Intercomparison of holographic imaging and single-particle forward light scattering in-situ measurements of liquid clouds in changing atmospheric conditions

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Abstract Upon a new measurement technique, it is possible to sharpen the determination of microphysical properties of cloud droplets using high resolving power imaging. The shape, size, and position of each particle inside a well-defined, three-dimensional sample volume can be measured without holographic methods without assumptions of particle properties. In-situ cloud measurements were carried out at the Puijo station in Kuopio, Finland, focusing on intercomparisons between cloud droplet analysers over the two months on September-November 2020. The novel holographic imaging instrument (ICEMET) was adapted to measure microphysical properties of liquid clouds and these values were compared to parallel measurements of cloud droplet spectrometer (FM-120) and particle measurements using a twin-inlet system. When the intercomparison was carried out during isoaxial sampling, our results showed good agreement in terms of variability between the instruments with the averaged ratios between ICEMET and FM-120 were 0.6 ± 0.2, 1.0 ± 0.5, and 1.2 ± 0.2 for total number concentration (Nd) of droplets, liquid water content (LWC), and median volume diameter (MVD), respectively. This agreement during isoaxial sampling was also confirmed by mutual information and Pearson correlation coefficients. The ICEMET observed liquid water content (LWC) was more reliably than FM-120 (without swivel-head mount), which was verified by comparing the estimated LWC to measured values whereas the twin-inlet DMPS system and FM-120 observations of Nd showed good agreement both in variability and amplitude. Field data revealed that ICEMET can detect small cloud droplets down to 5 μm via geometrical magnification.

1 Introduction

Clouds are essential elements of the atmosphere, e.g., in regulating the Earth’s surface temperature, and therefore, understanding cloud properties are critical for exact predictions of climate evolution (Seinfeld and Pandis, 2006). Investigation of aerosol-cloud interactions and indirect aerosol effects on climate requires an accurate assessment of the cloud microphysical properties, such as the liquid water content (LWC) and droplet size distributions, for reducing the uncertainties in climate models (Boucher et al., 2013). Despite an overall improvement in quantification and process understanding, aerosol-cloud interactions remain as dominant contributors to the uncertainty regarding both, human-induced effective radiative forcing, and temperature change over the industrial era (IPCC, 2007, 2021). Cloud-related forcing is very difficult to estimate because they vary between cloud types and every cloud type has distinctive hydrometeor microphysics, spatial and temporal distribution on the atmosphere (Wood, 2012).

Although remote sensing methods have been developed considerably in the last decade, in-situ measurements are still the most accurate method to determine in-cloud droplet and ice particle size distributions. The remaining challenges for in-situ
measurements include the reduction of instruments noise and identification of possible biases or retrieval problems by comparing different techniques and instruments, a problem that can be addressed through measurement redundancy studies (Madonna et al., 2014). In-situ measurements can generate detailed information on the cloud microphysical properties which can be used for validation of the algorithms applied in the models for cloud properties or intercomparison with remote sensing applications such as lidar.

The two most typical types of on-line instruments for measuring in-situ cloud droplet properties are cloud spectrometers that exploit light scattering from individual droplets and instruments that capture images from individual objects using methods of shadowgraphy or holography (Baumgardner et al., 2011). Instruments in the former category are, e.g., the forward-scattering spectrometer probe (FSSP), the cloud droplet probe (CDP), and the fog droplet spectrometer (FM-100 and FM-120, Droplet Measurement Technologies) (e.g., Knollenberg et al., 1981; Baumgardner et al., 2011, 2014) and those in the latter category, e.g., the Holographic Detector for Clouds (HOLODEC) (Fugal and Shaw, 2009), the HOLographic Imager for Microscopic Objects II (HOLIMO II) (Henneberg et al., 2013), HOLIMO 3G (Beck et al., 2017), and HALOHolo (Lloyd et al., 2020). Both methods have their advantages and disadvantages which are important to be recognized in order to optimize the utility of cloud measurements and analyses in different conditions.

In all in-situ instruments, a part of the sample is lost along the line between the sampling inlet and the detector. One point of interest is the difference between the flow rate in the inlet and the prevailing wind speed and direction. When wind conditions are varied, the losses especially for the larger droplets are a typical source of uncertainty in surface-based cloud spectrometer measurements (e.g., Spiegel et al., 2012; Guyot et al., 2015; Doulgeris et al., 2020). Losses can be very high, particularly when calculating the liquid water content (LWC) (Spiegel et al., 2012; Guyot et al., 2015; Doulgeris et al., 2020). These losses mainly occurred because the sampling is usually nonideal, meaning that the sample flow is neither isoaxial nor isokinetic. In addition to these, the assessment of the sampling volume can cause uncertainty for measurements (Guyot et al., 2015). Despite the above-mentioned uncertainties, previous studies have shown good correlations between the measurements with different cloud spectrometers for the sizing of droplets in well-characterized cases. Spiegel et al. (2012) demonstrated that there is typically only a minor inlet loss for the small droplet sizes smaller than 10 µm in diameter, i.e., the sizes that are usually the most numerous in cloud droplets. An important feature of cloud spectrometers is that also tiny cloud particles down to 1 µm can be observed using light scattering techniques.

Holographic imaging methods measure over a wide range of particle sizes. In comparison to cloud spectrometers, holographic imaging allows simultaneous measurements of particle position, size, and shape, meaning that not only spherical droplets but also ice crystals and, e.g., pollen particles could be analyzed through image analysis without additional assumptions of particle properties, such as shape or refractive index (e.g., Fugal and Shaw, 2009; Henneberger et al., 2013). Holographic systems have been successfully utilized in the research of ice crystals and mixed-phase clouds carried out on aircraft (Lloyd et al., 2020) and balloons (HoloBalloon, Ramelli et al., 2020), at mountain-based observatories (Henneberger et al., 2013, Lloyd et al., 2015; Hoyle et al., 2016; Schlenzkek et al., 2017), and on a mountain cable car (HoloGondel, Beck et al., 2017) as well as recently to identify pollen particles (Sauvageat et al., 2020). The minimum particle detection size is determined by the effective pixel size. This value varied typically between 6 µm and 10 µm. It is above the smallest diameter observed for cloud droplets which makes the measurements of full screening of the droplet size distributions difficult because the smallest liquid droplets cannot be detected. The challenge of the method is also that lots of computational power are required for data reconstruction and time-consuming image analyses. However, with the development of computer technology, the cost and time required for such a task have decreased.

In this paper, we intercompate the novel instrument ICEMET (Icing Condition Evaluation Method: Kaikkonen et al., 2020; Molkoselkä et al., 2021) to parallel measurements with a cloud spectrometer (FM-120) and to the cloud properties calculated from particle size distribution measurements (a twin-inlet DMPS system) utilizing on ground-based field measurements in
Puijo, Station for Measuring Ecosystem-Atmosphere Relations (SMEAR IV), station. We also use mutual information analysis and LWC estimates in order to verify measured-based results. Previously, the ICEMET has been tested in mixed-phase icing conditions in a wind tunnel and a wind turbine (Molkoselkä et al., 2021), and in this intercomparison, we focus on measurements of liquid clouds. Measurements at Puijo station allow intercomparison in different conditions varying from relatively clean to polluted air masses dominated with forest fire aerosols.

2 Methods

The in-situ measurements were conducted at the Puijo measurement station in Kuopio, Finland from 3 September 2020 to 3 November 2020. The station is located at the top of the Puijo tower (height 75 m) and suits well for in-cloud measurements (Leskinen et al., 2009; Portin et al., 2009; Leskinen et al., 2012; Portin et al., 2014; Ruuskanen et al., 2021). 306 m above sea level and 224 m above the surrounding lake level, in a semi-urban environment about 2 km northwest of the city center of Kuopio. The continuous measurements at the station include cloud droplet properties, aerosol size distribution, number concentration, and optical properties, as well as trace gas concentrations and several meteorological parameters (Fig. 1).

Figure 1: ICEMET sensor located in Puijo tower. The height of the ICEMET sensor is 53 cm and the weight is 8 kg. The wind wing is used to align the sensor according to the wind direction (Photo: A. Leskinen).

2.1 The holographic imaging system (ICEMET)

The recorded holograms presented in this paper were reconstructed using the method described by Kaikkonen et al. (2020) and Molkoselkä et al. (2021) using the ICEMET-Server -software version 1.6.0 (Molkoselkä, 2020). The main components of a digital inline holographic imager are a laser functioning as a point light source and a digital camera to digitize and record the hologram images. A geometric magnification effect, due to the use of a point light source, enlarges the diffraction patterns of the objects (Fig. 2). The size and the location of cloud droplets are determined in the hologram imaging as diffraction patterns. The reconstructed light field, i.e. the grayscale shadow images of the cloud droplets, are formed by numerically focusing in different depths from the hologram. The ICEMET uses a 5.6 mm laser diode (Ushio Opto Semiconductors) operating at 660 nm wavelength as the point light source and a Sony IMX264 greyscale image sensor with resolution 2048 × 2048 of 3.45 μm size pixels and a maximum frame rate of 35 frames per second (fps). In this study, a frame rate of 1 Hz was used to decrease
the amount of data during a two-month measurement campaign. The anti-icing of the sensor is implemented with a temperature controller and heating elements at a total maximum power of 500 W, allowing the lowest operation temperature of −40 °C.

The window disks are 10 cm in diameter, and the distance between the disks is 3 cm, limiting the sample region and the optical axis between the centers of the opposite disks (Figs. 1 and 2). The typical distance between the protective windows and analyzed region in cloud droplet measurements is typically 5 mm. This distance minimizes the boundary layer effect on the airflow from the sidewalls over a large wind speed range and maximizes the nearly isokinetic measurement volume size (Juttula et al., 2020). The resultant analyzed volume per frame is 0.3 cm³. The raw hologram is cropped, the background is subtracted, and the preprocessed shadow image is reconstructed using angular spectrum propagation to binarized individual images with custom-made software in ICEMET-Server (Molkoselkä et al., 2021) based on Fugal et al. (2009). An edge sharpness algorithm is used to calculate the position of each particle along the optical axis, and the centroid in the other two dimensions is calculated. The minimum particle detection size is defined as two times the effective pixel size. Due to varying geometric magnification inside the measurement volume, the effective pixel size is the largest at the outer plane of the measurement volume on the camera sensor side. The geometric magnification of the diffraction pattern at that plane is 1.3 fold, resulting in an effective pixel size of 2.65 µm and thus leading to a theoretical effective particle detection size limit (DL_{eff}) of 5.3 µm.

On the laser diode side, the effective pixel size is not the limit of droplet detection lower bound, but the optical resolving power, defined by the numerical aperture of the imaging system. The theoretical optical resolving power limited by the numerical aperture, in this case, is defined by the camera sensor size and the object’s distance from the camera. It has the lowest value at the laser diode side of the measurement volume, where the theoretical resolving power is 5.1 µm. From these theoretical calculations, it can be concluded that objects larger than 5.3 µm could be detected inside the whole measurement volume, it should however be noted, that this theoretical consideration neither takes into account the physical non-idealities of the sensor system nor the sub-pixel location differences of the particles with size close to the two effective pixels detection limit. The laser diode, the camera sensor, and the selected parameters in the hologram analysis affect the practical particle detection limit and cause the limit to vary slightly inside the measurement volume. The sub-pixel position of the droplets with diameters close to the two-pixel size limit concerning to the 2x2 camera pixels centroid has an effect on the droplet segmentation, as the displacement of a droplet from the 2x2 pixel centroid inevitably spreads the shadow image of the droplet also on to neighboring pixels. Then in the worst case, the intensity level on the closest 2x2 pixel area of the droplet centroid will fall under the set detection threshold and the droplet will not be segmented and detected. A more detailed description of the ICEMET-Server hologram analysis software can be found in (Molkoselkä et al., 2021).

An equivalent diameter (D_e) of a particle is defined as the diameter of a circle having an equal area as the particle projection. For the shadow images, the D_e is calculated by counting the number of pixels per particle when the effective pixel size is known. The Heywood Circularity Factor (HCF), which is the particle circumference divided by the perimeter of a circle with
the same area as the particle, is applied to distinguish circular droplets from ice crystals and other non-spherical objects. The droplet size distribution (DSD\(_{\text{IM}}\)) is constructed by categorizing the observed droplets into 195 sizes 1 µm bins from 5 to 200 µm and total number concentration \(N_{\text{IM}}\) (cm\(^{-3}\)) can be obtained from

\[
N_{\text{IM}} = \sum_{i=1}^{m} \frac{N_i}{V_s} = \sum_{i=1}^{m} \frac{N_i}{fps \cdot V_a \cdot \Delta t}
\]

where \(N_i\) is the number of droplets in \(i\)th size bin, \(V_s\) is the sampling volume (cm\(^3\)), fps is the frame rate (s\(^{-1}\)), \(V_a\) is the analyzed volume (cm\(^3\)), and \(D_t\) is the sampling duration (s), and \(m\) is the total number of size channels. Sampling volume (\(V_s\)) is calculated by multiplying the volume of a single frame by the number of frames. Liquid water content LWC\(_{\text{IM}}\) (mg m\(^{-3}\)) of droplets can be calculated from

\[
\text{LWC}_{\text{IM}} = \frac{\rho_w \pi \frac{3}{2} \sum_{i=1}^{m} N_i D_{i,e}^3}{V_s m_i} = \frac{\rho_w \pi \frac{3}{2} \sum_{i=1}^{m} N_i D_{i,e}^3}{V_s m_i} \tag{2}
\]

where \(\rho_w\) is the density of liquid water (kg m\(^{-3}\)) and \(D_{i,e}\) is the average diameter of the size channel (µm). The median volume diameter (MVD) is the size of the droplet (µm), below which 50% of the total water resides and it is calculated by linear interpolation over the droplet diameter using the cumulative LWC (e.g., Finstad et al., 1988).

The size calibration of the ICEMET sensor used in this study was conducted using 9.18 µm, 11.58 µm, 25.60 µm, and 49.2 µm sized certified National Institute of Standards and Technology (NIST) traceable monodisperse standard glass microspheres, and 5 µm sized non-traceable monodisperse silica microspheres (Whitehouse Scientific Ltd). A specific glass microsphere dispenser tool for calibrating the ICEMET sensor was developed from a glass bottle, brass pipes, a hand blower, and a silicone tube. In order to ensure repeatable positioning, the calibration setup has a jig that is attached to the upper housing of the sensor and a sidearm that holds the dispenser outlet pipe. The sidearm can be moved with 5 mm steps to five different locations between the two window disks. In the glass microsphere dispenser, the glass beads are poured into a 4 ml glass bottle, and two 90-degree angled brass pipes are inserted through the bottle top inside the bottle. When forcing air using the hand blower, a portion of the glass beads is dispersed into the air and blown towards the measurement volume of the ICEMET sensor.

The particles close to the resolving power limit using inline holographic systems are known to have a particle edge “roll-off” effect in the reconstructed shadow images due to finite camera pixel size, which makes the smallest particles appear larger than their true size and the effect is typically corrected using a correction curve on the smallest particle sizes (Henneberger et al., 2013). The ICEMET sensor sizing correction is based on the measurement of the NIST traceable standard glass microspheres size of 9.18 µm and the non-certified 5 µm sized silica microspheres. As the result, a correction factor line was calculated to adjust the sizes of the smallest droplets from 5 to 12.39 µm. The correction was made only for droplets with a diameter between 5 and 12.39 µm, whereas for droplets with a diameter of 12.39–200 µm no sizing correction was needed.

The size calibration of the ICEMET sensor give median diameters of 5.2, 9.2 ± 0.2, 11.6 ± 0.2, 25.6 ± 0.7 and 49.2 ± 0.7 µm (Fig. 3a). An example of the measured cumulative size distribution for the 25.6 µm particles is shown in Fig. 3b.
Figure 3: (a) The results of calibration measurements for ICEMET with a 95% confidence level given by the manufacturer after the size correction was applied. The 5 µm particles were not certified and thus have no uncertainty value was defined (black cross). (b) The measured cumulative size distribution using the ICEMET sensor using 25.6 µm monodisperse microspheres. The uncertainty limits specified by the manufacturer are marked as dashed lines.

For the smallest glass microspheres, a visual inspection of the particle images has revealed that if two or more microspheres are in contact with each other, there can be uncertainties in the detection of particles smaller than 20 µm. Two spheres can be in contact in a way that one bead is almost fully behind the other in the hologram and the aggregate can be counted as a single particle thus broadening the size distributions of the measured particles. These grouped glass spheres can be mostly filtered out using the HCF as a limit for the minimum roundness of the particles. It was also noted that the 11.58 µm glass microspheres measurement was slightly undersized after applying the size correction curve. In the future development of ICEMET, an extended set of certified monodisperse standards, including also sizes below 9 µm, will be used. This will result in a fully traceable correction curve for the whole measurement range and particularly improve the calibration accuracy of the smallest droplet sizes.

Because the focus of this study was investigating only cloud droplets, the particle image data from ICEMET was filtered using the Heywood Circularity Factor (HCF) of less than 1.23. The threshold value was obtained by visual inspection from the actual DSDIM and images from cloud event measurements in Puijo. Using this criterion, only cloud droplets were qualified and quantified, and all other objects and the noise were removed from further analyses (Fig. 4). ICEMET data quality was checked by monitoring the number of frames per one-minute sample. Heavy rain events sometimes cause large water splashes on the protective windows, which can result in a high number of detected OpenCV (Bradski, 2000; function which detects a change in the image color and marks it as contour) contours in the reconstructed hologram. If the number of detected contours exceeds 2000, the frame is removed from the analysis and when lower than 59 frames/minute were acquired, the measurement data was removed.
2.2 The fog monitor (FM-120)

The fog monitor (FM-120, Droplet Measurement Technologies Inc., USA) is a forward-scattering optical spectrometer that measures the intensity of the scattered light from the droplets that is proportional to the optical scattering cross-section. The FM-120 records the pulse heights of the light scattered by individual particles that pass through a focused 685-nm laser beam. A digitalized signal from sizing and qualifying detectors is converted to an optical scattering cross-section. Then the diameter of droplets is determined using scale factor obtained from calibration through Mie-theory calculations (Bohren and Huffman, 1983). Droplets are assumed to be perfect spheres of pure water with a size-independent refractive index equal to 1.33 (Harvey et al., 1998). The scattering intensity of each particle is digitized and represents a single event that is added to the corresponding size bin. In this campaign, the true sample flow (TAS), determined using a Pitot tube, was around 13 m/s, and the sample volume ($V_s$) was around 19 cm$^3$ with a 5 s integration time ($D_t$) (maximum sampling rate of 20 Hz) and the detector in-focus area ($S$) of 0.29 mm$^2$. The instrument had been recently calibrated by the manufacturer with glass beads, and the calibration was checked before and after the measurement campaigns by using similar glass beads of 5, 10, 20, 30, and 40 µm in diameter and found without apparent changes in instrument performance. Droplet size distributions (DSD$_{FM}$) were calculated from the 30 size bins between 2-50 µm and total number concentration ($N_{d,FM}$, cm$^{-3}$) was calculated from

$$N_{d,FM} = \sum_{i=1}^{m} \frac{N_i}{V_i} = \sum_{i=1}^{m} \frac{N_i}{TAS \times S \times D_t}$$

(3)

where $m$ is the number of channels used. The LWC$_{FM}$ (µg m$^{-3}$) and MVD$_{FM}$ (µm) can be derived from the DSD$_{FM}$ when the sample volume is known (see Section 2.1). The accuracy of FM-120 is estimated to be ±20% for the $N_{d,FM}$ and sizing, ±40% for the LWC$_{FM}$ when assuming spherical droplets with a density of water (Droplet Measurement Technologies, 2009).

2.3 Twin-inlet system

Beyond direct droplet observations, droplet number concentration was estimated using a twin-inlet DMPS system that collects particles and cloud hydrometeors through a total and an interstitial inlet installed on the top of the Puijo tower approximately 2.5 m above the roof (Portin et al., 2014). The total inlet sampled all aerosols and hydrometeors smaller than 40 µm in diameter while those with diameters below 1 µm are measured in the DMPS-interstitial. The upper part of the total inlet was heated to
30°C in order to remove the cloud-condensed water from the hydrometeors resulting in the total sample that consists of the residuals of dried particles aerosol and the inactivated particles. In the interstitial inlet, a PM₁ impacter (Digitel DMP10 with a PM₁ nozzle plate) was used to remove aerosol particles and hydrometeors larger than 1.0 µm in diameter leaving only the interstitial particles into the sample. The number concentration of the activated particles \( N_{act} \) was the difference of the number concentrations of the observed total and interstitial aerosol particles larger than 70 nm in diameter \( (N_{act} = N_{70_{tot}} - N_{70_{int}}) \). The 70 nm size limit was chosen because most particles below this size remain unactivated and therefore their contributions to \( N_{act} \) cancel out and can be neglected for simplicity and possible inaccuracies in the lower ends of the spectra of the individual instruments. The \( N_{70_{tot}} \) and \( N_{70_{int}} \) were determined from the size distributions measured simultaneously from each inlet using a DMPS system in the size range of 27-520 nm. Each DMPS consisted of a differential mobility analyzer (DMA, a Hauke type 28 cm long), a bipolar charger to obtain charge equilibrium, and a condensation particle counter. The performance of each DMPS system was checked regularly. More information about this sampling procedure can be found in the literature (e.g., Portin et al., 2014).

During cloud-free periods, the obtained aerosol size distribution from the total and interstitial lines, after correcting for sampling line losses, should be the same. With this assumption, the interstitial number size distributions were corrected (zero-correction) to match the total aerosol size distribution by using size-dependent correction factors (total/interstitial) determined during the cloud-free periods of the measurement campaign. By doing this, we could eliminate, e.g., the influence of unequal sampling line losses on the measured size distributions. The number of potential cloud condensation nuclei \( \text{CN}_{70} \), i.e. concentration of particles larger than 70 nm) particles was calculated from the DMPS size distributions.

### 2.4 LWC estimation

We applied a simple adiabatic model to estimate the maximum amount of LWC based on the cloud base height retrieved from the ceilometer observation. Only data values where cloud base height (CLBH) was unequivocally determined, and the observation altitude was minimum distance 50 m from cloud boundaries were accepted in this modelling study. Although this approach does not account for the entrainment mixing at the cloud top and is highly uncertain at low LWC values, it gives an estimate of the expected LWC values. Cloud top height (CTH) and CLBH were retrieved from time-dependent vertical profiles of radar reflectivity (dBz) measured with the cloud radar located at the Savilahti automated weather station. See the supporting information for detail (Supplement Sect. S1).

We also adapted a simple regression fog model to determine LWC (g m⁻³) using visibility measurements (Kunkel et al., 1983; Fišak et al., 2006)

\[
LWC = \left( \frac{1}{144.7 \cdot \text{VIS}} \right)^{\frac{1}{2.98}}
\]  

(4)

where \( \varepsilon \) is the threshold of contrast (0.2) and visibility (VIS, km) is measured using a weather sensor (Vaisala PWD52) at Puijo measurement station.

### 2.5 Mutual information analysis

The mutual information (MI) between two data sets \( X \) and \( Y \) measures the \( X-Y \) coverability or the amount of information that \( Y \) contains about \( X \). It is defined in terms of the Shannon-Wiener entropy measure (H) as

\[
MI(X, Y) = H(X) + H(Y) - H(X, Y)
\]  

(5)
where \(H(X)\) and \(H(Y)\) are the marginal entropies or dispersion of the probabilistic uncertainty of \(X\) and \(Y\), respectively (Madonna et al., 2014). The marginal entropy \(H(X)\) represents the dispersion of the probabilities of events \(p(x)\) in the data set \(X\) composed of \(x\) events. It is calculated as

\[
H(X) = -\int_{x} p(x) \log(p(x)) dx
\]

(6)

Therefore, the mutual information also called mutual correlation \(MC(X,Y)\) can be expressed as

\[
MC(X,Y) = \int_{x \in X} \int_{y \in Y} p(x,y) \log \left( \frac{p(x,y)}{p(x)p(y)} \right) dx dy
\]

(7)

where \(p(x,y)\) is the joint probability density function for the sets \(X\) and \(Y\) (Dawe and Austin, 2013).

When \(MC(X,Y)\) is equal to zero, then \(X\) and \(Y\) are totally uncorrelated and perfectly independent (Glenn et al., 2020). For discrete calculations, it is necessary to find the optimal binning that maximizes the value of \(MC\), as the terms of \(p(x), p(y), \) and \(p(x,y)\) are highly dependent on it. The mutual information is a robust statistical indicator because it does not constrain \(X\) and \(Y\) to a specific probability density function (PDF) and therefore, it is less sensitive to the presence of outliers than other indicators such as the Pearson correlation coefficient (Madonna et al., 2014). With unconstrained \(X\) and \(Y\), the \(MC\) preserves the intrinsic variability and therefore is able to capture both, linear and nonlinear relationships (Glenn et al., 2020).

In this way, the mutual correlation works as a reliable indicator of measurement uncertainty. It helps to explain the amount of information that is shared by \(X\) and \(Y\) or the degree of redundancy in the information given by \(X\) and \(Y\). Nevertheless, it has the disadvantage of inaccuracy when data sets are not large enough to calculate representative probability values. If data sets are too small, histograms used for probability estimation can become strongly biased due to the lack of information or reduced amount available for specific variable ranges. A very simple rule to reduce uncertainty in histogram-based probabilities is choosing a size bin in such a way that the number of bins becomes equal to the expected number of components in the distribution (Batina et al., 2011).

We performed a mutual information analysis on our data sets containing time series of binned and total droplet concentrations, as well as variables retrieved from the DSD such as LWC and MVD. Droplet microphysics observed by the twin-inlet system are averaged as 15-min resolution time series. The fmgonitor and ICEMET datasets have shorter time resolution, and therefore observations were averaged to have comparable observational intervals.

3 Results and discussion

3.1 Overview of conditions during intercomparison campaign

On average, the Puijo station is found to be surrounded by clouds 8% of the time, with the most frequent cloud season in the autumn and early winter when cloudy conditions are observed in the tower more than 13% of the time (Ruuskanen et al., 2021). The criteria for the occurrence and intensity of cloud, a typically on 1) visibility (Portin et al., 2009), 2) number concentration of cloud droplets (Ragno and Hobbs, 2005), 3) LWC (Hoyle et al., 2016), or 4) both the number of cloud droplets and LWC (Li et al., 2020). In this study, the data points that were measured outside of clouds or on the edges of clouds were removed, and we defined a cloud event as follows: 1) Cloud droplet number concentration > 50 cm\(^{-1}\) and 2) LWC > 10 mg m\(^{-3}\) over one-minute averages. For the two-month intercomparison period, a total of 35 cloud event was observed.

The mean temperature during the intercomparison campaign was 7.4 °C ranging from -3.7 °C to 17.7 °C (Fig. 5), the prevailing wind direction was around 160° with a mean wind speed of 8.9 m s\(^{-1}\) including winds from all directions. During the two-month intercomparisons, different types of air masses mixed with various sources were observed; for example, elevated aerosol concentrations from 23 September to 9 October 2020 (Fig. 5). By inspecting the air mass back trajectories calculated with the
PC-based HYSPLIT model (Stein et al., 2015; Rolph et al., 2017) we were able to connect the elevated concentrations to large forest wildfires that took place in central/eastern Europe at that time. In this case, the concentration of accumulation mode particles (100 nm < \(D_p< 1 \mu m\)) was about five times higher (Fig. 5) compared to the typical values at the Puijo station. Consequently, the wildfire plume affected the \(N_{act}\) and \(CN_{70}\) by increasing the \(N_{act}\) from the mean value of 157 cm\(^{-3}\) to 426 cm\(^{-3}\) and the \(CN_{70}\) from the mean value of 432 cm\(^{-3}\) to 1190 cm\(^{-3}\), respectively, thus providing highly varying conditions for intercomparison.

Figure 5: Variation of (a) particle size and concentration, (b) concentrations of cloud condensation nuclei (CN\(_{70}\)), cloud droplets (\(N_d\)), and activated particles (\(N_{act}\)) in the period of intercomparison campaign from 3 September 2020 to 3 November 2020 at the Puijo measurement station. Observed cloud events (c), the wind speed and directions (d) and ambient temperature (T) and relative humidity (RH) (e) are presented in the three lowest plots. The intensive smoke period is divided by red lines in plot (a).

3.2 Intercomparison between ICEMET and FM-120

3.2.1 Wind-isoxial conditions

Cloud droplet sampling may suffer from extra losses of droplets if the inlet is not facing the direction of the prevailing wind and the angular deviation from the isoaxial sampling (\(\theta\)) is getting larger (Guyot et al., 2015). Guyot et al. (2015) suggested that particle losses in FM-120 sampling because of anisoaxial sampling decrease with increasing wind speed for \(\theta<30^\circ\), while they increase with increasing wind speed for \(\theta>30^\circ\), particularly for large particles. We could verify this by comparing the cloud microphysical properties derived from the FM-120 measurements to those derived from the ICEMET measurements as a function of angular deviation from the isoaxial sampling because the ICEMET turns passively to the correct position thanks
to its vane while the FM-120 is facing the same direction all the time. This sampling effect is illustrated in Fig. 6 as the ratio of FM-120 to ICEMET derived properties, and we can see that the angular deviation from the isoaxial sampling influences particularly the LWC ratio (Figs. 6c-d). This is because LWC is typically dominated by large droplets that cannot enter the FM-120 inlet in anisoaxial sampling but are observed by the ICEMET. In our measurement campaign, the FM-120 inlet was facing East (90°), so in the intercomparisons, we emphasized the FM-120 data on prevailing wind directions of 60–120° (Fig. 6: blue lines), following the criteria suggested by Westbeld et al. (2009). The effect of the cut-off size (FM-120: 2 μm vs. ICEMET: 5.3 μm) was investigated by calculating \( N_d, FM \), \( LWC_{FM} \), and \( MVD_{FM} \) without the 3 smallest bins in size range of 5–50 μm (Figs. 6b, d, and f). The effect of cut-off size showed only a minor impact on calculated \( MVD_{FM} \) (+4%) and \( LWC_{FM} \) (-5%) but opposite to that, \( N_d, FM \) decreased on average of 35%.

The results revealed that the observed droplet size distributions (DSDs) showed similar behavior in time-series of integrated properties and shapes, but ICEMET observe wider \( DSD_{FM} \) values especially with increasing angular deviation which explains the higher calculated \( MVD_{FM} \) (Fig. 7). The shoulder in \( DSD_{FM} \) around 13.5–16 μm is probably due to irregularities in Mie-curve which is a common feature in optical counters (Gonser et al., 2011; Spiegel et al., 2012) and it has only a minor influence on calculated \( N_d, FM \), \( LWC_{FM} \) and \( MVD_{FM} \). ICEMET observed lower values than FM-120 for the smallest bins (Fig. 7). The discrepancies of the lowest bins may arise from the global threshold used in the particle segmentation phase after the hologram reconstruction. The global threshold is set to a high enough value so that no excessive amounts of false detected particles (noise artifacts) are found in the segmentation phase, which would waste computational calculation power later in the particle analysis. The use of a point source illumination also has an inherent property that the droplets closer to the laser experience a higher light field intensity, which results in a higher contrast diffraction pattern on the camera sensor, and the nearly Gaussian intensity profile in lateral direction also decreases the light intensity from the center of the hologram towards the edges of the hologram. Other influences on the segmentation of the smallest droplets include the non-ideal and elliptical laser illumination.
pattern, camera sensor non-idealities, and sub-pixel location of the smallest droplets close to camera sensor where the effective pixel size is larger, as was discussed in the section 2.1. These effects may cause that some of the smallest droplets on the camera side of the analyzed volume (Fig. 1) not to be found in the segmentation phase, which may decline the concentration of the smallest droplets (from 5 to 7 μm).

**Table 1: Summary of intercomparison for total dataset (In-cloud) and for isoaxial sampling (In-cloud IAS, θ ± 30°); mean values of LWC (mg m⁻³), MVD (μm), and Nₐ (cm⁻³) for ICEMET and FM-120. For the twin-inlet system, the number of Nₐₑₜ (cm⁻³) and CN₇₀ (cm⁻³) are presented.**

<table>
<thead>
<tr>
<th></th>
<th>ICEMET</th>
<th>FM-120</th>
<th>Twin-inlet system</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>In-cloud</td>
<td>IAS</td>
<td>In-cloud</td>
</tr>
<tr>
<td>LWC</td>
<td>80.5</td>
<td>48.7</td>
<td>37.9</td>
</tr>
<tr>
<td>MVD</td>
<td>9.6</td>
<td>8.9</td>
<td>7.3</td>
</tr>
<tr>
<td>Nₐ</td>
<td>200</td>
<td>167</td>
<td>233</td>
</tr>
<tr>
<td>Nₐₑₜ</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>CN₇₀</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
</tbody>
</table>
The detection accuracy of the 5–7 μm droplet size bins with ICEMET sensor could be increased with minor software changes, for example by limiting the measurement volume of this droplet size range to the higher magnification part of the measurement volume, where effective pixel size is smaller than the optical resolving power. Also making the segmentation of the droplet’s dynamic, varying by the location, could improve the detection accuracy of the droplets near the effective pixel size limit. It would be possible also to reconstruct the holograms to higher pixel number images to outcome the pixel size limitation in the segmentation phase. This could be done by reconstructing the shadow images for example to double the size of the original hologram. Then the effective pixel size could be halved, but this would increase the reconstruction and analysis time significantly, making it not a suitable solution using present computers.

Figure 8: Comparison of activated particle concentrations (N_{act}) with measured cloud droplet number concentrations (N_d) using FM-120 (upper figures) and ICEMET (lower figures) by angular deviation (θ) of 30° and for the total dataset (θ ± 180°). The upper figures (a) and (b) are colored by angular deviation from the isoaxial sampling (θ) and the lower figures (c) and (d) using a fraction of the lowest bins 1-3 (N_{d,FM2-5}). The dashed orange lines represent linear regression with a = slope, b = intercept, and R = Pearson correlation coefficient. Black lines represent 1:1 (solid), 1:2 (dashed) and 2:1 (dashed) value. Only data points where a fraction of N_{d,FM2-5} < 0.2 are presented.

In order to look more detail a representative intercomparison between the ICEMET and the FM-120, an example of an in-cloud period on 2.10.2020 was chosen (Fig. 9). These results revealed that instruments showed a good agreement in terms of variability during favorable meteorological conditions (isoaxial sampling, stable cloud cover without heavy rain). Figure 9 points also out that N_{d,FM} was systematically higher and MVD_{FM} lower (red lines) than those measured with ICEMET sensor (blue lines). As expected, larger the cut-off size of 5 μm for FM-120 (green line) improved agreement in terms of amplitude (values) between N_{d,FM} and N_{d,IM}. In summary, anisoaxial sampling and different measurement ranges can explain the most of differences between instruments’ observations.
Figure 9: Intercomparison of $N_d$, LWC and MVD values between ICEMET (subscript IM, blue line), and FM-120 (subscript FM, red markers/line) in the period of isoxial sampling (cloud event on 2 October 2020). $N_{d,FM}$ was also presented without the lowest bins in the size range of 5-50 $\mu$m in (a) and (d), marked as green markers/lines. The dashed orange lines represent linear regression with $a = \text{slope}$, $b = \text{intercept}$, and $R = \text{Pearson correlation coefficient}$. Black lines represent 1:1 (solid), 1:2 (dashed) and 2:1 (dashed) value.

3.2.2 The mutual information analysis

The variation in the wind direction did not affect the twin-inlet results like the FM-120 measurements, because the inlet of the Twin-inlet system is insensitive to the wind direction. Short-term variability in DMPS-measurements induced by wind direction is more related to variations in the aerosol properties caused by different types of air masses. For example, the local wind direction from 215° to 360° has no significant point aerosol sources and has therefore been defined as the clean sector at Puijo (Portin et al., 2014). The twin-inlet results represent an initial reference point in the mutual analysis. Like previous analyses, time series were filtered to separate observations corresponding to cloudy conditions (“in-cloud”, see Section 3.1).

To assess the effect of anisoxial sampling on the degree of mutual correlation, we also compared subsets of data containing only measurements performed with minimum angular deviation or with prevailing winds coming from the east (60 degrees to 120 degrees). When this criterion is also applied to “in-cloud” data sets, we referred it as “IAS”.

Results of the mutual information analysis for both, whole and selected data sets are shown in Table 2 together with Pearson correlation coefficients for comparison purposes. Marginal and joint entropies were calculated using histograms of the total droplet number concentrations, LWC, and MVD. For the “in-cloud” data set, optimal bin sizes for these variables were 1 cm$^{-3}$, 0.5 mg m$^{-3}$, and 0.03 $\mu$m, respectively. For the “IAS” data set, optimal bin sizes were 6 cm$^{-3}$, 1.8 mg m$^{-3}$, and 0.09 $\mu$m, respectively. These values were chosen to give several bins close to the number of data points available in each data set (Batina et al., 2011). The evidence of measurement agreement between the ICEMET and the FM-120 can be obtained from the mutual information shared by each instrument with the Twin-inlet system. When total droplet number concentrations from both, the
ICEMET and the FM-120 are compared to those observed by the twin-inlet system, the degrees of mutual correlation are very similar and high with values between 0.70 and 0.79. This confirms that they share a significant amount of information in terms of the \( N_d \) variability.

![Figure 10: The frequency of the measured (a) \( N_d \), (b) LWC, and (c) MVD values using FM-120 (x-axis) and ICEMET (y-axis) for the total dataset (including all wind directions).](https://doi.org/10.5194/amt-2021-423)

When the ICEMET and the FM-120 are compared to each other, mutual correlation values between in-cloud data sets are 0.71, 0.60, and 0.40 for \( N_d \), LWC, and MVD, respectively, indicating a decreasing trend in the degree of correlation from strong to moderate. While the \( N_d \) is not significantly changed by losses of large droplets during anisothermal sampling, variables such as LWC and MVD respond strongly to these losses due to their stronger functionality with droplet size. Figure 10 summarizes the relation of measured cloud microphysical properties between FM-120 and ICEMET (total dataset) in terms of the joint probability distribution. Probability distributions of individual variables are included in Figure S1 (Supplement Sect. S2). When the criteria of isothermal sampling of the FM-120 is incorporated, the mutual correlation among the different data sets increases significantly reaching values of 0.78, 0.71, and 0.64 for \( N_d \), LWC, and MVD, respectively. With reduced measurement uncertainty along with the droplet size range, the mutual correlation values are also closer to each other. While mutual information analysis can detect any kind of dependence, Pearson correlation coefficients strictly evaluate the linear dependence between variables and therefore, are more susceptible to the presence of extreme values or clusters. This explains why Pearson correlation coefficients for “in-cloud” data sets vary between 0.38 and 0.56 showing a lower degree of correlation than the correspondent MC values. When only the isothermal sampling criteria is considered, both mutual and Pearson correlation coefficients, confirm the good correlation between data sets (Table 2).

### Table 2: Pearson correlation coefficients (R) and mutual correlations (MC) between measured variables for total dataset (In-cloud) and isothermal sampling (In-cloud IAS, \( \theta \leq 30^\circ \)).

<table>
<thead>
<tr>
<th>Variable X</th>
<th>Variable Y</th>
<th>Selection criteria</th>
<th>Number of data points</th>
<th>MC</th>
<th>R (p&lt;0.05)</th>
</tr>
</thead>
<tbody>
<tr>
<td>( N_{act} )</td>
<td>( N_{d,FM} )</td>
<td>In-cloud IAS</td>
<td>857</td>
<td>0.71</td>
<td>0.80</td>
</tr>
<tr>
<td>( N_{act} )</td>
<td>( N_{d,IM} )</td>
<td>In-cloud IAS</td>
<td>92</td>
<td>0.72</td>
<td>0.82</td>
</tr>
<tr>
<td>( N_{d,FM} )</td>
<td>( N_{d,IM} )</td>
<td>In-cloud IAS</td>
<td>559</td>
<td>0.70</td>
<td>0.40</td>
</tr>
<tr>
<td>( N_{d,FM} )</td>
<td>( N_{d,IM} )</td>
<td>In-cloud IAS</td>
<td>51</td>
<td>0.79</td>
<td>0.53</td>
</tr>
<tr>
<td>( LWC_{FM} )</td>
<td>( LWC_{IM} )</td>
<td>In-cloud IAS</td>
<td>478</td>
<td>0.71</td>
<td>0.38</td>
</tr>
<tr>
<td>( MVD_{FM} )</td>
<td>( MVD_{IM} )</td>
<td>In-cloud IAS</td>
<td>47</td>
<td>0.78</td>
<td>0.67</td>
</tr>
<tr>
<td>( MVD_{FM} )</td>
<td>( MVD_{IM} )</td>
<td>In-cloud IAS</td>
<td>47</td>
<td>0.60</td>
<td>0.43</td>
</tr>
<tr>
<td>( MVD_{FM} )</td>
<td>( MVD_{IM} )</td>
<td>In-cloud IAS</td>
<td>47</td>
<td>0.71</td>
<td>0.43</td>
</tr>
<tr>
<td>( MVD_{FM} )</td>
<td>( MVD_{IM} )</td>
<td>In-cloud IAS</td>
<td>47</td>
<td>0.40</td>
<td>0.56</td>
</tr>
<tr>
<td>( MVD_{FM} )</td>
<td>( MVD_{IM} )</td>
<td>In-cloud IAS</td>
<td>47</td>
<td>0.64</td>
<td>0.75</td>
</tr>
</tbody>
</table>
In summary, it is expected to have mutual information below 100 % due to the differences in detection limits i.e. the smallest droplet size detected by different instruments. If cloud formation occurs with high aerosol loadings (e.g., wildfire air mass), droplet number concentrations in the size range between 1 – 5 μm can dominate the droplet spectra. Since the smallest cloud droplets cannot be detected, either by the FM-120 or by the ICEMET but are accounted for by the twin-inlet system, negative biases are inevitable. On the contrary, if cloud formation occurs with low aerosol loadings, the droplet spectrum moves to larger droplet sizes (e.g., clean air mass), and the mutual information shared by the three-data sets increases. In this case, larger droplets with a diameter above 50 μm are unaccounted for by the FM-120 and the twin-inlet system but detected by ICEMET. Given these facts, applying multiple instrumentations followed by combined data analysis is recommended to ensure the data continuity along the droplet spectrum. It is necessary to highlight that any statistical indicator of correlation cannot describe fully the physico-chemical processes that are driving cloud microphysics, but they can give insight into the dominant ones.

3.2.3 LWC analysis

LWC estimations using adiabatic and visibility-based models (see Section 2.4) point out that FM-120 underestimates LWC most of the time when $LWC_{FM}$ was measured without a rotating inlet (Fig. 11). The average $LWC_{FM}$ of 92 mg m$^{-3}$ was only 26–30% from the estimated values of 350 mg m$^{-3}$ and 310 mg m$^{-3}$ calculated using adiabatic and regression model, respectively. In comparison, an average $LWC_{IM}$ was 240 mg m$^{-3}$ which was 69% of the adiabatic value and 77% of a regression model. $LWC_{IM}$ was close to the value observed in the previous study in Puijo station (150 mg m$^{-3}$, Portin et al., 2014) when values were compared without cloud boundary limitations, at similar conditions than Portin et al. 2014, in which case $LWC_{IM}$ was 140 mg m$^{-3}$ and $LWC_{FM}$ was 44 mg m$^{-3}$.

![Figure 11](https://doil.org/10.5194/amt-2021-423)

Figure 11: Amount of LWC using a simple adiabatic model and visibility-based estimation compared to observed LWC measured utilizing cloud spectrometers (a) ICEMET (b) FM-120.

4 Conclusions

We have intercompared a novel digital lens-less holographic imaging system (ICEMET), a commercially available fog monitor (FM-120), and a twin-inlet DMPS system in warm liquid clouds. We found that the intercomparison between the ICEMET and the FM-120 were sensitive to angular deviations of wind direction (e.g., Spiegel et al., 2012), particularly when the FM-120 was installed in a steady position and without a rotating inlet that would enable isoxial sampling in changing wind directions. The ICEMET, in turn, has a vane and rotates according to the prevailing wind, which minimizes sampling losses.
Despite this, our results showed good correlations between the measurements performed by the ICEMET and FM-120, especially during isoaxial sampling. When the intercomparison was carried out for only isoaxial wind condition periods, the averaged ratios between ICEMET and FM-120 were 0.6 ± 0.2, 1.0 ± 0.5, and 1.2 ± 0.2, for Nd, LWC, and MVD, respectively. This agreement was also confirmed by mutual information and Pearson correlation coefficients.

Based on our findings in this study, with the version of ICEMET sensor and software used in this study cannot detect all cloud droplets close to 5 μm, which affects the observed total droplet number concentration, especially when the droplet size distribution is dominated by small droplets, which was the case during a forest wildfire plume period. In turn, the ICEMET measures LWC more reliably than FM-120 (without swivel-head mount), which was also verified by comparing the estimated theoretical maximum LWC to measured values. The LWC was also found to be the most sensitive to changes in wind direction. Independent LWC observations are recommended to improve the data analysis reliability when liquid clouds are investigated.

As a part of the research and development of holographic techniques, the detection accuracy of the smallest droplet sizes with ICEMET sensor could be increased with software changes, for example by adjusting the measurement volume or making a more dynamic droplet segmentation thresholding in the analysis software. Particularly, it will be practical to reconstruct the holograms to higher pixel number images to obtain the effective pixel size limitation in segmentation of the smallest droplets located closer to the camera sensor.

Data availability

The data from this paper can be obtained by contacting the authors of this article.

Competing interests

The authors declare that they have no conflict of interest.

Author contributions.

PT wrote the manuscript and analyzed data with contributions from all co-authors. SC analyzed and report MI data. PT, AL, and MK installed and operated all the instruments during the campaign. VK and EM performed ICEMET calibrations.

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References


