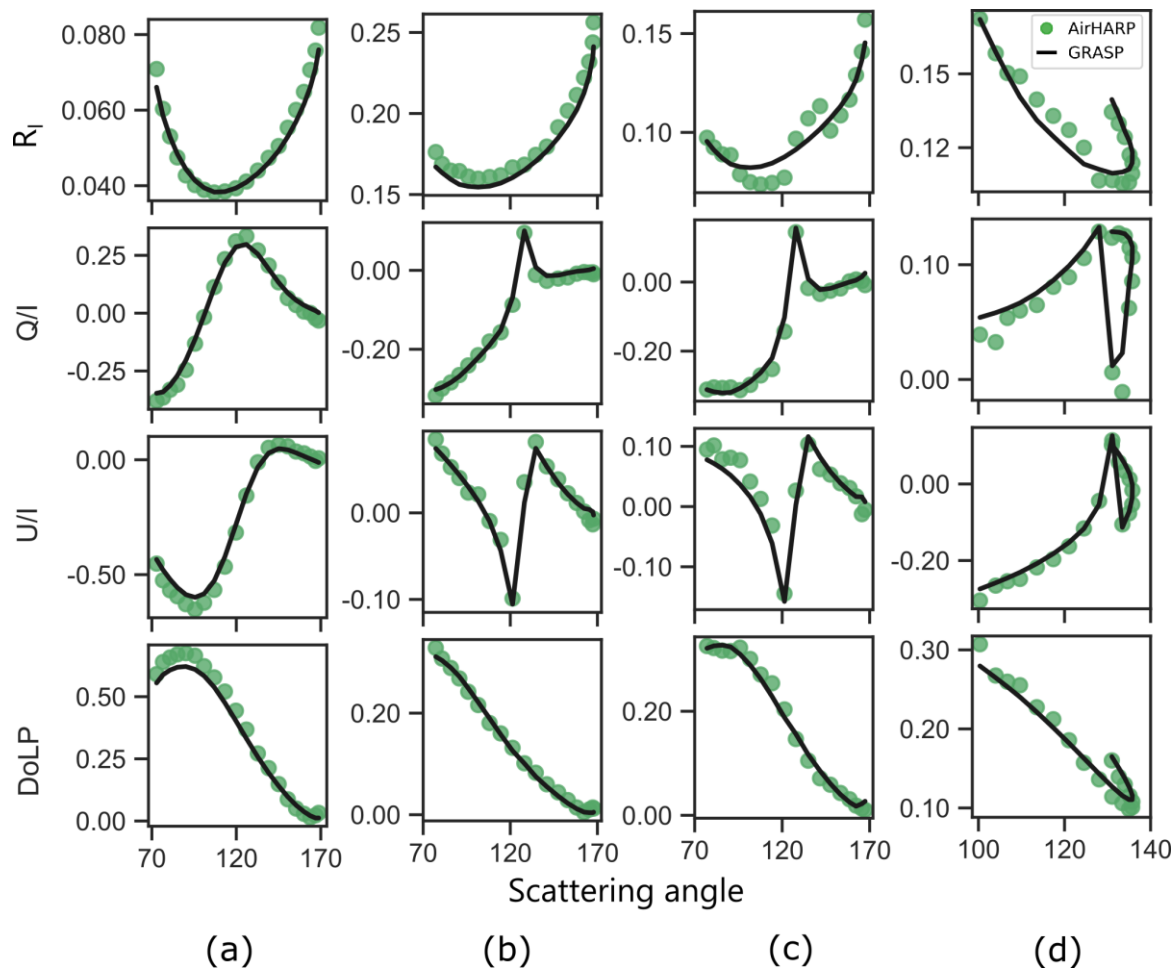


**Figure 56.** Scatter density plots for AirHARP measurement variables and GRASP fit for the ocean scene in Fig. 34(a). The subplots (a), (d), (g) and (j) are the 2D density plots for variable I at different spectral bands blue, green, red and NIR, respectively; (b), (e), (h) and (k) are for the variable Q/I; (c), (f), (i) and (l) are for the variable U/I. The dashed magenta line is the Ordinary Least Square (OLS) Fit for the measured and GRASP fitted variable. The solid black line is the 1:1 line for the measured and fitted variable. There are 72,000 data points for 440, 550, and 870 nm bands and 216,000 data points for the 670 nm band. For each plot, the histogram of measurement and GRASP fit for each variable are plotted on the top and right axis respectively.

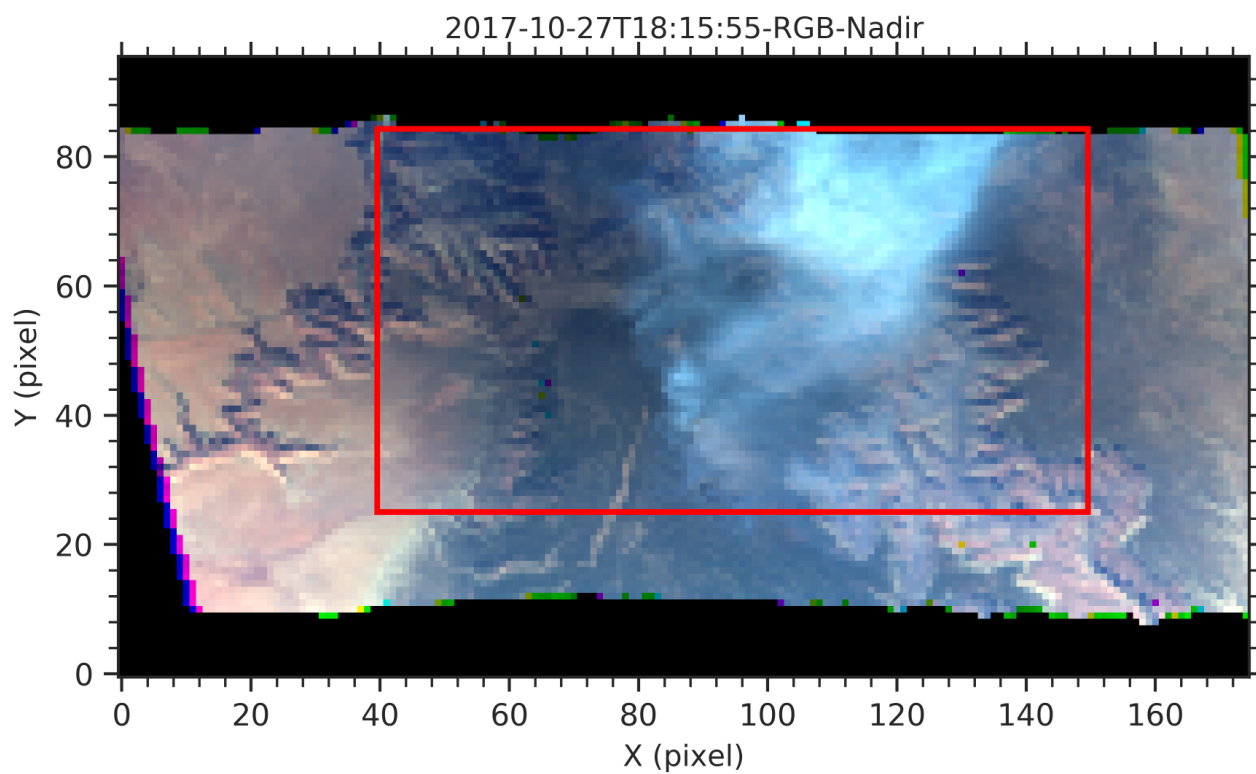
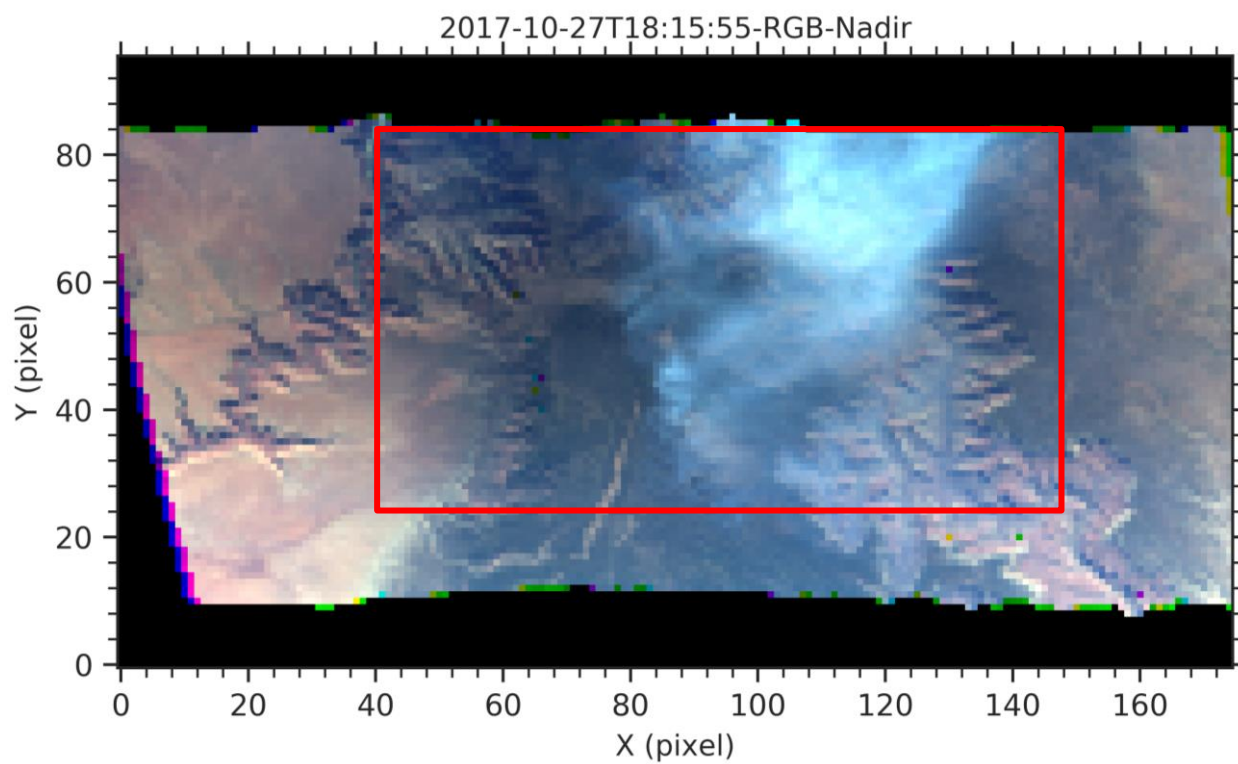




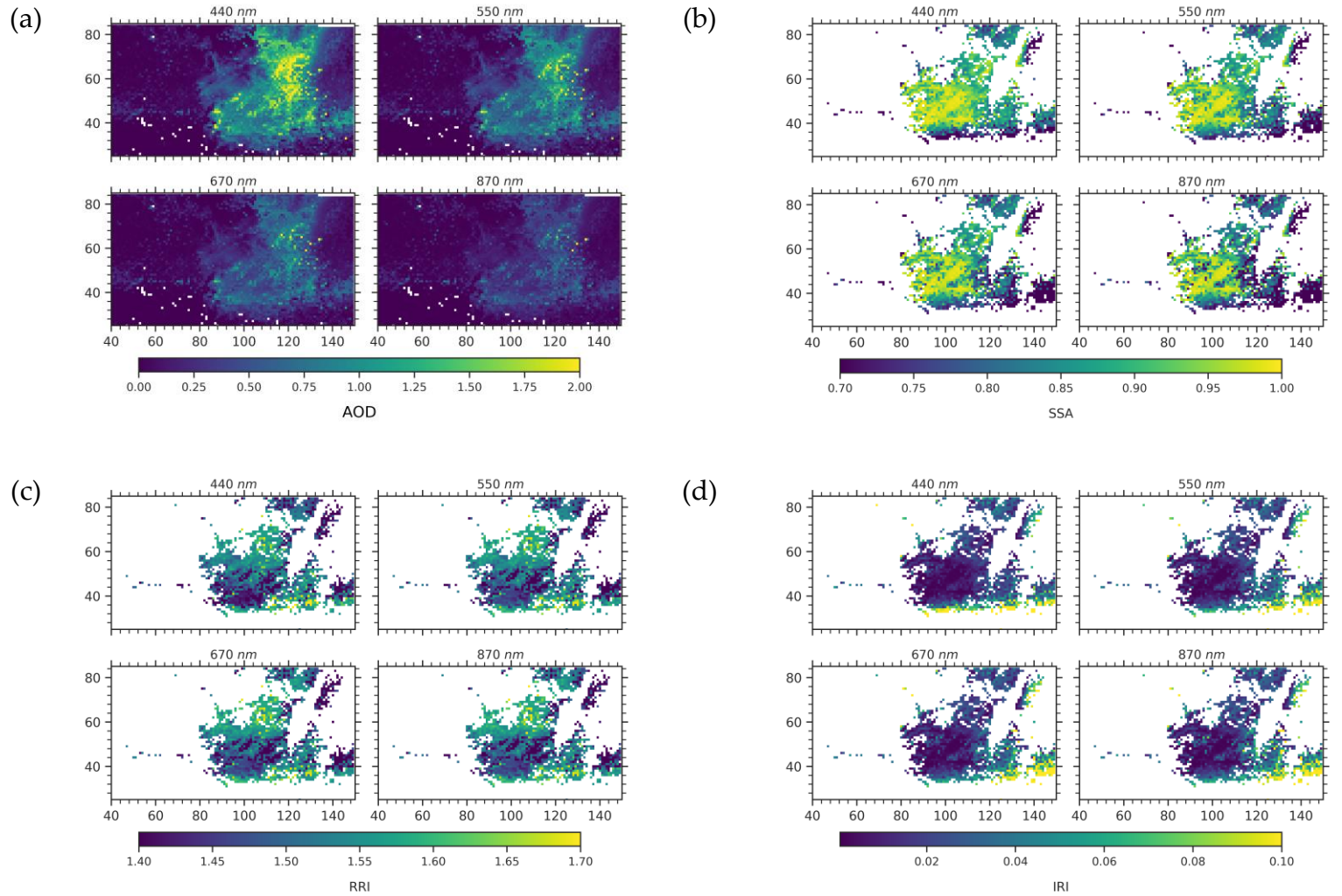




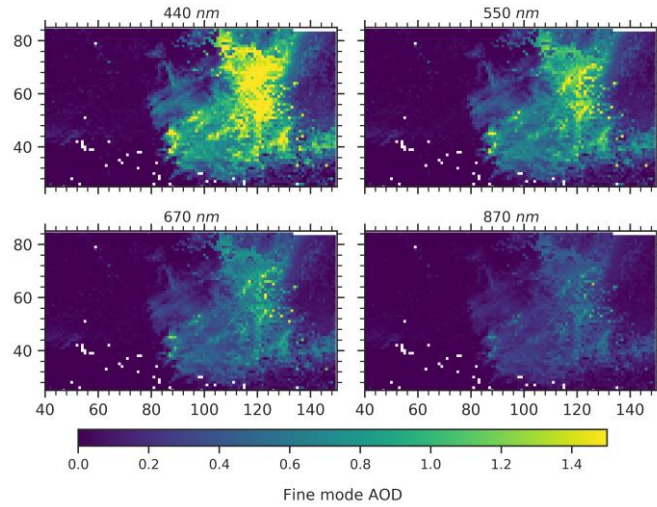
**Figure 67.** AirHARP measured  $I$ ,  $Q/I$ ,  $U/I$ , and DoLP (solid colored circles) and the GRASP fit (black solid lines) for selected pixels from the scene in Fig. 34(a,b,c) are plotted for the 550 nm band. Column (a) an offglint pixel from the scene on 23 October 2017 T21:30 UTC; (b) for a dry lake pixel from the flight leg on 25 October 2017 T18:26 UTC; (c) for a vegetation surface also from flight leg on 25 October 2017 T18:26 UTC; (d) for a smoke pixel from flight leg on 27<sup>th</sup> October 2017 T18:16 UTC.



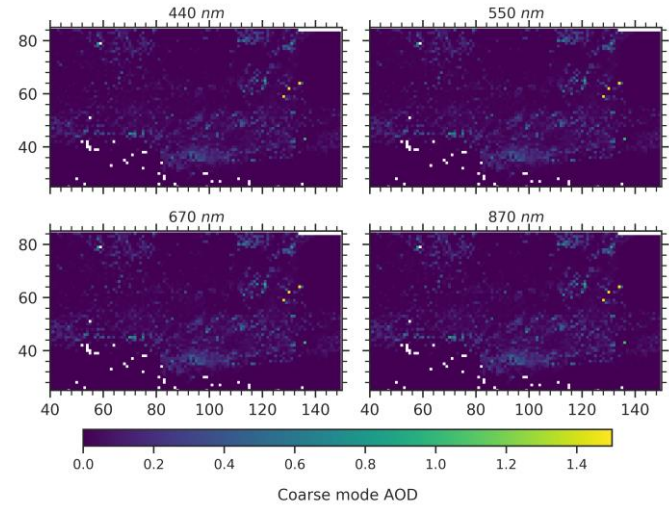
|910 **Figure 78.** RGB composite image of the 27<sup>th</sup> October 2017 T18:16 UTC smoke scene,  $X_1$  and Y axes are the number of pixels (550m x 550m) along the respective axes. Pixels inside the red rectangular box are used for the aerosol retrievals of AOD, SSA, RRI, IRI. These are plotted in Fig. 89.



915 **Figure 89.** (a) AOD map of a subsetting portion of the 27<sup>th</sup> October 2017 T18:16 UTC smoke scene that was marked by a red rectangular box in Fig. 78; (b) Single Scattering Albedo (SSA) for the same subsetting portion in (a) but the pixels with the goodness of fit,  $\chi^2_{norm} > 5$  and  $AOD_{440\text{ nm}} < 0.4$  are masked. (c) same as (b) except the real part of the refractive index (RRI) is plotted. (d) same as (b) except the imaginary part of the refractive index (IRI) is plotted. X and Y axes are the pixel coordinates

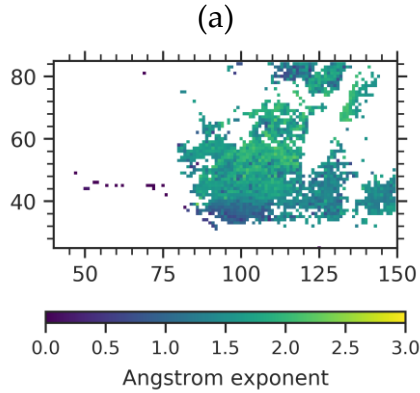


(a)

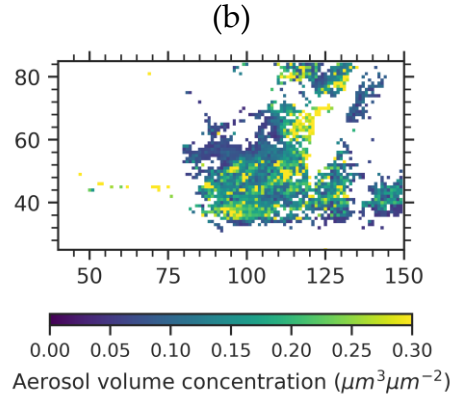


(b)

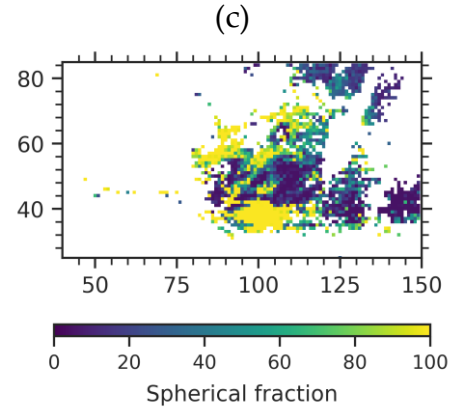
Figure 910. (a) Fine mode AOD map of a subsetting portion of the 27th October 2017 T18:16 UTC smoke scene that was marked by a red rectangular box in Fig. 78 for all AirHARP spectral bands; (b) same as (a) but for coarse mode AOD. X and Y axes are the pixel coordinates.



(a)



(b)

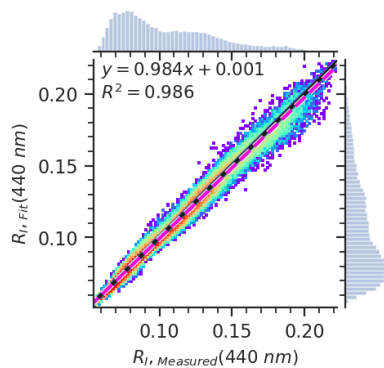
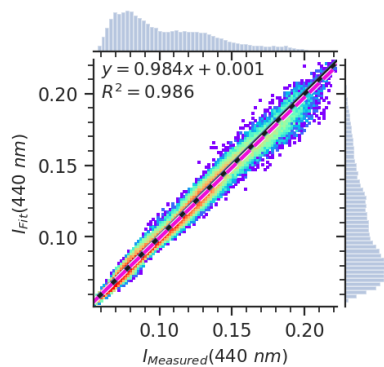


(c)

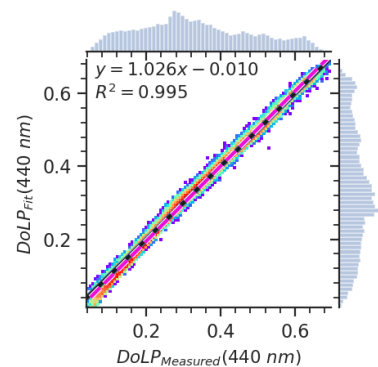
Figure 1011. Map of (a) angstrom exponent (AE), (b) aerosol volume concentration, and (c) spherical fraction (SF) of the scene shown in Fig. 89. Pixel filtering similar to the one applied for SSA, RRI, and IRI in Fig. 89 is applied to filter out bad pixels from AE, aerosol volume concentration, and SF map. X and Y axes are the pixel coordinates.



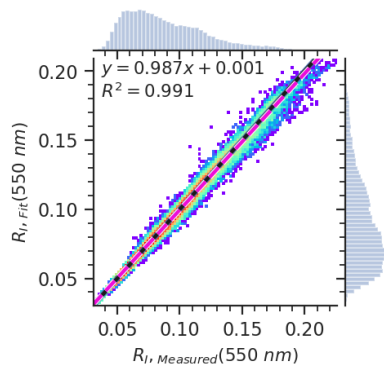
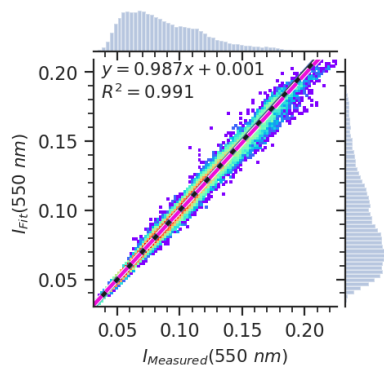
(a)



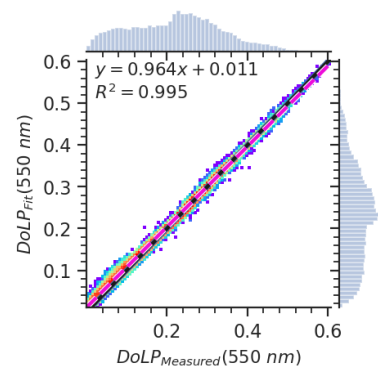
(b)



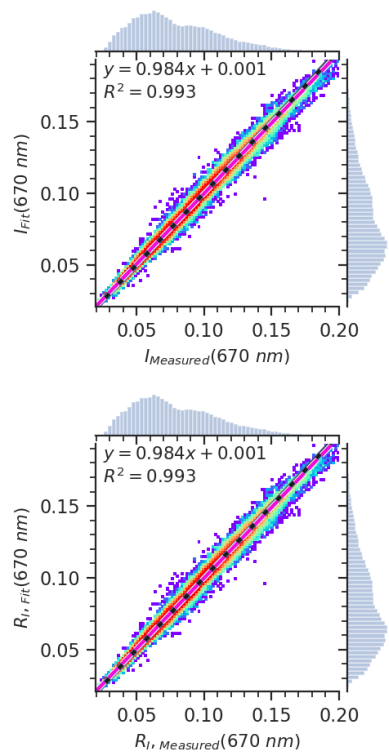
(c)



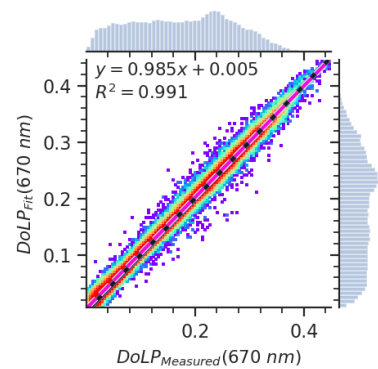
(d)



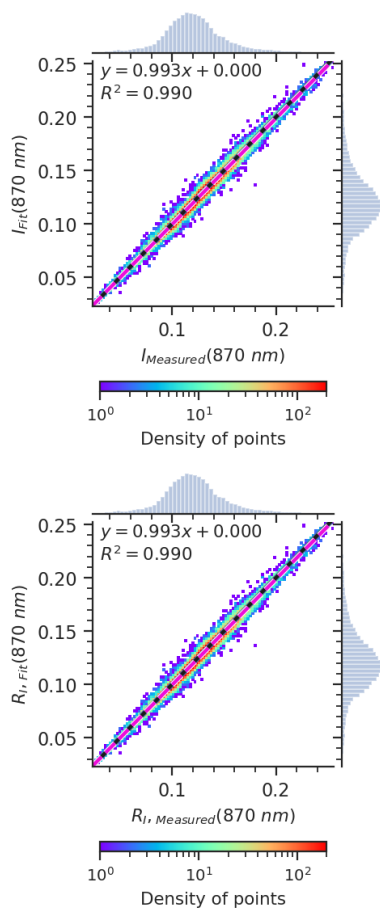
(e)



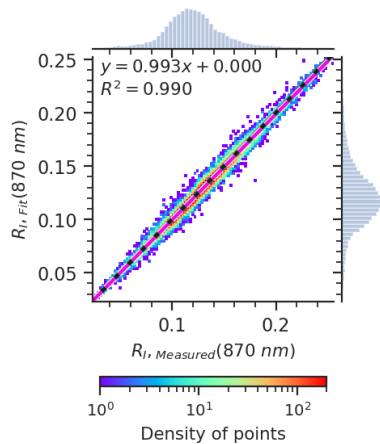
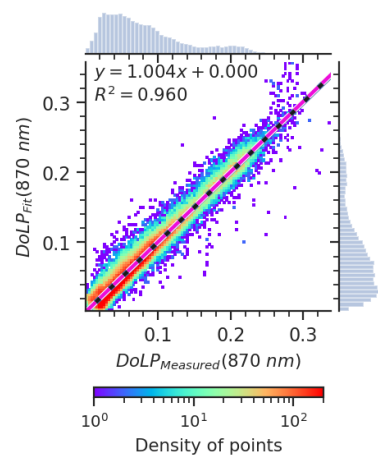
(f)



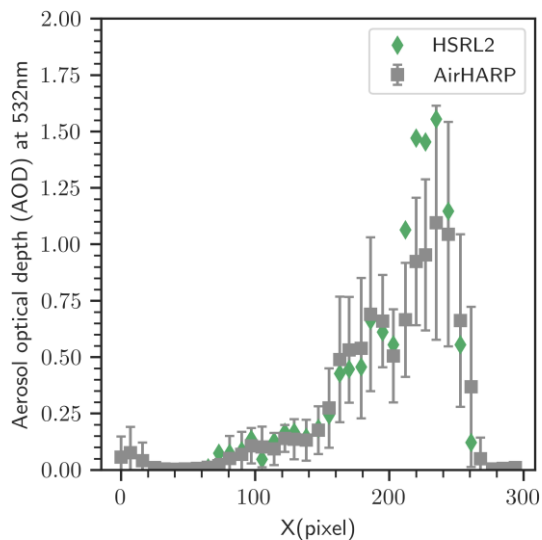
(g)



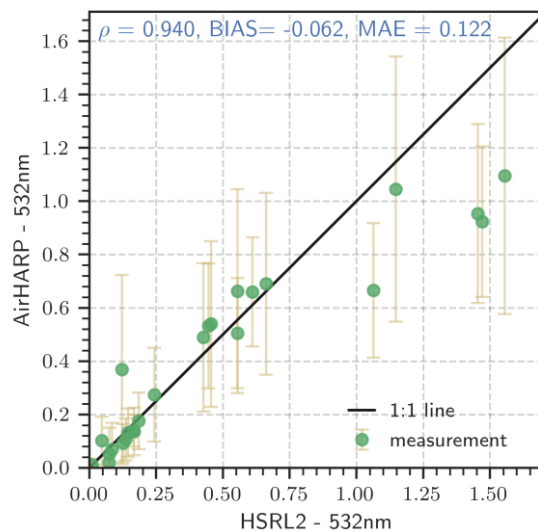
(h)



925 **Figure 4412.** Scatter density plot for AirHARP measurement variables and GRASP fit for the scene in Fig. 89. 1:1 line (black solid line), Ordinary Least Square (OLS) regression line (magenta dashed line), the OLS fit parameters and correlation ( $R^2$ ) are also reported in the same graph. For each plot, the histogram of measurement and GRASP fit for I and DoLP are plotted on the top and right axis respectively.

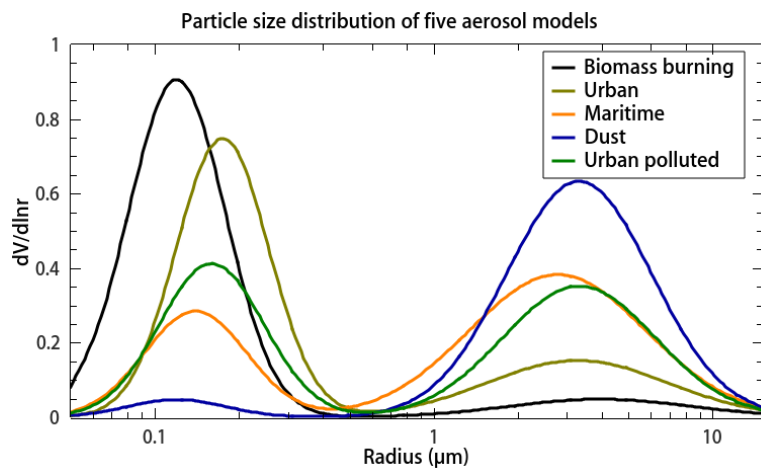


(a)

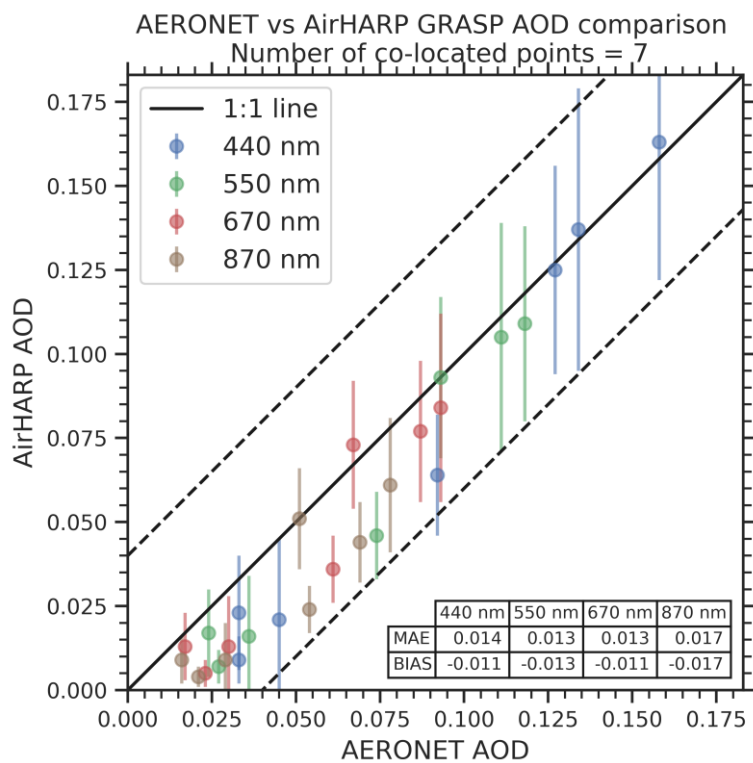


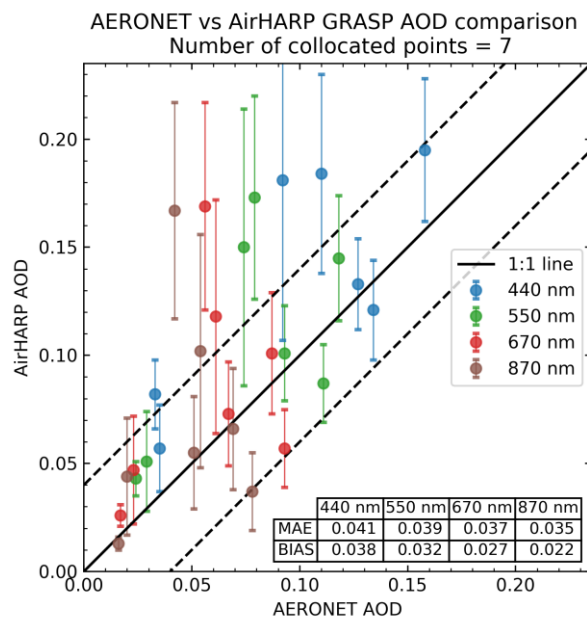
(b)

930 **Figure 12**. (a) AOD at 532 nm from AirHARP versus HSRL2 AOD at 532 nm along the flight track for the forest fire scene on 9<sup>th</sup> November 2017 T19:30 UTC; (b) Correlation plot for the HSRL2 AOD at 532 nm vs AirHARP AOD at 532 nm for the same flight.

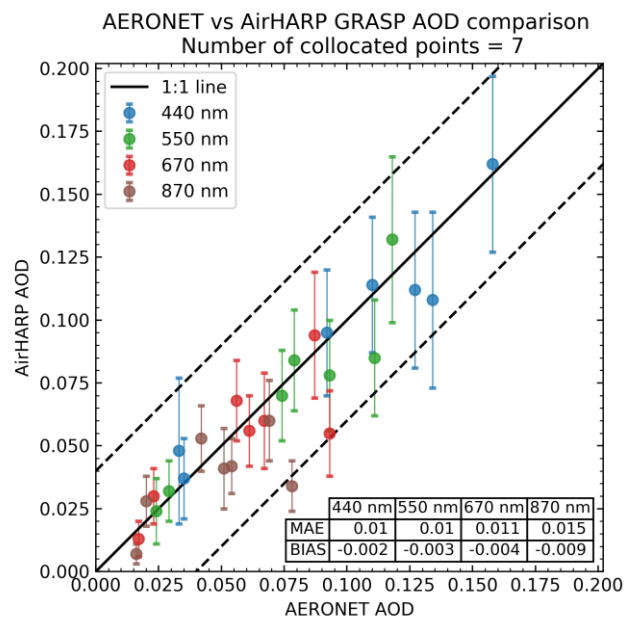


935 **Figure 13**. Particle size distribution of five aerosol types listed in the Table 6. This simplified aerosol-component-based kernels are used for the AirHARP AOD inversion over the collocated AERONET pixels during ACEPOL 2017 campaign.





(a)



(b)

Figure 14. Scattergrams of aerosol optical depth (AOD) retrieved using AirHARP observations over collocated AERONET pixels vs AERONET measured AOD interpolated at AirHARP spectral bands. Plotted are the areal mean AirHARP AODs calculated from all the qualified retrievals within a box of 5.5km x 5.5km around the AERONET station against the collocated AERONET pixel is used to calculate the spatial mean AOD (solid colored circles) over AERONET station using the AirHARP AOD retrievals. Each colored error bars indicate the standard deviation of AOD within the matching areal box. Mean Absolute Error (MAE) and BIAS for each spectral band are provided in the table inside the scattergram. The black solid lines in the plots are the 1:1 lines and the dashed lines are  $\pm 0.04$  AOD from the plot are 1:1 line  $\pm 0.04$ . (a) GRASP retrievals using the GRASP/Five mode kernel (Table 3) that has 15 free parameters and allows for retrieval of particle properties along with AOD; (b) same as (a) except using the GRASP/Models kernel (Table 4) that reduces free parameters to 6 and fixes particle properties based on Table 4 and only retrieves the concentration for each aerosol component.

**Table 1: Information on AirHARP spectral bands, viewing angles, and measured parameters**

Band nominal wavelength	No. of viewing angles	Measured Variables
440 nm	20	I, Q, U
550 nm	20	I, Q, U
670 nm	60	I, Q, U
870 nm	20	I, Q, U

**Table 2: Table of flights analyzed from the ACEPOL campaign which flew over the ocean, land, forest fire smoke, and AERONET sites.**

Date of flight	Time of flights (UTC)	Target Type
23-October-2017	21:30-21:36	Ocean
23-October-2017	21:53-21:59	Aeronet Station (CalTech)
25-October-2017	18:26-18:32	<del>Dry</del> <u>Rosamond dry lake (California, USA)</u>
25-October-2017	19:55-20:01	Aeronet Station (Bakersfield)
<del>25</del> <u>26</u> -October-2017	<del>18:55-20:21</del> <u>20:27-01</u>	Aeronet Station (Fresno_2)
26-October-2017	19:15-19:21	Aeronet Station (Bakersfield)
<del>26-October-2017</del>	<del>21:24-21:32</del>	<del>Aeronet Station (Railroad Valley)</del>
27-October-2017	18:16-18:22	Smoke over land
<del>07-November-2017</del>	<del>18:09-18:15</del>	<del>Aeronet Station (CalTech)</del>
07-November-2017	19:36-19:42	Aeronet Station (Fresno_2)
<del>07-November-2017</del>	<del>20:03-20:09</del>	<del>Aeronet Station (Modesto)</del>
09-November-2017	18:31-18:37	Aeronet Station (USGS_Flagstaff <u>ROLO</u> )
09-November-2017	19:31-19:37	Smoke over land



Table 3: Five log-normal modes used for particle size distribution in GRASP retrieval for AirHARP,  $r_v$  is the volume median radius, and  $\sigma_v$ , geometric standard deviation. In this kernel, other particle properties are free to be retrieved.

$r_v(\mu m)$	$\log(\sigma_v)$
0.1	0.35
0.1732	0.35
0.3	0.35
1.0	0.5
2.9	0.5

Table 4

**Table 4:** Definition of statistical parameters used in this study to find the correlation between measurement and models

Statistical Parameter	Mathematical Formulae
<del>The goodness of fit (<math>\chi^2_{norm}</math>)</del>	$\chi^2_{norm} = \frac{1}{N} \sum_{i=1}^N \frac{(y_i - x_i)^2}{S_y}$
<del>Pearson Coefficient (<math>\rho</math>)</del>	$\rho = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2 \sum_{i=1}^n (y_i - \bar{y})^2}}$
<del>Coefficient of Determination (<math>R^2</math>)</del>	$R^2 = \rho^2$
<del>Mean Absolute Error (MAE)</del>	$MAE = \frac{\sum_{i=1}^N ( y_i - x_i )}{N}$
<del>Bias</del>	$BIAS = \bar{y} - \bar{x}$

**Table 5:** Mean aerosol optical and microphysical properties retrieved for the smoke scene in Fig. 8 (for pixels with AOD<sub>440 nm</sub> > 0.4).

Spectral Band	Single Scattering Albedo	Spherical Fraction (%)	Angstrom Exponent <sup>#</sup>	Real Refractive Index (RRI)	Imaginary Refractive Index (IRI)
440 nm	0.870				
550 nm	0.855				
670 nm	0.838	49.9% <sup>@</sup>	1.53	1.55	0.024
870 nm	0.812				

<sup>#</sup>Angstrom Exponent calculated using the AOD at wavelength bands 440 nm and 870 nm of the AirHARP

<sup>@</sup>Retrieved spherical fraction includes significant number of pixels with SF ~ 99%

**Table 6:** Details on the complex refractive index, and particle size distribution parameters used for the aerosol models. C<sub>v</sub> is the concentration, ln(σ<sub>v</sub>) is the standard deviation of the distribution, and r<sub>v</sub> is the volume median radius. Fine and coarse mode parameters are indicated by f and c subscripts respectively.

Aerosol models	Real part of the refractive	Imaginary part of the refractive index (IRI)		C <sub>v,f</sub>	ln(σ <sub>v,f</sub> )	r <sub>v,f</sub>	C <sub>v,c</sub>	ln(σ <sub>v,c</sub> )	r <sub>v,c</sub>
		(440 nm, 550 nm, 670 nm, 870 nm)							

	<u>index</u>										
	<u>(RRI)</u>										
Biomass	1.510			0.050		0.91	0.40	0.120	0.09	0.75	3.95
Urban	1.395			0.003		0.75	0.38	0.018	0.30	0.75	3.27
Urban polluted	1.470			0.100		0.52	0.43	0.160	0.48	0.63	3.32
Maritime	1.370			0.0001		0.30	0.42	0.140	0.70	0.73	2.78
Dust	1.560	0.0029	0.0019	0.0013	0.0011	0.02	0.40	0.120	0.40	0.60	3.32

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**Table 5:** Definition of statistical parameters used in this study to find the correlation between measurement and models

<u>Statistical Parameter</u>	<u>Mathematical Formulae</u>
<u>The goodness of fit (<math>\chi^2_{norm}</math>)</u>	$\chi^2_{norm} = \frac{1}{N} \sum_{i=1}^N \frac{(y_i - x_i)^2}{S_y}$
<u>Pearson Coefficient (<math>\rho</math>)</u>	$\rho = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2 \sum_{i=1}^n (y_i - \bar{y})^2}}$
<u>Coefficient of Determination (<math>R^2</math>)</u>	$R^2 = \rho^2$
<u>Mean Absolute Error (MAE)</u>	$MAE = \frac{\sum_{i=1}^N ( y_i - x_i )}{N}$
<u>Bias</u>	$BIAS = \bar{y} - \bar{x}$

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**Table 6: Mean aerosol optical and microphysical properties retrieved for the smoke scene in Fig. 9 (for pixels with  $AOD_{440\text{ nm}} > 0.4$ ).**

<u>Spectral Band</u>	<u>Single Scattering Albedo</u>	<u>Spherical Fraction (%)</u>	<u>Angstrom Exponent<sup>#</sup></u>	<u>Real Refractive Index (RRI)</u>	<u>Imaginary Refractive Index (RRI)</u>
<u>440 nm</u>	<u>0.87±0.06</u>				
<u>550 nm</u>	<u>0.86±0.07</u>				
<u>670 nm</u>	<u>0.84±0.08</u>	<u>49.9±36 %<sup>@</sup></u>	<u>1.53±0.336</u>	<u>1.55±0.04</u>	<u>0.024±0.017</u>
<u>870 nm</u>	<u>0.81±0.09</u>				

<sup>#</sup>Angstrom Exponent calculated using the AOD at wavelength bands 440 nm and 870 nm of the AirHARP

<sup>@</sup>Retrieved spherical fraction includes a significant number of pixels with SF ~ 99%

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