

Data imputation in in situ measured particle size distributions by means of neural networks

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Abstract.

In air quality research, often only size-integrated particle mass concentrations as indicators of aerosol particles are considered. However, the mass concentrations do not provide sufficient information to convey the full story of fractionated size distribution, in which the particles of different diameters (D_p) are able to deposit differently on respiratory system and cause various harm. Aerosol size distribution measurements rely on a variety of techniques to classify the aerosol size and measure the size distribution. From the raw data the ambient size distribution is determined utilising a suite of inversion algorithms. However, the inversion problem is quite often ill-posed and challenging to solve. Due to the instrumental insufficiency and inversion limitations, imputation methods for fractionated particle size distribution are of great significance to fill the missing gaps or negative values. The study at hand involves a merged particle size distribution, from a scanning mobility particle sizer (NanoSMPS) and an optical particle sizer (OPS) covering the aerosol size distributions from 0.01 to 0.42 μm (electrical mobility equivalent size) and 0.3 μm to 10 μm (optical equivalent size) and meteorological parameters collected at an urban background region in Amman, Jordan in the period of 1 Aug 2016–31 July 2017. We develop and evaluate feed-forward neural network (FFNN) approaches to estimate number concentrations at particular size bin with (1) meteorological parameters, (2) number concentration at other size bins, and (3) both of the above as input variables. Two layers with 10–15 neurons are found to be the optimal option. Worse performance is observed at the lower edge ($0.01 < D_p < 0.02 \mu\text{m}$), the mid-range region ($0.15 < D_p < 0.5 \mu\text{m}$) and the upper edge ($6 < D_p < 10 \mu\text{m}$). For the edges at both ends, the number of neighbouring size bins is limited and the detection efficiency by the corresponding instruments is lower compared to the other size bins. A distinct performance drop over the overlapping mid-range region is due to the deficiency of a merging algorithm. Another plausible reason for the poorer performance for finer particles is that they are more effectively removed from the atmosphere compared to the coarser particles so that the relationships between the input variables and the small particles is more dynamic. An observable overestimation is also found in early morning for ultrafine particles followed by a distinct underestimation before midday. In the winter, due to a possible sensor drift and interference artefacts, the estimation performance is not as good as the other seasons. The FFNN approach by meteorological parameters using 5-min data ($R^2 = 0.22\text{--}0.58$) shows poorer results than data with longer time resolution ($R^2 = 0.66\text{--}0.77$). The FFNN approach by the number concentration at the other size bins can serve as an alternative way to replace negative numbers in size distribution raw dataset thanks to its high accuracy

40 and reliability ($R^2 = 0.97-1$). This negative numbers filling approach can maintain a symmetric distribution of errors and
41 complement the existing ill-posed built-in algorithm in particle sizer instruments.

42

43 **Keywords.**

44 Atmospheric aerosols particles, feed-forward neural network, interpolation, missing data, SMPS, OPS

45 **1 Introduction**

46 Particulate matter (PM) is the principal component of air pollution. PM includes a range of particle sizes, such as coarse
47 ($1 < \text{particle diameter } (D_p) < 10 \mu\text{m}$), fine ($0.1 < D_p < 1 \mu\text{m}$), and ultrafine particles (UFP, $D_p < 0.1 \mu\text{m}$). Through human's
48 inhalation, coarse particles usually are partly deposited in the head airway ($5-30 \mu\text{m}$) by the inertial impaction mechanism,
49 and are partly deposited in the tracheobronchial region, mainly through sedimentation ($1-5 \mu\text{m}$). The particles may be
50 further absorbed or removed by mucociliary clearance (Gupta and Xie, 2018). The remaining fine and UFP, due to their
51 high surface area to mass ratios (Kreyling et al., 2004), penetrate deeply into the alveolar region, where removal
52 mechanisms may be insufficient (Gupta and Xie, 2018). Evidence suggests that the adverse associations of short-term
53 UFP exposure with acute and chronic problems ranging from inflammation, exacerbation of asthma, and metal fume fever
54 to fibrosis, chronic inflammatory lung diseases, and carcinogenesis (Spinazzè et al., 2017) might be at least partly
55 independent of other pollutants (Ohlwein et al., 2019). Various studies have demonstrated that inhaled or injected UPF
56 could enter systemic circulation and migrate to different organs and tissues (Londahl et al., 2014; Xing et al., 2016).

57

58 Other than health effects, particles of various sizes also contribute to Earth's ecosystem and climate differently. For
59 instance, fine and UFP are capable of growing up to diameters of $0.02-0.1 \mu\text{m}$ within a day (Kulmala et al., 2004;
60 Kerminen et al., 2018) where they constitute a fraction of cloud condensation nuclei; thus, indirectly affecting the climate
61 (Kerminen et al., 2012). The drivers behind aerosol particles vary between natural and anthropogenic as well as primary
62 and secondary. Primary particles are emitted to the atmosphere as particles, such as sea salt or dust particles, while
63 secondary particles form in the atmosphere through gas-to-particle transformation, which has been known as new particle
64 formation (NPF) observed in various environments and contributing to a major fraction of the total particle number budget
65 (Kulmala et al., 2004; Kerminen et al., 2018). In addition, while fine particles cool the climate by predominantly scattering
66 shortwave radiation, coarse particles warm the climate system by absorbing both shortwave and longwave radiation (Kok
67 et al., 2017). Indeed, the complexity of urban aerosols is tribute to the fact that several sources can contribute in the same
68 particle size range (Rönkkö et al., 2017).

69

70 Currently, the most commonly reported aerosol variables are particle mass concentration and particle number
71 concentration. The former metric, which is dominated by coarser particles, is included as air quality indicators (e.g. mass
72 concentrations of both thoracic particles PM_{10} and fine particles $\text{PM}_{2.5}$); however, it has been argued that this might ignore
73 the potential adverse effect of UFP on health (Zhou et al., 2020). The latter one describes better the distribution of finer
74 particles, but it neglects the influence of coarse particles. Using either particle mass concentration or particle number
75 concentration solely is not enough to fully review the health effects and the Earth's climate system by aerosol particles.
76 Therefore, in order to understand the origin of atmospheric aerosol particles and their potential impacts at a specific
77 location, the whole size distribution of these particles needs to be studied (Zhou et al., 2020).

78

79 Recently, due to urbanization and increased population, megacities have increased their contribution to atmospheric
80 aerosol pollution massively Lelieveld et al. (2015). Middle East and North Africa (MENA) regions, with an average
81 annual growth rate of 1.74% in 2019 (World Bank Group, 2019), has one of the world's regions most rapidly expanding
82 populations. With the population of 578 million, several cities in MENA regions are among the 20 most polluted cities in
83 the world. The annual average concentrations of some pollutants, for example PM_{2.5} in MENA (54.0 µg m⁻³) often exceed
84 5 times the WHO recommended levels (10.0 µg m⁻³) (World Health Organisation, 2019). Many countries in MENA are
85 dealing with negative impacts of air pollution in terms of both economic burden and health aspect (Ahmed et al., 2017;
86 Goudarzi et al., 2019). Air Pollution in this region is estimated to cause 133,000 premature deaths annually, almost half
87 of which are attributed to natural sources of air pollution, such as windblown sea salt and desert dust (Gherboudj et al.,
88 2017). Apart from natural pollutants, anthropogenic activities also play a major role in driving the air quality. They include
89 the extensive development of petrochemical industry, vehicular emissions and open burning of waste (Arhami et al.,
90 2018).

91
92 However, aerosol studies in this region have not paid attention to the aerosol number size distribution so far. Among the
93 few studies published, most report mass concentration (Goudarzi et al., 2019; Arhami et al., 2018; Borgie et al., 2016),
94 while some focused on the total particle number in MENA regions. Studies on the size-fractionated number concentrations
95 are, nonetheless, scarce (e.g. Hakala et al., 2019) due to the unavailability of instruments for measuring UFP in many
96 air quality monitoring stations (Spinazzè et al., 2017). Determining aerosol number size distribution for a wide size range
97 in a reliable manner is a challenging task. The fact that the ambient distributions range from nanometers to several
98 micrometers dictates the use of multiple sizing techniques. For the sub-micron size range, electrical mobility equivalent
99 diameter is commonly used as the size parameter and the measurements are performed with Differential Mobility Particle
100 Sizer (DMPS) or Scanning Mobility Particle Sizer (SMPS) instruments (e.g. Wiedensohler et al., 2012) . These systems
101 determine the aerosol size according to electrical mobility equivalent size. The larger particles (approximately > 0.3 µm)
102 can be classified according to their aerodynamic or optical size (Kulkarni et al., 2011). In order to obtain the full aerosol
103 size distribution, this data needs to be merged. Unfortunately this task is not trivial as the merging requires knowledge on
104 the chemical composition (influencing the refractive index and thus the optical size), shape (influencing electrical mobility
105 equivalent size), or effective density (influencing aerodynamic size) (Kannosto et al., 2008).

106 In addition, the raw data from these instruments must be inverted to obtain the particle size distribution. This is not a
107 straightforward problem. A proper inversion algorithm is required to restore the particle size distribution from the raw
108 response (Cai et al., 2018) using recorded kernel functions which describe the probability of particles of a certain size
109 being measured at a certain flow rate, influenced by the measured activation curves and the detection efficiencies of the
110 instruments (Lehtipalo et al., 2014). Depending on the instruments used and the measurement environments, some use a
111 built-in inversion algorithm in the instruments, which replace negative raw values with artificial non-negative numbers.
112 Some develop their own inversion methods; however, they all have their drawbacks. Examples include that the least
113 square method may magnify the random errors in the raw counts in Condensation Particle Counter (CPC) into relatively
114 large uncertainties (Enting and Newsam, 1990), the stepwise method may cause non-negligible errors (Lehtipalo et al.,
115 2014), and that the smoothing step method may introduce bias in the shape of the inverted distribution function
116 (Markowski, 1987). Kandlikar and Ramachandran (1999) pointed out that there is not a single universal inversion
117 algorithm applicable to all situations. In this study, the built-in inversion algorithm was used. This algorithm can lead to
118 negative values when the kernel functions are not optimally configured, especially in the size range of low number

119 concentration. These negative values have no physical meanings. Some experts in the in situ measurement community
120 might just omit the negative values or simply use nearest neighbour linear interpolation to replace the negative values.
121 However, the former method might cause asymmetric error for very small measured number concentration values (Viskari
122 et al., 2012), while the latter could result in too high values concurrently. To fill this knowledge gap, statistical estimation
123 methods can serve as an alternative to estimate of size-fractioned number concentration by using other available
124 measurements.

125

126 The main objective of the paper is to estimate particle number concentration/ fill the negative values making up for the
127 shortcomings of the built-in inversion algorithm in particle sizer instruments. Extending from the previous study by
128 Zaidan et al. (2020), we build our imputation method with a finer temporal and size-bin resolution. In order to do so, we
129 place emphasis on estimating particle number concentration of a specific size bin by the interaction with other size bins
130 and meteorological variables. In this study, we propose three approaches in terms of different input variables by means
131 of neural networks: (1) only meteorological parameters, (2) only particle size distribution, and (3) both particle size
132 distribution and meteorological parameters. Based on the general data analysis of the particle size distribution and the
133 meteorological condition, we explain the source of different size bins at certain weather conditions and the correlation
134 among the particle size distribution and meteorological parameters in Sect. 3. We evaluate the proposed neural network
135 method and compare it with other simpler methods in Sect. 4.1. In Sect. 4.2, we further discuss the temporal pattern of
136 the proposed method in terms of its diurnal cycle, weekend effect and seasonal variation. Besides, we examine the possible
137 technical reasons for the pattern found and the application of the proposed method.

138 **2 Methods**

139 **2.1 Measurement sites and Instruments**

140 In this study, we collected a dataset obtained from a measurement campaign in Amman, the capital city of Jordan, between
141 1 August 2016 and 31 July 2017. The city represents an area with Middle Eastern urban conditions within the Middle
142 East and North Africa (MENA) region. This region serves as a compilation of different aerosol particle sources including
143 natural dust, anthropogenic pollution (e.g. generated from the petrochemical industry and urbanization), as well as new
144 particle formation.

145

146 The database includes particle size distribution and meteorological parameters, as mentioned in the first step in Figure 1.
147 The aerosol measurement was carried out at the aerosol laboratory located on the third floor of the Department of Physics,
148 University of Jordan (32°00' N, 35°52' E) in the neighbourhood of Al Jubeiha. The campus is situated at an urban
149 background region in northern Amman. In particular, the campaign measured the particle number size distribution using
150 a scanning mobility particle sizer (NanoScan SMPS 3910, TSI, MN, USA) with default settings. It monitors the particle
151 size distributions as electrical equivalent diameter 0.01–0.42 μm (13 channels). The size range of the SMPS system can
152 be extended to coarse particles with an additional compact instrument: an optical particle sizer (OPS 3330, TSI, MN,
153 USA). OPS measures optical diameter 0.3–10 μm (13 channels). This optical sizing method reports an optical particle
154 diameter, which is often different from the electrical mobility diameter measured by the SMPS technique. The
155 measurements were combined to provide a particle size distribution of wider particle diameter range 0.01–10 μm , which
156 is further described in Sect. 2.2. The SMPS inlet consists of copper tubing with a diffusion drier (TSI 3062-NC). The inlet

157 flow rate was 0.75 lpm ($\pm 20\%$) while the sample flow rate was 0.25 lpm ($\pm 10\%$). The flow rate of OPS was about 1 lpm.
158 The aerosol transport efficiency and losses through the aerosol inlet assembly and the diffusion drier was determined
159 experimentally in the laboratory: ambient aerosol sampling alternatively with and without sampling inlet, and the aerosol
160 data was corrected accordingly. The penetration efficiency was $\sim 47\%$ for 0.01 μm , $\sim 93\%$ for 0.3 μm and $\sim 40\%$ for 10
161 μm (Hussein et al., 2020). These deficiency of measurement at the upper and lower edges is somewhat in alignment with
162 other literatures. Particle size measured by nanoSMPS (Tritscher et al., 2013) tended to be underestimated for spherical
163 particles larger than 0.2 μm by up to 34% (Fonseca et al., 2016). Liu et al. (2014) clearly portrayed that the detection limit
164 of particle size below 0.03 μm is about $80\text{--}500\text{ cm}^{-3}$, which is up to 10 times larger than that of coarser particles, for other
165 versions of SMPS. Stolzenburg and McMurry (2018) explained that discrepancies could be resulted from Differential
166 Mobility Analysers (DMAs) with transfer functions that were degraded (i.e., broadened) by flow distortions caused by
167 particle deposition within the classifier tube, sizing errors due to errors in flowmeter calibrations or leaks, CPC
168 concentration errors due to improper pulse counting, and continuity failure in the DMA high voltage connection.

169

170 The meteorological measurement was performed with a weather station (WH-1080, Clas Ohlson: Art.no.36-3242,
171 Helsinki, Finland) with a time resolution of 5 minutes. The meteorological data were comprised of ambient temperature
172 (Temp, resolution 0.1°C), relative humidity (RH, resolution 1%), wind speed (WS), wind direction (WD, 16 equal
173 divisions) and air pressure (P, resolution 0.3 hPa) (Hussein et al., 2019; Hussein et al., 2020; Zaidan et al., 2020). Wind
174 direction is resolved into north and east direction, as WD-N and WD-E, respectively. The data collection process is
175 illustrated in the first step in the database block in Figure 1.

176 **2.2 Data pre-processing**

177 The next step in the database block in Figure 1 is data pre-processing. Since the sampling time resolution of SMPS and
178 OPS was 1 min and 5 min, respectively, we synchronised the data into 5-min averages. Since a part of the size ranges in
179 both instruments are overlapping with each other, the last two size bins in SMPS and the first size bin in OPS were
180 neglected. Finally, we merged the size range of electrical mobility diameter 0.01–0.25 μm by SMPS and optical diameter
181 0.32–10 μm by OPS, and obtain a wider particle size distribution which covers the diameter range 0.01–10 μm . Merging
182 electrical mobility diameter and optical diameter can be a challenge and the overlapping region is often calculated with
183 high uncertainty (DeCarlo et al., 2004; Tritscher et al., 2015). The challenge arises because the optical diameters are
184 measured based on the refractive index of the particles, which depends on their chemical composition. Therefore, the
185 sizing will vary over time. There is also a slight dependency with the SMPS system that is linked to the shape of the
186 particles, which influences their sizing.

187

188 We also calculated the particle number concentration with four particle diameter modes (size-fractionated number
189 concentration): nucleation (0.01–0.025 μm), Aitken (0.025–0.1 μm), accumulation (0.1–1 μm) and coarse mode (1–10
190 μm). Subsequently, the total number concentration was obtained as the sum of all these fractions. The size-fractionated
191 number concentrations were obtained by summing up the measured particle number size distribution over the specified
192 particle diameter range.

193

194 In order to perform data imputation with neural networks, aerosol and meteorological data were first linearly interpolated
195 in time in case of short missing data periods. For missing data over longer periods, the whole rows are eliminated. The

196 shorter missing data occurs due to technical faults while the longer missing periods are attributed to instrument
 197 maintenance (Zaidan et al., 2020). Only 71.8% of total data was retained for the next step in the measurement period.
 198 Since the data were obtained from different measured variables with various physical units and magnitudes, it was crucial
 199 to normalise the data. The scaling factor depends on which activation function is chosen. In this case, the datasets were
 200 scaled so that it has a mean of 0 and a standard deviation of 1 to transform them into the range of the activation function.
 201 The standardised data was then separated into different months for the reason of the seasonal variation in the atmospheric
 202 condition. The data was further divided into training set (70%) and testing set (30%). The processed data were also
 203 converted to hourly and daily averages for reporting purposes.

204 2.3 Setting of the neural network

205 After data collection and data pre-processing procedures, the next step is method optimisation (Figure 1). ANN models
 206 have been utilised in predicting air quality (Freeman et al., 2018; Maleki et al., 2019; Cabaneros et al., 2019; Zaidan et
 207 al., 2020; Fung et al., 2020). Neural networks provide a robust approach for approximating real-valued target functions
 208 because they can mimic the non-linearity of the functions and their optimisation methods are well developed (Zaidan et
 209 al., 2017). The architecture of neural networks consists of nodes as activation function (Figure 2), and the activation
 210 function in each layer determines the output value of each neuron that becomes the input values for neurons in the next
 211 hidden layer connected to it. In this paper, feed-forward neural network (FFNN) is used instead of a more sophisticated
 212 time delay neural network (TDNN) because some of the rows in the dataset were removed in the data pre-processing step
 213 due to the existence of missing data and TDNN cannot be performed without time continuity. FFNN usually consists of
 214 a series of layers. The first layer has a connection from the network input. Each subsequent layer has a connection from
 215 the previous layer. The final layer produces the network's output. A neuron can be thought as a combination of two parts:

$$z_j^{(L)} = \sigma\left(\sum_{i=1}^n w_{ji}^{(L)} x_i + b_j^{(L)}\right) \quad (1),$$

216 where $z_j^{(L)}$ and $b_j^{(L)}$ are the intermediate output and the bias term for the j^{th} neuron at L^{th} layer, respectively. $w_{ji}^{(L)}$ is the j^{th}
 217 weight for each data points x_i at L^{th} layer. The second part performs the activation function (sigmoid function in this
 218 study) on z_j to give out the output of the neuron:

$$\sigma(z_j^{(L)}) = \frac{1}{1 + \exp^{-z_j^{(L)}}} \quad (2),$$

219 The FFNN method was created, trained and simulated with MATLAB (version: 8.3.0.532), using Neural Network
 220 Toolbox. We initialised the weights randomly and the weights were updated through ‘‘Levenberg-Marquardt’’ algorithm
 221 optimisation that was the fastest available back-propagation training function (Chaloulakou et al., 2003). We performed
 222 several iterations within a cycle to minimise the training loss with Bayesian regularisation. These steps were done
 223 iteratively until the best combination of the number of hidden layers and the corresponding number of neurons that
 224 provided the minimum error was found. According to the review paper by Cabaneros et al. (2019), a shallow neural
 225 network with one hidden layer and enough neurons in the hidden layers can fit any finite input-output mapping problem
 226 for non-linear relationship. In the network training process, the number of neurons varied from 2 to 10 neurons per layer
 227 with an incremental factor of 2 neurons in each simulation, and from 10 to 25 per layer with an incremental factor of 5
 228 neurons in each simulation. To keep the method simple, we consider only one or two layers in the simulation process
 229 because the computing requirements could rise exponentially with the number of layers and neurons. Once we pick the
 230 suitable method configuration, the method estimates number concentration using testing data. Finally, the selected

231 performance metrics, described in Section 2.4, can be calculated and we evaluate which approach is the most suitable for
232 size distribution estimation.

233 **2.4 Other methods as comparison with the neural network method**

234 In order to demonstrate the performance of the FFNN method, we perform similar procedures applying other simpler
235 methods, which have been widely used as means of data imputation (Junger and Ponce De Leon, 2015). They include
236 univariate and multivariate methods. The former includes unconditional mean (UM), median (MD), linear interpolation
237 (LinI), logarithmic interpolation (LogI), next neighbour interpolation (nNI) and previous neighbour interpolation (pNI),
238 where nNI was implemented as the next value carried backward while pNI as the previous value carried forward. The
239 multivariate methods used in this study are conditional mean based on a linear regression of meteorological parameters
240 and other particle size number concentrations as inputs (CM–met and CM–PSD, respectively). These methods are
241 implemented as a comparison with the FFNN method.

242 **2.5 Performance metrics**

243 We choose the optimal combination of the number of hidden layers and the corresponding number of neurons by checking
244 its mean absolute error (MAE), which is a simple way to illustrate the residuals of the estimated values by the estimation
245 method. In order to identify which size bin manage to be predicted best, two metrics are used, namely coefficient of
246 determination (R^2) and normalised root-mean-square error (NRMSE). R^2 measures how well the observed outcomes are
247 replicated by the estimation method, based on the proportion of total variation of outcomes explained by the estimation
248 method. NRMSE represents the standard deviation of the estimated errors with respect to its mean. NRMSE is used rather
249 than commonly used RMSE because the number concentrations of the different size range are of different magnitudes.
250 The comparison in different size range becomes different if RMSE is not normalised with its mean.

$$\text{MAE} = \frac{\sum_{i=1}^n |y_i - \hat{y}_i|}{n} \quad (3)$$

$$R^2 = 1 - \frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{\sum_{i=1}^n (y_i - \bar{y})^2} \quad (4)$$

$$\text{NRMSE} = \frac{\sqrt{\frac{\sum_{i=1}^n (y_i - \hat{y}_i)^2}{n}}}{\bar{y}} \quad (5)$$

251 where y_i , \hat{y}_i and \bar{y} represent the i^{th} measurement value, the y^{th} estimated value by the estimation method and the mean of
252 the all the measurement data, respectively. n notates the total number of the valid measurement data.

253 **3 General data analysis**

254 **3.1 Environmental condition**

255 Hussein et al. (2019) and Zaidan et al. (2020) investigated and described the effect of local weather conditions,
256 respectively. Here we describe briefly the meteorological conditions during the measurement period as background
257 information. Starting from August 2016, the daily temperature decreased gradually from 40°C to its tough 0°C in February
258 2017. It rose gradually to 40°C in August 2017. During the measurement period, the hourly median value was 19.9°C
259 (Figure 3a). RH varied quite a lot from 10% to 100%, with an hourly median of 52.3%, and did not seem to have a
260 seasonal pattern (Figure 3b). In summer months, wind appeared be stronger but the wind direction is more stable, mostly

261 from northwest (270° – 360°). In cold months, averaged wind speed was lower but wind blew from fluctuating direction.
262 During the whole measurement period, wind speed ranged between 0 – 6 m s^{-1} and its median is 1.39 m s^{-1} (Figure 3c–d).
263 Air pressure varied in a range from 892 to 912 hPa and its hourly median was 900 hPa . In spite of the narrow range of
264 variation, winter months seem to have slightly higher air pressure than summer months (Figure 3e).

265
266 Meteorological conditions have been suggested to influence particle number concentration. Hussein et al. (2019)
267 demonstrated that number concentration had a rather complex relationship with temperature. Furthermore, number
268 concentration of submicron had a decreasing trend with respect to the wind speed which indicates that most of the
269 submicron fraction is originated from local sources such as combustion processes. Meanwhile, the number concentration
270 of coarse particles had higher concentrations at stagnant conditions and when the wind speed is higher than 5.5 m s^{-1} . It
271 is mainly because of road dust resuspension and might also be attributed to dust storm via long-range transport Hussein
272 et al., 2019. In this study, we further explore how wind direction influences the particle number concentration (Figure 4).
273 Wind coming from the northwest (225° – 325°) was generally stronger, but lower particle number concentration was
274 detected because the measurement area is at the outskirts of downtown. Wind from East and South (45° – 225°) has a lower
275 wind speed but a more intense hourly particle number concentration can be detected. From that direction sits the
276 urban city where all kinds of industrial activities take place. When considering only coarse particles, relatively high
277 number concentration is found when south-westerly wind is strong. This can further serve as an evidence that the source
278 of coarse particles in that region might come mostly from long range sea salt from Dead Sea or dust particles from nearby
279 deserts.

280 3.2 General pattern of particle size distribution

281 Hourly total number concentration ranged from $1.90 \times 10^3 \text{ cm}^{-3}$ to $1.52 \times 10^5 \text{ cm}^{-3}$ and its median was $1.36 \times 10^4 \text{ cm}^{-3}$. Figure
282 5a performed moderate seasonal pattern in general: lower in summer months and higher in colder months. Hussein et al.
283 (2019) also characterised the modal structure of the particle number size distribution for the same site. Four modes have
284 been detected by lognormal fitting, as known as DO-FIT algorithm and modal structure (Hussein et al., 2005; Hussein et
285 al., 2019), revealed that the mode number concentrations of the nucleation, Aitken, and coarse modes were lognormally
286 distributed around their geometric mean values: $0.022 \mu\text{m}$, $0.062 \mu\text{m}$, and $2.3 \mu\text{m}$ respectively. However, the accumulation
287 mode number concentration had two distinguished modes with particle diameter centred at $0.017 \mu\text{m}$ and $0.39 \mu\text{m}$. As
288 seen in Table 1, the total number concentration of all particle size ($1.70 \pm 1.26 \times 10^4 \text{ cm}^{-3}$) is mostly accounted by Aitken
289 mode (45 – 80% , average: $1.09 \pm 1.01 \times 10^4 \text{ cm}^{-3}$), followed by nucleation mode (10 – 50% , average: $0.48 \pm 0.32 \times 10^4 \text{ cm}^{-3}$).
290 Accumulation mode (0 – 15% , average: $0.13 \pm 0.08 \text{ cm}^{-3}$) comes third and only less than 0.5% of the total particle number
291 concentration contain coarse particles with an average of $2.13 \pm 2.80 \text{ cm}^{-3}$ (Figure 5b–e). Seasonal pattern of the total
292 number concentration resembles the Aitken composition: lower proportion in summer months and higher in colder
293 months. The ratio of nucleation mode performs in an opposite way. The seasonal variation of total number concentration
294 is due to the more suppressed boundary layer in winter (Teinilä et al., 2019) and the elevated wood combustion (Hellén
295 et al., 2017). The particle number of accumulation and coarse mode steadily stay at a low proportion line, which did not
296 account for the total number concentration. It is also noticed that dust episodes occurred with the concentrations that often
297 exceeded 2 cm^{-3} and the daily concentration in the course of these episodes can rise to 20 cm^{-3} . These episodes were often
298 found in spring from February to May and some episodes can last for up to one week.

299

300 Similar to many other urban environments, the diurnal pattern observed in this study reflects the combustion emissions
301 from traffic activity, which is more during the workdays (Hussein et al., 2019). The two peaks of the nucleation mode
302 and Aitken mode in the cold months are relevant for the morning and the afternoon traffic rush hours, which are similar
303 to those noticed in most cities in other countries. In warmer months, the diurnal cycles are not as distinct, but a sharp peak
304 of nucleation mode around noon is found, which is associated with the occurrence of new particle formation. These events
305 occurred very often in the summer as suggested by Hussein et al. (2020). The amplitude of diurnal cycles of coarse mode
306 is small while the patterns of accumulation are not clear (Figure 6).

307 **3.3 Correlation analysis**

308 Figure 7 demonstrated the interaction among the whole measured spectrum shows three range clusters based on their
309 correlation with the number concentration at other bin sizes: 0.01–0.205 μm , 0.205–0.875 μm and 0.875–10 μm . 0.01–
310 0.205 μm and 0.875–10 μm fall entirely within the size range detected by SMPS and OPS, respectively. The 5-min number
311 concentration of smaller size and bigger size bins have clear and strong correlation with the concentration of its
312 neighbouring size bin. However, particles of size 0.205–0.875 μm are located in the overlapping regions by the two
313 instruments; as a result, do not correlate well with other size bins. The correlation of 5-min particle size distribution with
314 meteorological parameters are generally low. Temperature appears to be the most correlated parameters for all bin sizes
315 among all the parameters we used in this study. Smaller size range have higher Pearson's correlation coefficient (R) than
316 larger size range for WD, WS and P.

317
318 The 5-min averaged data show similar correlation for the particle size distribution except for the smallest size bin. The
319 hourly and daily data have higher correlation with the other size bins which are also monitored by SMPS. The 5-min
320 averaged data show different correlation from the hourly and daily averaged data performed by Zaidan et al. (2020). The
321 correlations of 5-min size distribution with all meteorological variables are below 0.5 for all size range. However, for
322 hourly and daily averaged data, R is much higher in specific size bins. Hourly and daily temperature, in particular, show
323 increasing R with larger particle size for accumulation and coarse mode. Overall, the correlations increase with the longer
324 averaging windows. This might be due to the buffer period the meteorological conditions act on the dispersion of particles.
325 Based on this result, using data with finer temporal resolution might be considered to be less influential to the estimation
326 accuracy.

327 **4 Evaluation of the proposed method**

328 **4.1 General evaluation**

329 Figure 8 illustrates how well the three approaches of the proposed FFNN perform in term of R^2 and NRMSE.

330 **Approach 1 (Size distribution estimation based on meteorological parameters only, FFNN–met):** For more than half
331 out of the 23 size bins, 2 layers and 15 neurons is the best combination where the residuals are the lowest (Table 2).
332 Owing to the poor correlation with meteorological condition, we expect a low correlation of determination even using the
333 optimal configuration neural network ($R^2 = 0.22\text{--}0.58$). The R^2 are low at the nucleation mode ($0.01 < D_p < 0.03 \mu\text{m}$) of
334 the whole size distribution around nucleation mode ($R^2 \sim 0.2$). The rest of the size bins have better and more stable
335 performance ($R^2 = 0.4\text{--}0.58$). This shows that the instrument might have a poor detection efficiency for particles of smaller
336 size. The performance of FFNN method using 5-min data for all size bins ($R^2 = 0.22\text{--}0.58$) is worse than using daily data

337 ($R^2 = 0.77$) performed in Zaidan et al. (2020). Compared with hourly data ($R^2 = 0.66$), the overall performance of the
338 method using 5-min data is comparable ($R^2 = 0.67$).

339 **Approach 2 (Size distribution estimation based on other particle sections only, FFNN-PSD):** This approach works
340 well with most combination of number of layers and neurons. They do not show a clear difference among the combinations
341 we choose. There is no single combination which entirely outperform the others in all size bins. We summed up the MAE
342 for all size bins and decided to stick to 2 layers and 10 neurons with the overall lowest residuals (Table 2). R^2 are all
343 above 0.97 for all bin sizes, and NRMSE are 0.01–0.25 for all bin sizes. The results are expected because there are 22
344 inputs and one output. Relatively worse correlation at the edges of size bins ($0.01 < D_p < 0.02 \mu\text{m}$; $6 < D_p < 10 \mu\text{m}$) is found
345 because of the lack of nearby size bins which has high correlation with the corresponding size bin. Another reason could
346 be that the instrument has a higher detection limits for smaller particles (Liu et al., 2014). The poorer performance for
347 smaller size might be due to a coarser sizer resolution compared to other SMPS components (Tritscher et al., 2013), so
348 that NanoSMPS does not reflect the real enough size distribution in the atmosphere. Relatively poor estimation
349 performance at the middle size range ($0.15 < D_p < 0.5 \mu\text{m}$) in the whole measured spectrum is because of the overlapping
350 of instruments. This also ascertain the importance of creating a better algorithm when we merge two or more size
351 distribution by different instruments. In this study, the measuring techniques and the measuring targets are different by
352 the SMPS and OPS. The merging of the two measuring targets, the optical particle diameter and the electrical mobility
353 diameter, might create significant uncertainties (DeCarlo et al., 2004; Tritscher et al., 2015). The estimation of certain bin
354 size by other bin sizes can be thought of replacing negative values in the raw data by particle sizers. While some instrument
355 manufacturers create built-in algorithms to replace with artificial non-negative numbers, most end-users simply remove
356 the seemingly impossible negative values from the dataset. The perfect way to do it is to have a parallel instrument that
357 overlaps with that particle size range. However, in many cases, this is not possible as a result of financial constraints.
358 Therefore, we shall rely on the mutual relationship between the size sections in the aerosol population. Negative values
359 appear often at size bins with very low number concentration (usually in coarse mode). Instead of eliminating them, this
360 alternative could maintain the symmetry of the error distribution of the number concentration (Viskari et al., 2012) and
361 minimise the uncertainties caused.

362 **Approach 3 (Size distribution estimation based on meteorological parameters and other particle sections):** The
363 general results are similar as in PSD. However, the more input variables do not enable the approach to work better. At
364 some bin size the R^2 are even slightly smaller than PSD solely. Since meteorological data show low correlation with most
365 portion of measured spectrum. In that approach, the addition of meteorological parameters is not beneficial to the
366 estimation process. Due to the lack of improvement in the method development, we will only focus on the two methods:
367 FFNN-met and FFNN-PSD from now on.

368
369 In order to highlight the performance of the FFNN methods in terms of accuracy and reliability, we compare the FFNN
370 methods with other simpler methods, the results as shown in Table 3 for R^2 and Table 4 for NRMSE. The R^2 of the
371 univariate methods UM and MD are close to 0 because their imputation are over-simplified and imply the replacement of
372 a missing value by a constant. This can be further validated by the narrow range of the estimated particle concentrations
373 in Figure 9a–b. The remaining univariate interpolation methods LinI, LogI, nNI and pNI showed good results in general
374 ($R^2 = 0.82$ – 0.92 , $\text{NRMSE} = 0.57$ – 0.88), but failed to perform even fairly at some particle size bins. This implies that these
375 methods are not stable for the whole spectrum of the particle size distribution. Some of the estimated particle
376 concentrations are off from the 1:1 line, which implies that the estimation of some particle bins are not as accurate (Figure

377 9c–f). The performance results of the multivariate methods CM–met and CM–PSD are comparable to FFNN–met and
378 FFNN–PSD, but both CM methods show weaker performance than FFNN methods in terms of R^2 and NRMSE no matter
379 whether meteorological (CM–met: $R^2 = 0.52$, NRMSE = 1.39; FFNN–met: $R^2 = 0.67$, NRMSE = 1.13) or particle size
380 distribution data (CM–PSD: $R^2 = 0.99$, NRMSE = 0.17; FFNN–PSD: $R^2 = 1.00$, NRMSE = 0.07) is used as inputs. The
381 pattern of performance of the multivariate methods is also similar to those of FFNN, i.e., relatively poor performance at
382 the edges of size bins ($0.01 < D_p < 0.02 \mu\text{m}$; $6 < D_p < 10 \mu\text{m}$) and the overlapping region ($0.15 < D_p < 0.5 \mu\text{m}$). When
383 combining the whole spectrum, FFNN methods (Figure 9i–j) appear to have narrower bands than CM methods (Figure
384 9g–h) along 1:1 line, which indicate the methods work similarly across the particle size spectrum. Although the
385 multivariate method CM–PSD (Figure 9h) also rely on the mutual relationship between the size sections in the aerosol
386 population, this method is not as accurate and stable as our proposed FFNN–PSD.

387

388 From the perspective of physics, particles in the nucleation mode ($0.01 < D_p < 0.03 \mu\text{m}$) are more sensitive to
389 transformation processes due to their volatility and rather unstable nature (Morawska et al., 2008). This leads to a
390 relatively short lifetime in the atmosphere (Al-Dabbous et al., 2017), hence, the relationships between the input variables
391 and the nucleation mode are not well established. Al-Dabbous et al. (2017) demonstrated that accumulation mode particles
392 ($0.1 < D_p < 0.3 \mu\text{m}$) have much longer lifetimes compared to smaller particles, causing them to be transported for larger
393 distances (Laakso et al., 2003); therefore, the mapping of the relationships between long–range transported accumulation
394 mode particles and covariates is supposed not to well understood. However, the relative prediction ability in this study is
395 not lower given that local meteorological variables were used as input variables. The possible reason is that this mode
396 falls exactly in the instrumental overlapping regions, which leads to a lower predictability. The locally-produced Aitken
397 mode particles ($0.03 < D_p < 0.1 \mu\text{m}$) are less effectively removed by transformation processes (e.g. evaporation and
398 coagulation) from the atmosphere, compared with nucleation mode ($0.01 < D_p < 0.03 \mu\text{m}$), allowing the estimation methods
399 to better understand their relationships with the input variables, which is in alignment with Al-Dabbous et al. (2017).

400 **4.2 Temporal pattern**

401 Figure 10 shows the diurnal discrepancies during workdays and weekends. Relative particle number concentration was
402 defined by the estimated concentration with respect to the measured concentration. Values above 1 indicates
403 overestimation while values below 1 suggests underestimation. For approach 1 (FFNN–met), except for the overlapping
404 size bin, which are underestimated by more than 50% at all time range, the difference between estimated and measured
405 hourly number concentration is within 50% during both workdays and weekends. Overestimation is found in early
406 morning before 3 a.m. during workdays for all size bins, especially for UFP. Following the overestimation, at about 6
407 a.m. in the morning, the estimated number concentration appears to understate by up to 40%, especially at size bins below
408 $0.1 \mu\text{m}$. Along the day, the estimation uncertainties are rather small until in the evening from 6 p.m. to 11 p.m. where
409 estimated UFP number concentration show moderate overestimation one more time. It reveals that FFNN–met fails to
410 catch the diurnal pattern from 6 p.m. to 7 a.m. in particular for UFP. The pattern of the performance for weekends does
411 not appear to be as distinctive as on workdays. It shows the overestimation not only for UFP in early morning about 3
412 a.m., but also at the upper edge larger than $5 \mu\text{m}$ from 3 a.m. to 4 p.m.. At 7 p.m. onwards until noon, an underestimation
413 is found at all size bins. For approach 2 (FFNN–PSD), except the overlapping size bin, which has a significant
414 overestimation from 6 p.m. to 7 a.m., most show negligible 10% uncertainty during both workdays and weekends. The

415 performance over weekends show relatively stronger uncertainties. The smallest bin at 0.01 μm is slightly understated for
416 all hours of a day. Other than these, FFNN-PSD manages to catch fairly well the diurnal pattern for all size bins.

417

418 Figure 11 further shows the monthly deviation in estimation performance. For approach 1 (FFNN-met), higher R^2 is
419 found in November, February and April in the range of SMPS. Other than that, no observable variation in R^2 in approach
420 1 (FFNN-met). For approach 2 (FFNN-PSD), except in January when all the rows were eliminated because of the lack
421 of wind information, performance in the other months is steady for most size range. At 0.21 μm , the difference in
422 estimation performance varies across different months. R^2 in winter months are 0.76, 0.36 and 0.61, in November,
423 December and February, respectively, while R^2 exceeds 0.9 in other months. This unexpectedly low R^2 only occurs in the
424 winter months at the overlapping size range. It can be speculated that the measurements by the two instruments differ in
425 a larger extent during winter. This might be attributed to sensor drift and a number of interference artefacts for particle
426 measurements associated with several factors, such as relative humidity, temperature and other gas-phase species, which
427 were demonstrated by several researchers (e.g. Lewis et al., 2016; Popoola et al., 2016). Another reason for the difference
428 in estimation performance can be that the percentage of complete rows in these months are lower than the other months.
429 The drop in data points might impose an influence to the estimation performance. Especially in June, at the few size bins
430 close to the larger edge, R^2 ranges from 0.9 to 0.7. Besides that, some low R^2 can be also found in individual month at
431 both edges of size range, which does not appear to show any patterns.

432

433 In short, the estimation ability for lower edge ($0.01 < D_p < 0.03 \mu\text{m}$) is found worse in both approaches. The performance
434 of the FFNN method in mid-range ($0.15 < D_p < 0.5 \mu\text{m}$) and upper edge ($6 < D_p < 10 \mu\text{m}$) are relatively worse for the
435 approach with other fractionated size bins as input variables according to the aforementioned statistical performance
436 indicators. All statistical estimation simulations are based on the previous history of relationships between the inputs and
437 outputs. As a result, the estimation simulations for different size ranges have significantly unique connections. The
438 approach by meteorological parameters considers only 6 predictor variables so the accuracy is lower than FFNN-PSD. It
439 might not seem surprising that the deviations between the measured and estimated size distribution were not substantial
440 ($R^2 > 0.97$, $\text{NRMSE} < 0.25$) because FFNN-PSD takes 22 other size bins as predictor variables. This, still, gives a clue
441 that the proposed FFNN method can provide adequate solutions to particle size distribution prognostic demands.
442 Furthermore, this FFNN method outperforms the other selected widely used methods in terms of its accuracy and
443 reliability. The estimation of certain bin size by other bin sizes can be thought of replacing 'negative' values in the raw
444 data by particle sizers, including SMPS we used in this paper. Instead of eliminating the negative values, they can be
445 estimated by other size bins with a high accuracy in order to keep the symmetry in data error distribution (Viskari et al.,
446 2012).

447 **5 Conclusion**

448 This paper presents the evaluation of imputation methods by means of feed-forward neural network (FFNN) for estimating
449 particle number concentration at various particulate size bins. Input predictors include a merged particle size distribution,
450 by a scanning mobility particle sizer (NanoSMPS) and an optical particle sizer (OPS), which covers size range from 0.01
451 to 10, and meteorological parameters, including temperature (Temp), relative humidity (RH), wind speed (WS), wind
452 direction (WD) and ambient pressure (P). The measurements were collected in an urban background region in Amman,
453 the capital of Jordan in the period of 1 Aug 2016–31 July 2017. The total number concentration ($1.70 \pm 1.26 \times 10^4 \text{ cm}^{-3}$) in

454 the measurement period show moderate seasonal variability owing to the more suppressed boundary layer (Teinilä et al.,
455 2019) and the elevated wood combustion (Hellén et al., 2017) in wintertime. Similar to many other urban environments,
456 the diurnal pattern observed in this study reflects the traffic activity, which has a more pronounced pattern during
457 workdays (Hussein et al., 2019). The amount of coarse particles is negligible in terms of number concentration but dust
458 episodes were found often in spring during the measurement period.

459
460 We proposed three approaches with different input variables: (1) only meteorological parameters, (2) only number
461 concentration at the remaining size bins, and (3) both of the above. We performed optimisation to obtain the optimal
462 configuration of the FFNN methods, which are two layers with 10–15 neurons, balancing the accuracy and the computing
463 resources. The 5-min averaged meteorological parameters give varying number concentration estimation for various size
464 bins ($R^2 = 0.22\text{--}0.58$), which is outperformed by hourly and daily averaged data ($R^2 = 0.66\text{--}0.77$), as demonstrated by
465 Zaidan et al. (2020). The methods using the number concentration at the remaining size bins, both with or without
466 meteorological data, show expected perfect performance ($R^2 > 0.97$). We also compared the FFNN methods with other
467 commonly used methods and the results highlight the high accuracy and reliability of methods by means of neural
468 networks.

469
470 Relatively poor performance of the proposed FFNN methods is found in three regions. At the lower edge ($0.01 < D_p < 0.02$
471 μm) and the upper edge ($6 < D_p < 10 \mu\text{m}$), the number of neighbouring size bins is limited and also the detection efficiency
472 by the corresponding instruments is lower compared to the other size bins. Another noticeable region ($0.15 < D_p < 0.5 \mu\text{m}$)
473 is the overlapping section measured by the two particle sizers and the reason is because of the deficiency of merging
474 algorithm. For all the above approaches, the poorer performance for smaller particles in the nucleation mode could be due
475 to the fact that it is more effectively removed from the atmosphere compared to other modes (Al-Dabbous et al., 2017).
476 An observable overestimation is also found in early morning for ultrafine particles followed by a distinct underestimation
477 before midday. A larger derivation between the measured and the estimated number concentration is found in the winter,
478 which might be caused by sensor drift and interference artefacts (e.g. Lewis et al., 2016; Popoola et al., 2016). Despite
479 the high number of input predictors, the good estimation performance provides an alternative method to fill up the negative
480 values in size distribution raw dataset, which often exist due to misconfiguration problems. Instead of removing the
481 factually impossible data point, this way of replacing negative numbers can maintain a symmetric distribution of errors
482 (Viskari et al., 2012) and minimise the uncertainties caused.

483 **Code/Data availability**

484 The code and data is available upon request.

485 **Author contribution**

486 TH and MZ designed the experiments and TH carried them out. PLF and OS developed the code of the proposed FFNN
487 methods. PLF prepared the manuscript with contributions from all co-authors.

488 **Competing interests**

489 The authors declare that they have no conflict of interest.

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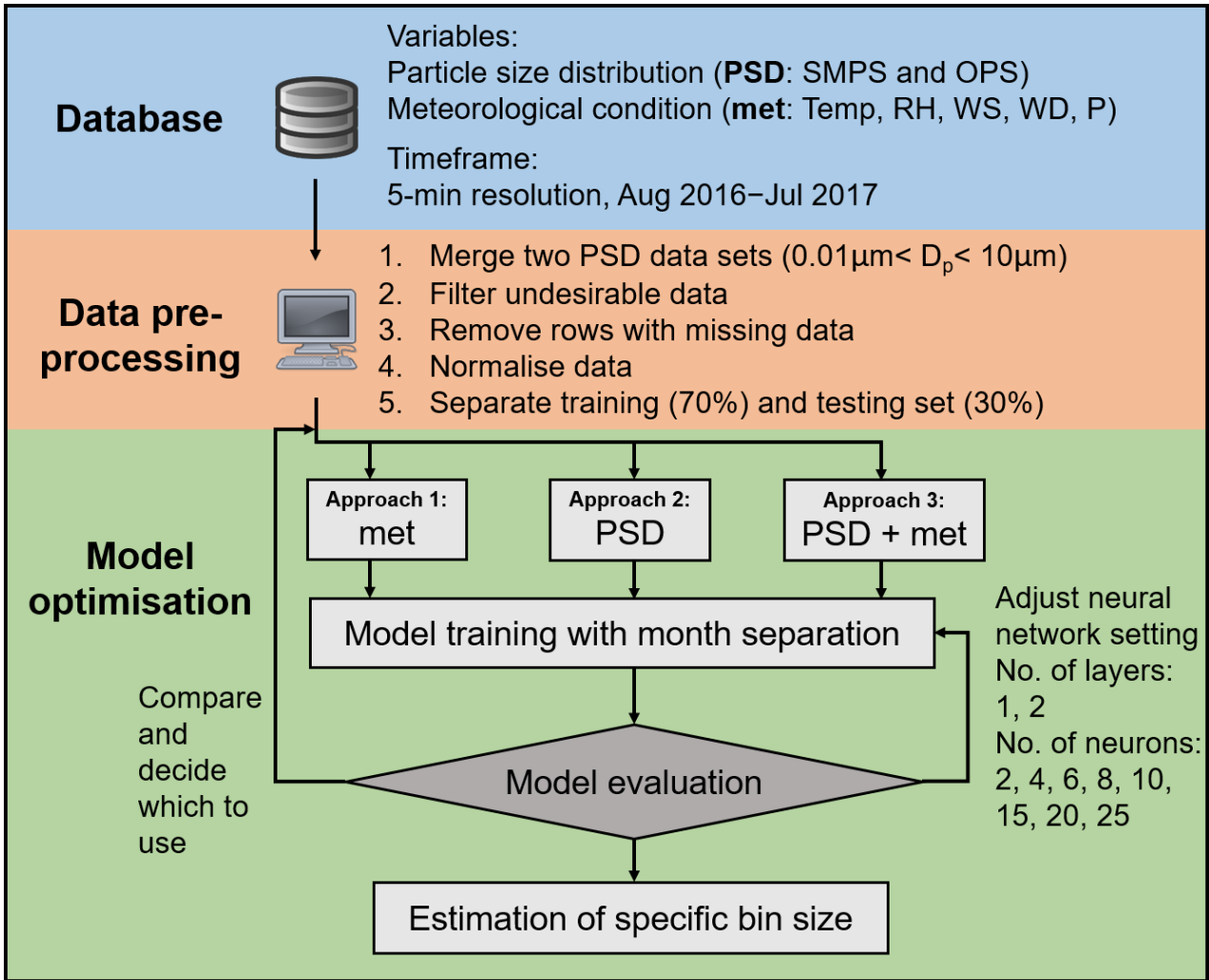


Figure 1. The block diagram describing the methodology of the proposed FFNN method.

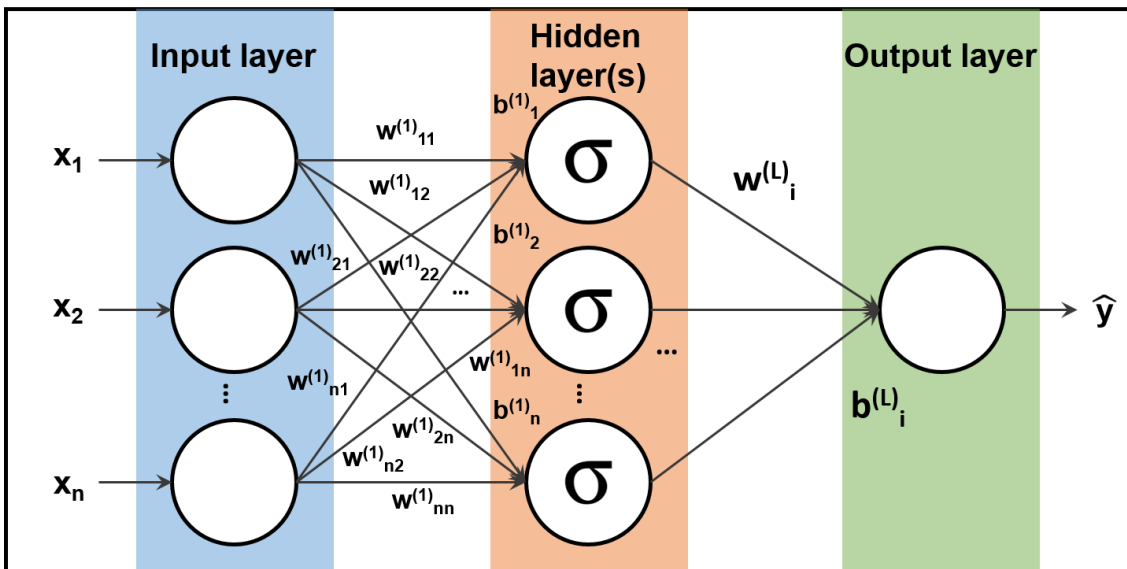


Figure 2. Schematic diagram of a neural network with one hidden layer of sigmoid activation function.

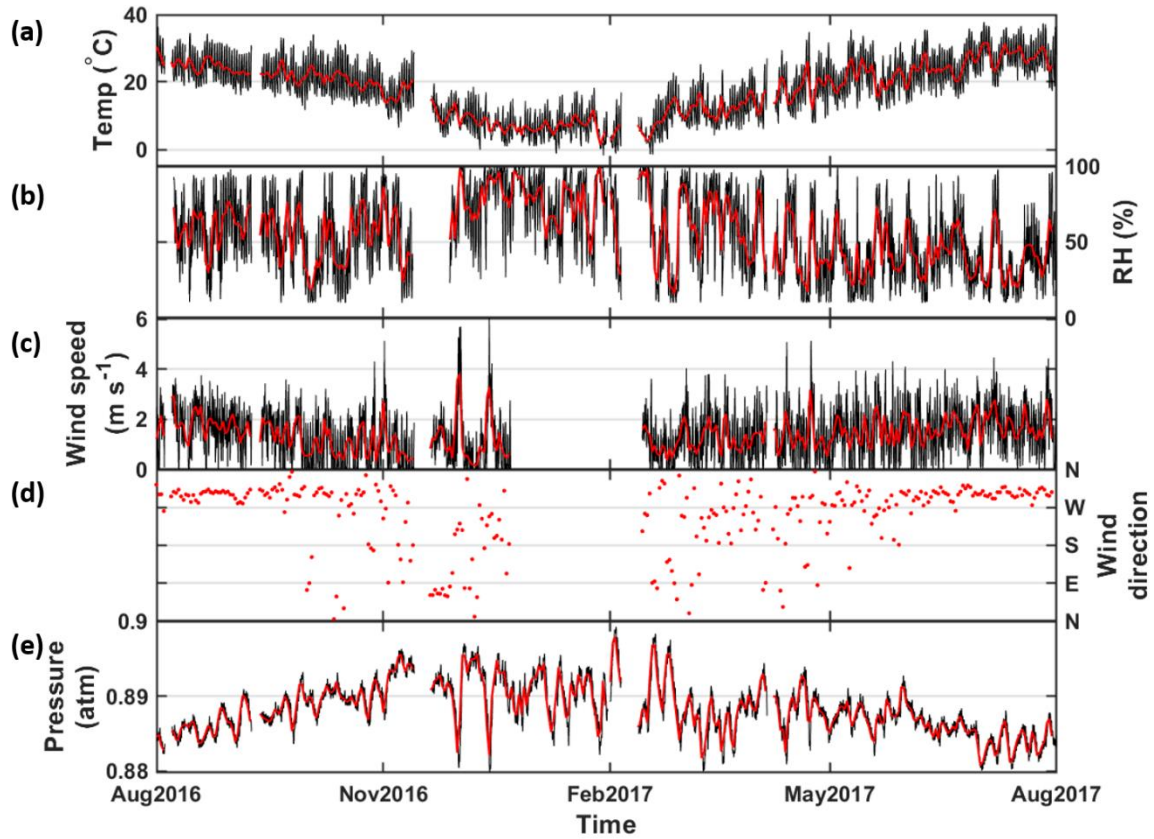


Figure 3. Timeseries of meteorological conditions during the measurement period Aug 2016–Jul 2017. (a–e) denotes temperature, relative humidity, wind speed, wind direction and air pressure, respectively. Black and red represent hourly and daily averaged data, respectively.

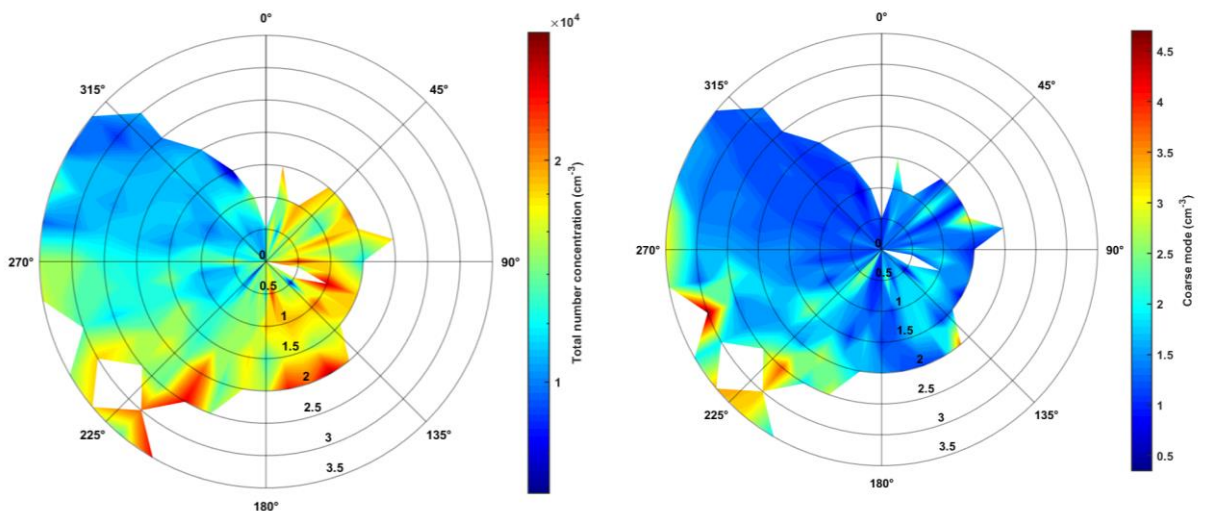


Figure 4. Windrose diagram of total particle number concentration at different direction (in theta axis) and different wind speed (in radial axis). Wind direction and wind speed data are grouped in every 10° and 0.5 m s^{-1} . Warmer color represent higher total particle number concentration. (a) total number concentration, log scale; (b) coarse mode, linear scale. Note the color scales are different.

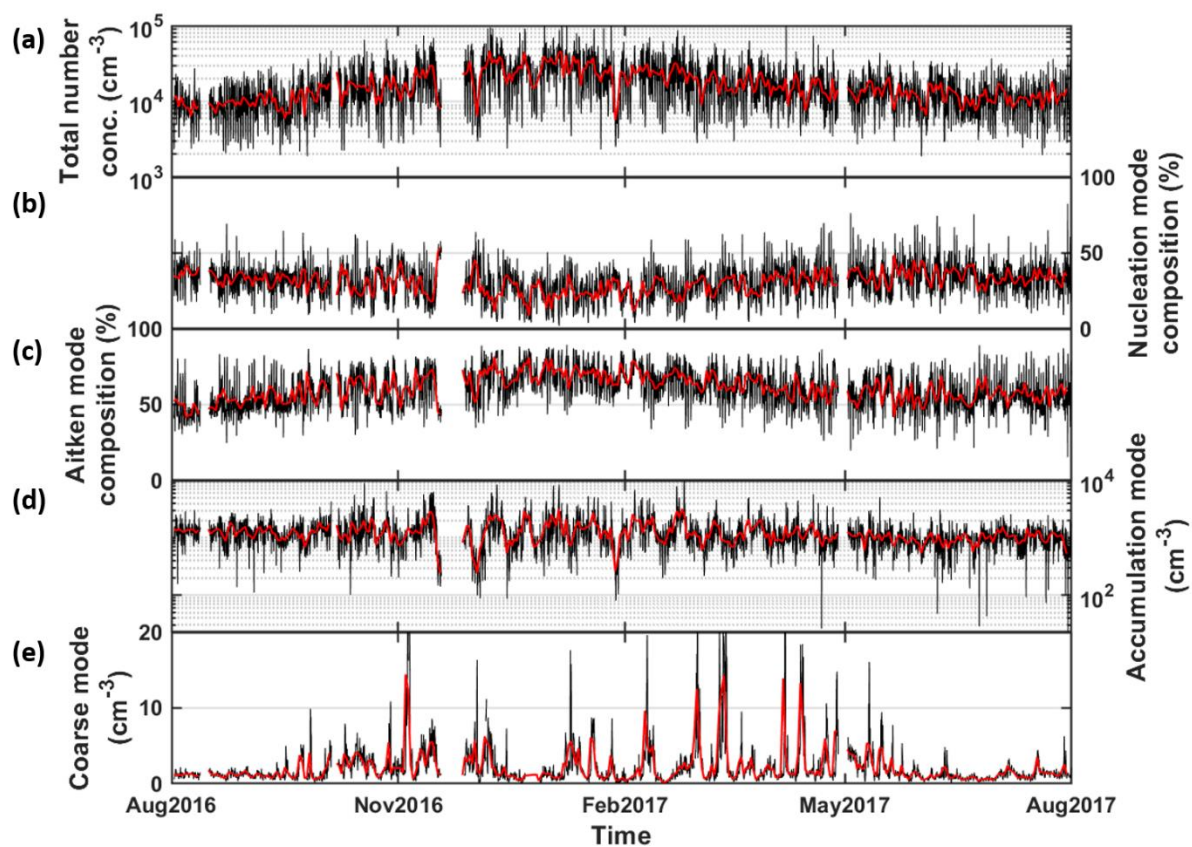


Figure 5. Timeseries of total particle number concentration (in cm^{-3}) of $0.01\text{--}10\mu\text{m}$ in (a). (b–c) indicate the contribution in percentage of nucleation mode and Aitken mode, respectively. (d–e) show the number concentration in accumulation mode and coarse mode, respectively. Black and red represent hourly and daily averaged data, respectively.

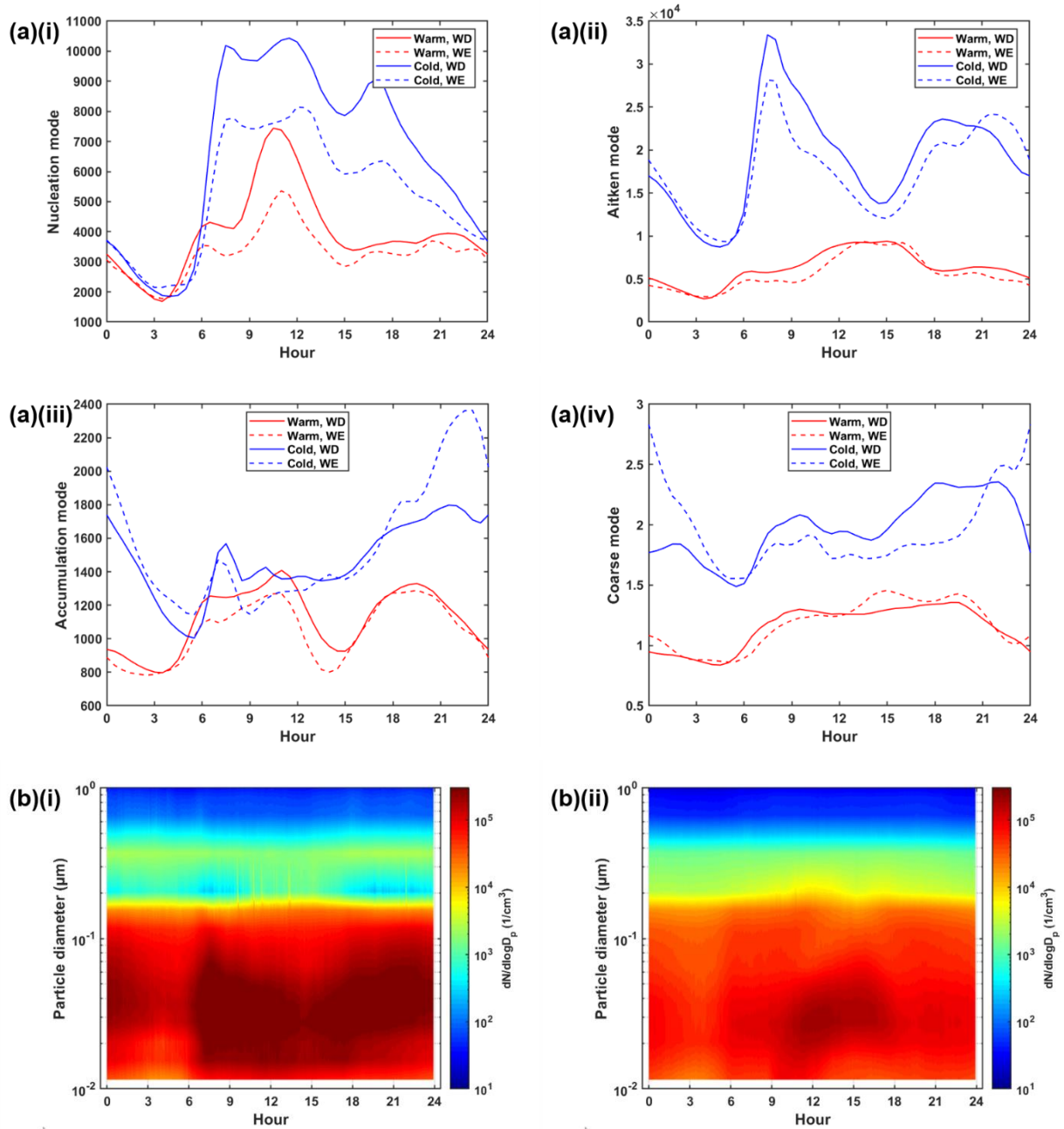


Figure 6. (a) Diurnal cycle of the (i) nucleation mode, (ii) Aitken mode, (iii) accumulation mode and (iv) coarse mode in warm (red) and cold months (blue) during workdays (solid) and weekends (dashed). (b) Particle size distribution in (i) cold and (ii) warm months, coloured by particle number concentration (cm^{-3}). Cold and warm months refer to December–February and June–August, respectively.

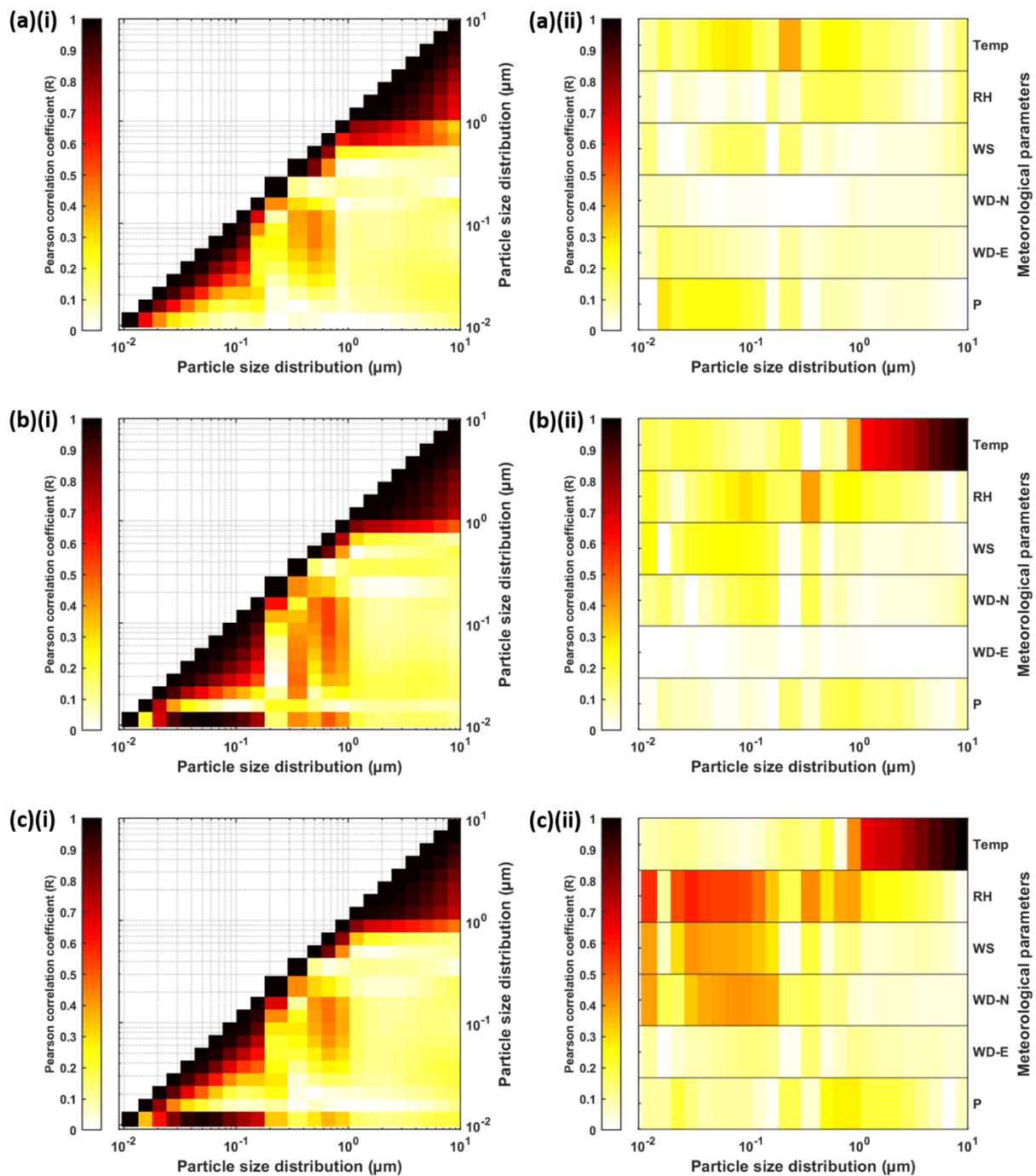
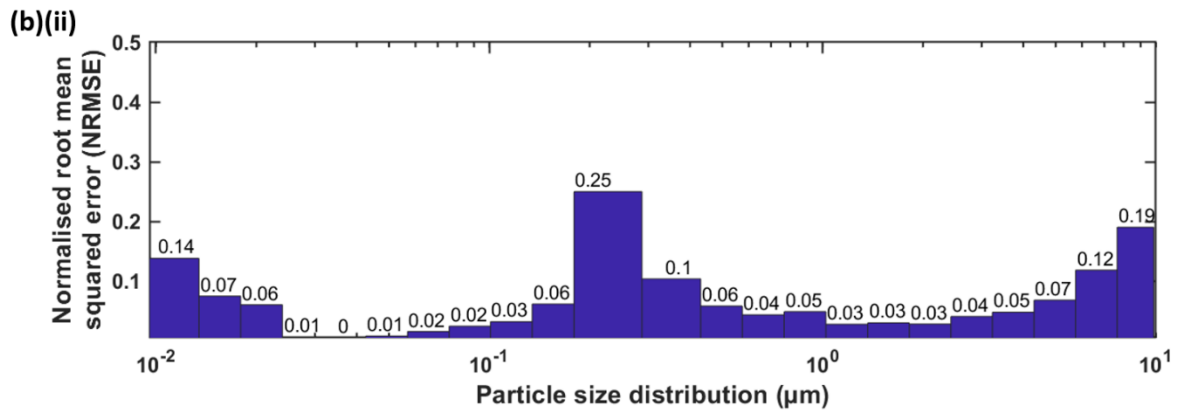
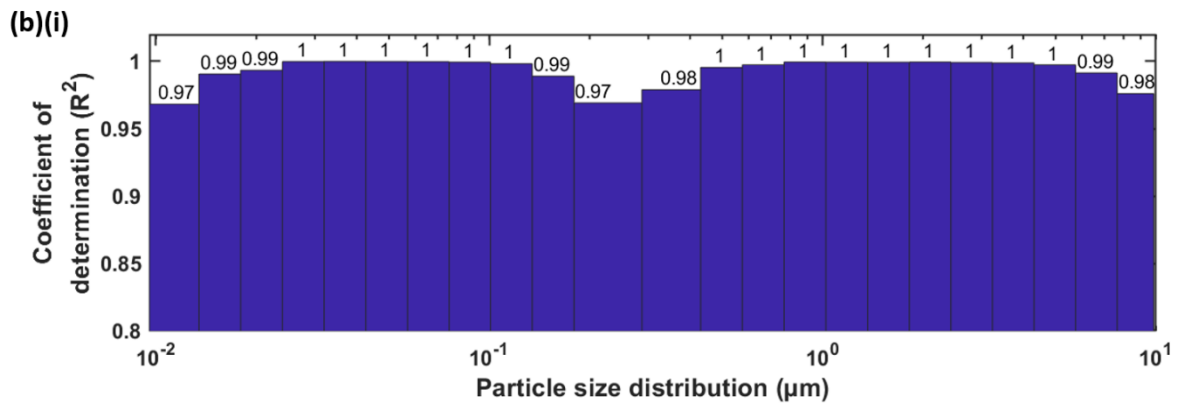
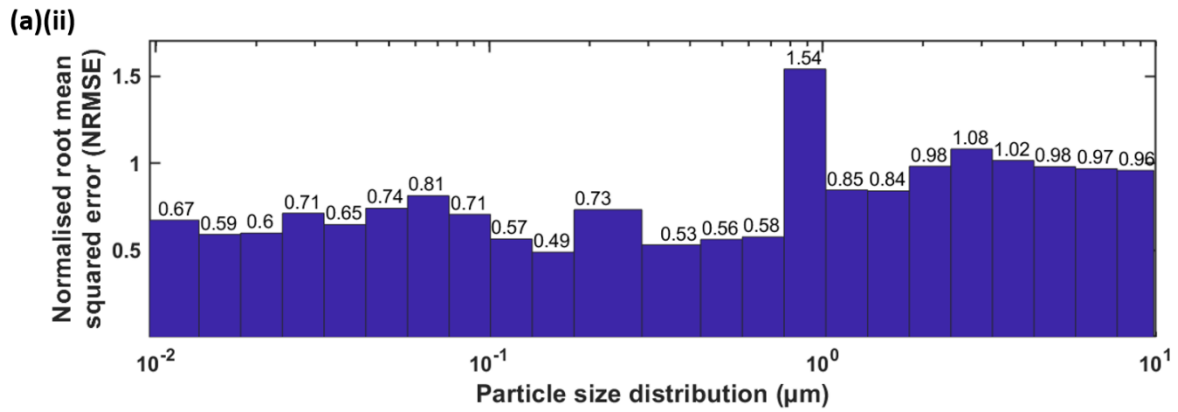
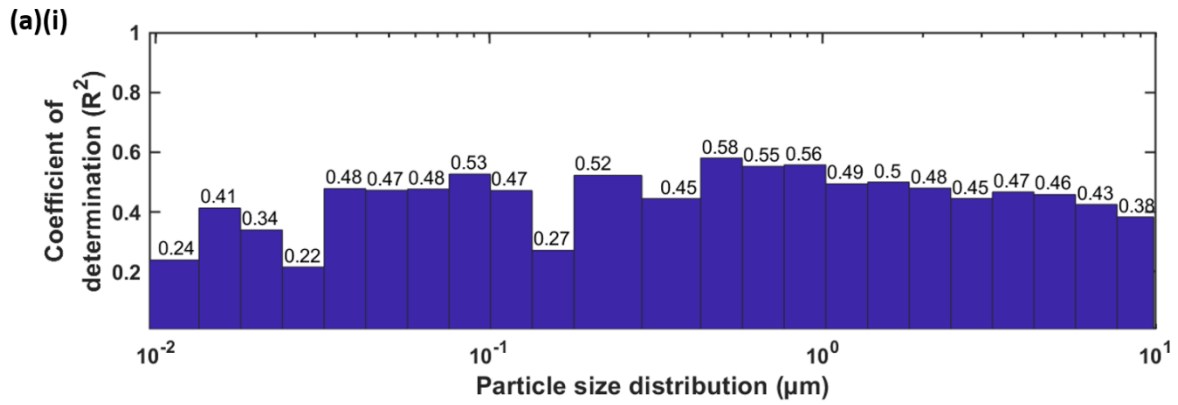


Figure 7. Matrix plots showing the Pearson correlation coefficient (R) of particle size distribution of (a) 5-min, (b) hourly, (c) daily averaging with (i) particle size distribution itself and (ii) meteorological parameters. Darker colour represents a higher correlation.



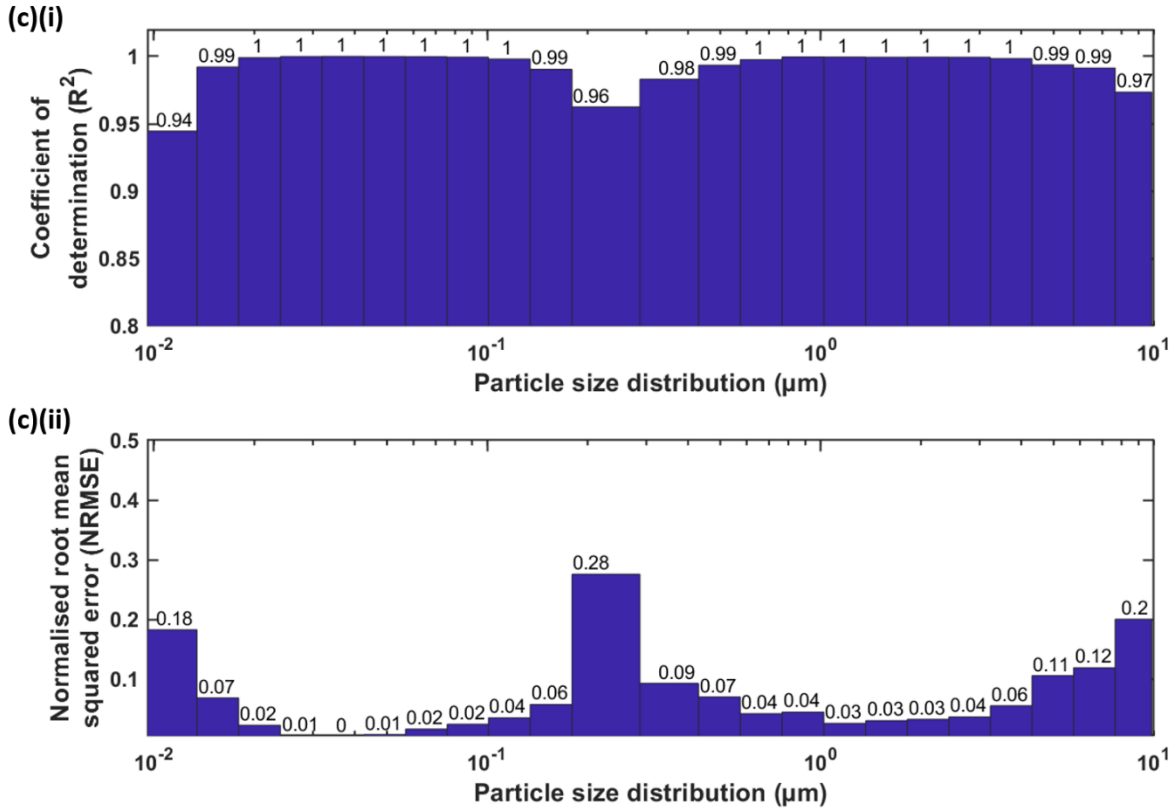


Figure 8. Bar chart showing the evaluation of FFNN approach with (a) only meteorological parameters (Approach 1, FFNN–met), (b) particle size distribution itself (Approach 2, FFNN–PSD), (c) both particle size distribution and meteorological parameters (Approach 3) as inputs. The evaluation metrics for the proposed method include (i) coefficient of determination (R^2) and (ii) normalised root mean squared error (NRMSE).

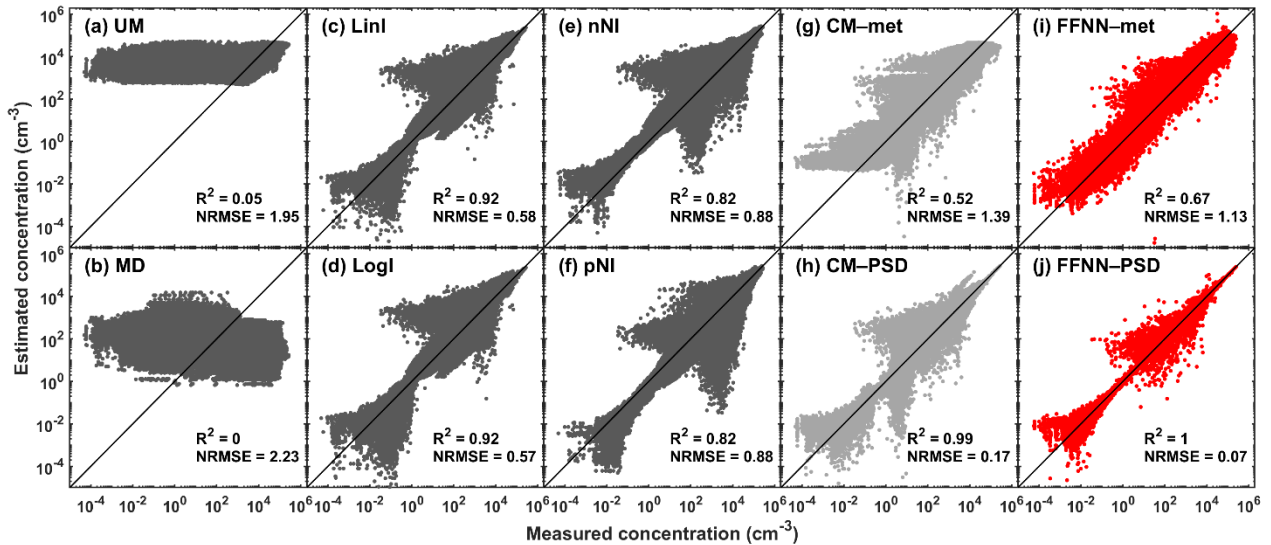


Figure 9. Scatter plots showing the estimated particle concentration (y-axis, in cm^{-3}) against the measured in situ particle concentration (x-axis, in cm^{-3}). (a–f) demonstrate cases of univariate methods including unconditional mean (UM), median (MD), linear interpolation (LinI), logarithmic interpolation (LogI), next neighbour interpolation (nNI) and previous neighbour interpolation (pNI), respectively, in dark grey dots. (g–h) represent multivariate methods conditional mean by regression of meteorological parameters and other particle size number concentrations as inputs (CM–met and CM–PSD, respectively) in light grey dots. (i–j) showcase the proposed feed-forward neural network with meteorological parameters and other particle size number concentrations as inputs (FFNN–met and FFNN–PSD, respectively) in red dots. The black solid line is 1:1 line which gives a reference of perfect estimation. The coefficient of determination (R^2) and the normalised root-mean-square error (NRMSE) of each method for all particle size bins are printed on the corresponding subplots.

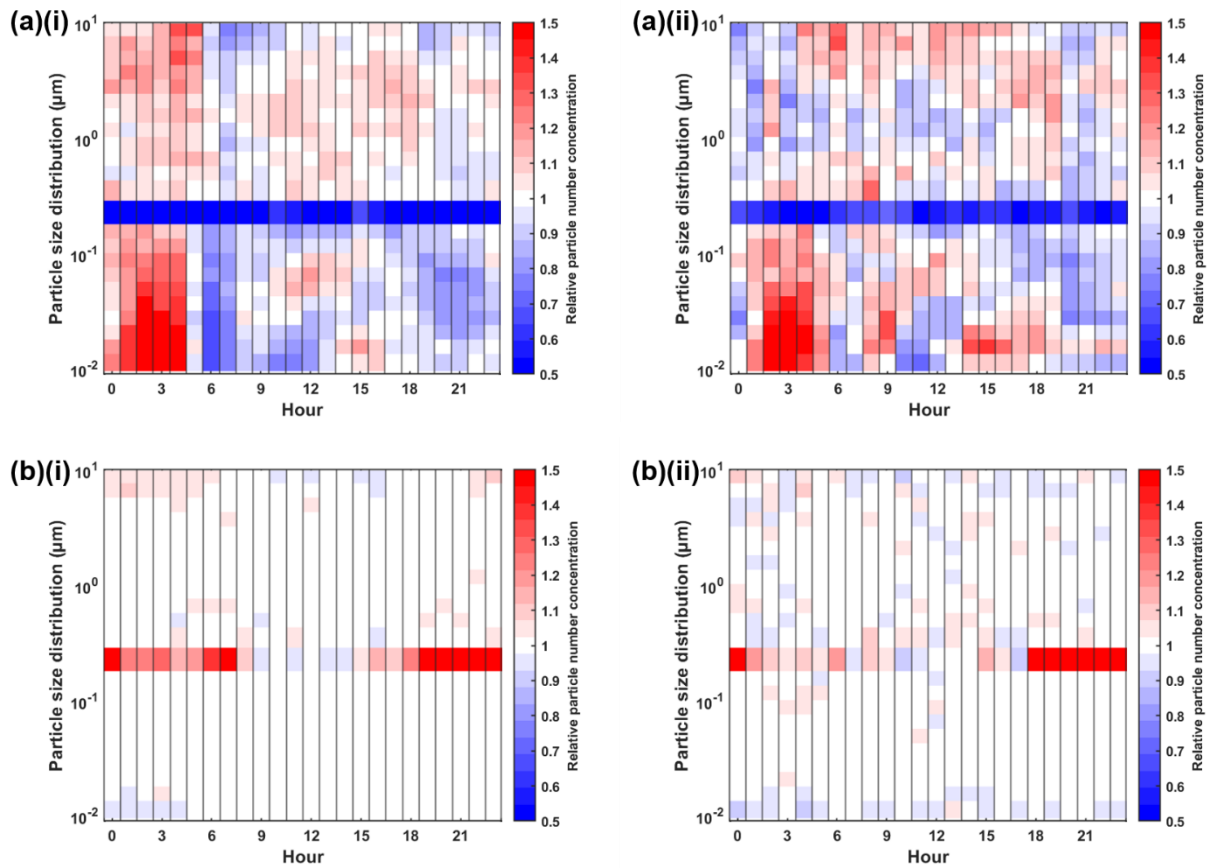


Figure 10. Heatmap showing the hourly median relative particle number concentration of the approach with (a) meteorological parameters (Approach 1, FFNN–met) and (b) particle size distribution (Approach 2, FFNN–PSD) as inputs across different hours of a day (i) in workdays and (ii) in weekends. The relative particle number concentration is defined as estimated concentration with respect to measured concentration. Red colour show overestimation while blue show underestimation.

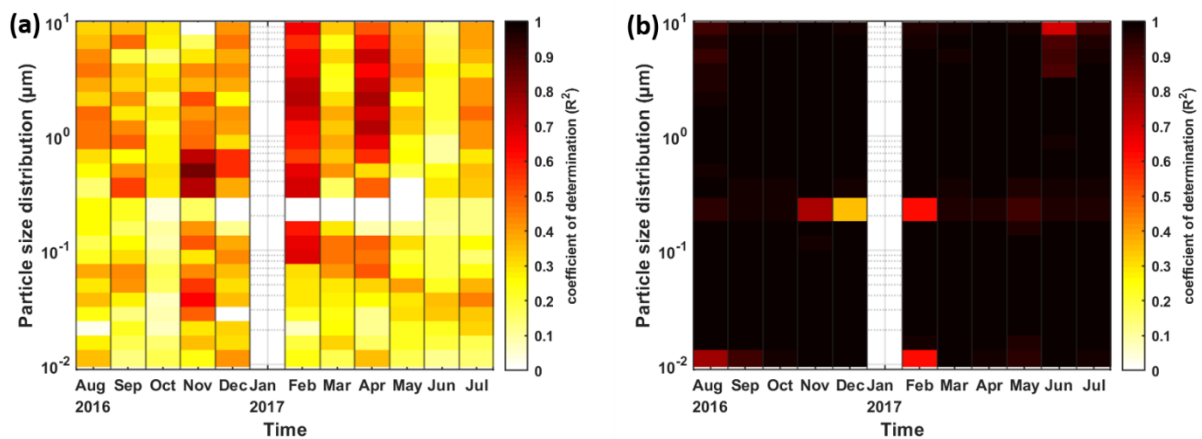


Figure 11. Heatmap showing the coefficient of determination (R^2) of the approach with (a) meteorological parameters (Approach 1, FFNN–met) and (b) particle size distribution (Approach 2, FFNN–PSD) as inputs for different months at different size bins. Darker colour represents a higher R^2 .

653 Table 1. Table showing the descriptive statistics (in cm^{-3}) of total number concentration, nucleation mode, Aitken mode,
 654 accumulation mode and coarse mode. The statistical values include mean, standard deviation, and percentile (10%, 25%,
 655 50%, 75% and 90%).

	Mean	std	10%	25%	50%	75%	90%
Total ($\times 10^4$)	1.70	1.26	0.57	0.85	1.35	2.16	3.31
Nucleation ($\times 10^4$)	0.48	0.32	0.16	0.26	0.41	0.63	0.90
Aitken ($\times 10^4$)	1.09	1.01	0.29	0.45	0.77	1.37	2.35
Accumulation ($\times 10^4$)	0.13	0.08	0.05	0.08	0.11	0.15	0.21
Coarse	2.13	2.80	0.55	0.84	1.29	2.33	4.3

656

657 Table 2. Table showing the best configuration in the form of (the number of layers; the number of neurons) for the
 658 approach by meteorological parameters (FFNN–met) and the number concentration at the other size bins (FFNN–PSD)
 659 as inputs. Mean absolute error (MAE, in cm^{-3}), coefficient of determination (R^2) and normalised root-mean-square error
 660 (NRMSE) are listed for different size bins on each row. The last row concludes the overall selection of the approach with
 661 the best configuration and its corresponding evaluation metrics.

Particle size (μm)	Approach 1 (FFNN–met)				Approach 2 (FFNN–PSD)			
	Best setting	MAE (cm^{-3})	R^2	NRMSE	Best setting	MAE (cm^{-3})	R^2	NRMSE
0.012	2; 10	2640	0.20	0.69	2; 10	334	0.99	0.11
0.015	2; 15	4850	0.42	0.59	2; 8	216	1.00	0.031
0.021	2; 15	6120	0.38	0.58	2; 15	97.8	1.00	0.014
0.027	2; 15	8470	0.41	0.62	1; 25	34.0	1.00	0.0032
0.037	2; 20	8240	0.46	0.66	2; 15	26.3	1.00	0.0024
0.049	2; 15	6610	0.48	0.74	2; 25	33.7	1.00	0.0049
0.066	2; 15	4690	0.46	0.83	2; 10	56.7	1.00	0.013
0.088	2; 15	3040	0.52	0.71	2; 4	66.2	1.00	0.018
0.12	2; 15	1810	0.52	0.54	2; 8	63.1	1.00	0.021
0.15	2; 10	917	0.29	0.49	2; 15	72.5	0.99	0.052
0.21	2; 6	327	0.55	0.71	2; 8	114	0.91	0.31
0.37	2; 10	95.8	0.43	0.54	2; 20	12.9	0.99	0.072
0.49	2; 15	12.1	0.50	0.61	2; 25	0.9630	1.00	0.043
0.66	2; 15	3.03	0.58	0.56	2; 15	0.1995	1.00	0.029
0.88	2; 15	5.65	0.62	1.43	2; 10	0.2202	1.00	0.040
1.17	2; 15	1.43	0.53	0.81	2; 8	0.0680	1.00	0.026
1.56	2; 20	1.44	0.54	0.81	2; 8	0.0816	1.00	0.031
2.08	2; 15	1.84	0.49	0.97	2; 8	0.0825	1.00	0.028
2.77	2; 15	1.02	0.44	1.09	1; 4	0.0573	1.00	0.037
3.70	2; 15	0.52	0.41	1.07	1; 8	0.0329	1.00	0.046
4.92	2; 15	0.28	0.44	1.00	1; 4	0.0254	1.00	0.068
6.56	2; 9	0.11	0.42	0.97	1; 6	0.0206	0.99	0.13
8.75	2; 10	0.060	0.39	0.95	2; 6	0.0169	0.98	0.20
overall	2; 15	2120	0.67	1.13	2; 10	76.6	0.999	0.067

662

663 Table 3. Table showing the comparison of different estimation methods, including unconditional mean (UM, column 2),
664 median (MD, column 3), linear interpolation (LinI, column 4), logarithmic interpolation (LogI, column 5), next neighbour
665 interpolation (nNI, column 6), previous neighbour interpolation (pNI, column 7), conditional mean by regression of
666 meteorological parameters and other particle size number concentrations as inputs (CM–met and CM–PSD, column 8 and
667 9, respectively) and the feed-forward neural network with meteorological parameters and other particle size number
668 concentrations as inputs (FFNN–met and FFNN–PSD, column 10 and 11, respectively). The coefficient of determination
669 (R^2) of each method are listed for different size bins on each row. Negative R^2 are represented as ‘0’ to indicate poor
670 accuracy at the particular particle size bin while ‘NA’ is used to represent the data is not available. The last row concludes
671 the overall evaluation metrics.

Particle size (μm)	Methods/ R^2									
	UM	MD	LinI	LogI	nNI	pNI	CM –met	CM –PSD	FFNN –met	FFNN –PSD
0.012	0	0	0	0	1.00	NA	0.04	0.91	0.20	0.99
0.015	0	0	0.66	0.71	0	0.49	0.14	0.85	0.42	1.00
0.021	0	0	0.92	0.91	0.62	0.33	0.1	1.00	0.38	1.00
0.027	0	0	0.91	0.93	0.69	0.90	0.11	1.00	0.41	1.00
0.037	0	0	0.97	0.97	0.91	0.85	0.12	1.00	0.46	1.00
0.049	0	0	0.98	0.99	0.80	0.80	0.13	1.00	0.48	1.00
0.066	0.14	0	0.96	0.97	0.66	0.81	0.14	1.00	0.46	1.00
0.088	0.31	0	0.97	0.98	0.60	0.64	0.12	1.00	0.52	1.00
0.12	0.41	0	0.92	0.96	0	0	0.07	1.00	0.52	1.00
0.15	0	0	0	0.20	0	0	0.03	0.97	0.29	0.99
0.21	0	0	0	0	0	0	0.24	0.65	0.55	0.91
0.37	0	0	0	0	0	0	0.04	0.9	0.43	0.99
0.49	0	0	0	0	0	0	0.06	0.97	0.50	1.00
0.66	0	0	0	0	0	0	0.07	0.96	0.58	1.00
0.88	0	0	0.20	0.19	0.23	0.11	0.09	0.76	0.62	1.00
1.17	0	0	0	0	0	0.99	0.04	1.00	0.53	1.00
1.56	0	0	0.97	0.97	0.99	0.85	0.04	1.00	0.54	1.00
2.08	0	0	0.84	0.83	0.91	0.67	0.03	1.00	0.49	1.00
2.77	0	0	0.90	0.96	0	0.60	0.02	1.00	0.44	1.00
3.70	0	0	0.76	0.87	0	0.62	0.02	1.00	0.41	1.00
4.92	0	0	0.85	0.94	0	0.41	0.02	1.00	0.44	1.00
6.56	0	0	0.27	0.55	0	0.57	0.03	0.99	0.42	0.99
8.75	0	0	0	0	NA	1.00	0.05	0.97	0.39	0.98
overall	0.05	0	0.92	0.92	0.82	0.82	0.52	0.99	0.67	1.00

672

673 Table 4. Table showing the comparison of different estimation methods, including unconditional mean (UM, column 2),
674 median (MD, column 3), linear interpolation (LinI, column 4), logarithmic interpolation (LogI, column 5), next neighbour
675 interpolation (nNI, column 6), previous neighbour interpolation (pNI, column 7), conditional mean by regression of
676 meteorological parameters and other particle size number concentrations as inputs (CM–met and CM–PSD, column 8 and
677 9, respectively) and the feed-forward neural network with meteorological parameters and other particle size number
678 concentrations as inputs (FFNN–met and FFNN–PSD, column 10 and 11, respectively). The normalised root-mean-square
679 error (NRMSE) of each method are listed for different size bins on each row. The last row concludes the overall evaluation
680 metrics.

Particle size (µm)	Methods/ NRMSE									
	UM	MD	LinI	LogI	nNI	pNI	CM –met	CM –PSD	FFNN –met	FFNN –PSD
0.012	0.84	1.24	1.62	1.73	NA	1.62	0.74	0.23	0.69	0.11
0.015	0.92	1.26	0.45	0.42	0.79	0.55	0.72	0.30	0.59	0.03
0.021	0.91	1.24	0.21	0.22	0.46	0.61	0.70	0.02	0.58	0.01
0.027	1.04	1.28	0.24	0.22	0.46	0.25	0.77	0	0.62	0
0.037	1.08	1.34	0.15	0.15	0.27	0.35	0.85	0	0.66	0
0.049	1.09	1.43	0.13	0.12	0.46	0.46	0.95	0	0.74	0
0.066	1.04	1.50	0.23	0.18	0.66	0.49	1.04	0.01	0.83	0.01
0.088	0.84	1.42	0.16	0.13	0.65	0.61	0.96	0.02	0.71	0.02
0.12	0.59	1.25	0.22	0.16	0.86	0.80	0.74	0.03	0.54	0.02
0.15	1.59	1.13	0.66	0.53	1.64	0.96	0.58	0.10	0.49	0.05
0.21	11.6	1.61	3.7	3.24	4.93	1.53	1.26	0.85	0.71	0.31
0.37	23.8	1.42	1.35	1.12	3.12	1.06	0.70	0.22	0.54	0.07
0.49	185	14.4	4.16	3.53	7.98	1.00	0.83	0.15	0.61	0.04
0.66	672	54.5	2.42	2.32	3.62	2.79	0.82	0.17	0.56	0.03
0.88	485	39.4	2.06	2.07	2.02	2.18	2.20	1.12	1.43	0.04
1.17	1750	143	4.45	3.88	7.84	0.11	1.16	0.07	0.81	0.03
1.56	1750	143	0.19	0.22	0.11	0.46	1.16	0.05	0.81	0.03
2.08	1510	124	0.54	0.57	0.40	0.78	1.34	0.04	0.97	0.03
2.77	2880	236	0.47	0.30	1.48	0.92	1.43	0.04	1.09	0.04
3.70	5750	472	0.69	0.50	1.83	0.86	1.38	0.05	1.07	0.05
4.92	11000	902	0.51	0.34	1.64	1.02	1.32	0.09	1.00	0.07
6.56	27100	2220	1.09	0.86	2.51	0.83	1.26	0.12	0.97	0.13
8.75	52600	4320	4.95	3.33	1.62	NA	1.2	0.21	0.95	0.20
overall	1.95	2.23	0.58	0.57	0.88	0.88	1.39	0.17	1.13	0.07

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