Differential absorption lidar for water vapor isotopologues in the 1.98 μm spectral region: sensitivity analysis with respect to regional atmospheric variability

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Abstract. Laser active remote sensing of tropospheric water vapor is a promising technology to complement passive observational means in order to enhance our understanding of processes governing the global hydrological cycle. In such context, we investigate the potential of monitoring both water vapor $H_2^{16}O$ and its isotopologue $HD^{16}O$ using a differential absorption lidar (DIAL) allowing for ground-based remote measurements at high spatio-temporal resolution (150 m and 10 min) in the lower troposphere. This paper presents a sensitivity analysis and an error budget for a DIAL system under development which will operate in the two-micrometer spectral region. Using a performance simulator, the sensitivity of the DIAL-retrieved mixing ratios to instrument-specific and environmental parameters is investigated. This numerical study uses different atmospheric conditions ranging from tropical to polar latitudes with realistic aerosol loads. Our simulations show that the measurement of the main isotopologue $H_2^{16}O$ is possible over the first 1.5 km of atmosphere with a relative precision in the water vapor mixing ratio of <1% in a mid-latitude or tropical environment. For the measurement of $HD^{16}O$ mixing ratios under the same conditions, relative precision is found to be slightly lower, but still sufficient for the retrieval of range-resolved isotopic ratios with precisions in δD of a few per mil. We also show that expected precisions vary by an order of magnitude between tropical and polar conditions, the latter giving rise to poorer sensitivity due to low water vapor content and low aerosol load. Such values have been obtained for a commercial InGaAs PIN photodiode, as well as temporal and line-of-sight resolutions of 10 min and 150 m, respectively. Additionally, using vertical isotopologue profiles derived from a previous field campaign, precision estimates for the $HD^{16}O$ isotopic abundance are provided for that specific case.

1 Introduction

35 In many important aspects, climate and weather depend on the distribution of water vapor in the atmosphere. Water vapor leads to the largest climate change feedback, as it more than doubles the surface warming from atmospheric carbon dioxide (Stevens et al., 2009). Knowing exactly how water vapor is distributed in the vertical is of paramount importance for understanding the lower-tropospheric circulation, deep convection, the distribution of radiative heating, surface fluxes magnitude and patterns, among other processes. Conventional radio-sounding or passive remote sensors, such as microwave

40 radiometers or infrared spectrometers, are well established tools used for water vapor profile retrieval in the atmosphere. However, apart from balloon-borne soundings, most of these instruments do not allow for determining how water vapor is distributed along the vertical in the 0–3 km above the surface which contains 80% of the water vapor amount of the atmosphere. Additionally, passive remote sensors will generally require ancillary measurements such as aerosols, temperature, or cloud heights to limit the errors on retrieved concentrations from radiance measurements. To complement these methods, active

45 remote sensing techniques are expected to provide higher resolution measurement capabilities especially in the vertical direction where the different layers of the atmosphere are directly probed with a laser. Among these active remote sensing techniques, Raman lidar is a powerful way to probe the atmosphere as it can give access to several atmospheric state parameters within a single line of sight such as temperature, aerosols, and water vapor mixing ratio (WVMR) (Whiteman et al., 1992). Benefiting from widely commercially available high-energy visible or UV lasers, as well as highly sensitive detectors, they

50 allow high accuracy, long range measurements despite the small Raman scattering cross-section. WVMR retrieval from Raman Lidar signal is however typically limited by parasitic daytime sky radiance and requires instrument constant and overlap function calibration (Whiteman et al., 1992; Wandiger and Raman, 2005). Conversely, the differential absorption lidar (DIAL) technique is in principle calibration free since the targeted molecule mixing ratio can be directly retrieved from the attenuation of the lidar signals at two different wavelengths, knowing the specific differential absorption cross-section of the targeted

55 molecule (Bösenberg, 2005). However, this benefit must be balanced with higher instrumental constraints especially on the laser source which is required to provide high power as well as high frequency agility and stability at the same time. For water vapor this method has been successfully demonstrated essentially using pulsed laser sources emitting in the visible or near infrared (Bruneau et al., 2001; Wirth et al., 2009; Wagner and Plusquellic, 2018), and recent progress in the fabrication and integration of tapered semiconductor optical amplifiers has enabled the development of small-footprint field-deployable

60 instrumentation (Spuler et al., 2015). The infrared region between 1.5 µm and 2.0 µm has also attracted interest for water vapor DIAL sounding, especially in the context of co-located methane and carbon dioxide monitoring (Wagner and Plusquellic, 2018, Cadiou et al., 2016). One of the potential benefits of co-located multiple species measurement would be to reduce the uncertainties related to the retrieval of dry-air volume mixing ratios for the greenhouse gas (GHG) of interest. This aspect has particularly been studied in the field of space-borne integrated path differential absorption (IPDA) lidar for carbon dioxide

65 (CO_2) monitoring in the 2.05 µm region where water vapor absorption lines may affect the measurement (Refaat et al., 2015). One of the great potentials of these multiple-wavelengths and multiple-species approaches would be their adaptability to

isotopologue measurements with the DIAL technique since isotopic ratio estimation is equivalent to multiple species measurement provided the targeted isotopologues display similarly suitable and well separated absorption lines in a sufficiently narrow spectral window.

70

Humidity observations alone are not sufficient for identifying the variety of processes accounting for the proportions and history of tropospheric air masses (Galewsky et al., 2016). Stable water isotopologues, mainly $H_2^{16}O$, $HD^{16}O$ and $H_2^{18}O$ differ by their mass and molecular symmetry. As a result, during water phase transitions, they have slightly different behaviors. The heavier molecules prefer to stay in the liquid or solid phase while the lighter ones tend to evaporate more easily, or prefer to stay in the vapor phase. This unique characteristic makes water isotopologues the ideal tracers for processes in the global hydrological cycle. Water isotopologues are independent quantities depending on many climate factors, such as vapor source, atmospheric circulation, precipitation and droplet evaporation, and ambient temperature. So far, no lidar system has been investigated for the measurement of water vapor isotopologues other than $H_2^{16}O$ (hereafter referred to as H_2O). Here, in the framework of the Water Vapor Isotope Lidar (WaVIL) project (Wavil, 2021), we investigate the possibility of a transportable differential absorption lidar to measure the concentration of both water vapor H_2O and the isotopologue $HD^{16}O$ (hereafter referred to as HDO) at high spatio-temporal resolution in the lower troposphere (Hamperl et al., 2020). The proposed lidar will operate in the two-micrometer spectral region where water vapor isotopologues display close but distinct absorption lines. Such an innovative remote sensing instrument would allow for the first time the monitoring of water vapor and HDO isotopic abundance profiles with a single setup, enabling the improvement of knowledge on the water cycle at scales relevant for meteorological and climate studies.

The purpose of this paper is to assess the expected performances of a DIAL instrument for probing of H_2O and HDO in the lower troposphere. In section 2, the choice of the sensing spectral range is substantiated, and the performance model is outlined. The approach for modelling transmitter, detection, and environmental parameters is detailed. The sensitivity analysis is based on representative average columns of arctic, mid-latitude, and tropic environments. The simulation results and an extensive error analysis are presented in section 3. To assess the random uncertainty in the retrieved isotopologue mixing ratio, major detection noise contributions are analyzed for a commercial InGaAs PIN and a state-of-the-art HgCdTe avalanche photodiode. Instrument- and atmosphere-specific systematic errors are discussed for different model environments. Finally, performance calculations were applied to vertical profiles retrieved from a past experimental campaign where a Raman lidar for water vapor measurements along with in-situ sensors for the HDO isotopologue measurements were deployed. A conclusion and perspectives for forthcoming calibration and validation field campaigns are given in section 4.

2 DIAL method and performance model for water vapor isotopologue measurement

2.1 Choice of the sensing spectral range

Remote sensing by DIAL relies on the alternate emission of at least two closely spaced laser wavelengths, one coinciding with an absorption line of the molecule of interest (λ_{on}) and the other tuned to the wing of the absorption line (λ_{off}), to retrieve a given species concentration. The key to independently measure HDO and H_2O abundances with a single instrument lies thus in the proper selection of a spectral region where: *i)* the two molecules display well separated, significant absorption lines while minimizing the interference from other atmospheric species, and *ii)* the selected lines should preserve relatively equal lidar signal dynamic and relative precision ranges for both isotopologues. This makes the line selection rather limited. Using spectroscopic data from the HITRAN 2016 database (Gordon et al., 2017), we investigated the possibilities for HDO sounding up to 4 µm, where robust pulsed nanosecond lasers or optical parametric oscillator sources based on mature lasers or nonlinear crystals components can be developed (Godard, 2007). Figure 1a shows that HDO lines are strong in the 2.7 µm region but overlap with an even more dominant H_2O absorption band. Considering the state of possible commercial photodetector technologies, we chose to limit the range of investigation to 2.6 µm, corresponding to the possibilities offered by InGaAs photodiodes. In the telecom wavelength range, which offers both mature laser sources and photodetectors, HDO absorption lines are too weak to be exploited for DIAL measurements over 1–3 km. The same argumentation holds for wavelengths towards 2.05 µm (see Fig. 1b) which have been extensively studied for space-borne CO_2 IPDA lidar sensing (Singh et al., 2017; Ehret et al., 2008). However, the 2 µm region seems to offer an interesting possibility in terms of absorption strength as well as technical feasibility of pulsed, high-energy, single-frequency laser sources (Geng et al., 2014). The spectral window between 1982–1985 nm is well suited to meet the mentioned requirements as illustrated in Fig. 1c. In this paper we will focus on the $H_2^{16}O$ line at 5043.0475 cm^{-1} (1982.93 nm) and the HD^{16}O lines at 5044.2277 cm^{-1} (1982.47 nm) and 5040.4937 cm^{-1} (1983.93 nm), respectively hereafter referred to as HDO options (1) and (2), allowing for a sufficiently high absorption over several kilometers with negligible interference from other gas species. Additionally, a second option for H_2O slightly detuned from the absorption peak at 1982.97 nm will be discussed as a possibility to reduce the temperature sensitivity of the DIAL measurement (hereafter referred to as H_2O option (2)). Wavelength switching will be realized on a shot-to-shot basis to consecutively address the chosen on-line wavelengths and the off-line wavelength at 1982.25 nm for H_2O (1/2) and HDO (1) or the off-line wavelength at 1983.72 nm for HDO (2). As shown in Fig. 1c, the HDO absorption line at 1982.47 nm is accompanied by a non-negligible H_2O absorption which has to be corrected for when retrieving the volume mixing ratio and thus adding a bias dependent on the accuracy of the H_2O measurement at 1982.93 nm. Furthermore, the interfering H_2O line has a ground-state energy of 2756 cm^{-1} (see Table 1) which makes it highly temperature sensitive. Probing HDO at 1982.47 nm thus requires highly accurate knowledge of the H_2O and temperature profile through auxiliary measurements (lidar, radio sounding). The alternative second option for HDO at 1983.93 nm avoids any H_2O interference, however with slightly weaker absorption optical depth it gives rise to smaller signal-to-noise ratios and consequently increased measurement statistical uncertainty.

Table 1: Spectroscopic parameters for selected absorption lines

	ν	λ	S	E''	γ_{air}	n_{air}
$H_2^{16}O$ (1)	5043.0476	1982.928	2.17×10^{-24}	920.21	0.0367	0.49
$HD^{16}O$ (1)	5044.2277	1982.464	1.17×10^{-24}	91.33	0.1036	0.71
$HD^{16}O$ (2)	5040.4937	1983.933	9.38×10^{-25}	116.46	0.1003	0.71
$H_2^{16}O$ at $HD^{16}O$ (1)	5044.2300	1982.463	2.29×10^{-25}	2756.42	0.0456	0.37

ν (cm^{-1}): wavenumber; λ (nm): vacuum wavelength; S (cm^{-1}/molecule cm^{-2}): line intensity at 296 K; E'' (cm^{-1}): lower-state energy;
γ_{air} (cm^{-1} atm^{-1}): air-broadened Lorentzian half-width at half-maximum (HWHM) at 1 atm and 296 K; n_{air}: temperature exponent for γ_{ai}
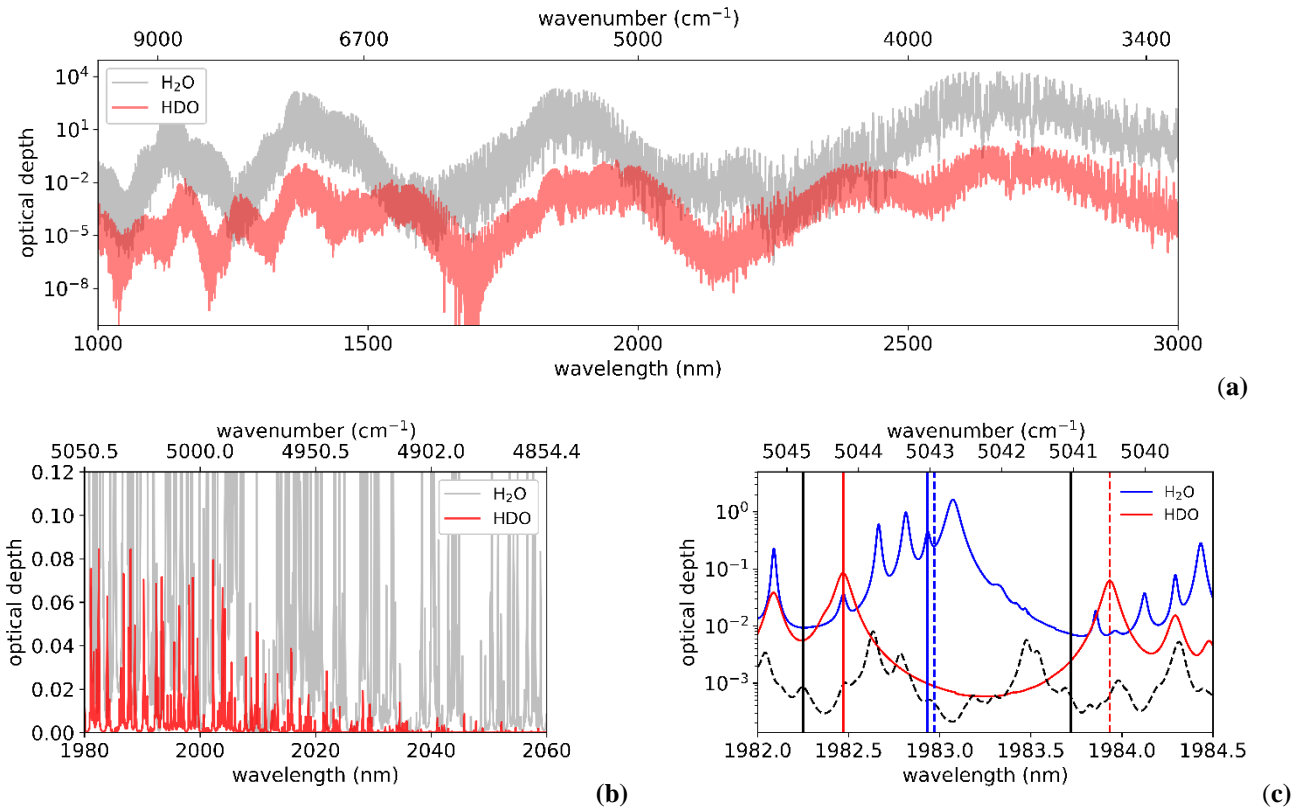
Figure 1: Optical depth over 1 km for $H_2^{16}O$ (H_2O) and $HD^{16}O$ (HDO) with uniform volume mixing ratios of 8400 ppmv and 2.6 ppmv, respectively (relative humidity of 50% at 15°C). (a) Spectral overview between 1 µm and 3 µm; (b) Close-up window for wavelengths around 2 µm with decreasing HDO absorption towards 2.05 µm; (c) Spectral range of interest for simultaneous H_2O and HDO sounding. The dashed black line represents the total optical depth of other species (CO_2, CH_4, N_2O) with their typical atmospheric concentrations. Vertical black lines indicate the positions of possible off-line wavelengths. On-line wavelengths are indicated for H_2O (vertical blue line for option 1 at 1982.93 nm, dashed blue line for option 2 at 1982.97 nm) and HDO (vertical red line for option 1 at 1982.47 nm, dashed red line for option 2 at 1983.93 nm). Spectra calculations are based on the HITRAN 2016 database assuming a temperature of 15°C and an atmospheric pressure of 1013.25 hPa.

In any of the proposed cases, addressing the on-line and off-line spectral features requires a tuning capability larger than 0.5 nm which can be offered, for instance, by an optical parametric oscillator source (Cadiou et al., 2016; Barrientos Barria et al., 2014), which is envisioned to be used for the WaVIL system. It should be noted that the chosen absorption lines do not fulfil the criterion of temperature insensitivity as outlined by Browell et al. which imposes the strict knowledge of the temperature profile along the lidar line of sight from auxiliary measurements for an accurate isotopologue retrieval.

2.2 DIAL performance model

The objective of the presented performance model is to elaborate the precision achievable with the proposed DIAL instrument of the volume mixing ratios of the water isotopologues H_2O and HDO and thus of the precision on the measurement of HDO abundance (noted δD) which expresses the excess (or defect) of the deuterated isotope compared to a reference value of $311.5 \cdot 10^{-6}$ (one HDO molecule for 3115 H_2O molecules) (Craig, 1961). Following the convention, the HDO abundance (in permil, ‰) is expressed as the deviation from that of the standard mean ocean water (SMOW) in the so-called notation:

$$\delta D = 1000 \times \left[\frac{[HDO]_{\text{sample}} / [H_2O]_{\text{sample}}}{[HDO]_{\text{SMOW}} / [H_2O]_{\text{SMOW}}} - 1 \right] \tag{1}$$

where [ ] represents the concentration of H_2O and HDO.

As schematically depicted in Fig. 2, the DIAL simulator consists of three sub-models describing atmospheric properties, lidar instrument parameters, and detector properties. Each model will be explained in a more details in the following paragraphs. The atmosphere model is based on a set of standard profiles of temperature, pressure, and humidity representative of different climate regions along with aerosol optical depth data of the AERONET database. Those data are exploited to calculate the atmospheric transmission using absorption cross-sections computed with the HITRAN2016 spectroscopic database (Gordon et al., 2017). Together with the model describing the lidar instrument, the calculated transmission data are used to feed the lidar equation in order to calculate the received power at each selected on-line and off-line wavelength. In a subsequent step, noise contributions arising from the detection unit are taken into account to estimate the signal-to-noise ratio. Then, we use an analytical approach based on an error propagation calculation to estimate the random error on the measured isotopic mixing ratios and thus the uncertainty of the δD retrieval obtained with the simulated instrumental parameters.

Starting from the lidar equation (Collis and Russell, 1976), the calculated received power as a function of distance r writes as:

$$P_r(r) = T_r \frac{A}{r^2} \beta_\pi(r) \, O(r) \, \frac{c}{2} \, T_{\text{atm}}^2(r) \, E_p \tag{2}$$

where T_r is the receiver transmission (assumed value of 0.5 for all calculations), A is the effective area of the receiving telescope, $\beta_\pi(r)$ is the backscatter coefficient, $O(r)$ is the overlap function between the laser beam and the field of view of the receiving telescope, c is the speed of light, $T_{\text{atm}}(r)$ is the one-way atmospheric transmission and E_p the laser pulse energy. The

DIAL technique is based on the emission of two wavelengths, one at or close to the peak of an absorption line (λ_{on}) and another tuned to the absorption line's wing (λ_{off}).
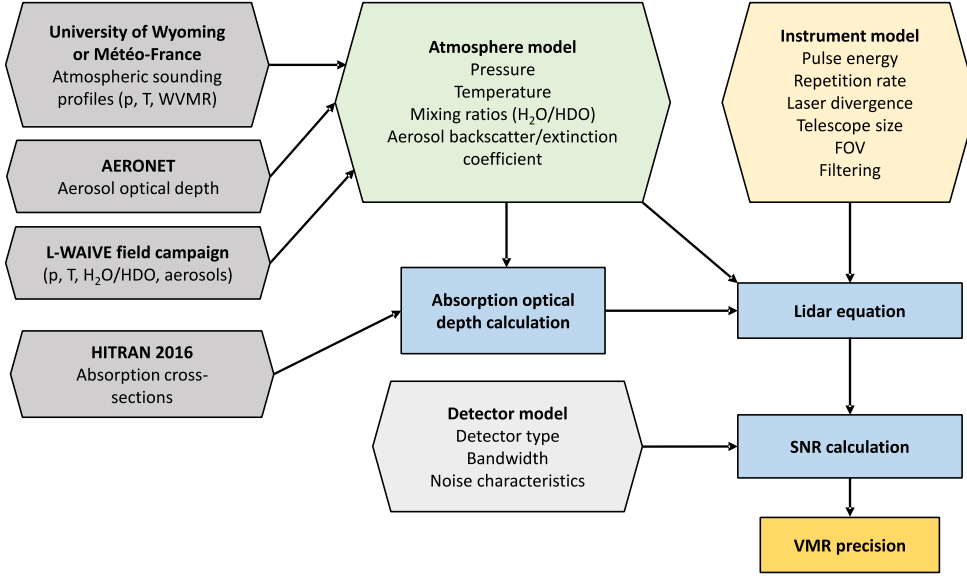
Figure 2: Block diagram of the DIAL simulator. Input models and databases in hexagons, principal calculations indicated by rectangles. p: pressure, T: temperature, WVMR: water vapor mixing ratio, FOV: telescope field of view. The signal-to-noise ratio (SNR) is used to calculate the statistical random error (precision) of the volume mixing ratio (VMR) of H₂O/HDO.

Provided that the two laser pulses are emitted sufficiently close in wavelength and in time for the atmospheric aerosol content to be equivalent, they experience the same backscattering along the line of sight, and the differential optical depth $\Delta\tau$ as the difference of on- and off-line optical depth at a measurement range r can be retrieved by:

$$\Delta\tau(r) \; = \; \frac{1}{2}\ln\left(\frac{P_{\text{off}}(r)}{P_{\text{on}}(r)}\right) \tag{3}$$

with P_{on} and P_{off} as the backscattered power signals for λ_{on} and λ_{off}, respectively. Using the optical depth measurement, the gas concentration can be retrieved at a remote range r within a range cell $\Delta r = r_2 - r_1$. Assuming Δr is sufficiently small, the water vapor content expressed as volume mixing ratio, which is assumed as constant within Δr, can then be derived by:

$$X_{\text{H2O}}(r_1 \to r_2) \; = \; \frac{\Delta\tau(r_2) - \Delta\tau(r_1)}{\int_{r_1}^{r_2} WF(r)\,dr} \tag{4}$$

with *WF(r)* representing a weighting function defined as:

$$WF(r) \; = \; \left(\sigma_{\text{on}}(r) - \sigma_{\text{off}}(r)\right)\rho_{\text{air}}(r) \tag{5}$$

where ρ_{air} is the total air number density and σ_{on} and σ_{off} are the on-line and off-line absorption cross-sections calculated with the HITRAN 2016 spectroscopic database assuming a Voigt profile representation of the form:

$$\sigma(v) = \sigma_0 \frac{y}{\pi} \int_{-\infty}^{\infty} \frac{\exp(-t^2)}{y^2 + (x - t)^2} dt \tag{6}$$

with

$$\sigma_0 = \frac{S}{\gamma_D} \left(\frac{\ln 2}{\pi}\right)^{1/2}$$

$$y = \frac{\gamma}{\gamma_D} (\ln 2)^{1/2}$$

$$x = \frac{v - v_0}{\gamma_D} (\ln 2)^{1/2}$$

where S is the line strength, γ_D is the Doppler width, γ is the pressure broadened linewidth, and v_0 is the line center position.

190 The temperature T dependence of the line strength is determined by the energy of the lower molecular state E'' according to:

$$S = S_0 \left(\frac{T_0}{T}\right)^{3/2} \exp\left[\frac{E''hc}{k}\left(\frac{1}{T_0} - \frac{1}{T}\right)\right] \tag{7}$$

where T_0 is the reference temperature, k is the Boltzmann constant, and c is the speed of light.

Equation (3) is valid for the detection of the main isotopologue H_2O. For HDO however, the presence of H_2O absorption at the on-line wavelength of HDO (see Fig. 1c) necessitates an additional consideration of that bias for the inversion. Taking this into account, Eq. (3) changes to:

195 $$\Delta\tau_{HDO}(r) = \frac{1}{2}\ln\left(\frac{P_{off}(r)}{P_{on}(r)}\right) - \Delta\tau_{H2O}(r) \tag{8}$$

where $\Delta\tau_{H2O}$ represents the H_2O differential optical depth at the HDO on-line wavelength λ_{HDO} which can be calculated with the knowledge of the volume mixing ratio X_{H2O} measured at λ_{H2O}.

To obtain an analytical expression for the random error in the concentration measurement, an error propagation calculation can be applied to Eqs. (3) and (4) assuming that the range cell interval Δr is sufficiently small and that the range cell resolution of the receiver is sufficiently high to consider $\Delta\tau(r_1)$ and $\Delta\tau(r_2)$ as uncorrelated. The absolute uncertainty in the volume mixing

200 ratio X expressed as standard deviation $\sigma(X)$ can be calculated from the signal-to-noise ratios of the on- and off-line power signals as follows:

$$\sigma(X) = \frac{\Delta f}{\sqrt{2} \, WF \, c}\left(\frac{1}{SNR_{on}^2} + \frac{1}{SNR_{off}^2}\right)^{1/2} \tag{9}$$

where Δf is the measurement bandwidth which is the same for the on- and off-line pulses since they are measured sequentially

205 by the same detector. Finally, with both uncertainties in the volume mixing ratios X_{H2O} and X_{HDO} known, an estimation of the uncertainty in δD is obtained by applying an error propagation calculation to Eq. (1) in order to get the expected uncertainty expressed as variance:

$$\sigma(\delta D) \; = \; (\delta D + 1) \left\{ \left(\frac{\sigma(X_{\mathrm{H2O}})}{X_{\mathrm{H2O}}} \right)^2 + \left(\frac{\sigma(X_{\mathrm{HDO}})}{X_{\mathrm{HDO}}} \right)^2 \right\}^{1/2} \tag{10}$$

2.3 Instrument and detector model

210 In order to estimate the feasibility of a DIAL measurement, calculations were performed for the transmitter and receiver parameters summarized in Table 2. The emitter of the DIAL system will be based on a generic optical parametric oscillator/optical parametric amplifier (OPO/OPA) architecture as the one developed in (Barrientos Barria et al., 2014). The combination of a doubly-resonant Nested Cavity OPO (NesCOPO) and an OPA pumped by a 1064 nm Nd:YAG commercial laser with 150 Hz repetition rate allows for single-frequency, high-energy pulses with adequate tunability. From this system

215 we expect an extracted signal energy of up to 20 mJ at 1983 nm. For a more conservative estimate, we will also consider a lower-limit pulse energy of 10 mJ for our simulations. The receiver part consists of a Cassegrain-type telescope with a primary mirror of 40 cm in diameter. For the detection part, calculations were performed in a direct-detection setup for i) a commercial InGaAs PIN photodiode and ii) a HgCdTe avalanche photodiode (APD) specifically developed for DIAL applications in the 2 µm range, presented in (Gibert et al., 2018). The telescope field of view is determined by an aperture in the telescope's focal

220 plane. For better comparability, we assume the same aperture diameter of 1.2 mm for both the PIN photodiode and the APD. Given the small active area of the APD, imaging of the field of view on the detector might prove extremely challenging in practice however. The measurement bandwidth of the DIAL system is effectively determined by an electronic low-pass filter in the detection chain. In the simulation we use a bandwidth setting of 1 MHz corresponding to a spatial resolution of the retrieved isotopologue concentrations of 150 m. For all our calculations we assume signal averaging over an integration time

225 of 10 min (45 000 laser shots for on- and off-line wavelength).

Table 2: DIAL instrument parameters

Transmitter		Receiver	
		i)	ii)
Energy	10–20 mJ		
Pulse duration	10 ns	Telescope aperture	40 cm	40 cm
Repetition rate	150 Hz	Detector type	InGaAs PIN	HgCdTe APD
λ_{on} H$_2$^{16}O (1)	1982.93 nm	Detector diameter	300 µm	180 µm
λ_{on} H$_2$^{16}O (2)	1982.97 nm	Field of view (FOV)	630 µrad	630 µrad
λ_{on} HD^{16}O (1)	1982.47 nm	NEP	600 fW Hz$^{-1/2}$	75 fW Hz$^{-1/2}$
λ_{on} HD^{16}O (2)	1983.93 nm	Bandwidth	1 MHz	1 MHz
Divergence	270 µrad		Responsivity: 1.2 AW^{-1}	Quantum efficiency: 0.8
				Excess noise factor: 1.2

In order to quantify the measurement uncertainty in the retrieved isotope mixing ratios, random and systematic sources of

230 errors are taken into account. Random errors in measuring the differential optical depth, and thus the species mixing ratio, are related to different noise contributions arising from the detection setups. For a single return-signal pulse, the associated noise

power P_n consists of a constant detector and amplifier noise expressed as noise equivalent power NEP, shot noise due to background radiation P_{sky}, shot noise dependent on the pulse power $P(\lambda)$, as well as speckle noise $P_{sp}(\lambda)$:

$$P_n = \sqrt{\left(NEP^2 + 2 \cdot e \cdot \left[P_{sky} + P(\lambda)\right] \cdot F \ / \ R\right) \cdot \Delta f \ + \ P_{sp}^2(\lambda)} \tag{11}$$

235 where e is the elementary charge, F the excess noise factor (in case of the APD), R the detector responsivity (depending on quantum efficiency in case of the APD) and Δf the measurement bandwidth. The NEP of 600 fW Hz$^{-1/2}$ for configuration i) featuring the InGaAs PIN photodiode is a conservative estimate by calculations based on the specifications of the photodiode and amplifier manufacturer (G12182-003K InGaAs PIN photodiode from Hamamatsu combined with a gain adjustable DHPCA-100 current amplifier from FEMTO). The background power P_{sky} depends on the background irradiance S_{sky} and the

240 receiver geometry according to:

$$P_{sky} = \frac{\pi}{4} \cdot S_{sky} \cdot \Delta\lambda_f \cdot A_{eff} \cdot \theta_{FOV}^2 \tag{12}$$

where $\Delta\lambda_f$, A_{eff} and θ_{FOV} are the optical filter bandwidth, effective receiver telescope area and field of view angle, respectively. A constant background irradiance of 1 W/m^2/µm/sr and an optical filter bandwidth of 50 nm are used for all calculations. Assuming Gaussian beam characteristics, the speckle-related noise power is approximately given by (Ehret et al., 2008):

245 $$P_{sp} = P(\lambda) \cdot \frac{\lambda \cdot 2\sqrt{\Delta f \cdot \tau_c}}{\pi \cdot R_{tel} \cdot \theta_{FOV}} \tag{13}$$

where R_{tel} denotes the telescope radius and τ_c the coherence time of the laser pulse corresponding to the pulse duration for a Fourier-transform-limited pulse. Finally, the overall time-averaged signal-to-noise ratio is given as the ratio of received power from Eq. (2) and total noise power from Eq. (11) multiplied by the square root of the number of laser shots N:

$$SNR = \frac{P_r}{P_n}\sqrt{N} \tag{14}$$

250 **2.4 Atmosphere model**

We constructed different atmospheric models for mid-latitude, arctic, and tropical locations to study the sensitivity of the DIAL measurement to environmental factors. The atmosphere model consists of vertical profiles of pressure, temperature and humidity (see appendix for origin of sounding data) which serve as input to calculate altitude-dependent absorption cross-sections using the HITRAN 2016 spectroscopic database. For the sake of simplicity, HDO mixing ratios were obtained from

255 H_2O profiles simply by considering their natural abundance of 3.11 10^{-4}, i.e., variability in terms of the isotopic ratio δD is not assumed in our model. For each location, a baseline model was constructed by using the columns of pressure, temperature and volume mixing ratios averaged over the year of 2019. To reflect seasonal variations in our sensitivity analysis, we use profiles with the lowest and highest monthly averages of temperature and humidity (Fig. 3 a–c). To complement the atmospheric model, data of level 2 aerosol optical depth (AOD) from the AERONET database (https://aeronet.gsfc.nasa.gov/) were used.

260   AERONET sun photometer products are usually available for wavelengths between 340 nm and 1640 nm. For extrapolation to the 2 µm spectral region, we used the wavelength dependence of the AOD described by a power law of the form (Angström, 1929):

$$\frac{AOD(\lambda)}{AOD(\lambda_0)} = \left(\frac{\lambda}{\lambda_0}\right)^{-\alpha} \tag{15}$$

where $AOD(\lambda)$ is the optical depth at wavelength λ, $AOD(\lambda_0)$ is the optical depth at a reference wavelength, and α represents
265   the Angstrom exponent. The Angstrom exponent was obtained by fitting Eq. (15) to the available AOD data in the above-mentioned spectral range in order to extrapolate further to 1.98 µm. Histograms of the yearly distribution of the extrapolated AOD at 1.98 µm are shown in the right column of Fig. 3 (g–i). Median values of the AOD are used for the baseline model. The lowest (AOD_{10}) and highest (AOD_{90}) decile values serve as input for the sensitivity analysis to model conditions of low and high aerosol charge, respectively. As a next step, vertical profiles of aerosol extinction are constructed by making basic
270   assumptions about their shape and constraining their values by the extrapolated AOD. In our baseline model, the vertical distribution of aerosols is represented by an altitude-dependent Gaussian profile of the extinction coefficient with varying half-width depending on the location (Fig. 3 d–f). This type of profile roughly corresponds to the ESA Aerosol Reference Model of the Atmosphere (ARMA) (ARMA, 1999) which is plotted for each region normalized to the AOD_{90}-derived extinction profile maximum.

275   However, the distribution of tropospheric aerosols varies widely from region to region (Winker et al., 2013). To broadly reflect the different boundary layer characteristics for each environment, the extinction profile was adapted accordingly. In mid-latitude regions, vertical aerosol distributions vary widely due regional and seasonal factors (Chazette and Royer, 2017). The PBL height can range from a few hundred meters up to 3 km (Matthias et al., 2004; Chazette et al., 2017). Assuming that aerosols are mostly confined to the PBL and that the free-tropospheric contribution to aerosol extinction is weak, the half-
280   Gaussian-shaped baseline model used for the simulations gives rise to 85% of AOD within the first 1.5 km. Since high aerosol loads in the free troposphere due to long-range dust transport are not uncommon over Western Europe (Ansmann et al., 2003), a dust scenario profile constrained by the highest-decile AOD was also investigated. Dust aerosols are represented by a Gaussian profile above the PBL extending well up to a height of 5 km. For this case, aerosol extinction in the PBL below 1.5 km accounts for half of the total AOD, while dust in the free troposphere accounts for the other half. At high latitudes, the
285   boundary layer tends to be stable and extends from a few meters to a few hundred meters above ground. Our baseline Arctic extinction profile thus contains 95% of the AOD within the first 1.5 km since most aerosols are confined within the first kilometer of the troposphere as observed by space-born lidar during long-term studies of the global aerosol distribution (Di Pierro et al.,2013). The occurrence histogram in Fig. 3h shows very low values of AOD for most of the time in the available photometer products from February to September. The long-tailed wing of the asymmetric distribution towards higher values
290   can be explained by seasonally occurring episodes of arctic haze due to anthropogenic aerosols transported from mid-latitude regions (winter to spring) and boreal forest fire smoke during the summer season (Tomasi et al., 2015; Chazette et al., 2018).
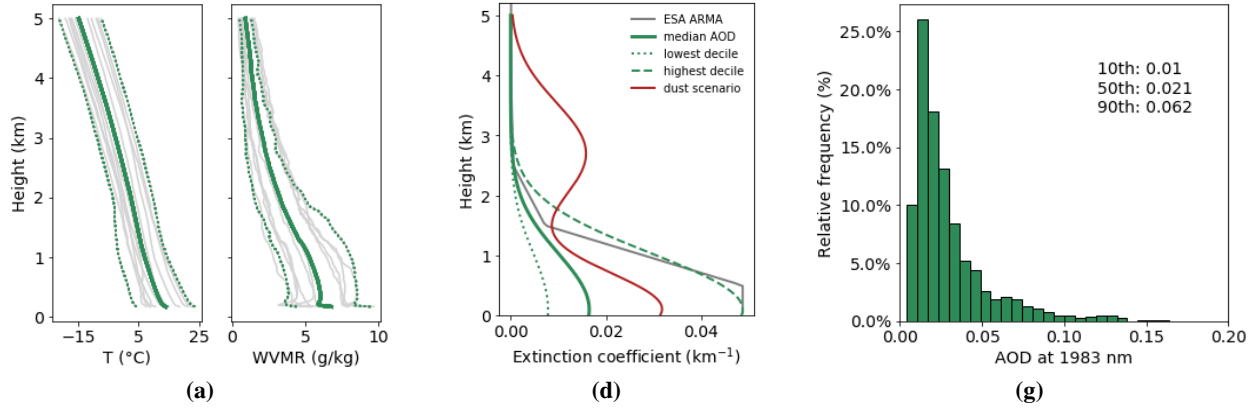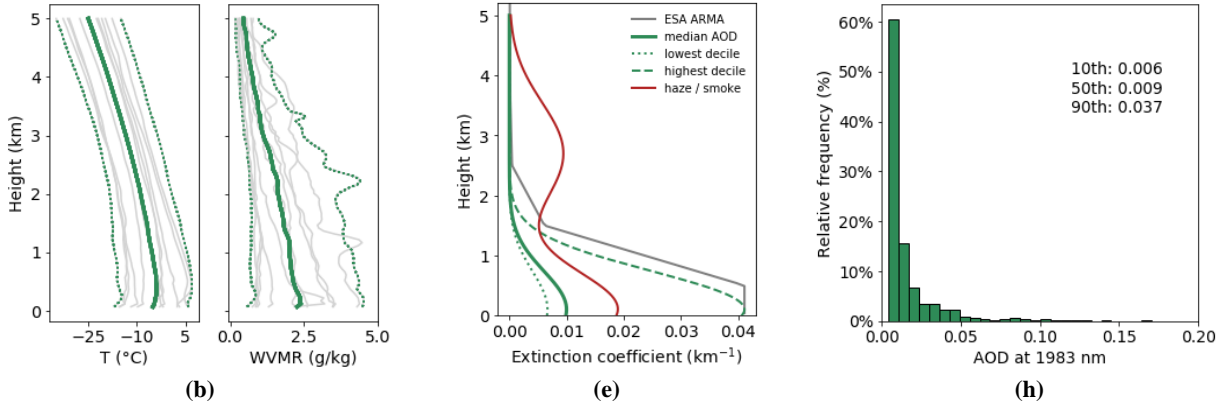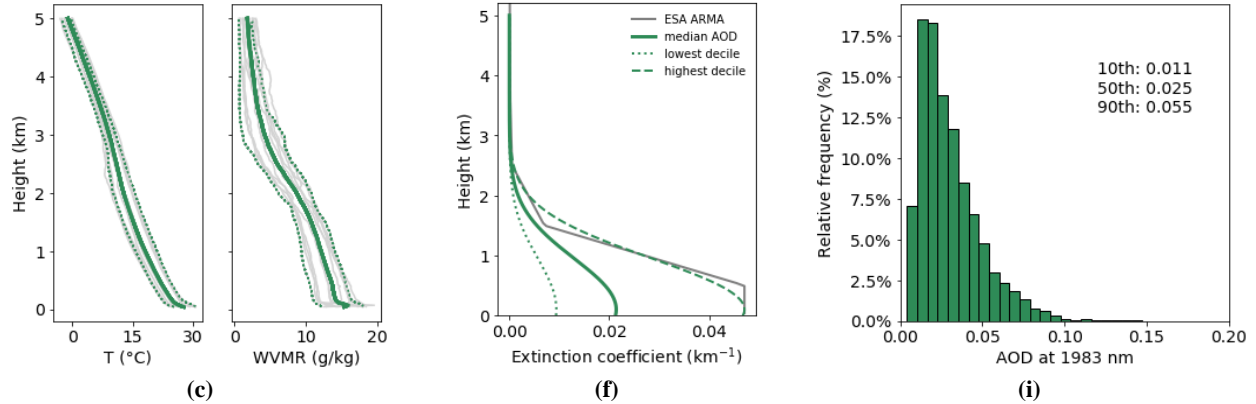
Figure 3: Atmosphere models: (a–c) Vertical sounding profiles of pressure, temperature, and water vapor mixing ratio (WVMR). Grey lines indicate monthly averages, solid green line is the yearly average of 2019 (baseline profile). Dotted lines indicate profiles of lowest and highest monthly temperatures and WVMR; (e–f) Model profiles of aerosol extinction coefficient; (g–h) Distribution of the aerosol optical depth at 1983 nm for AERONET level 2.0 data of 2019.

Similar to the dust scenario for the mid-latitude model, haze and smoke events are modelled by an additional Gaussian profile in the free troposphere constrained by the highest-decile AOD. Extinction profiles representing the tropical environment of La Réunion Island, where sea salt aerosols can be assumed to be the dominant aerosol species, are chosen such that 90% of the AOD is contributed to the first 1.5 km.

300   Vertical profiles of the aerosol backscatter coefficient were calculated assuming, for the sake of simplicity, a constant extinction-to-backscatter ratio (lidar ratio) of 40 sr throughout all sets of extinction profiles.

3 Simulation results and discussion

3.1 Instrument random error

This section aims to quantify the random error on the mixing ratio measurement depending on instrument settings such as laser
305   pulse energy and the type of detector employed. All calculations are based on the mid-latitude baseline atmosphere model assuming vertical sounding of the lower troposphere with aerosols confined to the lowest 2 km. Considering a simple calculation of random errors we will discuss their implications on the precision of the measurement of range-resolved δD profiles. Given the instrument parameters presented in Table 2, the dominant noise contributions are estimated which are shown for a single on-line pulse in Fig. 4 for both detector configurations.

310

(a)   (b)
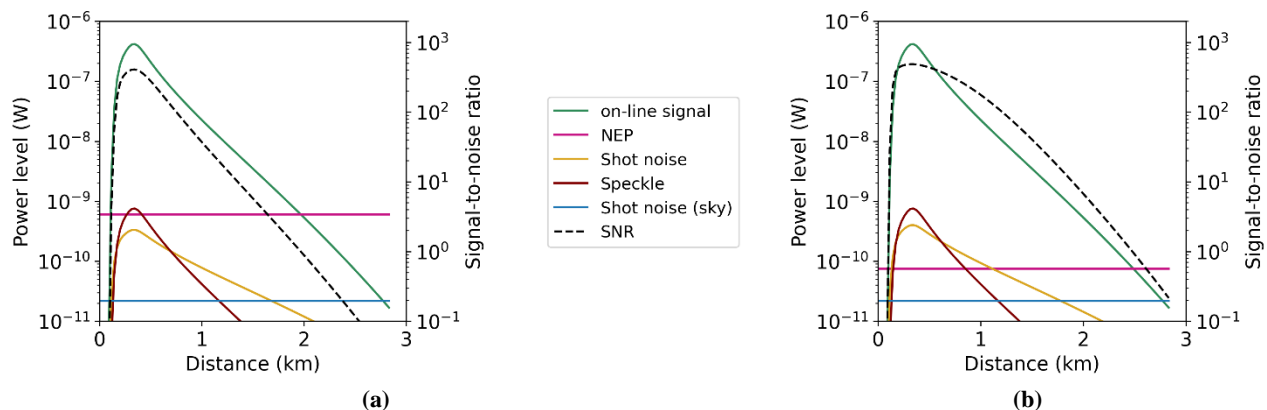
Figure 4: Received power according to Equation (2) (solid green line) and power-equivalent levels of major noise contributions related to the H₂O on-line signal for a single 20 mJ pulse and resulting signal-to-noise ratio (SNR, dashed black line, right vertical axis) as function of lidar range: (a) InGaAs PIN detector; (b) low-noise HgCdTe APD.

As expected, the electronic noise level is significantly reduced by roughly one order of magnitude for the HgCdTe APD
315   combined with a transimpedance amplifier due to a low combined NEP of 75 fW Hz$^{-1/2}$ compared to 600 fW Hz$^{-1/2}$ for the amplifier of the InGaAs PIN detector. In fact, shot noise and speckle are predominant for the APD for the first kilometer of range whereas the electronic noise of the transimpedance amplifier is the predominant contribution over the entire range for the commercial PIN detector. Signal-to-noise ratios up to 10^2 are obtained for a single measurement pulse within the first

kilometer. Integrating over 45 000 laser shots (equivalent to 10 min averaging time if on- and one off-line wavelengths are

320   addressed sequentially) would increase the signal-to-noise ratios to over 10^4 in the first kilometer for both detectors and to

values around 10^2 at a 2 km range for the commercial PIN detector and 10^3 for the HgCdTe APD.

The expected relative random errors on the mixing ratios of H_2O and HDO are shown separately for each detector in the upper

and lower panels of Fig. 5. We examined two scenarios with different laser pulse energies of 10 mJ and 20 mJ, a measurement

bandwidth of 1 MHz (150 m range cell resolution) and an integrating time of 10 minutes for a repetition rate (on-off rate) of

325   150 Hz. The simulation based on the 20 mJ configuration gives an estimation of the best-case precision limit of the DIAL

system. The second configuration with 10 mJ pulse energy can be understood as a lower limit on the precision of measuring

mixing ratios of H_2O and HDO, and finally δD.
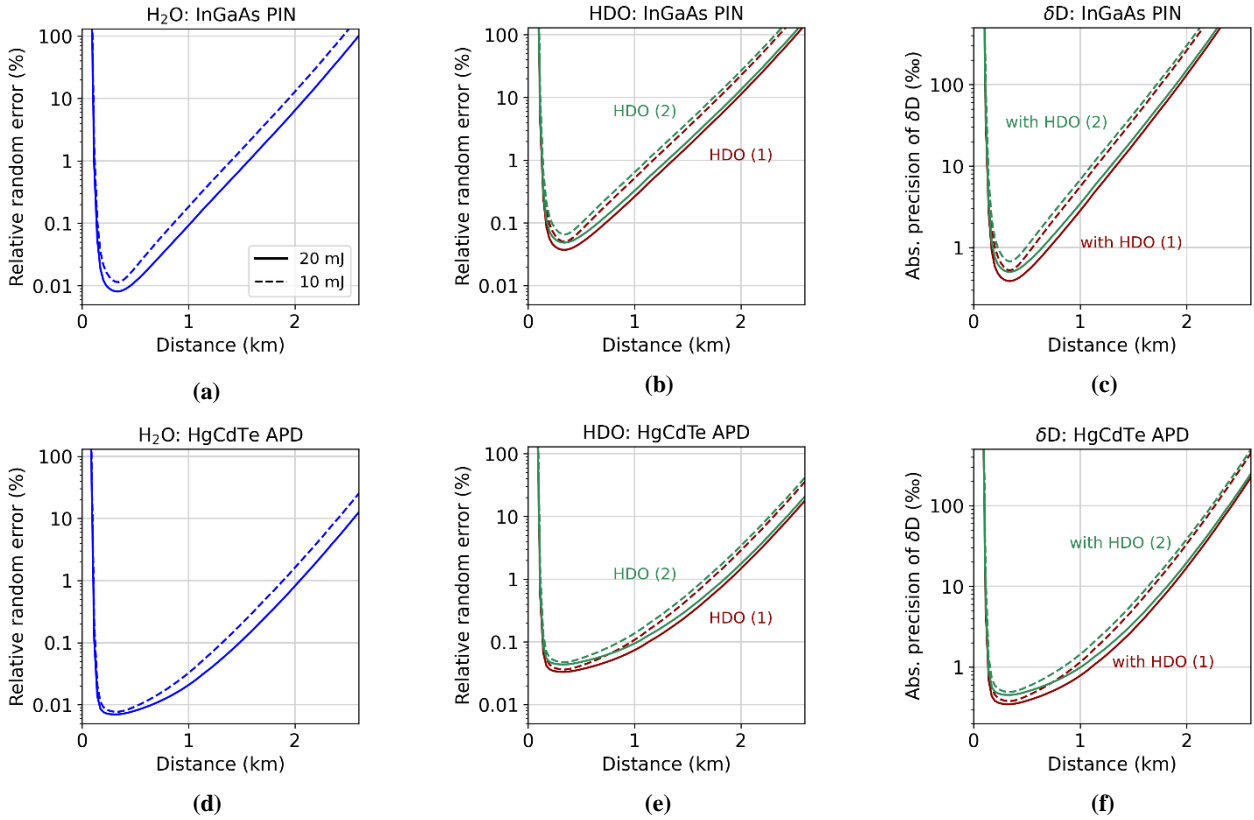
Figure 5: Expected relative random error on the volume mixing ratio of H_2O and HDO for different pulse energies (solid lines: 20 mJ, dashed lines: 10 mJ) and detectors: (a-c) InGaAs PIN detector; (d-e) HgCdTe APD; (c/f) Corresponding absolute uncertainty

330   (standard deviation) on δD as a function of distance from the lidar instrument. A detection bandwidth of 1 MHz is assumed and signal averaging time is 10 min.

As shown in Fig. 5, a relative random error of well under 1% on the mixing ratio of both H_2O and HDO can be achieved within

the first kilometer for both detectors and 20 mJ pulse energy. The degraded precision for measuring HDO is due to its lower

differential absorption compared to H_2O. The slight difference in optical depth for the two HDO options leads only to a small

335   loss in precision for wavelength option 2. For the low-noise APD shown in the bottom panel of Fig. 5, the simulations show

that even for the conservative assumption of 10 mJ pulse energy, the relative error stays below 1% for both H_2O and HDO over a range of 1.5 km corresponding to typical heights of the planetary boundary layer. H_2O uncertainties were calculated for sounding at the peak of the absorption line (option 1). The simulation results also reveal a sharp rise in the random uncertainty towards longer distances which is attributed to the drastic decline of aerosol backscatter in the free troposphere in our model.

340 The sharp fall of the random error within the first 200–300 m is due to the increasing overlap between laser beam and telescope field of view imaged onto the detector described by the overlap function $O(r)$ in Eq. (2). This overlap term is zero right in front of the lidar instrument and reaches unity after around 450 m for the here described configuration. It should be noted that for the range zone of non-uniform overlap, slight differences between the on- and off-line overlap, for example due to laser beam pointing, can induce significant systematic errors. From a practical point of view, the expected lowest instrument range is thus

345 closer to 0.5 km than the distance suggested by the location of the random error minima around 250 m.

Figures 5c and 5f show the expected precision in δD which depends on the relative random errors of the volume mixing ratios for H_2O and HDO (see Eq. (9)). For the commercial InGaAs PIN photodiode we find for the best-case configuration (20 mJ pulse energy, 1 MHz bandwidth) that the absolute value of uncertainty in δD is below 3‰ within a range of 1 km. The 10 mJ configuration also allows for measurement of δD, however with deteriorated absolute precision up to 10‰ within the first

350 kilometer. For greater ranges, the precision levels decline rapidly and are not sufficient to resolve variations of δD in the order of a few tens of permil. The use of a HgCdTe APD detector can overcome this limitation where calculations indicate that an absolute precision level better than 10‰ within a range of close to 2 km can be achievable with 20 mJ laser energy.

3.2 Sensitivity to atmospheric variability

355 The sensitivity of the DIAL instrument to the variability in temperature, humidity, and aerosol load was investigated for the mid-latitude, arctic and tropical atmosphere models. In the following analysis, the relative random error (precision) is used to compare the influence of each atmospheric parameter under investigation. Simulation results are summarized in Fig. 6 for targeting H_2O at 1982.93 nm (blue) and HDO at 1983.93 nm (red). Here again, we consider a measurement bandwidth of 1 MHz (150 m range cell resolution), and an integrating time of 10 minutes for a repetition rate of 150 Hz. All calculations

360 have been performed with the InGaAs PIN detector and assuming a laser pulse energy of 20 mJ.

Starting with temperature, no effect on the measurement random error was found when simulating under conditions of lower and higher temperature compared to the average atmospheric columns. Comparing the three baseline models of mid-latitude, tropical and arctic environments, the performance simulations find that highest precision measurements can be achieved under tropical conditions due to high humidity levels and favourable aerosol backscattering. Relative random errors lower than 0.1%

365 for H_2O are achievable within the first kilometer. The precision for H_2O degrades faster than for HDO with increasing range due to strong absorption leading to low return signals. On the contrary, random uncertainties for the arctic environment are almost one order of magnitude higher due to rather dry conditions in terms of WVMR and low aerosol content observed at the Eastern Greenland AERONET station of Ittoqqortoormiit. A high sensitivity to seasonal variability of the humidity profile was

observed for the arctic model, whereas variations of humidity in the tropics throughout the year are small and thus only slightly

370   affect the expected measurement precision. The simulations also clearly show the influence of aerosols on the performance of DIAL measurements. For all three locations, the precision gain between the low-charge (lowest-decile AOD) and high-charge (highest-decile AOD) aerosol model is roughly one order of magnitude. The presence of free-tropospheric aerosols, for example due to long-range dust transport in the mid-latitudes and arctic haze or boreal forest fire smoke in the Arctic, leads to significant improvements in the precision at altitudes beyond the atmospheric boundary layer.

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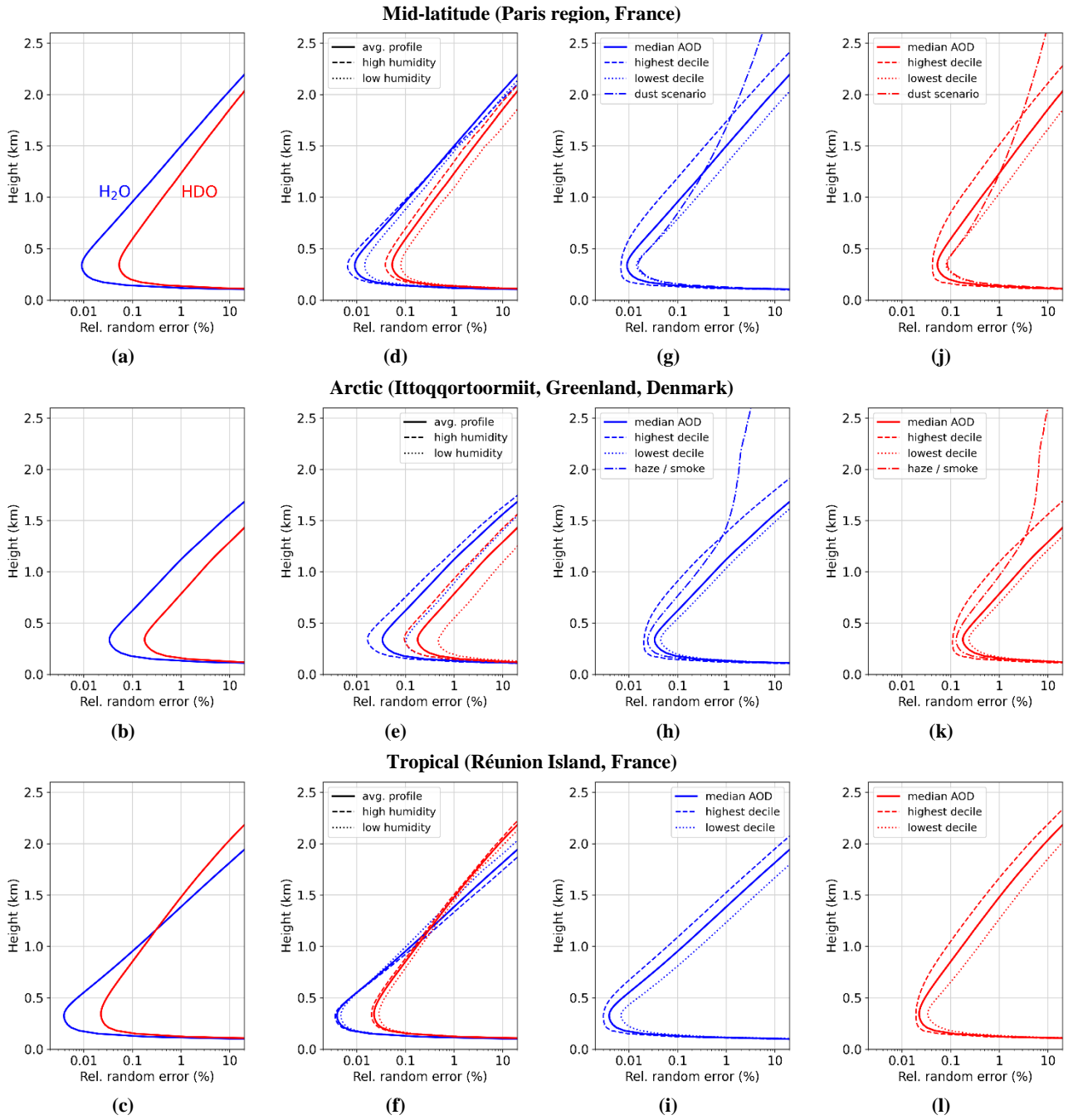
Figure 6: Sensitivity with respect to variability of atmospheric parameters: resulting statistical uncertainty for range-resolved DIAL measurement of H$_2$O (blue, option 1 at 1982.93 nm) and HDO (red, option 2 at 1983.93 nm). Simulation parameters: 20 mJ pulse energy, 1 MHz bandwidth, 10 min integration time, InGaAs PIN detector. (a–c) Reference model based on average columns of pressure, temperature, and humidity. Aerosol baseline profile using median AOD assumed; (d–f) Sensitivity to water vapor variability; (g–i) Sensitivity to different aerosol profiles (H$_2$O); (j–l) Sensitivity to different aerosol profiles (HDO).

3.3 Systematic errors

Systematic errors are associated with an uncertainty in the knowledge of atmospheric, spectroscopic, and instrument-related parameters when obtaining the VMR from the measured differential optical depth according to Eq. (4). Expressed in a general form, errors were estimated by calculating the VMR retrieval sensitivity to a deviation δY from a reference parameter Y:

$$\varepsilon_s = \max\left\{\frac{|X(Y) - X(Y \pm \delta Y)|}{X(Y)}\right\} \tag{16}$$

For the case of atmospheric systematic errors, the reference parameter Y used for the VMR retrieval stands for either the vertical pressure or temperature profile of the baseline atmospheric model. The systematic error due to an uncertainty in the knowledge of the temperature profile was calculated for temperature deviations δT from the reference profile ranging from ± 0.5 K to ± 2 K. This range of accuracy can be obtained by in situ sensors or an additional lidar instrument for the temperature profile which is necessary to calculate the temperature-dependent absorption cross sections for the concentration retrieval. As shown in Fig. 7, this kind of error can lead to a significant contribution to the error budget. The analysis shows that sounding H_2O at the absorption peak is especially sensitive to temperature uncertainties and that a measurement with the on-line wavelength shifted off the absorption peak (H_2O option 2) significantly reduces this bias. Table 3 gives an overview of the calculated biases comparing the three different atmospheric models. Note the significant temperature bias for HDO option 1 in regions with high water vapor content due to the highly temperature sensitive H_2O interference line. Similarly, a pressure deviation δp ranging from 0.5 hPa to 2 hPa was used to estimate the error due to an uncertainty in the pressure profile. In this case, H_2O wavelength option 2 is more sensitive to such an uncertainty. The resulting bias on the measurement of HDO is found to be negligible. Note the difference between the two options for probing H_2O. Shifting the online wavelength off the absorption peak (option 2) results in a noticeable reduction in the temperature error. However, this comes at the expense of increased pressure error and lower signal-to-noise ratio and thus increased random error for unchanged laser energy, integration time, and bandwidth. Considering the mentioned systematic error contributions, option 2 for H_2O proves to be the preferred wavelength choice with the intention of reducing the systematic error, especially if the temperature profile along the line of sight is not known with accuracy better than ± 0.5 K.
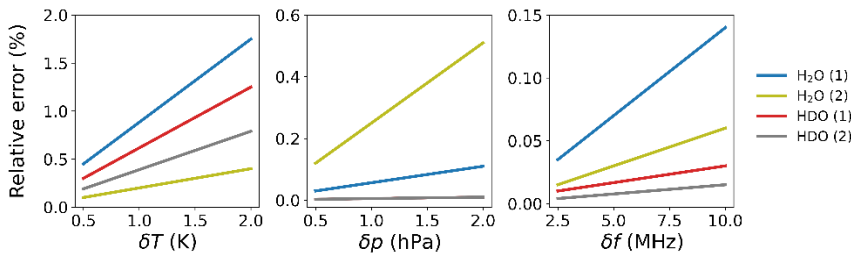
Figure 7: Maximal relative error in the VMR retrieval (over 3 km range, mid-latitude baseline) due to uncertainties in the profiles of temperature (δT) and atmospheric pressure (δp) as well as transmitter on- and off-line wavelength (δf). (1) and (2) stand for the two possible on-line wavelength options for measuring H_2O.

For the case of instrument-related errors, we estimated systematic errors arising from the laser wavelength locking control and spectral quality of the laser beam. To estimate the sensitivity to laser line stability a laser frequency deviation δf ranging from 2.5 MHz to 10 MHz corresponding to wavelength stabilities reliably achievable over several minutes with our envisioned OPO/OPA approach coupled to a commercial wavemeter, which can suffer thermal drifts of a few MHz over several tens of minutes. The relative wavelength error was calculated according to Eq. (16) by introducing a wavelength detuning δf to the on- and offline wavelengths. Due to the narrower absorption line of H_2O at 1982.93 nm, we find that such wavelength detuning results in a greater error compared to the spectrally larger HDO line. Option 2 for H_2O measurement reduces the wavelength error. The systematic error due to the finite laser linewidth was estimated numerically by substituting the absorption cross sections of Eq. (5) by the effective absorption cross sections defined as:

$$\sigma_{eff} = \frac{\int L(v,r) \cdot \sigma(v,r) \cdot dv}{\int L(v,r) \cdot dv} \tag{17}$$

where L represents spectral intensity distribution of the laser transmitter and v denotes the wavenumber. The laser spectral distribution L is assumed to be an altitude-independent Gaussian function with a width of 50 MHz (FWHM), which correlates roughly to the 10 ns pulse duration assuming transform-limited pulses. For comparison, the air broadened Laurentzian widths of the absorption lines under standard atmospheric conditions are on the order of a few GHz. The calculated relative error is on the order of 0.1% for the narrowest (thus most critical) H_2O line at 1982.93 nm.

Another systematic error arises for sounding HDO at 1982.47 nm (option 2) from the insufficient knowledge of the optical depth due to the non-negligible H_2O absorption feature. Assuming a relative uncertainty of 2% in the VMR profile of H_2O, which is a conservative estimate for the combined systematic error of the H_2O measurement due to temperature, pressure, and wavelength uncertainty, calculations reveal relative errors in the VMR retrieval varying between 0.28% for the arctic model and 0.83% for the tropical model. Considering this additional bias and the highly temperature sensitive H_2O interference line for HDO option 1, option 2 should be the preferred wavelength option for HDO in any case. It should be noted that even for the measurement of H_2O an interference contribution due to higher HDO absorption at the off-line wavelength leads to a bias. However, this error is relatively small compared to other systematic errors and the achievable random error.

Finally, systematic errors in the VMR retrieval due to uncertainties related to spectroscopic parameters were analyzed by introducing deviations between 1% to 5% to the HITRAN 2016 parameters of line intensity and air-broadened width and deviations of 1% to 10% to the temperature-dependence width coefficient and the pressure shift parameter. The resulting systematic errors are shown in Fig. 8 for each parameter. Uncertainties in parameters of line intensity and air-broadened width largely contribute to the error budget highlighting the importance of the precise knowledge of these quantities. It should be noted that the assumed uncertainties have a rather demonstrative character as their precise quantification is still the subject of ongoing spectroscopic studies. A summary of the presented systematic errors in the form of an error budget for each of the three atmospheric models is given in Table 3.
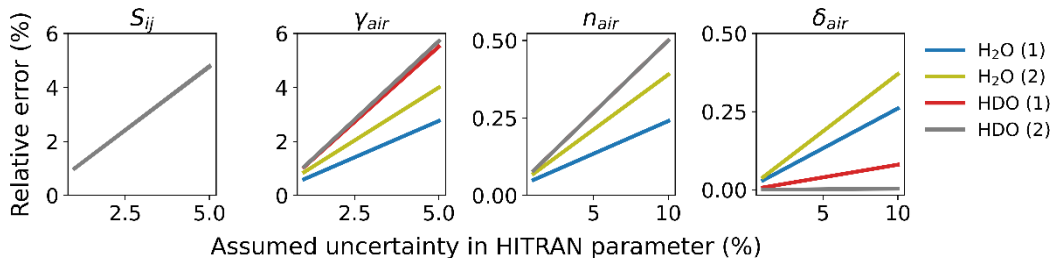
Figure 8: Maximal relative error in the VMR retrieval (over 3 km range, mid-latitude baseline) due to uncertainties in HITRAN parameters. S_{ij}: line intensity; γ_{air}: air-broadened half width; n_{air}: coefficient of the temperature dependence of γ_{air}; δ_{air}: pressure shift.

445

Table 3: Systematic errors for mid-latitude, arctic, and tropical atmospheric models (maximal error over 3 km range). (1) and (2) denote the two wavelength options for H_2O and HDO measurements.

| Parameter | Assumed uncertainty [1] | Maximal relative error ε_s (%) | | | | | | | | | | | |
| | | Mid-latitude | | | | Arctic | | | | Tropic | | | |
		H_2O (1)	H_2O (2)	HDO (1)	HDO (2)	H_2O (1)	H_2O (2)	HDO (1)	HDO (2)	H_2O (1)	H_2O (2)	HDO (1)	HDO (2)
Temperature	±1 K	0.85	0.21	0.61	0.39	0.95	0.27	0.19	0.40	0.79	0.15	1.12	0.37
Pressure	±1 hPa	0.08	0.27	<0.01	<0.01	0.06	0.26	<0.01	<0.01	0.05	0.25	<0.01	<0.01
On/off wavelength	5 MHz	0.07	0.03	0.02	<0.01	0.07	0.04	0.02	<0.01	0.07	0.03	0.03	<0.01
VMR of H_2O bias	2% [2]	-	-	0.52	-	-	-	0.28	-	-	-	0.83	-
HITRAN 2016 parameters													
Line intensity	1%	1.00	1.00	1.01	1.00	1.00	1.00	1.01	0.99	1.00	1.00	1.01	0.99
Air-broadened width γ_{air}	1%	0.60	0.86	1.05	1.06	0.59	0.87	1.07	1.06	0.57	0.83	1.05	1.05
T-exponent of γ_{air}	5%	0.14	0.20	0.33	0.33	0.21	0.31	0.49	0.49	0.07	0.1	0.16	0.16
Pressure shift	5%	0.15	0.19	0.03	<0.01	0.15	0.16	0.04	<0.01	0.13	0.21	0.03	<0.01
Combined (geometric sum)		**1.48**	**1.39**	**1.69**	**1.54**	**1.53**	**1.42**	**1.59**	**1.58**	**1.41**	**1.35**	**2.02**	**1.50**

[1] relative uncertainty if stated in %
[2] conservative estimate of combined systematic error for H_2O measurement

450

3.4 Precision estimate applied to field campaign data

In order to complete our previous numerical studies and relate to more realistic atmospheric conditions, we present here the results of performance calculations initialized with observations obtained during the L-WAIVE (Lacustrine-Water vApor Isotope inVentory Experiment) field campaign at the Annecy lake in the French alpine region (Chazette et al., 2020). This

455 experiment was specifically carried out in order to obtain reference profiles that can be used to simulate the WaVIL lidar vertical profiles. Hence, the data include vertical profiles of pressure and temperature as well as vertical profiles of H_2O and HDO isotopologue concentrations which were obtained by an ultra-light aircraft equipped with an in-situ cavity-ring-down-

spectrometer (CRDS) isotope analyzer. As aerosols were present above the planetary boundary layer on 14 June 2019, we chose data acquired from that day, ranging up to an elevation of 2.3 km. To simulate atmospheric conditions during the

460 measurement campaign as realistically as possible, we used aerosol extinction data from the lidar WALI (Weather and Aerosol Lidar) (Chazette et al., 2014) operated during the L-WAIVE campaign on the same day (see Fig. 9a). The backscatter coefficient was estimated with a lidar ratio of 50 sr and extrapolated to a wavelength of 2 µm using the Angstrom exponent derived from sun-photometer measurements. For the purpose of our simulation study, we do not take into account any measurement uncertainties in the described profiles. Figures 9b and 9c show the in-situ measured δD profile from the field

465 campaign and the hypothetical precision of δD as shaded area depending on detector characteristics and laser energy if that same profile was measured with the here presented DIAL system (precision estimate based on wavelength option 1 for H_2O and option 2 for HDO).

(a) (b) (c)
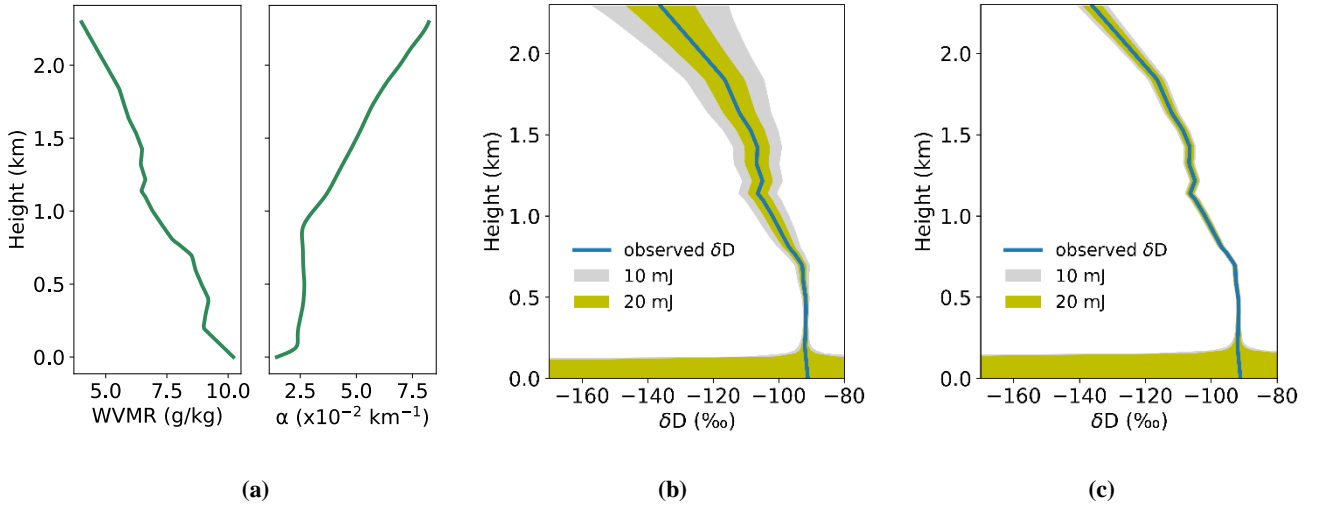
Figure 9: (a) Experimental profiles of water vapor mixing ratio (WVMR) and aerosol extinction coefficient (α) obtained from the L-WAIVE field campaign. Expected precision in the isotopic ratio in terms of δD for the InGaAs PIN photodetector (b) and the low-
470 **noise HgCdTe avalanche photodiode detector (c). Shaded areas indicate the absolute uncertainty based on random noise in terms of standard deviation for laser energies of 10 mJ and 20 mJ. High uncertainty in the first 200 m is due to low signal caused by overlap function increasing from zero to unity (see Eq. (2)). Calculations based on a measurement bandwidth of 1 MHz (150 m spatial resolution) and an integration time of 10 min.**

For the commercial InGaAs PIN photodiode the simulations show for the optimum case of 20 mJ laser energy that the

475 uncertainty related to noise is sufficiently low so that the characteristic variations in the experimentally obtained δD profile could be fully resolved with the proposed DIAL system. In terms of absolute precision, which is visualized as the width of the shaded error band around the in-situ profile, δD could be determined with a precision better than 5‰ within the first 1.5 km and better than 10‰ at a range height of 2 km. A setup with 10 mJ would deliver an absolute precision close to 20‰ at that height. The expected precisions are on the order of or better than the columnar measurements obtained with other remote

480 sensing techniques deployed from the ground (between 5 and 35‰ for Fourier Transform Infrared Spectrometer and Total Carbon Column Observing Network) or from space (~40‰ for the Tropospheric Emission Spectrometer and the Infrared

Atmospheric Sounding Interferometer, see Table 1 of Risi et al., 2012) but with a much greater resolution on the vertical. On the other hand, the expected precision is roughly 2 to 4 times lower than for in situ airborne CRDS measurements with a similar vertical resolution (see Table 3 of Sodemann et al., 2017). Simulations performed with the HgCdTe APD indicate extremely promising precision levels over the entire range of under 3‰ and 5‰ (in absolute terms) for 20 mJ and 10 mJ, respectively. It should be noted that the presented profiles represent a rather favourable case since the aerosol backscatter coefficient increases with altitude (due to the presence of an elevated dust layer) which is the contrary to the baseline atmospheric models described in the previous numerical analysis. These simulations incorporating observed H_2O and HDO profiles clearly show the potential of a ground-based DIAL instrument to measure isotopic mixing ratios with high spatio-temporal resolution in the lower troposphere.

4 Conclusion

Probing the troposphere for water isotopologues with high spatio-temporal resolution is of great interest to study processes related to weather and climate, atmospheric radiation, and the hydrological cycle. In this context, the Water Vapor Isotope Lidar (WaVIL), which will measure H_2O and HDO based on the differential absorption technique, is under development. The spectral window between 1982–1984 nm has been identified to perform such measurements. The selected absorption lines of H_2O and HDO have a sufficiently high line strength to probe the lower 1.5 km of atmosphere with better than 1% relative error in the tropics and mid-latitude regions with high water vapor concentrations. The selected absorption lines are temperature sensitive, requiring an accurate knowledge of the temperature profile along the line of sight for the concentration retrieval. Such a profile would have to be provided by auxiliary measurements, for example by using a Raman lidar.

We performed a sensitivity analysis and an error budget for this system taking instrument-specific and environmental parameters into account. The numerical analysis included models of mid-latitude, polar, and tropical environments with realistic aerosol loads derived from the AERONET database extrapolated to the 2 μm spectral region. We showed that the retrieval of H_2O and HDO mixing ratios is possible with relative random errors better than 1% within the atmospheric boundary layer (<2 km) in mid-latitude and tropical conditions, the latter giving rise to the highest precision due to favourable differential absorption. Based on these precisions of the mixing ratio measurements, the isotopic abundance expressed in δD notation can be derived with a precision necessary to resolve vertical variations in δD of a few tens of permil. Performance simulations also revealed differences in precision of almost one order of magnitude between the tropical and arctic model. Reduced precision under arctic conditions is due to low water vapour content and reduced aerosol load. These findings have been obtained for laser pulse energies of 20 mJ, a measurement bandwidth of 1 MHz (150 m range resolution), an integration time of 10 min, and a commercial InGaAs PIN photodiode. As an interesting perspective option, we also investigated the theoretical performance of a state-of-the-art HgCdTe avalanche photodiode featuring a NEP reduced roughly by one order of magnitude. The use of such a detector would relax the requirement on laser energy and integration time and enable high-precision, range-resolved measurement of the isotopic ratio.

An error budget has been performed to outline systematic errors due to uncertainties in atmospheric, spectroscopic, and instrument-related parameters. The H_2O on-line wavelength at 1982.93 nm shows a pronounced temperature sensitivity imposing strict requirements on accurate temperature profiles for the VMR retrieval. This can be mitigated by tuning the on-line wavelength to 1982.97 nm which, however, comes at the cost of slightly increased pressure sensitivity and slightly reduced differential absorption. For the HDO isotopologue, two wavelength options have been studied. Option 2 with the on-line wavelength at 1983.93 nm was found to be more suitable since it has no H_2O interference (as is the case for HDO option 1 at 1982.47 nm). The slightly smaller differential absorption for option 2 is a price worth paying and the resulting increase in random error can be offset by longer signal averaging. Including systematic errors due to inexact spectroscopic parameters in our analysis, we highlighted the importance of their accurate knowledge for DIAL measurements and the necessity for ongoing spectroscopic studies of water vapor isotopologues in the two-micrometer region.

Finally, using a measured H_2O/HDO profile obtained during the recent L-WAIVE field campaign, our calculations have shown that sufficient precision in the mixing ratios of H_2O and HDO can be achieved with the presented system parameters so that characteristic, vertical variations of the isotopic content δD observed during the field campaign could be resolved with the proposed DIAL system, showing the potential to complement existing methods. Although an effort has been made to conduct the sensitivity analysis and error budget as thoroughly as possible, it should be nevertheless noted that the predicted performance of the presented DIAL system can be understood as a best-case scenario. Assumptions made for the transmitter model, such as no laser beam pointing or perfect spectral purity, are very challenging aspects in the actual laser development. Future work will consist of improving our knowledge in the spectroscopy of HDO in the 1982–1984 nm spectral region and testing the DIAL system in the framework of a forthcoming field campaign.

Appendix A

Table A1 lists databases and locations used to derive the three atmospheric models discussed in this paper. Available data from the year of 2019 was used for all locations.

Table A1. Overview of atmospheric sounding and AERONET sites used to derive an atmosphere model for the sensitivity analysis. For all sites data from 2019 was used. Note that for the arctic station, AERONET photometer products are from February until September.

	Sounding profiles (pressure, temperature, humidity)	AERONET (Level 2 aerosol optical depth)
Mid-latitude station: Paris region, France	Trappes 48.77°N, 2.01°E Météo France data (https://donneespubliques.meteofrance.fr/)	Palaiseau 48.71°N, 2.22°E
Arctic station: Ittoqqortoormiit, Denmark	Ittoqqortoormiit 70.49°N, 21.95°W University of Wyoming data (http://weather.uwyo.edu/upperair/sounding.html)	Ittoqqortoormiit 70.49°N, 21.95°W February – September 2019
Tropical station: La Réunion Island, France	La Réunion (Gillot) 20.89°S, 55.51°E Météo France data (https://donneespubliques.meteofrance.fr/)	La Réunion (St. Denis) 20.90°S, 55.49°E

Author contribution

Conceptualization of measurement concept, J.H., J.-B.D., M.R., R.S., A.G., J.-M.M., J.T., P.C. and C.F.; lidar performance simulator, J.H.; L-WAIVE campaign data curation, H.S., A.S., J.T. and P.C.; writing—original draft preparation, L.R., C.C., M.R. and J.H.; writing—review and editing, all authors; project administration, C.F. and C.E.; All authors have read and agreed to the published version of the manuscript.

Competing interests

The authors declare that they have no conflict of interest.

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