# Towards improved turbulence estimation with Doppler wind lidar VAD scans

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## 1 Review response

We want to thank the two anonymous reviewers for their valuable feedback and valid points of criticism to our manuscript.

#### 1.1 Review Comment 1

no futher comments

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#### 5 1.2 Review Comment 2

#### 1.3 RC2, General Comments

1. The revised manuscript is improved, and I believed should be published with minor revisions. I believe the authors should be careful about claiming "the first comparison of in-situ aircraft data with lidar turbulence retrievals", as I point out in the comments below. There are statements to this effect in the abstract and the conclusions section. The term "turbulence retrieval" is too ambiguous. The author should be more specific, i.e. replace "turbulence retrieval" with "TKE and TKE dissipation rate retrieval."

We will be more specific with the turbulence retrieval and refer to "ground-based retrievals of TKE and its dissipationn rate with the VAD method".

#### 1.4 RC2, Specific Comments

- 1. The revised abstract provides a better and more quantitative summary of the results. The grammar (specifically in the abstract) is still a bit rough. For example, the second sentence states "DWL measurements extend beyond the observations with meteorological masts and are comparably flexible in their installation." I believe the thought being expressed here is that the DWLs provide wind measurements above the level of meteorological masts while being much easier and much less expensive to deploy.
  - We apologize for our English grammar, and rephrase according to the suggestion in the revised manuscript.

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- 2. Revision is better. Although I would suggest changing "... TKE dissipation rate is estimated through a fit of the theory of the longitudinal Kolmogorov-structure function" to "... TKE dissipation rate is estimated through a fit of the theoretical longitudinal Kolmogorov-structure function." I'm not sure about the hyphenation though.

  Changed.
- 3. Although the statement should probably be broken down into two sentences. For example, "A fit of the equation ... to the observed azimuth structure function yields estimates of epsilon. In equation (4) ck is the Kolmogorov constant..."

  Changed.
  - 4. Reads much better now. In the revision I would suggest "...  $\sigma_a^2$  is the lidar measured variance without instrumental error  $\sigma_e^2$ , and  $\sigma_t^2$  is the turbulent broadening of the lidar measurement.
- 30 Changed.
  - 5. Better. but I would suggest "...random errors will be smaller for small separation angles." Changed.
  - 6. The revision is better, but there is still a little room for improvement. The author states "the best-fit model PDFs are found to to obtain the corresponding standard deviations..." I think whatthe author means is that Equation (23) is fit to the observed distributions of ..., ..., and ... by adjusting the values of sigma and P.

    Changed.
  - 7. No need to expand the discussion, but you should clarify the point that a first guess estimate of the variance is obtained directly from the data (is that true?). Since the true distribution is not Gaussian the final variance estimate is obtained by integrating equation (23) in the range from +/- 3.5\*sigma, according to Stephan et al. (2018).
- 40 Changed.

- 8. I would also suggest adding the reference to Smalikho (2003) in the appendix where you mention the FSWF-retrieval method.

  Done.
- 9. The author states: "For the first time, the DWL VAD turbulence retrievals are compared to in-situ measurements of a research aircraft..." I would be careful here. We have published comparisons of vertical velocity distributions measured from Doppler lidar to those measured on a research aircraft (e.g. "Overview of the HI-SCALE Field Campaign: A New Perspective on Shallow Convective Clouds", BAMS, by J. Fast, and there are probably other examples). Technically that could be viewed a "turbulence retrieval." The author should be more specific here, e.g. "For the first time, retrievals of TKE and TKE dissipation rate derived from DWL VAD data are compared to in-situ measurements from a research aircraft..."
  - As stated above we are more specific in the revised manuscript, changing the term to "ground-based DWL VAD retrievals

of TKE and its dissipation rate". However, we can not agree that the vertical velocity distributions that are shown in the the reference should be called a "turbulence retrieval".

10. In the first sentence the use of the term "turbulence" is ambiguous. The author should be more specific here (i.e. TKE and epsilon). Also, the author should remove "systematically" from the first sentence.

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We do not think that the term turbulence is "ambiguous", but to be very explicit, we change the sentence according to the recommendation.

- 11. The second sentence is a little perplexing. I'm not sure if the author is suggesting that this is the first time anyone has observed the volume averaging effect or if this is the first time that these four different retrieval methods have been used on the same dataset, or if this is first time that the methods have been applied to the 50 and 90-m levels, or if this is the first time the method has been applied to "... such a big dataset", or something else. Why does it matter how big the dataset is? This statement attempts to point out how this work is novel, but the meaning is obscure. Please clarify.
  - We did not suggest that the well-known volume averaging effect has not been observed before. To be less "perplexing" and "obscure", we rephrase this statement and expand upon it: "The MOL-RAO experiment allowed us to investigate and validate the methods with a database of 30 days containing a broad variety of atmospheric conditions, with wind speeds ranging from  $0..12~{\rm m\,s^{-1}}$  and TKE from  $0..5~{\rm m^2s^{-2}}$ . This goes beyond short-term studies of only few days and specific atmospheric conditions that had been investigated by ?. Furthermore, two sonic anemometers allowed to investigate the dependence of the retrieval on the measurement height."
- 12. In the last sentence, I would suggest changing "tackles" to "handles" or "attempts to handle" Done.

# 2 Relevant changes to the manuscript

We list here the relevant changes to the manuscript:

- 1. Abstract:
  - Text modifications in response to referee comments.
- 75 2. Section 3:
  - Text and equation modifications in response to referee comments.
  - 3. Conclusions:
    - Text modifications in response to referee comments.
    - Added a reference to a recent study about turbulence anisotropy.
- 4. Appendix:
  - Text modifications in response to referee comments.

# References

Smalikho, I. N. and Banakh, V. A.: Measurements of wind turbulence parameters by a conically scanning coherent Doppler lidar in the atmospheric boundary layer, Atmospheric Measurement Techniques, 10, 4191–4208, https://doi.org/10.5194/amt-10-4191-2017, 2017.

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Abstract. The retrieval of turbulence parameters with profiling Doppler wind lidars (DWL) is of high interest for boundary-layer meteorology and its applications. The DWL measurements extend beyond the observations with meteorological masts and are comparably flexible in their installationprovide wind measurements above the level of meteorological masts while being easier and less expensive to deploy. Velocity-azimuth display (VAD) type scans can be used to retrieve turbulence kinetic energy (TKE) dissipation rate through a fit of measured azimuth structure functions to a theoretical model. At the elevation angle of 35.3° it is also possible to derive TKE. Modifications to existing retrieval methods are introduced in this study to reduce the errors due to advection and enable retrievals with a low number of scans. Data of two experiments are utilized for validation: First, measurements at the Observatory Lindenberg – Richard-Aßmann Observatory (MOL-RAO) are used for validation of the DWL retrieval with sonic anemometers on a meteorological mast. Second, distributed measurements of three DWL during the CoMet campaign with two different elevation angles are analyzed. For the first time, the DWL VAD turbulence retrievals ground-based DWL VAD retrievals of TKE and its dissipation rate are compared to in-situ measurements of a research aircraft (here: DLR Cessna Grand Caravan 208B) which allows measurements of turbulence above the altitudes that are in range for sonic anemometers.

From the validation against the sonic anemometers we confirm that lidar measurements can be significantly improved by the introduction of the volume averaging effect into the retrieval. We introduce a correction for advection in the retrieval which only shows minor reductions in the TKE error for  $35.3^{\circ}$  VAD scans. A significant bias reduction can be achieved with this advection correction for the TKE dissipation rate retrieval from  $75^{\circ}$  VAD scans at the lowest measurement heights. Successive scans at  $35.3^{\circ}$  and  $75^{\circ}$  at the CoMet campaign are shown to provide TKE dissipation rates with a good correlation of R > 0.8 if all corrections are applied. The validation against the research aircraft encourages more and targeted validation experiments to better understand and quantify the underestimation of lidar measurements in low turbulence regimes and altitudes above tower heights.

#### 1 Introduction

The observation of turbulence in the atmosphere and in particular the atmospheric boundary layer (ABL) is of great importance for basic research in boundary-layer meteorology as well as in applied fields such as aviation, wind energy (van Kuik et al.,

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2016; Veers et al., 2019) or pollution dispersion (Holtslag et al., 1986).

A wide range of instruments are used to measure turbulence: sonic anemometers are nowadays the most popular in-situ instrument which can be installed on meteorological masts and provide continuous data of the three-dimensional flow and its turbulent fluctuations (Liu et al., 2001; Beyrich et al., 2006). For in-situ measurements above the height of towers, airborne systems are applied such as manned aircraft (Bange et al., 2002; Mallaun et al., 2015), remotely-piloted aircraft systems (RPAS, van den Kroonenberg et al., 2011; Wildmann et al., 2015) or tethered lifting systems (TLS, Frehlich et al., 2003) which can be equipped with turbulence probes such as multi-hole probes or hot wire anemometers. A different category of instruments are remote-sensing instruments such as radar, sodar and lidar which can measure wind speeds and allow the retrieval of turbulence based on assumptions of the state of the atmosphere and the structure of turbulence. In this study, we focus on ground-based Doppler wind-lidars (DWL), which have become increasingly popular in boundary-layer research because of their ease of installation, invisible and eye-safe lasers, their reliability and high availability which is only restricted by clouds/fog and rain or very low aerosol content in the atmosphere.

A variety of methods already exist to retrieve turbulence from DWL measurements. They can be categorized according to the respective scanning strategy applied: the simplest scanning pattern is a constant vertical stare to zenith, which allows to obtain variances of vertical velocity and estimates of turbulence kinetic energy (TKE) dissipation rate (O'Connor et al., 2010; Bodini et al., 2018). More complex are conical scans (velocity azimuth display, VAD) with continuous measurements along the cone (Banakh et al., 1999; Smalikho, 2003; Krishnamurthy et al., 2011; Smalikho and Banakh, 2017). These scans include information on the horizontal wind component as well. A simplification of VAD scans are Doppler-beam-swinging (DBS) methods, that reduce the number of measurements taken along the cone to a minimum of 4-5 beams and thus increase the update rate for single wind profile estimations (Kumer et al., 2016). Both, VAD and DBS are popular scanning strategies that are applied in commercial instruments. Kelberlau and Mann (2019a, b) introduced new methods to obtain better turbulence spectra from conically scanning lidars by corrections for the scanner movement. Significantly different scanning strategies are vertical (or horizontal) scans which can also provide vertical profiles of turbulence (Smalikho et al., 2005), but even allow deriving two-dimensional fields of TKE dissipation rate (Wildmann et al., 2019). Multi-Doppler measurements require more than one lidar with intersecting beams, but do not need assumptions on homogeneity to measure turbulence at the points of the intersection directly (Fuertes et al., 2014; Pauscher et al., 2016; Wildmann et al., 2018). For operational or continuous monitoring of vertical profiles of turbulence in the ABL, VAD or DBS scans are most suitable. At an elevation angle of 35.3°, a VAD scan allows to retrieve TKE, its dissipation rate, integral length scale and momentum fluxes according to a method that was first developed for radar by Kropfli (1986) and adapted for lidar later by Eberhard et al. (1989) using the variance of radial velocities along the scanning cone. Further improvements of this method have been implemented by Smalikho and Banakh (2017) and Stephan et al. (2018), which also account for lidar volume averaging effects. We introduce modifications on the estimation of structure function and variances in order to be able to retrieve turbulence parameters from a smaller number of VAD scans. For conditions with significant advection, the method can cause errors, especially at low altitudes where the cone diameter of the VAD scan is small. With this study, we propose a method to reduce this error. We also apply the turbulence retrieval to VAD scans with 75° elevation angle, which still allows to retrieve TKE dissipation rate. In this case the advection

correction is particularly important. The experiments that were carried out are explained in Sect. 2. The methods and the new developments are explained in Sect. 3. A focus of this study is on the validation of the lidar measurements with sonic anemometers and airborne in-situ measurements. The results of the validation are presented in Sect. 4. Conclusions and an outlook are given in Sect. 5.

#### 5 2 Experiment description

In this study, data from two different experiments are analyzed. Both of the experiments and the instrumentation is introduced in this section.

## 2.1 The MOL-RAO Falkenberg field site

The Meteorological Observatory Lindenberg – Richard-Aßmann Observatory (MOL-RAO) is part of Deutscher Wetterdienst (DWD), the national meteorological service of Germany. The observatory is situated in the East of Germany, approximately 65 km to the South-East of the center of Berlin. MOL-RAO runs a comprehensive operational measurement program to characterize the physical structure and processes in the atmospheric column above Lindenberg. Measurements of ABL processes form an essential part of it, they are carried out at the boundary layer field site (in German: Grenzschichtmessfeld, GM) Falkenberg, about 5 km to the South of the main observatory site. The GM Falkenberg is situated in a rural landscape dominated by forest, grassland and agricultural fields (see Fig. 1). A central measurement facility at the Falkenberg site is a 99m tower, equipped with booms to carry sensors every 10 m.

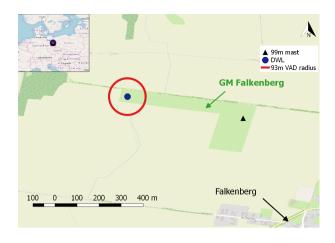
Since 2014, MOL-RAO is using a DWL "Stream Line" (Halo Photonics Ltd.) for boundary layer measurements. From that time the device has been extensively tested with respect to its operational use for wind and turbulence measurements. This included, for instance, tests on the technical robustness and data availability under all weather conditions, but also tests of different scanning strategies and retrieval methods for the 3D wind vector and for the TKE. The position of the DWL during a measurement period from 2 April 2019 through 30 April 2019 was at the western edge of the field site, at about 500 m distance from the 99m tower. It should be noted that there is a small patch of forest about 300 m to the W-NW of the lidar site. During this period the system continuously performed VAD scans with an elevation angle of 35.3° elevation which will be analysed for turbulence retrievals in this study.

Continuous turbulence measurements (20 Hz sampling frequency) using sonic anemometer of type USA-1 (METEK GmbH) are performed at the 50m and 90m levels of the tower and have been used for validation purposes. The instruments are mounted at the tip of the booms pointing towards South.

#### 2.2 The CoMet (CO<sub>2</sub> and Methane) Mission 2018

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Within the scope of the CO<sub>2</sub> and Methane Mission (CoMet) that was conducted in spring 2018, three Doppler wind lidars of type Leosphere Windcube 200S (details see Tab. 1) were installed in Upper Silesia (Poland) with the purpose of providing spatially distributed wind and turbulence measurements in the ABL. CoMet aims at a better understanding of the budgets



**Figure 1.** Sketch of the measurement site at MOL-RAO, GM Falkenberg. Map data ©OpenStreetMap contributors 2019. Distributed under a Creative Commons BY-SA License.

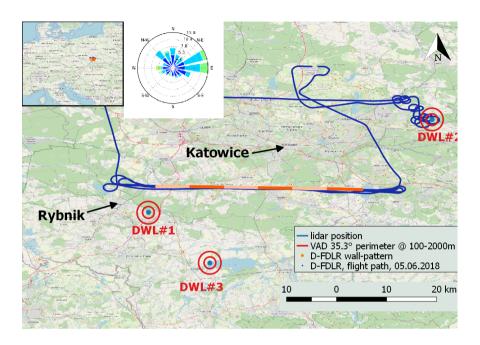
of the two most important anthropogenic greenhouse gases (GHGs), CO<sub>2</sub> and CH<sub>4</sub>. For this purpose, the research aircraft HALO (high altitude and long range) was taking remote sensing and in-situ measurements over large parts of the European continent. A dedicated area of high interest was the region of Upper Silesia, where large amounts of methane are known to be released due to the intensive coal extraction activities in the respective Coal Basin. During the CoMet campaign, the DLR Cessna Grand Caravan 208B (D-FDLR) aircraft was equipped with in-situ instruments to measure greenhouse gases as well as thermodynamic variables.

The DWL measurements are particularly helpful to support the CoMet measurements by providing wind information which is essential to derive emission flux estimates from passive remote sensing (Luther et al., 2019) or in-situ measurements of mass concentrations (Fiehn et al., 2020). The DWL wind information can also be used to validate modeled wind of the transport models for greenhouse gases. The lidars were remotely operated during the whole CoMet campaign period from 16 May 2017 to 17 June 2017 and were continuously measuring. The locations of the three lidars were planned to cover the whole region of interest and were finally chosen based on logistical constraints.

The lidars were operating in VAD modes with two different elevation angles. Since the focus for the CoMet campaign was on continuous wind profiling and a good height coverage was desired, the lidars were programmed to perform VADs with an elevation angle of 75° (see Tab. 1, VAD75) for a longer period, i.e. 24 scans ( $\approx$ 29 minutes), followed by only six scans ( $\approx$ 7 minutes) at 35.3° elevation (VAD35) for turbulence retrievals.

As shown in Fig. 2, the three lidars were separated by several tens of kilometers and were located in different terrain types. While DWL#1 was in a mixed rural and urban area, DWL#2 was in a mostly forested environment and DWL#3 was in close vicinity to the lake Goczalkowicki. The main wind direction during the campaign was from the East, with particularly strong winds during nighttime low-level jet (LLJ) events. In this study we analyze statistics of the whole campaign, as well as a case study on 5 June 2017, on which D-FDLR was performing long straight and level legs between 800 m and 1600 m as indicated in the flight path in Fig. 2. Since the D-FDLR was focusing on GHG measurements at the hotspots of the Upper Silesian

Coal Basin, there are no more straight and level flight paths that allow for turbulence retrieval. On this day however, the research aircraft provides a unique possibility to validate lidar measurements with in-situ measurements at higher altitudes that cannot be reached with sonic anemometers. The flow probe and inertial measurement unit on the D-FDLR are well-established instruments that allow reliable measurements of the 3D-wind vector and turbulence (Mallaun et al., 2015).



**Figure 2.** Sketch of the measurement site in Upper Silesia. Red circles show the extent of the VAD-scan at 35.3° for 100 m and 2000 m at the respective lidar location. The orange line marks the flight path of D-FDLR on 5 June 2017. The different shades of orange are used to indicate a subdivision of the flight leg in shorter sublegs. Map data ©OpenStreetMap contributors 2019. Distributed under a Creative Commons BY-SA License.

Table 1. Main technical specifications of the Doppler wind lidars.

	Windcube 200S, VAD75	Windcube 200S, VAD35	Stream Line
Wavelength $\lambda$	1.54 μm	1.54 μm	1.5 μm
Pulse length $ au_p$	200 ns	200 ns	180 ns
Time window $T_w$	288 ns	144 ns	240 ns
Bandwidth	$26.7 \text{ m s}^{-1}$	$26.7 \; \mathrm{m \; s^{-1}}$	$19.4 \text{ m s}^{-1}$
Elevation angle $\varphi$	75°	35.3°	35.3°
Angular speed	$5^{\circ} \mathrm{s}^{-1}$	$5^{\circ}\mathrm{s}^{-1}$	$5^{\circ} \mathrm{s}^{-1}$
Pulse repetition frequency	20 kHz	20 kHz	15 kHz
Accumulation time	200 ms	200 ms	133 ms
CNR filter	-200 dB	-200 dB	-150 dB

#### 5 3 Methods

#### 3.1 Sonic anemometer turbulence measurements

From the sonic anemometers on the meteorological mast, TKE and TKE dissipation rate are calculated. TKE is calculated from the sum of variances  $E_{\rm TKE}=0.5\left(\sigma_u^2+\sigma_v^2+\sigma_w^2\right)$ . TKE dissipation rate  $\varepsilon$  is estimated through a fit of the theory of the longitudinal Kolmogorov-structure theoretical longitudinal Kolmogorov structure function in the range  $\tau_1=0.1~{\rm s}$  to  $\tau_2=2~{\rm s}$  to the measured second-order structure function of horizontal velocity. Muñoz-Esparza et al. (2018) showed that the structure function method is more robust than estimates from spectra. For this study, in order to have the best possible comparison to the lidar measurements the values for  $\varepsilon$  are calculated for 30-minute intervals. The geometry of the sonic anemometer setup disturbs the measurements for wind directions from 330° to 50° (see also App. D). Data for these wind directions are removed from the analysis.

#### 15 3.2 VAD turbulence measurements

Methods to retrieve turbulence parameters from VAD scans are well-known and a variety of different methods exist. The method we refine in this study is based on the theory that was originally described by Eberhard et al. (1989) for lidar measurements. The variance of radial velocities  $\sigma_r^2$  depends on the range gate distance R, the azimuth angle  $\theta$  and the elevation angle  $\varphi$ . It is calculated from the measured radial velocities  $V_r$ :

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$$v_r(R, \theta, \varphi, t) = V_r(R, \theta, \varphi, t) - \langle V_r(R, \theta, \varphi) \rangle$$
 (1)

$$\sigma_r^2 = \langle v_r(R, \theta, \varphi, t)^2 \rangle \tag{2}$$

From a partial Fourier decomposition (see App. A) and for the special case of  $\varphi = 35.3^{\circ}$  a simple equation for  $E_{\rm TKE}$  is derived:

$$E_{\text{TKE}} = \frac{3}{2} \overline{\sigma}_r^2 |_{\varphi = 35.3^{\circ}}$$
 (3)

In this equation,  $\overline{\sigma}_r^2$  is the mean of the variance of radial velocites over all azimuth angles. In the following, we will refer to this method as E89-retrieval.

In order to retrieve estimations of TKE dissipation rate  $\varepsilon$  from VAD scans, a similar approach to the method for sonic anemometers can be followed. A fit of the equation

$$D_r(\psi) = (4/3)C_K(\varepsilon \psi R')^{2/3} \quad , \tag{4}$$

to the azimuth structure function with yields an estimate for  $\varepsilon$  according to Smalikho and Banakh (2017). In Eq. 4  $D_r$  is the transverse structure function of radial velocities,  $C_K$  the Kolmogorov constant,  $\psi$  the azimuth angle increment and  $R' = R\cos\varphi$  retrieves an estimate for  $\varepsilon$  according to Smalikho and Banakh (2017). We will refer to this method as S17A in the following.

Scanning with Doppler lidar in a classical VAD with continuous motion of the azimuth motor involves a volume averaging of radial velocities in longitudinal (along the laser beam) and transverse (orthogonal to the beam) direction. The E89 and S17A methods do not consider this effect and will thus yield a systematic underestimation of TKE and  $\varepsilon$ . Smalikho and Banakh (2013) proposed a theory that considers the volume averaging and allows the retrieval of  $\varepsilon$  from conical scans, independent of the elevation angle. In Smalikho and Banakh (2017), this method has been combined with the E89-method to yield TKE,  $\varepsilon$  and the momentum fluxes. It is based on the decomposition of radial velocity variance  $\sigma_r^2$  into its subcomponents, i.e.

$$\sigma_L^2 = \sigma_a^2 + \sigma_e^2 \quad , \tag{5}$$

$$\sigma_a^2 = \sigma_r^2 - \sigma_t^2 \quad , \tag{6}$$

$$15 \quad \sigma_r^2 = \sigma_L^2 + \sigma_t^2 - \sigma_e^2 \tag{7}$$

where  $\sigma_L^2$  is the lidar measured variance,  $\sigma_a^2$  as is the lidar measured variance without instrumental error  $\sigma_e^2$ , and  $\sigma_t^2$  is the turbulent broadening of the lidar measurement  $\sigma_t^2$ . In Smalikho and Banakh (2017), all of these variances and structure functions are calculated for single azimuth angles and then averaged. We describe in Sect.3.2.1 why we use total variances and structure functions of all radial velocities.

The measured azimuth structure function  $D_a(\psi_l)$  is a function of the separation angle  $\psi_l$ , where l is the index of the discrete separation angle of the scan. It can be decomposed into the lidar measured structure function  $D_L(\psi_l)$  and the instrumental error  $\sigma_e^2$ :

$$D_L(\psi_l) = \langle \left[ v_r(\theta) - v_r(\theta + \psi_l) \right]^2 \rangle \tag{8}$$

$$D_a(\psi_l) = D_L(\psi_l) - 2\sigma_e^2 \tag{9}$$

$$\sigma_r^2 = \sigma_L^2 + \sigma_t^2 - \frac{1}{2} D_L(\psi_l) + \frac{1}{2} D_a(\psi_l) \quad . \tag{10}$$

It shows that since the instrumental error  $\sigma_e^2$  is assumed to be a constant offset of azimuth structure function  $D_a(\psi_l)$  and the lidar measurement  $D_L(\psi_l)$ , l can be chosen arbitrarily here. It is set to l=1 because potential random errors like unstationary flow will be least effective smaller for small separation angles. Using Eq.3 and Eq. 21 (see Sect.3.2.1), TKE can be redefined as a function of the measured line of sight variances  $\sigma_L^2$ , the measured lidar azimuth structure function of radial velocities  $D_L(\psi_1)$  and a residual term G, which includes the two unknowns  $\sigma_t^2$  and  $D_a(\psi_1)$ :

$$E_{\text{TKE}} = \frac{3}{2} \left[ \sigma_L^2 - \frac{D_L(\psi_1)}{2} + G \right] \quad , \tag{11}$$

$$G = \sigma_t^2 + \frac{1}{2}D_a(\psi_1) \tag{12}$$

In Banakh and Smalikho (2013), a relationship between the two unknowns and TKE dissipation rate is theoretically derived from the two-dimensional Kolmogorov-Obhukov spectrum as

$$\sigma_t = \varepsilon^{2/3} F(\Delta y) \tag{13}$$

$$D_a(\psi_l) = \varepsilon^{2/3} A(l\Delta y) \quad , \tag{14}$$

where  $F(\Delta y)$  and  $A(l\Delta y)$  are model functions that include the lidar filter functions (see App. B). The lidar filter functions in longitudinal direction depend on pulse width of the laser beam  $\Delta p$  and the time window  $T_w$  of the data acquisition. The transverse filter function is defined by  $\Delta y = R\Delta\theta\cos\varphi$ , which is the distance the lidar beam moves along the cone during one accumulation period. The parameters for the lidars in this study are provided in Tab. 1 and are calculated from information given by the manufacturer for the specific lidar type. Hence, G depends on the turbulence dissipation rate  $\varepsilon$ :

$$G = \varepsilon^{2/3} \left[ F(\Delta y) + \frac{A(\Delta y)}{2} \right] \tag{15}$$

Using Eq. 14 and 9,  $\varepsilon$  can be retrieved from  $D_a(\psi_l) - D_a(\psi_1)$ :

$$\varepsilon = \left[ \frac{D_L(\psi_l) - D_L(\psi_1)}{A(l\Delta y) - A(\Delta y)} \right]^{3/2} \tag{16}$$

This equation does not depend on the elevation angle, so that the method allows the retrieval of  $\varepsilon$  from VAD scans with elevation angles different from 35.3° as well. Figure 3 gives an example of the different structure functions that are calculated in this method (i.e.  $D_L$ ,  $D_a$  and A) and also gives a comparison to the structure function  $D_s$  as calculated from sonic anemometer measurements. Smalikho and Banakh (2017) found a separation angle of  $l\Delta\theta=9^\circ$  an appropriate value for ABL measurements. In this study, all VAD scans are performed with a resolution of  $\Delta\theta=1^\circ$ , so that l=9. In Fig. 3 the range that is thus used for the structure function fit is indicated by the bold black line.

The retrieval method for  $\varepsilon$  using Eq. 16 and TKE using Eq. 11 will be referred to as S17 in the following.

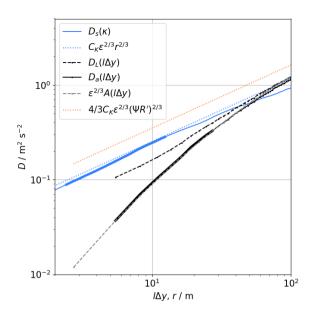


Figure 3. Example of structure functions of sonic anemometer (blue) and lidar (grey) at 90 m height on 4 April 2019, 1200-1230 UTC. The dashed black line shows the measured lidar structure function  $D_L$ , the solid black line  $D_a$  is corrected for the systematic error  $\sigma_e$  (see Eq. 9). The grey dashed line gives the model structure function A and the dotted lines indicate the reconstructed inertial subrange for the calculated values of  $\varepsilon$ . The parts with bold lines are those ranges that are used for the structure function fits.

#### 3.2.1 Modifications for small number of scans

The VAD at  $\varphi = 35.3^{\circ}$  during the CoMet-campaign was not run continuously, but only six individual scans are performed successively before switching back to the VAD at  $\varphi = 75^{\circ}$  as described in Sect. 2.2. This means that only six data points are available to calculate variance and mean of the radial velocities at each azimuth angle, which cannot be considered a solid statistic. We introduce two modifications of data processing to overcome this problem which are based on the assumptions of stationary and homogeneous turbulence.

#### Practical implementation of the ensemble average

5 In Eq. 2,  $\langle V_r(R,\theta,\varphi) \rangle$  can be calculated as the arithmetic mean of radial velocities at specific azimuth angles:

$$\langle V_r(R,\theta,\varphi)\rangle = \frac{1}{N} \sum_{n=0}^{N} V_r(R,\theta_n,\varphi) \quad , \tag{17}$$

where N is the number of scans. Instead of this approach, we suggest to use the reconstructed radial velocity from the retrieved wind field over all individual scans as the expected value in the variance calculation. For the retrieval of the three wind components  $(\hat{u}, \hat{v}, \hat{w})$ , filtered sine-wave fitting (FSWF) is applied (Smalikho, 2003). The reconstructed radial velocities  $\hat{V}$  are

10 then used as the expected value in the variance calculation:

$$\hat{V} = \hat{w}(R)\sin\varphi + \hat{v}(R)\cos\varphi\cos\theta + \hat{u}(R)\cos\varphi\sin\theta \tag{18}$$

$$\langle V_r(R,\theta,\varphi)\rangle = \hat{V}(R,\theta,\varphi)$$
 (19)

With this approach, all measurement points in the VAD with the same elevation angle are used to obtain the expected value  $\langle V_r \rangle$  and thus, a better statistical significance is achieved. This method has also been proposed in Smalikho and Banakh (2017) as a practical implementation of Eq. 2.

#### Averaging of variances

In Smalikho and Banakh (2017), the variances of the lidar measurements are defined as the average of variances at individual azimuth angles:

$$\overline{\sigma}_r^2 = \frac{1}{M} \sum_{m=0}^M \sigma_r^2(\theta_m) \tag{20}$$

The variances  $\sigma_r^2(\theta_m)$  are variances of a subsample of radial velocities of the VAD (i.e. those at a specific azimuth angle  $\theta_m$ ). We use a simple relation between the variances of subsamples and the total variance of a dataset (see Appendix C). Applying this to the radial velocity variances yields:

$$\sigma_r^2 = \frac{k-1}{n-1} \sum_{m=1}^g \sigma_r^2(\theta_m) + \frac{k(g-1)}{k-1} \overline{v}_r \quad , \tag{21}$$

where k is the number of samples at each azimuthal angle, g is the number of subsamples and n is the number of total samples in the dataset (n = gk). Since the mean of the radial velocity fluctuations is zero by definition, Eq. 21 becomes:

$$\sigma_r^2 \approx \overline{\sigma}_r^2(\theta_m) \quad . \tag{22}$$

#### 15 3.2.2 Filtering of bad estimates

Improvements of turbulence estimates in low signal conditions can be achieved with filtering of bad estimates as described in Stephan et al. (2018). This approach is not based on the calculation of the azimuth structure function from measured radial velocities, but uses probability density functions (PDFs) and their corresponding standard deviations. The model PDF is defined as a Gaussian function with a filter term P:

$$20 \quad p_M(x) = \frac{1 - P}{\sqrt{2\pi}\sigma} \exp\left[-\frac{1}{2}\left(\frac{x}{\sigma}\right)^2\right] + \frac{P}{B_v} \quad , \tag{23}$$

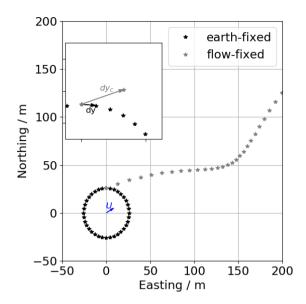


Figure 4. Sketch of measurement points of a VAD scan in an earth-fixed versus a flow-fixed coordinate system.

where P is the probability of bad estimates of x,  $\sigma$  is the standard deviation of the PDF and  $B_v$  is the velocity bandwidth of the lidar. For the measured variables Eq. 23 is fit to the observed distributions of  $v_r(R,\theta)$ ,  $\Delta v_r(R,\theta+\Delta\theta)$  and  $\Delta v_r(R,\theta+l\Delta\theta)$ ; the best-fit model PDFs are found to to obtain the corresponding standard deviations by adjusting the corresponding values  $\sigma_1$ ,  $\sigma_2$  and  $\sigma_3$  and probability of bad estimates  $P_1$ ,  $P_2$  and  $P_3$ . The values of  $\sigma_i$  are used as the first guess of the standard deviation of the distributions. However, since the PDFs cannot be assumed Gaussian in atmospheric turbulence, the standard deviations are finally calculated as the integral over the measured PDFs in the range  $\pm 3.5\sigma$  according to Stephan et al. (2018). Replacing  $\sigma_L^2$  with  $\sigma_1^2$ ,  $D_L(\psi_1)$  with  $\sigma_2^2$  and  $D_L(\psi_l)$  with  $\sigma_3^2$  in Eqs. 11 and 16 yields:

$$E_{\text{TKE}} = \frac{3}{2} \left[ \sigma_1^2 - \frac{\sigma_2^2}{2} + G \right]$$
 and (24)

$$\epsilon = \left[\frac{\sigma_3^2 - \sigma_2^2}{A(l\Delta y) - A(\Delta y)}\right]^{3/2} \tag{25}$$

As suggested in Stephan et al. (2018), Eqs. 24 and 25 are only used if P > 0. We also introduced a quality control to discard any measurements with P > 0.5 for best results. In practice, this method will thus only be applied in some conditions when the signal is weak and can extend the range of vertical profiles to some degree.

#### 3.2.3 Correction for advection

The azimuth structure function and the volume average filter are distorted by advection through a modification of  $\Delta y$ . The effect is illustrated in Fig. 4. It shows that the distance between measurement points in a flow-fixed coordinate system is unequally spaced and on average larger than in the earth-fixed coordinate system. We propose a simplified correction. When advection is not considered, the spacing between samples is given by

$$\Delta y = \Delta \theta R \cos \varphi \quad . \tag{26}$$

An estimate of the mean spacing can be obtained from

$$\Delta y \approx \frac{1}{N} \sum_{i=0}^{N} \sqrt{dx_i^2 + dy_i^2} \quad , \tag{27}$$

where  $dx_i = x_{i+1} - x_i$ . We propose a simplified correction in which

$$\Delta y_c \approx \frac{1}{N} \sum_{i=0}^{N} \sqrt{dx_{c,i}^2 + dy_{c,i}^2} \quad , \tag{28}$$

where

$$5 \quad dx_{c,i} = dx_i + \cos \Psi U \Delta t \tag{29}$$

$$dy_{c,i} = dy_i + \sin \Psi U \Delta t \tag{30}$$

(31)

Here, R is the range gate distance,  $\varphi$  is the elevation angle,  $x_i$  and  $y_i$  are the measurement point locations,  $\Psi$  is wind direction, U is wind speed and  $\Delta t$  is the accumulation time of the lidar. The terms  $\cos \Psi U \Delta t$  and  $\sin \Psi U \Delta t$  describe the effect of advection on the measurement location in x- and y-direction respectively. Using the corrected measurement location displacements  $dx_{c,i}$  and  $dx_{c,i}$ , we can calculate a corrected mean transverse sensing volume  $\Delta y_c$ . This method does not account for the unequal spacing, but corrects the average separation of data points, which is particularly important for the statistical evaluation of turbulence.

The effects of advection on the turbulence estimation is largest in the lowest levels of the VAD-scans, because  $\Delta y$  is small compared to  $U\Delta t$  in this case. The retrieval method including the filtering for bad estimates, and the advection correction is referred to as W20 in the following.

**Table 2.** Overview of turbulence retrieval methods and the applied filters and methods

	E89	S17A	S17	W20
TKE	yes	yes	yes	yes
arepsilon	no	yes	yes	yes
lidar volume averaging effect	no	no	yes	yes
CNR filter	yes	yes	yes	no
filter of bad estimates	no	no	no	yes
integral length scale filter	yes	yes	yes	yes
advection filter	no	no	yes	no
advection correction	no	no	no	yes
variance modifications	yes	yes	yes	yes

#### 3.2.4 Quality control filters

In order to fulfill the assumptions that are made with regards to the turbulence model and the turbulence retrieval method, the data is filtered according to the criteria given in Smalikho and Banakh (2017):

$$20 \quad l\Delta y \ll L_v \quad , \tag{32}$$

$$L_v > \max\{\Delta z, \Delta y\} \tag{33}$$

$$R'\omega_s \gg |\langle \mathbf{V} \rangle|$$
 (34)

For the purpose of evaluating the methods in a broad range, we set mild criteria for Eq. 32 and 34 using

$$l\Delta y < 2L_v$$
 and (35)

$$25 R'\omega_s > 2|\langle \mathbf{V} \rangle| . (36)$$

Equations 32 and 33 are criteria that require the integral length scale  $L_v$  to be larger than the sensing volume of the lidar in transversal  $(\Delta y)$  and longitudinal  $(\Delta z)$  direction. Unfortunately, there is no independent measurement of  $L_v$  at all heights of the VAD scan, so that it is derived from the lidar measurement itself as  $L_v = 0.3796 \frac{E^{3/2}}{\varepsilon}$  (Smalikho and Banakh, 2017).

The filter criteria in Eq. 34 is a filter for conditions with significant advection which distorts the measured structure functions and is only applied if the method described in Sect.3.2.3 is not used.

Except for the retrieval method W20, which uses the filtering of bad estimates, we set fixed CNR filter thresholds adapted to the lidar type. Since the turbulence retrievals are very sensitive to bad estimates, we set the CNR thresholds to conservative values that are given in Tab. 1.

An overview of all retrieval methods and their characteristics and filters that are applied is given in Tab. 2.

#### 5 3.3 Turbulence estimation from airborne data

The estimation of turbulence parameters from the wind measurement system on the DLR Cessna Grand Caravan 208B (Mallaun et al., 2015) is done very similarly to the in-situ estimations from the sonic anemometer. TKE is calculated from the sum of variances as described in Sect. 3.3. Dissipation rate is also calculated from the second order structure function, but with different bounds for the time lag. For the flight data we use  $\tau_1 = 0.2$  s and  $\tau_2 = 2$  s, corresponding to approximately 13-130 m lag at 65 m s<sup>-1</sup> mean airspeed.

To evaluate the heterogeneity of turbulence due to changing land use along the flight legs of more than 50 km length, we divided the legs into sub-legs of 6.5 km (i.e. 100 s averaging time) and calculate turbulence for each leg individually. The location of the legs and the sublegs is shown in Fig. 2.

#### 4 Validation

#### 4.1 Comparison to sonic anemometer

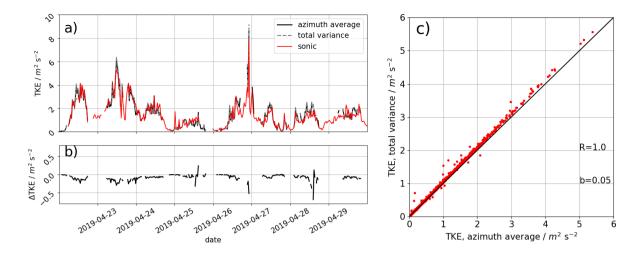
0 Best possible validation of the methods introduced in Sect. 3 can be performed with the lidar in close proximity to the meteorological mast such as at the measurement site at MOL-RAO. The sonic anemometers at 50 m and 90 m on the mast almost coincide with measurement levels of the lidar at 52 m and 93.6 m respectively. Since the VAD-retrieval with elevation angle of 35.3° yields TKE as well as its dissipation rate, both turbulence parameters can be compared to values obtained from the sonic anemometers. In this section we will evaluate the methods described in Sect. 3.2 and in particular the validity of the assumptions made in Sect. 3.2.1 and the efficiency of the advection correction described in Sect. 3.2.3.

#### 4.1.1 Validation of modified variance

In Sect. 3.2.1 we introduced two modifications on the calculation of the averaged lidar radial velocity variances. These changes are especially necessary if a low number of VAD scans is used for turbulence retrieval. In the MOL-RAO experiment, VAD scans are run continuously with  $\varphi=35.3^\circ$ , so that the modifications can be tested against the original version of the retrieval method. The sonic anemometer at 90 m of the meteorological mast serves as an independent validation measurement. Figure 5a shows a time series of the two methods and the sonic anemometer in a time period in which all systems were providing good data almost without interruption (22 April - 29 April 2019). The lidar retrieval with both variance methods follows the sonic anemometer TKE estimation very well through the diurnal cycles, with some occasional overestimation that will be discussed in Sect. 4.1.2. Figure 5b gives the difference ( $\Delta$ TKE) between azimuth average and total average to show that it is typically below 0.5 m<sup>2</sup>s<sup>-2</sup> except for some periods with strong gradients in TKE. Figure 5c shows the scatterplot which directly compares the S17 retrieval calculated with azimuth averaged variances to the S17 retrieval using total variances. There is a higher estimation of TKE in the total variance method which increases with TKE. We cannot fully explain this effect at this point, but it might be due to the small scale turbulence that cannot be resolved with the 72 s sampling rate of radial velocities at individual azimuth angles. It is small enough to be neglected for further analysis.

#### 30 4.1.2 Comparison of lidar retrievals

The MOL-RAO dataset allows us to compare the retrievals without consideration of lidar volume averaging (E89 and S17A) to the S17 retrieval and its modified version W20 introduced in this study. For this purpose, the individual retrieval results are compared to the sonic anemometer estimates of TKE and its dissipation rate  $\varepsilon$ . Figure 6 shows the scatter plots for TKE at the two measurement levels. For each method, the coefficient of determination  $R_c^2$  of the linear regression between sonic measurement and lidar retrieval is given, as well as a bias which is calculated as  $b = \overline{(y-x)}$  for TKE and  $b_{\log} = \overline{(\log_{10} y - \log_{10} x)}$  for  $\varepsilon$ . We find that with the E89-method, TKE is systematically underestimated, as expected. In contrast to that, the S17-method yields slightly overestimated TKE-values, if no advection filter is applied (light red dots), but a good agreement with the sonic anemometer in the absence of advection (red dots). The overestimation of TKE is larger for the lower level at 50 m compared

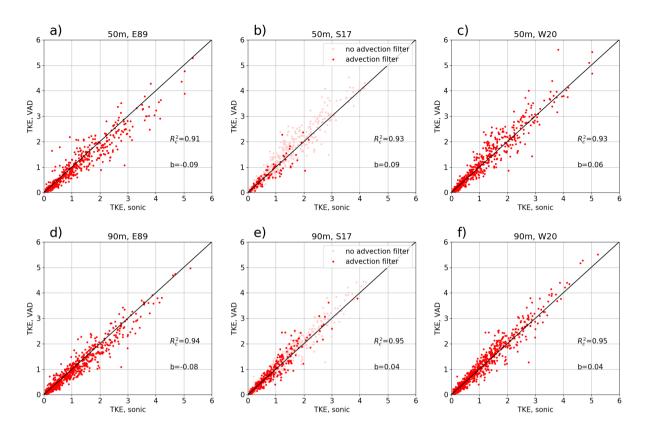


**Figure 5.** Time series of TKE from lidar retrievals compared to a sonic anemometer at 90 m above ground level (a), the difference between the lidar retrieval with averaged variances (Eq. 20) at specific azimuth angles  $\theta$  to the modified, total variance method (Eq. 21) (b) and the scatterplot for the whole experimental period (c).

to the 90-m level which we attribute to the smaller averaging volume  $\Delta y$ . Our refined version of the retrieval, including the advection correction improves the results slightly and especially for the high turbulence cases (corresponding to high wind speeds) at the 50-m level, as the scatterplots show. Figure 7 gives the scatterplot comparison of  $\varepsilon$ -retrieval from S17A, S17 and W20 with the sonic anemometer respectively. E89 does not provide an estimate for  $\varepsilon$ . Even more clearly than for TKE, the underestimation of the method without consideration of lidar volume averaging (S17A) is found. Also, a now positive bias of  $b = 0.09 \ m^2 \ s^{-2}$  of lidar estimates with the S17-method at the 50-m level is reduced with the advection correction to  $b = 0.06 \ m^2 \ s^{-2}$ . It is evident from the  $\varepsilon$ -estimates that all lidar retrievals underestimate turbulence significantly compared to the sonic anemometer in the low turbulence regimes, and in particular for values smaller than  $2 \cdot 10^{-3} \ m^2 \ s^{-3}$ , which is why these values have been excluded for the estimation of biases (grey dots).

#### 4.1.3 Evaluation of advection error

To evaluate the error that is caused by advection in the S17-retrieval, all data that was collected at MOL-RAO was binned into wind speeds with a bin-width of 1 m s<sup>-1</sup>. The mean absolute error between the lidar retrievals and the sonic anemometers at the respective level is calculated and shown in Figure 8 for TKE and  $\varepsilon$ . Although the averaged errors of TKE are small in general, it shows that the W20-method does reduce the error in comparison to the S17 method at the 50-m level. The error for  $\varepsilon$  at the 50-m level increases with wind speed, but less for the W20-method. Hardly any improvement is found for the already small errors of TKE and  $\varepsilon$  at 90 m.



**Figure 6.** Scatter plot of lidar TKE retrieval against sonic anemometer TKE at 50-m level (a-c) and 90-m level (d-f). E89-retrieval is shown in (a) and (d), S17-retrieval in (b) and (e) and W20-retrieval in (c) and (f). The light red dots in (b) and (e) show all TKE estimates without filter for advection, the dark red dots have the advection filter applied.

#### 4.2 Comparison of elevation angles

VAD-scans with 35.3° allow to retrieve TKE as well as momentum fluxes using the methods described in Sect. 3. The disadvantage compared to VAD scans with larger elevation angles is that at the same range of the lidar line-of-sight measurement, lower altitudes are reached. If the limit of range is not given by the ABL height in any case, this can lead to significantly lower data availability at the ABL top. Another advantage of greater elevation angles is that the horizontal area that is covered with the VAD and thus the footprint of the measurement is much smaller than with low elevation angles. From the theory derived in Sect. 3.3, we see that the dissipation rate retrieval does not depend on the elevation angle and can thus be obtained from VAD scans with 75° elevation angle as well if the assumptions of isotropy and homogeneity hold. However, since the VAD at 75° has the more narrow cone, the separation distances  $\Delta y$  at respective measurement heights are smaller and thus the sensitivity to advection errors is expected to be larger. The measurements with two different elevation angles at the CoMet-campaign allow to compare dissipation rate retrievals for both kinds of VAD scans with the restriction that they are not simultaneous, but

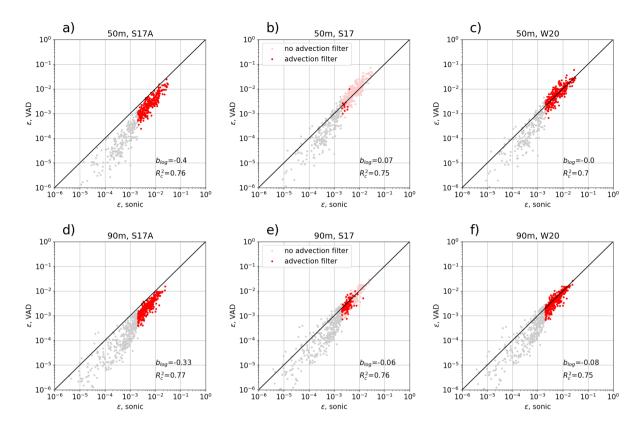


Figure 7. Scatter plot of lidar dissipation rate retrieval against sonic anemometer dissipation rate. The light red dots in (b) and (e) show the results without advection filter. The light grey dots are all estimates below  $2 \cdot 10^{-3}$  m<sup>2</sup>s<sup>-3</sup>. Grey dots are not used for calculation of R nd  $b_{\log}$ .

#### sequential.

Figure 9 shows the comparison of both types of VADs in scatter plots of three measurement heights for the whole campaign period and DWL#1. In general, a large scatter is found between the two types of VAD which can be attributed to the different measurement times, different footprint and heterogeneous terrain. Applying a filter for significant advection as described in Sect. 3.2.4 removes most of the measurement points at the 100 m level in the 75° VAD. Without the filter (grey and red points), large, systematic overestimation against the VAD at 35.3° is found, which can still be seen at 500 m, but is not found at 1000 m any more. With the advection correction of W20, the systematic error is reduced, but the random errors remain.

As for the comparison with the sonic anemometer, we evaluate the error in dependency of wind speed by binning the data in wind speeds between  $0 \,\mathrm{m\,s^{-1}}$  and  $10 \,\mathrm{m\,s^{-1}}$  (see Fig. 10). A clear trend is found for the 100 m-level which can be significantly reduced with the W20 method. A very small difference between the two elevation angles at the 500-m level is only reduced very little in the W20 method.

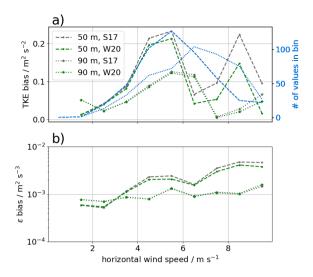


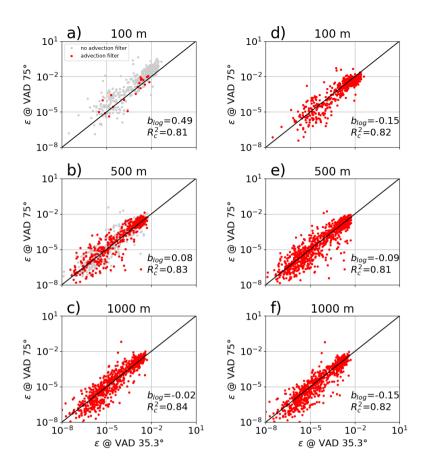
Figure 8. Difference of lidar retrieval of TKE (a) and TKE dissipation rate (b) compared to sonic anemometer as a function of wind speed.

#### 4.3 Comparison to D-FDLR

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At CoMet, no meteorological tower with sonic anemometers on levels that could be compared to the Doppler lidars was available. Instead, the aircraft D-FDLR was operating with a turbulence probe and provided in-situ turbulence data. On 5 June 2018, the aircraft was flying a so-called 'wall'-pattern, with long, straight and level legs at five altitudes (800 m, 1000 m, 1100 m, 1300 m and 1600 m). At least the lowest three levels of this flight allow a comparison to measurement levels of the top levels of lidar measurements on this day. Figure 11 shows the measured TKE of D-FDLR in the five flight levels. Only at the lowest two light levels (i.e. 800 m and 1000 m), significant turbulence is measured, with strong variations along the flight path.

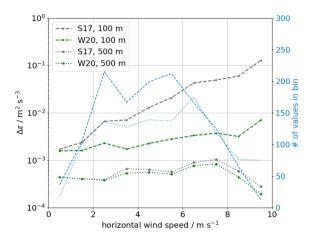
Figure 12 shows the measurements from D-FDLR and the lidars DWL#1 and DWL#3 that were taken between 1400 and 1530 UTC as vertical profiles. The solid red line gives the average of all sub-legs along the 50 km flight of D-FDLR, and the shaded areas give the range between the minimum and the maximum at each height. It shows nicely how the measurements of turbulence at the DWL#3-site are significantly lower than at DWL#1, which we attribute to the lake fetch. The D-FDLR measurements of TKE almost match with the DWL#1 site and are all higher than at the DWL#3-site, which fits to the environmental conditions of heterogeneous land-use. Figure 12a also gives the comparison between E89-, S17- and W20-estimates of the same dataset. Here, it shows that the difference between S17 and W20 only occurs at the very lowest level, but the underestimation of the E89-method is found up to 750 m. In dissipation rate estimates, the DWL#1 measurements are at the low end of the range that was measured with D-FDLR and the lake-site measurements are even smaller. The estimates from  $35.3^{\circ}$ -scans and  $75^{\circ}$ -scans agree very well, especially at the higher levels, which shows that the assumption of isotropy and homogeneity seem to hold. The presumed underestimation of  $\varepsilon$  of lidar retrievals compared to in-situ measurements at absolute



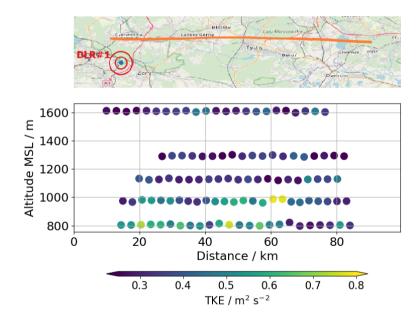
**Figure 9.** Scatter plot of lidar dissipation rate retrieval from VAD scans with 75° elevation angle versus 35.3°. On the left, retrievals without advection correction are shown for the three different levels (a) 100m, (b) 500m and (c) 1000m. On the right the corresponding scatter plots with advection correction are presented (d-f).

values of  $10^{-3}$  m<sup>2</sup> s<sup>-3</sup> is consistent to what was found for the comparison to sonic anemometer measurements. This single case of airborne measurements compared to lidar retrievals at higher altitudes can however not provide any statistical validation.

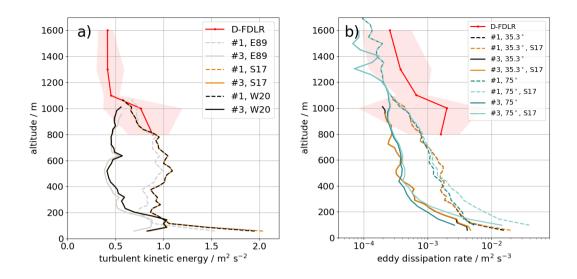
Figure 13 shows measurements of  $\varepsilon$  retrieved with the W20-method for the VAD scans with 75° elevation and all three lidars. It shows that the growth of the boundary-layer with its increased turbulence can be nicely captured by the lidars. There are some differences between the three locations, especially lower turbulence close to the ground at the DWL#3-location and a higher boundary layer at the DWL#2 location. More studies will be necessary in future, analyzing the data of the whole campaign to improve the understanding of land-atmosphere interaction in this case.



**Figure 10.** Difference of lidar  $\varepsilon$ -retrievals of both kinds of VAD as a function of wind speed.



**Figure 11.** D-FDLR TKE measurements at five flight levels. Map data ©OpenStreetMap contributors 2019. Distributed under a Creative Commons BY-SA License.



**Figure 12.** Vertical profile of TKE (left) and  $\varepsilon$  (right) compared to measurements by D-FDLR.

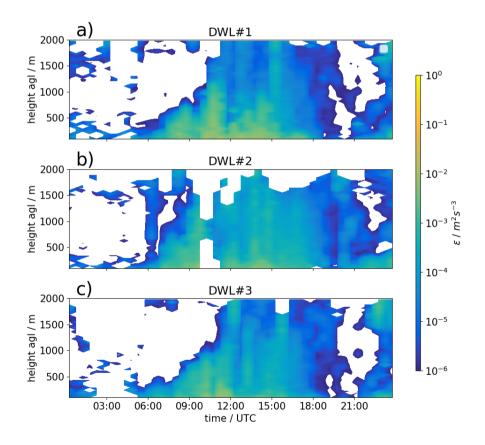


Figure 13. Diurnal cycle of TKE dissipation rate on 5 June 2018 at the three lidar locations calculated with the W20-method.

#### 5 Conclusions

In this study, we used four different methods to retrieve turbulence parameters from the same data obtained through lidar VAD scans. The MOL-RAO experiment allowed us to investigate and validate the methods with a database of 30 days containing a broad variety of atmospheric conditions, with wind speeds ranging from  $0..12 \text{ m s}^{-1}$  and TKE from  $0..5 \text{ m}^2\text{s}^{-2}$ . This goes beyond short-term studies of only few days and specific atmospheric conditions that had been investigated by Smalikho and Banakh (2017). Furthermore, two sonic anemometers allowed to investigate the dependence of the retrieval on the measurement height. The experimentshows that methods which do not account for the lidar volume averaging effect underestimate turbulence TKE and its dissipation rate compared to sonic anemometers at 50 m and 90 msystematically. This has been shown for the first time with such a big dataset. The S17-method tackles handles this problem, but introduces an overestimation in our dataset. Parts of this overestimation can be attributed to advection, which distorts the retrieval of the azimuth structure function and the transverse filter function in the lidar model. The advection effects are relevant at the lowest measurement heights where the spatial separation of lidar beams along the VAD cone  $\Delta y$  is small. This effect is stronger than increasing wind speeds at higher altitudes in our observations. We propose a correction for this issue and show here that our method reduces the systematic errors compared to the sonic anemometers at the 50-m level. To confirm that advection is the reason for this improvement we show that the bias increases with wind speed. With all retrievals, dissipation rates of values smaller than  $10^{-3}~\mathrm{m^2\,s^{-3}}$  are underestimated by the lidars, likely because the small scale fluctuations that are carrying much of the energy in these cases, cannot be resolved any more. A remaining piece of uncertainty are the lidar parameters  $\Delta p$  and  $T_w$ which are given by the manufacturer for the lidar type, but could potentially differ for individual lidars. Exact knowledge about these parameters could reduce the uncertainty of the model functions F and A (see App. B) and thus improve the corrections of the volume averaging effects. It is conceivable that the observed overestimation of the S17 (and W20) based TKE can partly also be attributed to these uncertainties.

The aircraft measurements that were carried out during the CoMet campaign were used to show the agreement of the lidar retrievals with in-situ measurements at higher altitudes. It is the first time that these lidar measurements have been compared to in-situ aircraft data. Unfortunately, only measurements of one day allowed a comparison and the spatial separation of the measurements introduces additional uncertainty. It was found that TKE estimates from lidar and aircraft compare rather well, but the small values of dissipation rates at these heights are underestimated by the lidar to a similar order of magnitude as for low turbulence conditions in the sonic anemometer comparison. Dedicated experiments will be necessary in future to provide more comprehensive validation datasets for turbulence retrievals with lidar VAD scans. Given the larger separation distances  $\Delta y$  of the lidar beams at higher altitudes, the assumption that  $l\Delta y \ll L_v$  is more likely to be violated. Airborne in-situ measurements are the best way to validate the assumptions and the lidar retrievals in these cases.

The CoMet dataset was also used to show that with VAD-scans with larger elevation angle (here:  $75^{\circ}$ ) can be used to retrieve TKE dissipation rate with the same method as for VAD-scans with  $35.3^{\circ}$  and the results are comparable. For this narrow VAD cone scans, we showed that the advection correction is much more important than for lower elevation angles and strong overestimation of  $\varepsilon$  can occur in conditions with high wind speeds if it is not applied. The distribution of three lidars in Upper

Silesia in areas of different land-use shows the variability of turbulence and boundary-layer flow in this area. Using the VAD scans with different elevation angle have recently been used to describe anisotropy of turbulence in a stable boundary-layer (Banakh and Smalikho, 2019) and can in future potentially help to analyze horizontal heterogeneity in the boundary layer and its impact on the calculation of area-averaged fluxes.

Data availability. The data are available from the author upon request.

#### Appendix A: Fourier decomposition

Eberhard et al. (1989) show that radial velocity variance can be decomposed into the components u, v and w of the meteorological wind vector:

$$\langle v_r^2(R,\theta,\varphi)\rangle = \langle [V_r(R,\theta,\varphi,t) - \langle V_r(R,\theta,\varphi)\rangle]^2 \rangle$$

$$= \frac{\cos^2 \varphi}{2} \left[ \langle u^2 \rangle + \langle v^2 \rangle + 2\tan^2 \varphi \langle w^2 \rangle \right]$$

$$+ \sin 2\varphi \langle uw \rangle - \sin 2\varphi \langle vw \rangle \sin \theta$$

$$+ \frac{\cos^2 \varphi}{2} \left[ \langle u^2 \rangle + \langle v^2 \rangle \right] \cos 2\theta - \cos^2 \varphi \langle uv \rangle \sin 2\theta$$
(A1)

A partial decomposition of Eq. A1 yields:

$$5 \langle u^2 \rangle + \langle v^2 \rangle + 2 \tan^2 \varphi \langle w^2 \rangle = \frac{1}{\pi \cos^2 \varphi} \int_0^{2\pi} \langle v_r^2 \rangle d\theta$$

$$= \frac{2}{\cos^2 \varphi} \langle \langle v_r^2 \rangle \rangle_{\theta}$$
(A2)

$$\langle uw \rangle = \frac{1}{\pi \sin^2 \varphi} \int_0^{2\pi} \langle v_r^2 \rangle \cos \theta d\theta \tag{A3}$$

$$\langle vw\rangle = \frac{-1}{\pi \sin^2 \varphi} \int_0^{2\pi} \langle v_r^2 \rangle \sin \theta d\theta \quad . \tag{A4}$$

These equations provide the basis for the retrieval of TKE and momentum fluxes from lidar VAD measurements.

#### 10 Appendix B: Lidar filter functions

Theoretical models for the spectral broadening of lidar measurements  $(F(\Delta y))$  and the structure function  $(A(l\Delta y))$  are derived in Banakh and Smalikho (2013) from the two-dimensional Kolmogorov spectrum for lidar measurements of turbulence:

$$\Theta(\kappa_z, \kappa_y) = C_3(\kappa_z^2 + \kappa_y^2)^{-4/3} \left[ 1 + \frac{8}{3} \cdot \frac{\kappa_y^2}{\kappa_z^2 + \kappa_y^2} \right]$$
(B1)

$$F(\Delta y) = \int_{0}^{\infty} d\kappa_z \int_{0}^{\infty} d\kappa_y \Theta(\kappa_z, \kappa_y) \left[ 1 - H_{\parallel}(\kappa_z) H_{\perp}(\kappa_y) \right]$$
 (B2)

$$A(l\Delta y) = 2\int_{0}^{\infty} d\kappa_z \int_{0}^{\infty} d\kappa_y \Theta(\kappa_z, \kappa_y) H_{\parallel}(\kappa_z) H_{\perp}(\kappa_y) \left[1 - \cos(2\pi l \Delta y_i \kappa_y)\right] \quad , \tag{B3}$$

where  $H_{\parallel}$  is the longitudinal and  $H_{\perp}$  the transverse filter function of lidar measurements in the VAD scan:

$$H_{\parallel}(\kappa_1) = \left[ \exp\left[ -(\pi \Delta p \kappa_1)^2 \right] \frac{\sin(\pi \Delta R \kappa_1)}{\pi \Delta R \kappa_1} \right]^2 \tag{B4}$$

$$H_{\perp}(\kappa_2) = \left[\frac{\sin(\pi \Delta y \kappa_2)}{\pi \Delta y \kappa_2}\right]^2 \quad , \tag{B5}$$

where  $\Delta p$  is derived from the FWHM pulse width  $\tau_p$ ,  $\Delta R$  from the time window  $T_w$  and  $\Delta y$  from the VAD azimuth increment  $\Delta \theta$ :

$$\Delta p = 0.5c \left( \frac{\tau_p}{2\sqrt{\log 2}} \right) \tag{B6}$$

$$\Delta R = 0.5cT_w \tag{B7}$$

$$\Delta y = R\Delta\theta\cos\varphi \tag{B8}$$

(B9)

## Appendix C: Sum of variance of subsamples

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For statistically independent subsamples  $X_i$  with size  $k_i$ , the total variance of the dataset can be derived as follows:

$$E_j = E[X_j] = \frac{1}{k_j} \sum_{i=1}^{k_j} X_{ji}$$
 (C1)

$$V_j = \text{Var}[X_j] = \frac{1}{k_j - 1} \sum_{i=1}^{k_j} (X_{ji} - E_j)^2 \quad , \tag{C2}$$

10 where i is the index of the subsample and i the index of the element in the subsample.

$$Var[X] = \frac{1}{n-1} \sum_{j=1}^{g} \sum_{i=1}^{k_j} (X_{ji} - E[X])^2$$
(C3)

$$= \frac{1}{n-1} \sum_{i=1}^{g} \sum_{i=1}^{k_j} ((X_{ji} - E_j) - (E[X] - E_j))^2$$
(C4)

$$= \frac{1}{n-1} \sum_{i=1}^{g} \sum_{i=1}^{k_j} (X_{ji} - E_j)^2 - 2(X_{ji} - E_j)(\mathbb{E}[X] - E_j) + (\mathbb{E}[X] - E_j)^2$$
 (C5)

$$= \frac{1}{n-1} \sum_{j=1}^{g} (k_j - 1) V_j + k_j (\mathbf{E}[X] - E_j)^2 \quad , \tag{C6}$$

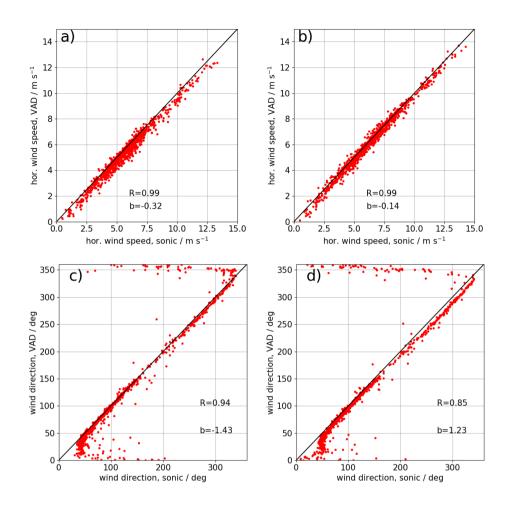
where  $n = \sum k_j$ . Eventually, for equally sized subsamples one obtains:

$$Var[X] = \frac{1}{n-1} \sum_{j=1}^{g} (k-1)V_j + k(g-1)Var[E_j]$$
(C7)

$$= \frac{k-1}{n-1} \sum_{j=1}^{g} V_j + \frac{k(g-1)}{k-1} \text{Var}[E_j]$$
 (C8)

#### Appendix D: Validation of wind retrieval

The FSWF-retrieval (Smalikho, 2003) is used to obtain the three-dimensional wind vector from the lidar VAD scans. The results of the retrieval is compared to the sonic anemometers at 50 m and 90 m and shown in Fig. D1. To show the distortion of the mast, no data have been removed in the retrieval of wind speed and wind direction for this figure.



**Figure D1.** Scatter plot of horizontal wind speed retrieved from lidar measurements compared to sonic anemometer measurements at 50 m (a) and 90 m (b) and wind direction (c and d).

# **Appendix E: Nomenclature**

пррепаіх	2. Nomenciature
$\lambda$	laser wavelength
$ au_p$	lidar pulse length (full width half maximum, FWHM)
$T_w$	lidar time window
$\varphi$	elevation angle
$\overset{\cdot}{ heta}$	azimuth angle
u	wind component towards East
v	wind component towards North
w	upward wind component
$\sigma_u^2$	<i>u</i> -wind component variance
$\sigma_u^2 \ \sigma_v^2 \ \sigma_w^2$	v-wind component variance
$\sigma_w^2$	w-wind component variance
$ au_i$	time separation
$V_r$	radial wind component
$v_r$	radial wind component difference from mean
$\sigma_r^2$	radial wind component variance
$\stackrel{'}{R}$	range gate distance
$E_{ m TKE}$	turbulence kinetic energy
arepsilon	TKE dissipation rate
$C_K$	Kolmogorov constant
$\psi$	azimuth angle increment
$\kappa$	wave number
r	separation distance
$\sigma_L^2$	variance of lidar measurements
$egin{array}{c} \sigma_L^2 \ \sigma_e^2 \ \sigma_a^2 \ \sigma_t^2 \end{array}$	lidar instrumental noise
$\sigma_a^2$	variance of lidar measurements without instrumental noise
$\sigma_t^2$	turbulent broadening of the Doppler spectrum
$\Delta R$	distance between neighboring range gate centers
$D_r$	azimuth structure function
$D_s$	longitudinal structure function measured by sonic anemometer
$D_L$	lidar measurement of azimuth structure function
$D_a$	$D_L - 2\sigma_e^2$
A	theoretical model for azimuth structure function
F	theoretical model for turbulent broadening of the Doppler spectrum
$\Delta y$	distance of lidar beam movement during one accumulation period
$\Delta y_c$	modified $\Delta y$ for advection
$p_M$	model PDF
P	probability of bad estimates
$L_v$	integral length scale
$\omega_s$	angular velocity of VAD scan
$\Psi$	wind direction
U	horizontal wind speed
$\Delta t$	accumulation time 28
$R_c$	linear regression correlation coefficient
h	mangurament hing

b measurement bias

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