# Authors' reply to reviewer comments

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For the manuscript: "Advances in the True Eddy Accumulation Method: New theory, implementation, and field results" by Emad & Siebicke, https://doi.org/10.5194/amt-2021-319

# General comment

We thank Christoph Thomas for his constructive, motivating, and detailed feedback on the manuscript. Please find below our point-by-point reply to the comments.

- Our answers and comments are in blue.
- Summary of changes to the manuscript is in orange.

# **Overview** statement:

This paper summarizes recent advances in developing the True Eddy Accumulation (TEA) as the only viable alternative to the eddy covariance (EC) method for determining direct ecosystem-scale fluxes for gas and potentially (not addressed here) particulate species for which fast-response analyzers do not exist. The authors are experts in this field and have been leading the development of TEA, I believe they are the only team currently working on it. In this sense, I commend these advances and was eager to learn about the progress this technique has made moving from its infancy to a more refined, potentially operational stage. I do have, however, serious doubts that the manuscript can be published in its current or mildly revised form because its structure does not lend itself for easy reading and application by non-experts of the flux community, and therefore is unlikely to have the impact it deserves. I am convinced of the merit of the TEA method, the quality of the proposed advances, and the expertise of its authors. In my opinion the manuscript suffers from the following substantial issues in descending order of importance:

1. The one manuscript combines three papers with three different foci: a) modifying the original TEA equation to non-vanishing mean vertical wind conditions, b) combining multiple flux estimates at time scales smaller than the intended averaging time scale, the author term 'STEA', which offers obvious practical advantages, and c) addressing and quantifying the effect of fixed buffer volumes and spectral water cross sensitivity of the CRDS analyzer for flow-through TEA applications. While all foci are relevant for the TEA method in general, combining them into one manuscript is not only confusing the reader, but causes it to lose focus, and burying important results in a shear endless stream of information. I am opposed to least-publishable-unit papers, and like the idea of one-stop-shopping about TEA, but I believe it contains too many entangling aspects. It's a tough 29-page read.

We agree the manuscript was long in its original form and has many ideas that made it difficult to read. We split the manuscript after consulting with the editor into two papers. The first paper deals with the theory parts of TEA under non vanishing mean vertical wind velocity. The second paper will contain the field measurements of the STEA method and other aspects related to the system design and operation such as buffer volumes. We believe these aspects are more relevant to the field experiments.

# Changes:

The manuscript was split into two related papers

- 1. True eddy accumulation Part 1: Solutions to the problem of non-vanishing mean vertical wind velocity
- 2. True eddy accumulation Part 2: Theory and experiment of the short-time eddy accumulation method
- 2. The desire to produce TEA fluxes most closely matching those from EC is fundamentally ill-posed, and only relevant in the infancy stage of the method to prove 'yes we can do it'. I sincerely hope we have moved beyond this stage. Interpreting EC fluxes as true ecosystem behavior (as opposed to studying turbulence only) suffers from many known issues, and often invokes strong simplifications to methods and measurements. Instead, the user of the exciting TEA method and reader of the manuscript is interested in quantifying the total flux (ie the left-hand side of Reynold's second postulate, their equation (2)). In this sense, finding a complicated mathematical method to subtract the advective transport (ie flux by the mean flow) from the TEA flux for non-vanishing mean vertical motions conditions in their equation (16) is ill-posed. At least the authors portrait it this way and motivate their correction. In fact, the right-hand side term in (16) may be a necessary correction when the mean vertical motion does not vanish, but it is sold as a TEA equivalent to the WPL correction, which physically is incorrect. To elaborate, I believe the authors misinterpret the existing and well-accepted WPL correction, which states that the simple turbulent covariance term needs to be corrected for i) flux contributions from the contraction-expansion argument of air parcels passing through the fixed sampling volume of a gas analzers, and ii) a finite non-zero mean vertical motion for moist-air flux.

We acknowledge our terminology might have caused some confusion about the motivation and nature of this correction. The term eddy covariance was used in the context of the general method of eddy covariance rather than the "eddy flux" or the "turbulent flux". Similarly, the "advective term" that requires removal is the biased advective term, not the WPL term.

While both TEA and EC are formulated to measure the ecosystem flux,  $\overline{wc}$ . It's well known, it's not possible to calculate the total ecosystem flux from the measured w and c, since any additional bias (offset) will not affect in the covariance term but will appear in the measured term  $\overline{wc}$  which can be several times larger than the flux.

This measured biased advective term  $\bar{w}\bar{c}$  is trivial to discard in EC by block averaging or other means (thus using EC as a reference). While in TEA the nature of the real time sampling does not allow easy removal of this term. Our motivation here is to investigate the size of the error in the flux due to this biased advective term and explore ways to minimize or correct it. In this regards, we do not think TEA has any potential advantage over EC for measuring the true ecosystem flux. Given a sufficiently fast gas analyzer, TEA has the same amount of information as EC does but with the additional constraint of the real-time requirements. Therefore, the the true physical advective term "WPL term" it is not possible to be measured directly with TEA and need to be estimated by other means (similar to EC).

#### Changes:

- Better defined and unified terminology regarding the nature of the removed term across the paper.

- We adopted the term "biased advective term" to avoid confusion with WPL.
- 3. The use of the transport asymmetry coefficient  $\alpha_c$  has theoretical appeal but estimating it from available fastresponse scalar concentration/ sonic temperature for gas species, for which TEA is the ONLY available direct flux method, is flawed because of imperfect scalar-scalar similarity. Nobody requires TEA for estimating CO2 fluxes, for which results from a field study are shown, but fluxes for reactive gas species undergoing photo-

chemical changes during eolian transport, and not just through surface sinks and sources (applicable to nonreactive scalar air temperature, carbon dioxide and water vapor concentrations, etc) are very unlikely to obey the invoked scalar-scalar similarity. They are many recent studies on this issue relating to the relaxed eddy accumulation (REA) group of methods, and now by introducing it to TEA through  $\alpha_c$  it gets contaminated too. Not sure if this is a true advance. I also struggle with the various definitions of  $\alpha_c$ , which may be inconsistent (see detailed comments below) and its physical interpretation.

We think the new formulation using the asymmetry coefficient,  $\alpha_c$  brings multiple advantages to TEA measurements even if no estimate for its value was made.

- 1. Most importantly, this formulation isolates the error in the flux and imposes an upper bound on its value without direct dependence on the scalar background concentration. Irrespective of the scalar, the upper bound for the error in the flux is  $\overline{w}/\overline{|w|}$  of the flux. This is valid when the values of  $|\alpha_c|$  are assumed to be below 1 for stationary turbulence. The arguments for this assumption are detailed below.
- 2. Unifying different formulas for TEA showing what is accounted for in each formula. e.g., using the mass difference as opposed to concentrations.
- 3. Possibility for removing or minimizing the error using the probabilistic approach or invoking scalar similarity which, we agree, neither is ideal but we think there is no way around this.

Regarding the different definitions of  $\alpha_c$ . We acknowledge that some details of how the different definitions link to each other was missing or not clear. In short,  $\alpha_c$  is defined as the ratio of the covariances

$$\alpha_c \equiv \frac{\overline{|w|'c'}}{\overline{w'c'}} \tag{1}$$

The link to the quadrants comes form the fact that  $|\overline{w}|'c'$  is equal to  $|\overline{w}'|c'$  when  $\overline{w} = 0$ , and a good approximation if  $\overline{w} \neq 0$ . We can write  $|\overline{w'}|c' = S1 + S4 - S2 - S3$ . We will add more details on this approximation and why it does not change the general conclusion. The expression in terms of quadrants allows  $\alpha$  to be written in terms of updraft flux (S1 + S4) and downdrafts flux (S2 + S3) as

$$\alpha_c = \frac{\mathrm{flux}^{\uparrow} - \mathrm{flux}^{\downarrow}}{\mathrm{flux}^{\uparrow} + \mathrm{flux}^{\downarrow}} \tag{2}$$

Here, updraft or downdraft fluxes refers to the wind direction and not the sign of the flux. From this equation, it is clear values of  $\alpha$  larger than 1, would indicate that updraft flux (S1 + S4) and downdraft flux (S2 + S3) have opposing signs. This would mean the quadrants will form a pattern similar to a butterfly which means for positive values of the wind the scalar wind are correlated and for negative values they are anti-correlated (or the other way around). This pattern is highly unlikely with stationary flows. The values of  $\alpha_c$  observed from our experiment support this analysis as seen below.



Stationarity test is done following (Foken and Wichura, 1996)

# Changes:

We added additional details to how the different definitions relate to each other and a new plot for the observed values of  $\alpha$  for four scalars.

- 4. The style of the manuscript varies from section to section from equation-rich and full text explanations to bulletitem to-do list instructions. I realize that this diversity may be caused by alternating authors and could be helpful in in the field, but the manuscript would benefit from homogenization. Quite a few equations can easily be omitted to slim down and sharpen focus, but some require mor detailed derivations and explanations. I believe that the most important 1) could be addressed by splitting the one manuscript into several independent, but related parts (an option other boundary-layer micrometeorological journals offer), similar to a mini-series of publications. The handling editor will know and decide. Please find my additional detailed comments below.
- We have opted for splitting the manuscript into two related papers and made many editorial changes to improve the flow and structure of the manuscript. We think the diversity originates from the different topics covered. We hope splitting would offer a more homogeneous reading experience.

# Detailed comments (kept short for clarity)

1. Line 32: please add 'out of the family of accumulation methods'.

### Changes:

# Suggested change added

2. Line 40: Please see general comment 2) above, I think it the desire to match the EC flux is flawed, but the true (total) flux should be in the center of our attention when conducting ecosystem studies.

#### Changes:

We rephrased this sentence to clearly reflect the aim of the research as mentioned in our reply to general comment 2.

3. Line 49: REA can lead to both under- and overestimation when compared to the EC flux, so I wouldn't call it just as a 'loss'. The sign of the change depends on the exact REA method used.

We agree loss is not an accurate characterization of the error.

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Changes:
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We changed it to systematic error.

5. Line 58: I think a first brief definition of  $\alpha_c$  is in order here, while I do have my doubts about its utility (see general comment 3) above). However, introducing it as a coefficient representing the disparity in the vertical transport between up and downdrafts is helpful.

We think the utility and definition should be more clear now as addressed in our reply to general comment 3.

6. Line 60ff: Here is the first break from 'sub-manuscript' a to b (see general comment 1) above).

Addressed in general comment 1.

7. Equation (3): It is uncommon to see the EC flux mathematically being defined in the time domain, but in reality it is (almost exclusively) done this way. I believe using number N instead of time increments is more universal, but is a matter of taste.

We agree this is a practical definition as we confirmed with the phrase "ensemble averages are estimated experimentally" The choice of dt was to be consistent with the definition as a continuous function.

8. Line 87: The statement about the merit of the WPL correction is incorrect, see general comment 2) above. Standard 1-D EC-based mass balance methods eliminate this term by setting  $\overline{w} \equiv 0ms^{-1}$  through rotation, but in reality it is a true physical term which requires accounting. This is what the WPL does. Flux estimates including the WPL term do therefore not 'correct' the covariance flux  $\overline{wtot}$ , but estimate the 'true' full transport  $\overline{wc}$ .

We agree that the characterizing of the WPL term as a correction is not accurate. We incorrectly used the term "eddy flux" to refer to the total ecosystem flux  $\overline{wc}$ . We corrected it to reflect that  $\overline{w'c'}$  is an approximation to the total ecosystem flux and the mean advective term,  $\overline{wc}$  in Eq. 2 is the "Web term".

Changes:

We used the correct terminology and restructured the paragraph to reflect the relation between the physical WPL term and the measured biased advective term.

9. Line 92: What do you mean by offset? Offsets are instrument-specific properties due to improper calibration or referencing. True physical non-zero vertical motions is a different phenomenon. Please be precise in terminology. I find this paragraph confusing, consider omission?

We used offset to refer to any non-turbulent component in w that will appear in the measured advective term  $\bar{c} \bar{w}$ . We think this paragraph is necessary to disentangle the relation between the physical advective WPL term and the biased measured one that we are trying to remove. We restructured this paragraph to make the distinction clear.

10. Line 101 and throughout: use often state 'computations at the end of the averaging interval', but more precise of 'for the averaging interval', since the decision of sampling into up- or down reservoir is done while sampling, and not just at the end.

Changes:

# Changed as suggested.

11. Line 102: I recommend using a different symbol than  $T_{avg}$  for the averaging interval length, as it may be confused with temperature.

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Changes:
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The averaging interval was changed to  $\Delta t$  instead of  $T_{avg}$ .

12. Equation (6): I recommend removing it here, it does not lend anything to this section, and is only needed later in section 2.4 and Appendix A.

*Changes:* Equation (6) removed as suggested.

13. Equation (8) and (9) can be combined, since V is defined in equation (7). We agree

*Changes:* Equations were combined as suggested.

14. Line 33: I believe it may be helpful to point out that the magnitude of w needs to be taken first, then comes the averaging. If reversed, the statement does not apply.

# Changes:

We agree, we added further explanation to emphasize this.

15. Line 136: See general comment 2) above. While your proposed correction takes a similar mathematical form, you do not discard the advective transport, but flux uncertainty because the assumption of zero mean-vertical velocity is not fulfilled. This difference is important!

This is correct. We have emphasized the correct use of terminology.

16. Equations (11) and (12): This is a key step, explain!

# Changes:

We added further explanation. In particular, now we simplified the derivation by starting from c|w| without the need for the weighted mean. Eq. 9 in the new manuscript.

17. Line 164: add an 'and' between |w| and c.

*Changes:* Missing 'and' added as suggested.

18. Equation (16) and (17): rearranging is fine, but the utility is not obvious to me. Do we need (17)?

Equation 17 is the resulting corrected TEA flux, we think it is good to have although easily obtained from Eq. 16.

19. Equation (18): not needed, consider omitting.

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Changes: Equation removed as suggested.
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20. Equations (19) and (24): I struggle in combining these two different definitions: do you mean the magnitude of the terms  $flux \uparrow$  and  $flux \downarrow$ , or do these terms actually preserve their sign? To me, equation (24) is the inverse of (19). However, later in the results section (line 468 ff) you report values of  $\alpha$  between 0.2 and -0.18 for CO2, so

 $|\alpha| < 1$ . I do not see how these values agree with equation (19), which should exceed unity. The numerator c'|w'| has to be larger than the denominator  $\overline{c'w'}$ . Please clarify!

Updraft and downdraft fluxes here are flux transported with positive and negative wind velocity, the sign of the flux is preserved. We have changed the order of the definitions to introduce the quadrants first then define updraft and downdraft fluxes using quadrants as we discussed in our reply to general comment 3. Eq. (19) is simply stating the covariance as  $\overline{wc} - \overline{cw}$  as a step to construct the analytical solution. We think it might be distracting, so we removed it.

21. Equations (20) and (21): without showing how you solve the integrals these equations have little to no utility. Simply stating equations (22) and (23) may suffice.

*Changes:* Equations 19-21 were removed as suggested.

22. Line 194: Sentence is incomplete at a critical point (after the parantheses).

*Changes:* The paragraph was restructured and the sentence was changed.

23. Equation (24): still struggling, please see earlier comment.

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Changes:
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The definition was changed in term of the quadrants. We hope the definitions are more clear now.

24. Equations (25) to (30): this is not needed and a diversion. Please consider removing. I think you should keep the textual description of how to estimate it from quadrant analysis (it is a nicely analytical vehicle indeed), but it exact mathematical form distracts. Actually, I think it is better suited than the analytical approach in equation (23). Maybe toss this? Either way, please revise this section 2.3.1 and slim it down to the essential punchline.

The section was restructured and heavily edited to introduce the quadrants first, the analytical value of alpha, and then the value form scalar similarity.

25. Section 2.4: submanuscript b) continues.... See general comment 1) above.

*second manuscript* This section is now part of the second manuscript.

26. Equation (36): does not lend anything, it simply rewrites the averaging. Consider omitting.

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second manuscript
Equation removed as suggested.
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27. Section 2.5: submanuscript c) starts... See general comment 1) above. I suggest moving the fundamentals of the time constant discussion from the results section (particularly Fig. 9) to the materials &methods section.

#### second manuscript

This section is now part of the second manuscript. The section was shortened to improve readability and the figure was moved to methods as suggested.

28. Line 263: please explain what this statement means.

# second manuscript

The following explanation was added: The short accumulated samples in the STEA method are individually separated as they are forwarded to the gas analyzer, this discrete behavior is best modeled with a discrete-time system as shown in Eq. 8 29. Line 274ff: Please include only the periods for which data are presented, anything else is irrelevant.

*second manuscript* Additional periods were removed.

30. Figure 2: Caption: pneumatic schematic? Not hydraulic suggesting you move incompressible fluids.

second manuscript Changed as suggested

31. Line 304: 2. Does this mean, TEA sampling needs to start sampling wind velocities 2 days prior to taking the first measurements, or one discards the first 2 days in post-processing?

second manuscript We have the system progressively calculates the rotation angles but later the first two days were excluded as they will more variable rotation angles.

32. Line 320, Fig 3: How large is the variability (ie one form of error) for the repeated samples of the same sampling volume? It appears it may be on the order of 0.5 ppm? Interesting and important to know.

#### second manuscript

Indeed, the average standard deviation for short averaging intervals was 0.501 ppm as shown in the Allan deviation plot below



# *Changes:* Added variability of measurements to the text.

33. Line 341ff: How do you correct for water vapor cross sensitivity as the wapor concentration remains identical? Maybe I do not understand the method correctly, please explain.

### second manuscript

We have notice we missed some key information. This procedure utilizes the effect of air drying due to decompression to deliver a variable water vapor content. Starting from humid atmospheric air near saturation (RH ~ 90%, T=21). Air is sucked and compressed into the stainless steel buffer volumes to a pressure of (2.6 bar). The water partial pressure in the pressurized buffers will become higher than

saturation vapor pressure and water will precipitate leading to dryer air. Then, air is decompressed and forwarded to the analyzer. As the buffer pressure is reducing, water content will increase. Using this method we were able to modulate the water content in air from 6000 to 14000 ppm.

#### Changes:

We changed the text to reflect the used method more accurately.

34. Line 353: Please do not use the word 'deadband' here, as it is commonly used in the REA/ TEA community for discarding samples of small flux contribution (HREA) or small vertical velocity. This may lead to confusion, how about 'line flushing volume' or similar?

second manuscript We changed the deadband to "Flushing time"

35. Line 367: what is a dynamic flux unit? Please explain.

*second manuscript* We changed to the actual unit.

36. Section 2.8.4: Much of this is very technical and difficult to understand. These details distract from the true advances you propose, see general comment 1) above. For me, this belongs to submanuscript c).

*second manuscript* This section was shortened and improved.

37. Line 391: Iinear detrending, really? Why?

Detrending used here in the context of block averaging. We removed it to avoid confusion.

38. Section 2.10, line 400: you despike the time series of final computed fluxes excluding everything exceeding  $2\sigma$ ? This can only be justified by assuming a well behaved biological functioning of the carbon uptake, but not by turbulence transport. How much does that obscure true TEA flux uncertainty?

# second manuscript

We agree despiking is not ideal as it could obscure valid flux measurements. However, for our dataset. Spikes were mostly due to problems with the open-path gas analyzer. Including the spikes in the analysis had very little effect on the comparison between EC and STEA, It improved the slope to 1.03 and slightly reduced  $R^2$  by 0.1.

Changes:

We relaxed the conditions for spike removals to exclude only the very obvious erroneous values. The new threshold (6 hour window, 2  $\sigma$ ) removes only 3 spikes from the whole dataset.

39. Section 2.11: so many filters and flags, I wonder what the TEA fluxes look like without applying all those....

# second manuscript

The flags were necessary to exclude periods where one or both of the systems did not work well. In particular, rain and violations of the assumptions of the EC method accounted for the majority of excluded values which sometimes produced nonphysical fluxes (<  $100 \ \mu mol \ m^{-2} \ s^{-1}$ ). Therefore, the flags were only applied for the linear fit which is particularly sensitive to outliers to get a meaningful measure for comparing the two methods. No points were excluded from Fig. 7. which shows even without removing low quality fluxes, the fit is still reasonably good.

40. Section 3.1.1: please see general comment 3) above, and detailed comment t). I struggle with estimating numerical values for  $\alpha$  and relating them to your observations. Invoking scalar similarity weighs heavily on this TEA 'advance'. Have you investigated the scalar-scalar similarity for your field experiments? Even among conservative scalars it changes dramatically with time.

We have improved the definitions of  $\alpha$  as we detailed in our reply to comment 3. We hope it clarifies the numerical values of  $\alpha$ 

Changes:

The numerical values of  $\alpha$  were discussed in terms of the sign and magnitude.

41. Section 3.2: Much is repetition from section 2.8, please only report results and their discussion here.

second manuscript

Changes:

The earlier repetitions from section 2.8 were removed. We left the discussion on the advantages of the STEA method and how to achieve a flow-trough system with STEA as we think they highlight key findings of this study.

42. Line 525f: Please explain this to the reader, it is technical jargon.

#### Changes:

We added further explanation about the meaning of time-invariance and its relation to the buffer volumes model.

43. Line 539: Replace 'stable' by 'stationary'.

second manuscript Changed as proposed.

44. Line 545ff: Could the results be reversed here between long- and short-term rotation window?

#### second manuscript

We think the short-term rotation window will minimize the residual vertical wind velocity in most cases. However, we think these findings are site-specific and need to be evaluated in more complex sites.

45. Section 3.3.3: is this truly needed?

#### second manuscript

We think it is necessary to highlight the difference of WPL relevancy for flux calculation between EC and TEA. However, we agree it might be misplaced in results section, so we moved it to the methods section.

The section was shortened and moved to the methods section to

46. Line 578ff: Comparing the absolute uncertainties across studies is not useful as the site conditions and sampling methods are very different. This needs to be communicated in terms of relative flux estimate uncertainty.

#### second manuscript

We agree and have changed to using the random error estimate from our measurements and added a note about the limitation of RMSE for comparing different studies since we could not find a relative measure for comparing different gas analyzers.

#### Changes:

We used the random error calculated from our EC measurements to get an estimate about the contribution of the random sampling error to the uncertainty and added a sentence to highlight the limitation of RMSE for comparing cross-studies flux measurements.

47. Section 3.4: as this appears to be a key goal for the authors, I would like to see a comparison of their full new TEA method (equation 34) with the traditional TEA method (not including the proposed corrections), as well as the magnitude of the correction terms (second and third term in equation 16) separately. This will ultimately demonstrate the utility of the proposed corrections.

# second manuscript

Under the specific conditions of our site, the third correction term using  $\alpha$  was small (less than 1.5% of the total flux). This was due to the flat topography and the use of online treatments to minimize the vertical wind and was highlighted in the results section but not shown in the figure comparing the two methods. However, not accounting for the second term and using the mass difference between updraft and downdraft, effectively measuring *overlinewc*, will result in a much larger error. The mean absolute error, in this case, is 170% of the turbulent flux.

Christoph Thomas, University of Bayreuth

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