Development and Evaluation of Correction Models for a Low-Cost Fine Particulate Matter Monitor

Brayden Nilson[12], Peter L. Jackson[1], Corinne L. Schiller[12], Matthew T. Parsons[2]

5 [1]Department of Geography, Earth and Environmental Sciences, University of Northern British Columbia, Prince George, V2N 4Z9, Canada
[2]Air Quality Science – West, Meteorological Service of Canada, Environment and Climate Change Canada, Vancouver, V6C 3S5, Canada

10 *Correspondence to*: Brayden Nilson (brayden.nilson@ec.gc.ca)

Abstract. Four correction models with differing forms were developed on a training data set of 32 PurpleAir-Federal Equivalent Method (FEM) hourly fine particulate matter ($PM_{2.5}$) observation colocation sites across North America (NA). These were evaluated in comparison with four existing models from external sources using the data from 15 additional NA colocation sites. Colocation sites were determined automatically based on proximity and a novel quality control process. The Canadian AQHI+

15 system was used to make comparisons across the range of concentrations common to NA, as well as to provide operational and health-related context to the evaluations. The model found to perform the best was our Model 2, $PM_{2.5\text{-corrected}} = PM_{2.5\text{-cf-1}} / (1 + 0.24 / (100 / RH_\% - 1))$ – RH is limited to the range [30 %, 70 %], which is based on the RH growth model developed by Crilley et al. (2018). Corrected concentrations from this model in the moderate to high range, the range most impactful to human health, outperformed all other models in most comparisons. Model 7 (Barkjohn et al., 2020) was a close runner up and excelled in the low

20 concentration range (most common to NA). The correction models do not perform the same at different locations, so we recommend testing several models at nearby colocation sites and utilizing that which performs best if possible. If no nearby colocation site is available, then we recommend using our Model 2. This study provides a robust framework for the evaluation of low-cost PM2.5 sensor correction models and presents an optimized correction model for North American PA sensors.

Keywords: North America, air quality, $PM_{2.5}$, low-cost sensors, colocation, corrections

25 **1 Introduction**

Fine particulate matter ($PM_{2.5}$) is a primary air pollutant of concern for human health in Canada and the USA (EPA, 2021; Government of Canada, 2021) as well as world-wide. $PM_{2.5}$ consists of suspended aerosols with diameters ≤ 2.5 μm which when inhaled can enter the lower respiratory tract and potentially pass through into the blood (Feng et al., 2016). $PM_{2.5}$ can have high spatial and temporal variability and impact highly populated areas (Li et al., 2019). Globally, concentrations of $PM_{2.5}$ are highest

30 in South Asia, Africa, and the Middle East, while North America has some of the lowest concentrations on average (Health Effects Institute, 2020). Smoke from wildfires is increasingly becoming an issue for $PM_{2.5}$ concentrations in North America and other parts of the world. Both chronic and acute exposure to $PM_{2.5}$ have been linked to a higher risk of mortality from cardiovascular and respiratory diseases (Lelieveld et al., 2015; Mcguinn et al., 2017; Bowe et al., 2019).

Near-real-time observations of $PM_{2.5}$ have historically been restricted by cost and access. As a result, many cities rely only on a

35 single $PM_{2.5}$ monitor (or none at all) provided by governmental networks. These Federal Equivalent Method (FEM) monitors are expensive, require a large shelter, and require regular maintenance to provide accurate and reliable data. However, rigorous testing and standardization ensures FEM observations are equivalent to reference monitoring methods. Recently, a growing interest in low-cost/small sensor technology has allowed for a rapid expansion of observation networks. However, these low-cost sensors are

not as accurate as the FEM monitors, necessitating additional processing and testing before knowing how to interpret their data

40 and understanding how they may be used (Datta et. al, 2020; Zamora et. al 2019).

FEM monitors can be one of multiple potential sensor types; each of which measures $PM_{2.5}$ using different techniques (such as beta attenuation, gravimetric, and/or broadband spectroscopy). These sensors are rigorously tested and compared with 24-hour average reference measurements from Federal Reference Monitors (FRM) to ensure comparability. FEM monitors are in well-controlled shelters with incoming air being dried to minimise any humidity impacts.

45 The North American (NA) network of FEM monitors for $PM_{2.5}$ and other air pollutants contribute to the Canadian Air Quality Health Index (AQHI) system (for monitors in Canada) and the US Air Quality Index (AQI); both used to provide health advisories for periods of unhealthy levels of air pollution. The Canadian AQHI system is based on rolling three-hour averages of three pollutants: $PM_{2.5}$, NO_2 and O_3 (Stieb et al. 2008). The AQHI+ system is a simplification of AQHI which relies only on hourly-averaged $PM_{2.5}$ and shares the index value and associated health messaging (BC Lung Association, 2019). In British Columbia,

50 the AQHI+ overrides the regular AQHI formulation during events with high concentrations of $PM_{2.5}$, such as wildfire smoke conditions. The AQHI+ can consequently be used to facilitate direct health-related comparisons with low-cost sensors, which currently do not detect the other criteria air pollutants sufficiently (BC Lung Association, 2019). This system is based on the Canadian AQHI and was initially developed for British Columbia (but is now used mostly across Canada) to provide more accurate health messaging during wildfire smoke conditions (for which $PM_{2.5}$ is a main concern). AQHI+ ranges from 1 to 11, with the last

55 value represented as '10+' (Eq. 1).

$$AQHI+ = \ ceiling\left(\frac{PM_{2.5}}{10}\right) domain: [1, 11] \qquad (1)$$

Low-cost sensor technology has been developed in recent years that can be used to provide increased spatial and temporal resolution of $PM_{2.5}$ measurements. In this study, low-cost sensors from PurpleAir (2021) which use two nephelometers to detect $PM_{2.5}$ were compared with colocated FEM monitors. A nephelometer estimates the particulate concentration by measuring light from a source that is scattered by particles. The relationship between scattering and particulate concentration is affected by particle

60 refractive index, shape, density, and size distribution: nephelometers are calibrated for a known particulate. Error is introduced when the actual particle characteristics are different from those used for nephelometer calibration. $PM_{2.5}$ measured by these sensors are impacted by humidity, as liquid water can condense on the particles which may be interpreted as larger/more particles by the sensor. FEM monitors handle this issue by using an internal humidity probe and either an inlet heater or dryer to control the relative

65 humidity (British Columbia Ministry of Environment, 2020; Peters et. al 2008). These methods are not feasible for low-cost sensors, and therefore humidity effects as well as other biases that may exist need to be corrected. Multiple correction models are being produced by different groups to minimise these errors; many of which utilize RH in a correction formula (e.g., Ardon-Dryer et al. 2019, Barkjohn et al. 2020).

PurpleAir (PA) monitors are targeted to citizen scientists and air quality professionals alike as small, low-cost, easy-to-install

70 devices and as such, have proliferated to form a global network of sensors with thousands of devices in NA alone. These monitors contain two Plantower PMS5003 nephelometers which each detect $PM_{2.5}$ (named "A" and "B"), as well as separate sensors for measuring RH and temperature. $PM_{2.5}$ concentration is reported by the sensors using two different proprietary correction factors ("$PM_{2.5}$ CF 1" and "$PM_{2.5}$ CF ATM") which convert the estimated particle count in size bins into the reported concentrations. The "CF ATM" correction factor is derived from Beijing atmospheric conditions while "CF 1" was derived from a lab study using

75 symmetrical particles of a known size and is recommended for use in industrial settings (Zhou, 2016). The "CF 1" data were found to correlate better with FEM observations in our data set. A recent study has developed a particle count correction factor using US-based sites which shows promise however that was not tested here (Wallace et al., 2021). $PM_{2.5}$ concentrations from the PA

monitors have shown promising results when a colocation study derived correction model is applied but tend to overestimate FEM readings otherwise (Kim et al., 2019; Malings et al., 2019; Li et al., 2020; Feenstra et al., 2020; Tryner et al., 2020).

80   Issues of comparability arise as these low-cost monitors typically rely on light scattering based detection alone. This method is inherently less reliable than most FEM monitoring methods (Mehadi et al., 2020). Humidity has a large impact on the accuracy of the PA observations since these low-cost sensors do not purposely dry the air (some lowering of RH likely occurs from the heat produced by the electronics). At RH levels around 50 % and higher, low-cost $PM_{2.5}$ monitors can start counting aerosol water as larger particles as water accumulates on the particles and impacts the accuracy of light scattering based methods (Jayaratne et al.,

85   2018; Magi et al., 2019; Zamora et al., 2019). In addition, we and others have found the PA temperature observations to be biased high (and in turn RH biased low) because of internal heat produced by the electronics as well as incoming solar radiation (which has varying impacts depending on the physical location and placement of each monitor). However, the $PM_{2.5}$ observations still correlate well with gravimetric (Tryner et al., 2020), broadband spectroscopy (Kim et al., 2019; Li et al., 2020) and beta attenuation monitors (Zheng et al., 2018; Kim et al., 2019; Magi et al., 2019; Mehadi et al., 2020; Si et al., 2020), allowing for a correction

90   model to be developed and applied.

Many correction models have already been developed for PA monitors, several of which have been selected here for comparison. The US Environmental Protection Agency (EPA) recently released a multiple linear regression correction model which includes a RH term (Barkjohn et al., 2020). Several simple linear corrections are detailed on the PA mapping site (PurpleAir, 2021) including ones from LRAPA (2019) and Kelly et al. (2019). A recent study by Ardon Dryer et al. (2019) produced multiple corrections at

95   different colocation sites in the US. We selected their multiple linear model (including both temperature and RH) for the average of sensors at their Salt Lake City site. We found this correction to perform best for our dataset in comparison with the others provided in the study.

In this study, a novel method for detecting and preparing PA-FEM monitor colocations sites is developed and implemented. Using the resulting dataset, multiple PA $PM_{2.5}$ correction models are developed and evaluated in comparison with those from outside

100   parties. The correction which best improves the moderate to high concentration range (30 µg m^{-3}–100 µg m^{-3}) across multiple sites is selected as performing best in relation to health interpretations.

2 Methods

2.1 Colocation Site Selection and Data Retrieval

An automated algorithm to detect potential PA/FEM monitor colocation sites and apply quality control (QC) methods was

105   developed to identify the sites that were colocated, defined as being within 50 m of each other (as of November 2020), and remove any periods of invalid data. Monitor coordinates were provided through the AirNow (for FEM monitors) and PA databases. Based on this, 86 sites were identified; however, further analysis was necessary to remove sites or periods of time where the PA monitors were likely not colocated. FEM monitor detector types were retrieved from the US AQS database (EPA, 2020) for the US stations; Canadian station information was collected through contact with the monitor operators.

110   FEM observation data were obtained from the AirNow database (AirNow, 2021) which provided hourly $PM_{2.5}$ concentration observations from sites across North America. PA data was retrieved from their ThingSpeak repository as hourly averages for comparison with the FEM monitors (PurpleAir 2021). Sensor A and sensor B "CF=1" data from each PA monitor were averaged together to produce a single record. Historically, the "CF=1" and "CF=ATM" were erroneously mislabelled in the PA data; this has since been resolved and it was ensured that the actual "CF=1" data were being used here.

2.2 Quality Control

Once the sites were chosen, the observation data were flagged as invalid using both automated tests and manual inspection. Emphasis was placed on using the data available from the PA monitor only as much as possible in order to ensure these QC methods would still be applicable at sites without a collocated FEM monitor. However, the final step of the QC process used the FEM data as well as those from PA to calculate the overall $PM_{2.5}$ correlation; this was to ensure the automated collocation site detection did not inadvertently select a non-collocated monitor.

The first automated flagging did internal comparisons between the sensor A and sensor B in each PA monitor to identify failures from a particular sensor within the monitor (assuming both sensors have not failed in a similar way). Hours were flagged invalid where data from either A or B were missing, or where the absolute error between A and B for that hour was both greater than 5 μg m⁻³ and greater than half of the mean of A and B.

An automated flag was also developed to identify when a sensor was indoors rather than out based on the temperature and RH daily profiles. PA monitors measure relative humidity (RH) and temperature, we used these observations to flag entire months as invalid based on the variability of those data within each month. Individual months were flagged as invalid where the standard deviation in both temperature and RH for that month were less than 3 units or were identified as abnormally low using the Hampel Identifier, a commonly used outlier detection method for small sensors (Pearson 2002). Any month with less than 72 hours of data was also marked as invalid.

Manual inspections identified several individual hours for specific PA and FEM monitors that were marked invalid due to abnormally high concentrations reported. Data from AirNow have not been QC'ed by the responsible authorities, necessitating this check. In addition to this, any PA monitors with less than 2 months of valid data were dropped from the analysis; most of these had sporadic or very poorly correlated observations.

Sites with multiple colocated PA monitors were averaged together to produce a single data record for each site after flagging and removing any invalid data. Colocation sites with less than half a year of valid colocation data were then removed to ensure representative data coverage from each site. We further removed several sites after viewing scatter plots of their valid PA and FEM $PM_{2.5}$ observations and determining the performance to be unsatisfactory relative to the other sites. The final set of colocation sites (47 in total) were then selected as those with at least half a year (4380 hours) of valid data from both PA and FEM and a minimum correlation of 50 % for all valid hourly observations over the period of record.

PA RH values were restricted to the range 30 %–70 % (any values above/below this were set to 30 % or 70 %, respectively) as these values are near the efflorescence and deliquescence points typical of fine particulate matter (Parsons et al. 2004, Davis et al. 2015). Corrections utilizing RH tended to overcorrect observations at these extreme RH values. The RH data from the PA monitors were not corrected for the temperature bias resulting from the internal electronic heat produced near the sensor and direct solar radiation. Solar radiation impacts were too difficult to estimate given the variations in siting at each of the locations.

2.3 Correction Development

Multiple model forms were tested, including simple linear (Eq. 2), piecewise linear with up to three break points (Eq. 3), and polynomial models (Eq. 4); each with and without RH as an additional term. A temperature term was also tested; however, its impact was found to be minimal. Piecewise models which were built starting from the second segment tended to perform better in the mid-range $PM_{2.5}$ concentrations than those built starting from the first segment. Models which use RH-based corrections to account for particle growth prior to correcting were also tested (Eq. 5; Crilley et al., 2018). The k value in this equation represents the hygroscopicity parameter, derived from κ–Köhler theory (Petters and Kreidenweis, 2007). Multiple k values were determined for the Eq. 5 model using regression across three 30 μg m⁻³–40 μg m⁻³ bins (Low: 0 μg m⁻³–30 μg m⁻³, Moderate: 30 μg m⁻³–60 μg

m^{-3}, High: 60 μg m^{-3}–100 μg m^{-3}) as well as anything greater than 100 μg m^{-3} (Very High). An 'optimal' k value was then selected

155   such that the moderate to high range of concentrations would be improved the most using our evaluation framework presented here. More complex models, such as neural network-based corrections, were not tested due to the difficulty of transferability and useability for real time data.

$$Corrected = a * PM_{2.5} + b \tag{2}$$

$$Corrected = PM_{2.5} < x: a * PM_{2.5} + b; \ x \leq PM_{2.5} < x_2: a * PM_{2.5} + b \ ..... \tag{3}$$

160   $$Corrected = a * PM_{2.5} + b * PM_{2.5}{}^2 + c \tag{4}$$

$$Corrected = \frac{PM_{2.5}}{1 + k / (100 / RH - 1)} \tag{5}$$

Our correction development process was iterative and many model forms were tested. The current correction models commonly used are simple linear regressions (Kelly et al., 2019; Feenstra et al., 2019; LRAPA, 2019) or multiple regressions including an RH and/or a temperature term (Arden Dryer et al., 2019; Magi et al., 2019; Barkjohn et al., 2020). Segmented (or 'piecewise')

165   linear regressions have also been developed (Malings et al., 2019) as well as non-linear RH-based adjustments (Chakrabarti et al., 2004; Crilley et al., 2018; Tryner et al., 2020). The models which will be presented here are those that continually performed the best as our evaluations changed and improved. No correction model will work perfectly in every location, so it is important to test which correction works best at a given location.

2.4 Correction Evaluation

170   The correction models were applied to the testing data set and a suite of statistical comparisons were made to evaluate how well the developed correction models perform. In addition, comparisons with corrections from other studies were made to compare with our results.

When evaluating correction models, it is important to use a suite of statistical evaluation techniques, as each technique will have its own interpretation. We feel that correlation, while commonly used, by itself is not a good comparative measure as simple linear

175   models will not alter the correlation and more complex models tend to minimally change the correlation in our experience. Several comparative statistics are used commonly (Feenstra et al., 2019; Datta et al., 2020; Zamora et al., 2019; Tryner et al., 2020), including root mean square error (RMSE) and mean error/bias (ME/MB). However, these measures are not normalised making comparisons between sites difficult. Normalised statistical methods such as normalised RMSE (NRMSE) and mean fractional error/bias (MFE/MFB) allow for compatibility between sites/studies and reduce the locational context necessary to determine the

180   significance of the reported improvement (Boylan and Russell 2006).

We used the AQHI+ scale to evaluate correction performance across a range of concentrations to make our evaluations relevant to health outcomes (eq. 1; BC Lung Association, 2019). This helps reduce biasing comparison statistics, both with the majority of low AQHI+ observations and the much less common, high concentrations that are much more important from a health perspective. As concentrations in the middle and high end of the AQHI+ scale have the greatest impact on human health and a person's decisions

185   about changing their behaviour, performance at AQHI+ levels > 3 (> 30 μg m^{-3}) should be given greater consideration when selecting a correction model. Conversely, the observations of AQHI+ ≤ 3 (≤ 30 μg m^{-3}) represent most observations experienced in North American cities; better performance at these levels will ensure better day-to-day functionality of the correction but will have less impact from a health perspective.

3 Results and Discussions

190   Following the QA/QC process, 47 colocation sites were selected for developing and testing the corrections (Table 1; Figure 1). Of these 47 sites, 32 were selected for the training dataset (for developing the correction models) and the remaining 15 were used for the testing dataset. The mean start date was January 24, 2019, for the training sites and November 18, 2018, for the testing sites; all sites had data until the end of the year 2020. The number of days with valid colocation data at each site ranged from 212.5 to 1258.5 (nearly 3.5 years); with an interquartile range (IQR) of 379 days to 723 days. For the training sites the hourly valid data

195   capture ranged from 42.4 % to 98.9 %, with an IQR of 77.1 % to 92.5 %. The testing sites were similar, with valid data captures ranging from 66.7 % to 98.6 % and an IQR of 80.4 % to 88.1 %. The mean PA PM$_{2.5}$ concentration was larger than that from the FEM monitor for all but five sites.

Table 1. Selected PurpleAir (PA)/FEM colocation sites (Tr. = Training, Te. = Testing). Pearson's Correlation (*r*) between valid PA/FEM PM2.5 observations provided for each site. IDs corresponding to the map in Figure 1 are provided. Detection methods are provided for
200   **the site where this information was available (Beta = Beta Attenuation, FDMS = FDMS Gravimetric, Spec. = Broadband Spectroscopy).**

ID	FEM Site Name	Set	Detector	# PAs	Days Valid	r	ID	FEM Site Name	Set	Detector	# PAs	Days Valid	r
1	Abbotsford Airport	Tr.	Beta	3	844.6 (98.9%)	0.91	25	Redwater	Tr.	Spec.	1	662.9 (86.2%)	0.97
2	Blair Street	Tr.	FDMS	1	383 (88.2%)	0.61	26	Riverside - Rubidoux	Tr.	Beta	9	1169.8 (95.3%)	0.86
3	Boston - Von Hillern	Tr.	Beta	2	266.9 (94.4%)	0.70	27	San Diego-Sherman Elem.	Tr.	N/A	3	288.2 (85.4%)	0.87
4	Carpenter	Tr.	Beta	2	1127.3 (91.9%)	0.63	28	Santa Barbara	Tr.	Beta	1	588.8 (90.2%)	0.81
5	Ctclusi Radar Hill - OR	Tr.	N/A	1	293.5 (63.7%)	0.87	29	Santa Maria - Broadway	Tr.	Beta	1	614 (88.1%)	0.83
6	Darrington – Fir St	Tr.	Beta	1	398.7 (90.6%)	0.95	30	Tacoma - Alexander Ave	Tr.	N/A	1	756.8 (98.8%)	0.91
7	Downtown Sacramento	Tr.	Beta	29	717.4 (89.2%)	0.97	31	Thousand Oaks	Tr.	Beta	1	562.5 (92.6%)	0.82
8	Edmonton Woodcroft	Tr.	FDMS	1	374 (95.4%)	0.75	32	Vancouver - NE 84th Ave	Tr.	Beta	1	428.8 (54.7%)	0.92
9	Rio Mesa School #2	Tr.	Beta	1	694.1 (90.9%)	0.73	33	Arendtsville	Te.	Beta	2	404.2 (86.3%)	0.90
10	Fresno - Garland	Tr.	Beta	2	758.8 (80%)	0.92	34	Atascadero2	Te.	Beta	1	916 (82.4%)	0.89
11	Eastgate	Tr.	Spec.	1	258.9 (59.9%)	0.89	35	Bee Ridge	Te.	Spec.	1	311.8 (60.9%)	0.80
12	Indpls - Washington Park	Tr.	Spec.	1	728.3 (71.4%)	0.75	36	Burnaby South	Te.	Beta	1	411.5 (91.4%)	0.93
13	Lake Sugema	Tr.	N/A	2	448.5 (96%)	0.75	37	Eugene - Highway 99	Te.	Beta	1	838.5 (97%)	0.94
14	Lancaster Dw	Tr.	Beta	1	355.2 (77.7%)	0.90	38	Grass Valley	Te.	Beta	1	370.5 (80.8%)	0.97
15	Lee Vining	Tr.	Spec.	1	416.8 (90.2%)	0.99	39	Greenwood	Te.	Spec.	1	473.2 (76%)	0.91
16	Math & Science Ctr	Tr.	Spec.	1	583.8 (84.4%)	0.90	40	Hillsboro - Hare Field	Te.	N/A	1	400.3 (92%)	0.99
17	Mcmillan Reservoir	Tr.	Beta	1	212.5 (62%)	0.75	41	Iowa City, Hoover School	Te.	Spec.	2	715.9 (98.3%)	0.90
18	Oakridge - Willamette	Tr.	Beta	3	439.5 (99.4%)	0.98	42	Keene	Te.	Beta	2	936.3 (89.5%)	0.82
19	Ojai - Ojai Ave.	Tr.	Beta	1	276.8 (90.5%)	0.85	43	LLCHD BAM	Te.	N/A	1	654.2 (66.4%)	0.70
20	Pendleton - Mckay Creek	Tr.	N/A	1	355.7 (55%)	0.97	44	Ncore	Te.	N/A	2	374.6 (67.2%)	0.89
21	Piru - Pacific	Tr.	Beta	1	504.6 (80.8%)	0.79	45	White Mt Research Cntr.	Te.	N/A	1	664.9 (88.8%)	0.95
22	Portland - Se Lafayette	Tr.	N/A	1	775.3 (96.6%)	0.96	46	PRG Plaza 400	Te.	Beta	3	1258.5 (97.8%)	0.94
23	Public Health	Tr.	Spec.	2	872.5 (94.5%)	0.84	47	Simi Valley - Cochran St.	Te.	Beta	1	675.9 (87.4%)	0.87
24	Red Bluff - Walnut Office	Tr.	Beta	1	602.8 (73.9%)	0.92		AVERAGE	-		2.1	578 (84.5%)	0.87

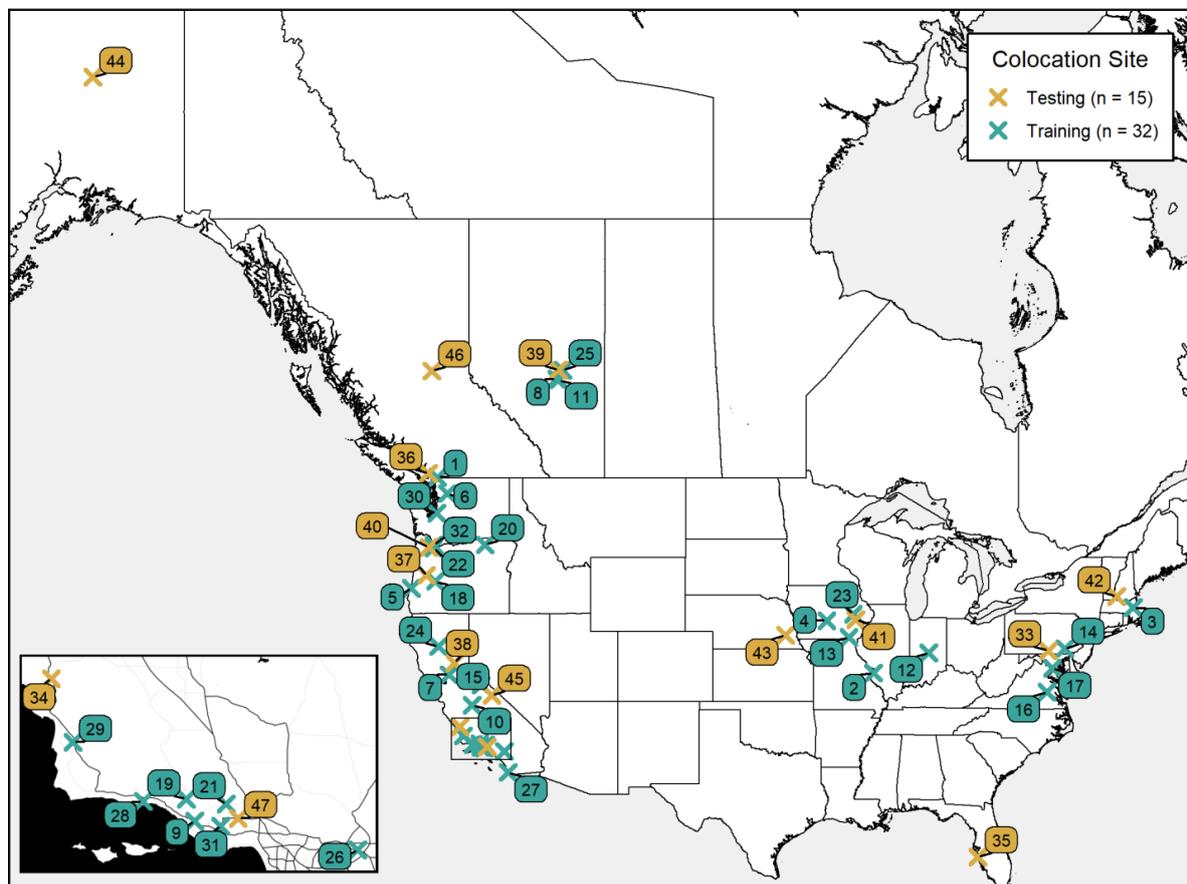



Figure 1: Locations of selected PurpleAir/FEM colocation sites. Of the 47 sites, 32 were used for training the correction models and the remaining 15 were used for testing. Inset map tiles by Stamen Design, under CC BY 3.0. Data by OpenStreetMap, under ODbL.

205   The mean averages of the PA $PM_{2.5}$ concentrations at each site tended to be higher than their FEM counterparts in both data sets except at the lowest humidity levels (Figure 2). PA concentrations tended to be biased increasingly higher as humidity increases; this was not the same case for the FEM monitors which typically have their intake stream heated or dried to lower the RH impacts. The mean testing site concentrations had similar ranges for matching monitor types between the two data sets; however, many of the testing data sites tended to have lower concentrations on average than the training sites.

210   The FEM monitors in this study utilized one of three main $PM_{2.5}$ detection methods (Figure 3): beta attenuation (26 locations), broadband spectroscopy (9 locations) and FDMS gravimetric (2 locations). There were ten locations with unknown monitor types, all in the USA. It is most likely that these are beta attenuation monitors based on the high ratio of these detectors in the USA versus others and the comparability between site mean AQHI+ error shown in Figure 3; however, some may be broadband spectrometers or gravimetric monitors. There were no significant differences between the mean of the site mean PA AQHI+ errors for each of

215   the FEM sensor types (Kruskal–Wallis $p > 0.05$).

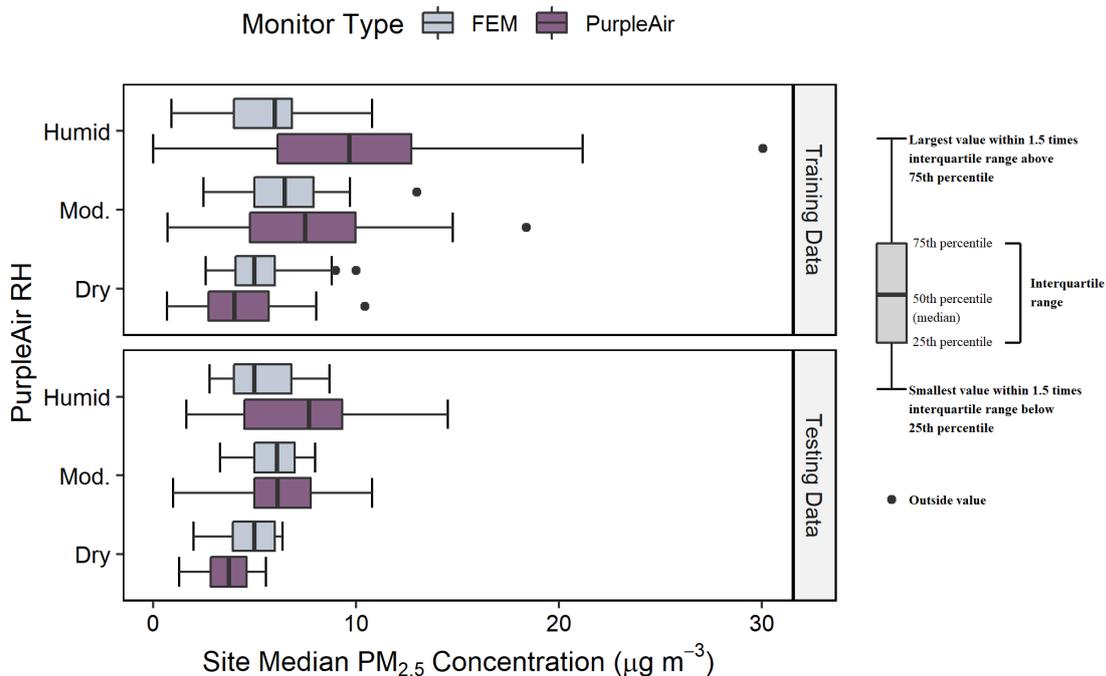



Figure 2. Distributions of the Federal Equivalent Method (FEM) and PurpleAir training/testing sites median PM2.5 concentrations (µg m⁻³) at dry (0 %–33 %), moderate (34 %–66 %) and humid (67 %–100 %) relative humidity (RH) groupings. The boxplot format is indicated on the right.

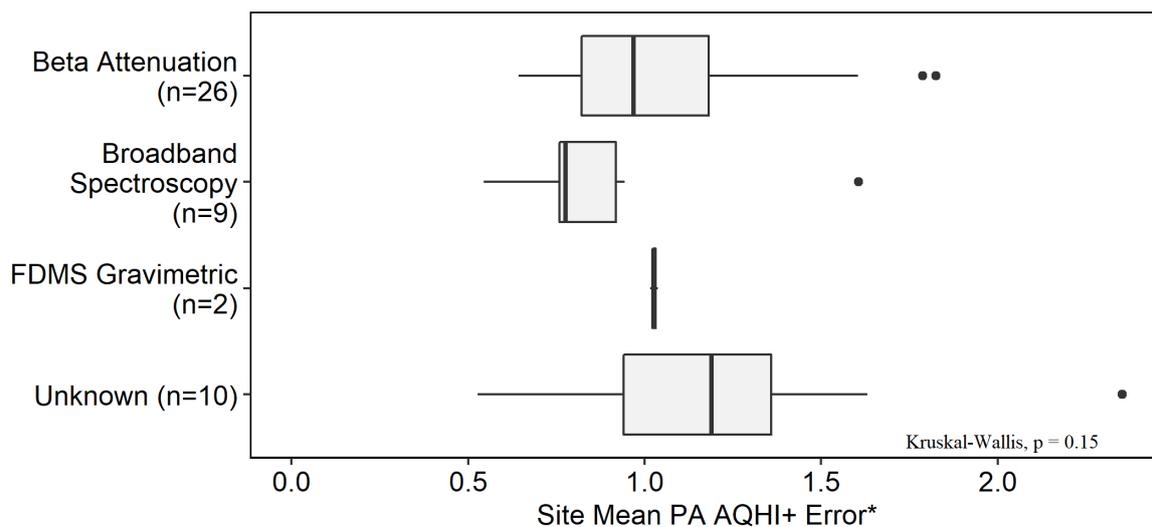
*Hours where the FEM AQHI+ == 1 were removed.

220

Figure 3. Distributions of the site mean PurpleAir AQHI+ error for each of the known FEM detector types. Hours where the Federal Equivalent Method (FEM) AQHI+ was equal to 1 were removed. The Kruskal–Wallis global p-value (>0.05) is provided in the bottom right, indicating no significant differences between the group means.

3.1 Correction Development

225 Eight correction models were selected for evaluation (Table 2) including four developed in this study from regressing the training data (Models 1–4) as well as four others available from the literature (Models 5–8). Nearly all these correction models utilize the 'PM$_{2.5}$ CF 1' column provided by PA, except Model 6 and Model 8 which use 'PM$_{2.5}$ CF ATM'. Model 1 is a multiple linear model including a RH term. Model 2 uses a RH growth adjustment (k=0.24) to reduce the PM$_{2.5}$ concentration as RH increases (see Eq. 5). Model 3 is a second-degree polynomial with a RH term included. Model 4 is a 3-breakpoint piecewise model with breakpoints

230 selected to visually fit the data best over multiple iterations. The last four equations are provided from studies by other parties and consist of two simple linear models (Models 5 and 6), a multiple linear model including RH (Model 7) and a multiple linear model including both RH and temperature (Model 8).

Table 2. PurpleAir correction models selected for evaluation. The 'Min' column indicates the minimum corrected value at a RH of 70% (*and a temperature of 20 ºC for Model 8).

Correction	Form	Source	Min	Formula
No Model	-	-	0	pm25_cf1
Model 1	Linear (+RH)	-	-2	0.708 * pm25_cf1 - 0.115 * rh + 5.78
Model 2	RH Growth	-	0	pm25cf1 / (1 + 0.24 / (100 / rh - 1))
Model 3	Polynomial (+RH)	-	0.3	0.53 * pm25_cf1 + 0.000952 * pm25_cf1^2 - 0.0914 * rh + 6.3
Model 4	Piecewise @ 2.5/40/300	-	1.9	pm25_cf1 ≤ 2.5: 0.92 * pm25_cf1 + 1.86 2.5 < pm25_cf1 ≤ 40: 0.42 * pm25_cf1 + 3.1 40 < pm25_cf1 ≤ 300: 0.87 * pm25_cf1 - 14.8 pm25_cf1 > 300: 1.16 * pm25_cf1 - 100.6
Model 5	Linear	1	2.6	0.778 * pm25_cf1 + 2.65
Model 6	Linear	2	-0.7	0.50 * pm25_atm - 0.66
Model 7	Linear (+RH)	3	-0.2	0.534 * pm25_cf1 - 0.0844 * rh + 5.71
Model 8	Linear (+RH +T)	4	1.5*	(pm25_atm + 3.04 + 0.07 * temp - 0.02 * rh) / 1.55

1. Kelly et al. (2019) 2. LRAPA (2019) 3. Barkjohn et al. (2020) 4. Ardon-Dryer et al. (2019)

235 The corrected data from the models typically had a minimum value of at or just below 0 µg m^{-3}, except for Models 4, 5, and 8 which had a higher minimum value (around 2 µg m^{-3}). Models 1, 6 and 7 produced negative values during periods of low concentrations and high humidity (which need to be removed or replaced with 0 after correcting). A constant temperature of 20 ℃ was assumed here for Model 8 to calculate the minimum corrected value.

3.2 Correction Evaluation

240 Raw PA observations were biased positively at FEM AQHI+ levels between 1 and 9, peaking at an AQHI+ of 4 to 7, as shown in Figure 4. An AQHI+ bias at or near zero is preferred, especially at the higher FEM AQHI+ levels most impactful to human health. Models 2 and 7 minimised this bias the most on average. Model 2 was biased slightly high at AQHI+ of 6 or lower, and slightly high onwards with a minimum at 10 AQHI+. Model 7 performed similarly; however, it was biased slightly low throughout except at an AQHI+ of 1 and had the worst performance at 8 and 10 AQHI+. Models 1 and 8 were the next best; however, they were both

245 increasingly negatively biased at higher FEM AQHI+ levels. Model 5 and Model 6 had relatively large positive and negative biases in the 3–9 and 3–10+ AQHI+ levels, respectively. Further comparisons were only made on Models 1, 2, 7, and 8 as they showed the best performance here.

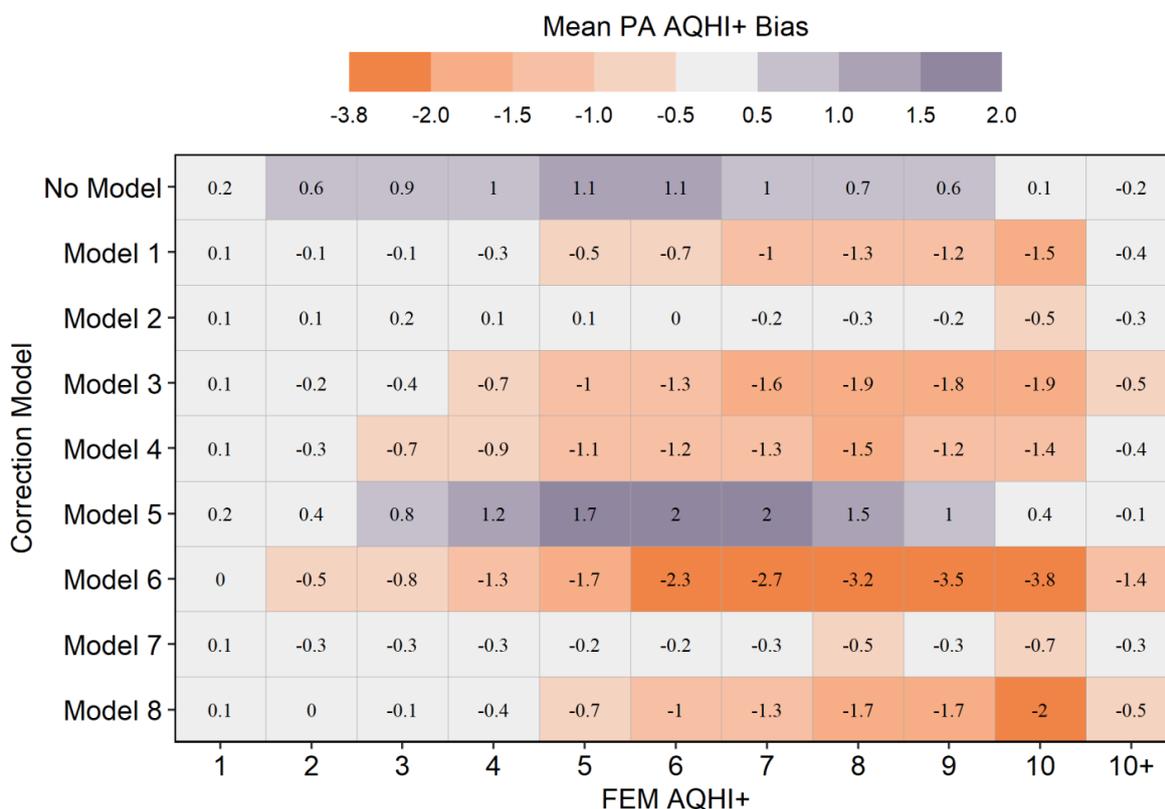



Figure 4. Mean PurpleAir AQHI+ bias for each correction model (including the raw data) at Federal Equivalent Method (FEM) AQHI+
250 **levels. A value at or near 0 is preferred, especially for higher AQHI+.**

The NRMSE, NMB, MFE and MFB for the PA monitors were worse at lower concentrations and improved as concentrations increased (Figure 5). We saw similar performance between models; all of which improved upon the raw PA observations at most concentrations. Models 1 and 8 worsened the MFE and bias measurements in the moderate to high range, while Models 2 and 7 had the best performance outside of the low concentration range. Model 7 was best for the very low observations (AQHI+ of 1);

255 however, Model 2 tended to perform better starting at 2–3 AQHI+.

Goal and acceptable levels for MFE and MFB are suggested in Boylan and Russell (2006). Raw PA data meets the goal level of 50 % for all but the lowest AQHI+ for MFE where it still meets the acceptable level of 75 %. Only Models 7 and 8 bring these lowest concentrations into/near the goal level. Both uncorrected and corrected observations were within the goal range for MFB (±30 %). We assumed goal and acceptable levels for NRMSE of 50 % and 70 %, respectively, to align with the levels defined for

260 MFE. Using these standards, the uncorrected PurpleAir data is unacceptable at AQHI+ equal to 1 and gets increasingly better until it reaches the goal level in the high concentrations. Each correction model brings the data into the goal level except at AQHI+ equal to 1 where it is only acceptable. A goal level of ±30 % was assumed for the NMB like that for the MFB and the level defined for mean bias (MB) defined in Chang and Hanna (2004). Only the uncorrected data for AQHI+ values between 2–3 exceeded this goal level across our sites.

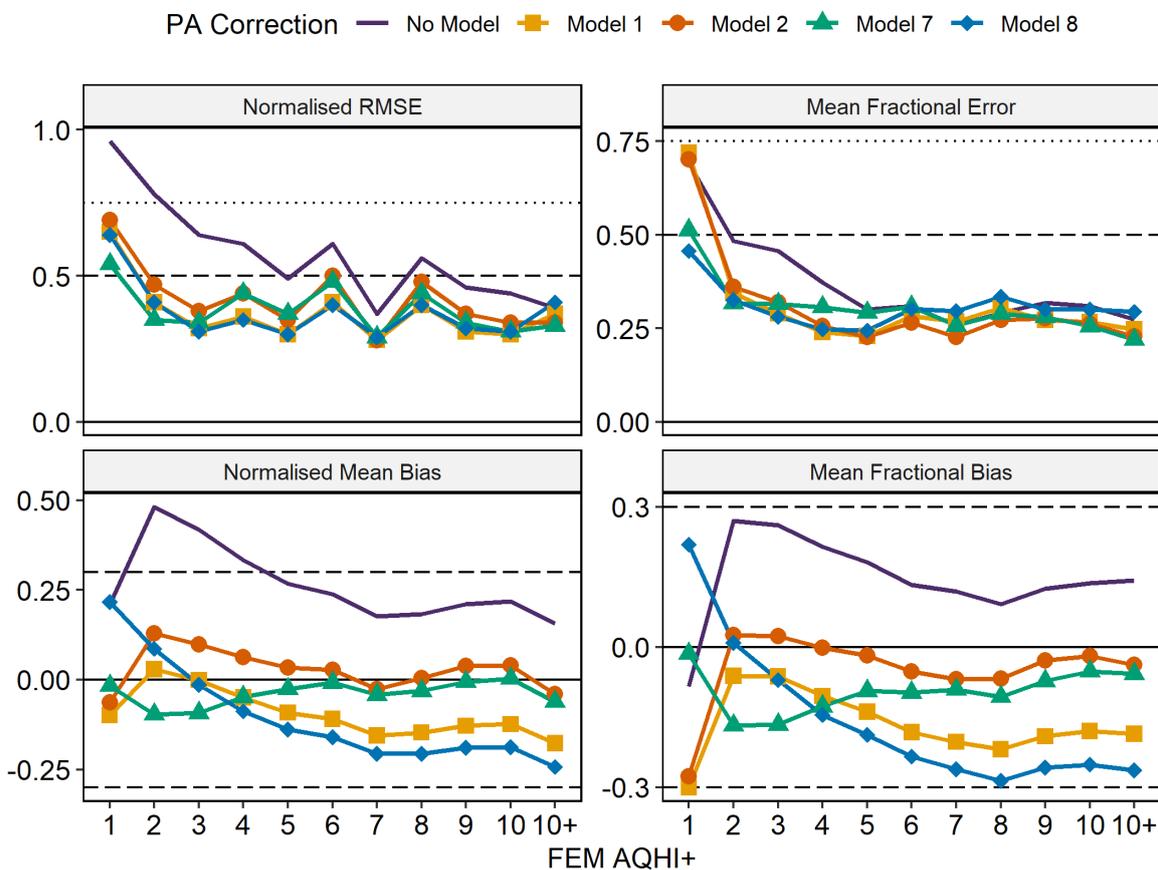



Figure 5. Comparison statistics across Federal Equivalent Method (FEM) AQHI+ levels for select correction models. Goal and acceptable levels are displayed where possible for RMSE (0.75 & 0.5), MFE (0.75 & 0.5), NMB (±0.3& ±0.6) and MFB (±0.3 & ±0.6).

These statistical comparisons were also made on coarser AQHI+ groupings (Table 3). A ranking score was calculated for each model using the mean average of the ranks (from 1 to 5) for each statistic within an AQHI+ group. A lower score indicates better relative performance within that AQHI+ range. Models 2 and 7 performed the best in the high and very high AQHI+ categories. However, the models did not perform as consistently well in the low and moderate ranges. Models 7 and 8 tended to be the best for the low range, while Models 2 and 1 were better for the moderate range.

The error/bias in AQHI+ from the uncorrected PA monitors was greatest in the moderate to high range (Figure 6). The selected corrections produced similar improvements to each other, all improving upon the PA's ability to correctly determine the hourly AQHI+ except for at the most extreme concentrations (> 100 μg m⁻³). For AQHI+ bias model 1 improved upon Model 7, which has the same form, except at very high FEM concentrations. This was not the case for the mean AQHI+ bias; however, as Model 1 becomes increasingly negatively biased as FEM concentrations increase. Model 2 was the best overall performer for both AQHI+ error and bias, being marginally outperformed only in the low concentration range. This was followed by Model 7 which performed well for all but the mean AQHI+ error in the moderate concentration range. Model 8 performed sufficiently; however, it tended to bias the AQHI+ observations low, especially in the moderate concentration range.

Table 3. PurpleAir (PA) normalised mean bias (NMB), normalised root mean square error (NRMSE), mean fractional error (MFE) and mean fractional bias (MFB) at low/moderate/high/very high Federal Equivalent Method (FEM) AQHI+ levels for each PA correction model. A crude score is calculated by averaging each statistics integer rank (from 1 to 5) for the models within that AQHI+ group. The top performing models are highlighted.

FEM AQHI+	Model	NMB	NRMSE	MFE	MFB	Score
	No Model	0.33	0.96	0.65	**-0.01**	4
	Model 1	-0.04	0.56	0.64	-0.25	3.5
Low [1-3]	Model 2	**0.02**	0.62	0.63	-0.21	3
	Model 7	-0.05	**0.49**	0.47	-0.04	**2**
	Model 8	0.15	0.55	**0.43**	0.17	2.5
	No Model	0.3	0.59	0.35	0.2	5
	Model 1	-0.07	0.37	**0.24**	-0.12	2.3
Moderate [4-6]	Model 2	0.05	0.44	0.25	**-0.01**	**2.1**
	Model 7	**-0.03**	0.44	0.3	-0.11	2.6
	Model 8	-0.12	**0.35**	0.25	-0.17	3
	No Model	0.19	0.47	0.28	0.11	4
	Model 1	-0.15	**0.33**	0.28	-0.2	2.8
High [7-9]	Model 2	**0**	0.38	**0.25**	**-0.06**	**1.8**
	Model 7	-0.03	0.36	0.27	-0.09	2.3
	Model 8	-0.2	0.34	0.31	-0.27	4.3
	No Model	0.16	0.39	0.28	0.14	3.5
	Model 1	-0.17	0.38	0.25	-0.18	3.5
Very High [10+]	Model 2	**-0.03**	**0.34**	0.23	**-0.03**	**1.4**
	Model 7	-0.06	**0.34**	**0.22**	-0.06	1.6
	Model 8	-0.24	0.42	0.3	-0.26	5

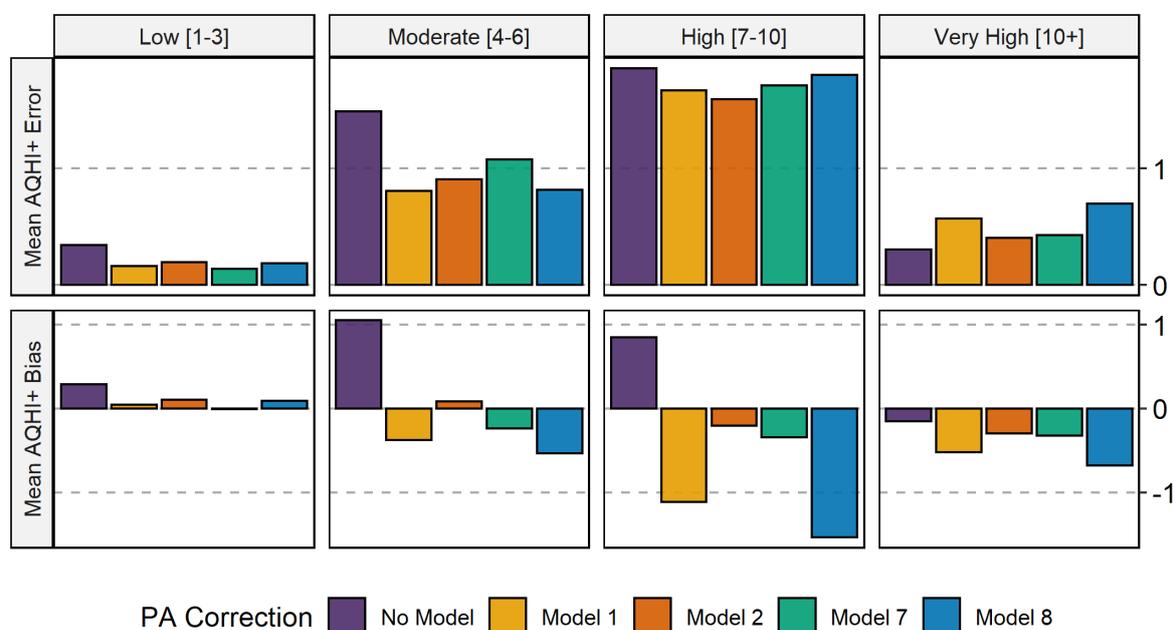



Figure 6. Mean PurpleAir (PA) AQHI+ error and bias for low/moderate/high/very high Federal Equivalent Method (FEM) AQHI+ levels for selected correction models.

290   Model 2 produces a mean AQHI+ bias and error consistently closer to 0 than the other correction models (or no model at all) across the range of observed concentrations. Only at the lowest concentrations do the other models marginally outperform Model 2 across our testing sites for most of the comparisons made.

4. Conclusions

The concentrations of PM$_{2.5}$ reported from the PA monitors were biased high compared to the FEM monitors at most colocation sites, especially for the lower concentration range. This bias is attributed to both the method of detection as well as hygroscopic growth from increased humidity. No significant differences were detected between FEM sensor methods, which are rigorously tested and evaluated to ensure this consistency. Based on our colocation method there is a risk that some sites are not true colocation sites, however, given the proximity of the sensors and good correlation (>60 %) we decided the potential impact would be minimal. The Canadian AQHI+ system was useful as a framework for evaluating correction models across a range of concentrations infrequent high values or numerous low values can skew performance statistics when evaluating the full range at once.

The selected corrections discussed here improve the performance of PA similarly, however, Model 2 had consistently better performance, especially at moderate to high concentrations that are important to health. This was followed closely by Model 7. Models 1 and 8 perform well, especially in the low to moderate range, however they do not perform as well at higher concentrations. Models 3 through 6 tended to overcorrect (or under correct for the case of Model 5) the PA data in the moderate to high range. It should be noted that the average performance across the testing sites and over time was evaluated here; performance at colocation sites and across time was not the same. In addition, while our correction model focuses on correcting the impacts of humidity, other characteristics like refractive index and particle shape, density, and size distribution may account for differences in PM$_{2.5}$ estimates.

Future studies should focus on developing and evaluating correction models as more data become available from the PA network, as well as installing and documenting additional colocation sites. Specifically, the k-value utilized in our Model 2 should be adjusted and re-evaluated as more collocation data become available. Valid collocation data are imperative for both developing and evaluating small sensor performance before and after applying a correction formula. These corrections should be evaluated in comparison with the others available to ensure comparable or improved performance. In addition, the improved particle bin correction factor proposed by Wallace et al. (2021) should be implemented for these sites and an adjusted RH correction model should be developed.

We recommend testing the performance of several models at specific sites of interest and selecting the best performing model for a given site. Models 1, 2, 7 and 8 presented here are good starting points. As more colocation data become available seasonal and area specific correction models should be examined. Performance in the moderate to high concentration range should be focused on as these are the most important from a health perspective; the low concentrations are less important while also being the most observed levels in the US and Canada. Correlation is useful for evaluating overall sensor performance at a site, but not as useful for evaluating and comparing correction performance. Normalised methods such as NRMSE, MFB or MFE are good measures, but we recommend evaluations across a range of PM$_{2.5}$ concentrations, such as using the AQHI+ framework as presented here. If one intends to develop a site-specific correction model, we recommend using the same form as our Model 2 while adjusting the k value. For scenarios where testing models on individual locations is not an option, such as applying a correction in an area without a nearby PA-FEM colocation site, we recommend using our Model 2.

5. Author Contribution

B. Nilson developed the analysis code and drafted the initial manuscript with contributions from all authors. P. L. Jackson, C. Schiller, and M. T. Parsons provided regular guidance and feedback throughout the project.

6. Code/Data Availability

330 Code/data from this study are available upon request to the authors.

7. Competing interests

The authors declare that they have no conflict of interest.

8. Acknowledgements

Data sourced from the PurpleAir ThingSpeak database (PurpleAir) and the US AirNow database (FEM). Funding and Support

335 from ECCC and from the Natural Sciences and Engineering Research Council of Canada (NSERC) through a Discovery Grant

(RGPIN2017-05784) to Peter Jackson.

References

Ardon-Dryer, K., Dryer, Y., Williams, J. N., and Moghimi, N.: Measurements of PM2.5 with PurpleAir under atmospheric
conditions, Atmos. Meas. Tech., 13, 5441–5458, doi:10.5194/amt-13-5441-2020, 2020.

340 Barkjohn, K. K., Gantt, B., and Clements, A. L.: Development and Application of a United States wide correction for PM2.5
data collected with the PurpleAir sensor, Atmos. Meas. Tech. Discuss. [preprint], doi:10.5194/amt-2020-413, in review,
2020.

BC Lung Association: State of the air 2019, https://bc.lung.ca/sites/default/files/1074-
State%20Of%20The%20Air%202019_R9.pdf, last access: 20 April 2021, 2019.

345 British Columbia Ministry of Environment: The British Columbia Field Sampling Manual Part B Air and Air Emissions Testing,
https://www2.gov.bc.ca/assets/gov/environment/research-monitoring-and-
reporting/monitoring/emre/bc_field_sampling_manual_part_b.pdf, last access: 10 August 2021, 2020.

Bowe, B., Xie, Y., Yan, Y., and Al-Aly, Z.: Burden of Cause-Specific Mortality Associated With PM2.5 Air Pollution in the
United States, JAMA Netw. open. 2(11):16pp, doi:10.1001/jamanetworkopen.2019.15834, 2019.

350 Boylan J. W., and Russell A. G.: PM and light extinction model performance metrics, goals, and criteria for three-dimensional
air quality models, Atmos. Environ., 40(26), 4946–4959, doi:10.1016/j.atmosenv.2005.09.087, 2006.

Chang J. C., and Hanna S. R.: Air quality model performance evaluation, Meteorol. Atmos. Phys., 87, 167–196,
doi:10.1007/s00703-003-0070-7, 2004.

Crilley, L. R., Shaw, M., Pound, R., Kramer, L. J., Price, R., Young, S., Lewis, A. C., and Pope, F. D.: Evaluation of a low-cost
355 optical particle counter (Alphasense OPC-N2) for ambient air monitoring, Atmos. Meas. Tech., 11, 709–720,
doi:10.5194/amt-11-709-2018, 2018.

Datta, A., Saha, A., Zamora, M. L., Buehler, C., Hao, L., Xiong, F., Gentner, D. R., and Koehler, K.: Statistical field calibration
of a low-cost PM2.5 monitoring network in Baltimore, Atmos. Env., 242, 117761, doi:10.1016/j.atmosenv.2020.117761,
2020.

360 Davis, R. D., Lance, S., Gordon, J. A., Ushijima, S. B., and Tolbert, M. A.: Contact efflorescence as a pathway for crystallization
of atmospherically relevant particles, Proc. Natl. Acad. Sci., 112 (52), 15815-15820, doi:10.1073/pnas.1522860113, 2015.

[EPA] Environmental Protection Agency: Air Quality System (AQS), https://www.epa.gov/aqs, last access: 22 June 2021, 2020.

[EPA] Environmental Protection Agency: Criteria Air Pollutants, https://www.epa.gov/criteria-air-pollutants, last access: 22 June
2021.

365 Feenstra, B., Papapostolou, V., Hasheminassab, S., Zhang, H., Boghossian, B., Cocker, D., and Polidori, A: Performance evaluation of twelve low-cost PM2.5 sensors at an ambient air monitoring site, Atmos. Environ., 216, 116946, doi:10.1016/j.atmosenv.2019.116946, 2019.

Feng, S., Gao, D., Liao, F., Zhou, F., and Wang, X: The health effects of ambient PM2.5 and potential mechanisms, Ecotoxicol. Environ. Saf., 128:67-74, doi:10.1016/j.ecoenv.2016.01.030, 2016.

370 Government of Canada: Air Pollution Common Contaminants, https://www.canada.ca/en/environment-climate-change/services/air-pollution/pollutants/common-contaminants.html, last access: 22 June 2021, 2017.

Health Effects Institute: State of Global Air 2020, https://www.stateofglobalair.org/sites/default/files/documents/2020-10/soga-2020-report-10-26_0.pdf, last access: 22 June 2021, 2020.

Jayaratne, R., Liu, X., Thai, P., Dunbabin, M., and Morawska, L.: The influence of humidity on the performance of a low-cost
375 air particle mass sensor and the effect of atmospheric fog, Atmos. Meas. Tech., 11(8), 4883–4890, doi:10.5194/amt-11-4883-2018, 2018.

Kelly, K. E., Whitaker, J., Petty, A., Widmer, C., Dybwad, A., Sleeth, D., Martin, R., and Butterfield, A.: Ambient and laboratory evaluation of a low-cost particulate matter sensor, Environ. Pollut., 221, 491–500, doi:10.1016/j.envpol.2016.12.039, 2017.

380 Kim, S., Park, S., and Lee, J: Evaluation of Performance of Inexpensive Laser Based PM2.5 Sensor Monitors for Typical Indoor and Outdoor Hotspots of South Korea, Appl. Sci., 9(9), 1947, doi:10.3390/app9091947, 2019.

[LRAPA] Lane Regional Air Protection Agency: PurpleAir Monitor Correction Factor History, https://www.lrapa.org/DocumentCenter/View/4147/PurpleAir-Correction-Summary, last access: 1 September 2021, 2019.

Lelieveld, J., Evans, J. S., Fnais, M., Giannadaki, D., and Pozzer, A.: The contribution of outdoor air pollution sources to
385 premature mortality on a global scale, Nature, 525(7569), 367–371, doi:10.1038/nature15371, 2015.

Li, H. Z., Gu, P., Ye, Q., Zimmerman, N., Robinson, E. S., Subramanian, R., Apte, J.S., Robinson, A. L., and Presto, A. A.: Spatially dense air pollutant sampling: Implications of spatial variability on the representativeness of stationary air pollutant monitors, Atmos. Environ. X, 2, 100012, doi:10.1016/j.aeaoa.2019.100012. 2019.

Li, J., Mattewal, S. K., Patel, S., Biswas, P.: Evaluation of Nine Low-cost-sensor-based Particulate Matter Monitors, Aerosol Air
390 Qual. Res., 20(2), 254–270, doi:10.4209/aaqr.2018.12.0485, 2020.

Magi, B. I., Cupini, C., Francis, J., Green, M., Hauser, C.: Evaluation of PM2.5 measured in an urban setting using a low-cost optical particle counter and a Federal Equivalent Method Beta Attenuation Monitor Evaluation of PM2.5 measured in an urban setting using a low-cost optical particle counter and a Federal Eq, Aerosol Sci. Technol., 54(2), 147–159, doi:10.1080/02786826.2019.1619915. 2019.

395 Malings, C., Tanzer, R., Hauryliuk, A., Saha, P. K., Robinson, A. L., Presto, A. A., and Subramanian, R.: Fine particle mass monitoring with low-cost sensors: Corrections and long-term performance evaluation, Aerosol Sci. Technol., 54(2), 160–174, doi:10.1080/02786826.2019.1623863, 2019.

Mcguinn, L. A., Ward-Caviness, C., Neas, L. M., Schneider, A., Di, Q., Chudnovsky, A., Schwartz, J., Koutrakis, P., Russell, A. G., Garcia, V., et al.: Fine particulate matter and cardiovascular disease: Comparison of assessment methods for long-term
400 exposure, Environ. Res. J., 159, 16–23, doi:10.1016/j.envres.2017.07.041, 2017.

Mehadi, A., Moosmüller, H., Campbell, D. E., Ham, W., Schweizer, D., Tarnay, L., and Hunter, J.: Laboratory and field evaluation of real-time and near real-time PM2.5 smoke monitors, J Air Waste Manag Assoc, 70(2), 158–179, doi:10.1080/10962247.2019.1654036, 2020.

Parsons, M. T., Knopf, D. A., and Bertam, A. K.: Deliquescence and Crystallization of Ammonium Sulfate Particles Internally
405 Mixed with Water-Soluble Organic Compounds, J. Phys. Chem. A., 108(52), 11600-11608, doi:10.1021/jp0462862, 2004.

Pearson, R.: Outliers in process modelling and identification, IEEE T Contr. Syst. T., 10(1), 55-63, doi:10.1109/87.974338, 2002.

Peters, T. M., Riss, A. L., Holm, R. L., Singh, M., and Vanderpool, R. W.: Design and evaluation of an inlet conditioner to dry particles for an aerodynamic particle sizer, J. Environ, Mon, 10(4), 541-551, doi:10.1039/b717543d, 2008.

410 Petters, M. D. and Kreidenweis, S. M.: A single parameter representation of hygroscopic growth and cloud condensation nucleus activity, Atmos. Chem. Phys., 7, 1961–1971, doi:10.5194/acp-7-1961-2007, 2007.

PurpleAir: Real Time Air Quality Monitoring, https://www.purpleair.com/map, last access: 18 June 2021.

Stieb, D. M., Burnett, R. T., Smith-Doiron, M., Brion, O., Hwashin, H. S., and Economou, V.: A New Multipollutant, No-Threshold Air Quality Health Index Based on Short-Term Associations Observed in Daily Time-Series Analyses, J. Air
415 Waste Manag. Assoc., 58:3, 435-450, doi:10.3155/1047-3289.58.3.435, 2008.

Si, M., Xiong, Y., Du, S., and Du, K.: Evaluation and calibration of a low-cost particle sensor in ambient conditions using machine-learning methods, Atmos. Meas. Tech., 13(4), 1693–1707, doi:10.5194/amt-13-1693-2020, 2020.

Tryner, J., L'Orange, C., Mehaffy, J., Miller-Lionberg, D., Hofstetter, J. C., Wilson, A., and Volckens, J.: Laboratory evaluation of low-cost PurpleAir PM monitors and in-field correction using co-located portable filter samplers, Atmos Environ,
420 220(117067), doi:10.1016/j.atmosenv.2019.117067, 2020.

Wallace, L., Bi, J., Ott, W. R., Sarnat, J., and Liu, Y.: Calibration of low-cost PurpleAit outdoor monitors using an improved method of calculating PM2.5, Atmos Environ, 256, doi:10.1016/j.atmosenv.2021.118432, 2021.

Zamora, M. L., Xiong, F., Gentner, D., Kerkez, B., Kohrman-Glaser, J., Koehler, K.: Field and Laboratory Evaluations of the Low-Cost Plantower Particulate Matter Sensor, Environ. Sci. Technol., 53(2), 838–849, doi:10.1021/acs.est.8b05174, 2019.

425 Zheng, T., Bergin, M. H., Johnson, K. K., Tripathi, S. N., Shirodkar, S., Landis, M. S., Sutaria, R., Carlson, D. E. : Field evaluation of low-cost particulate matter sensors in high-and low-concentration environments, Atmos. Meas. Tech., 11(8), 4823–4846. doi:10.5194/amt-11-4823-2018, 2018.

Zhou, Y.: Digital universal particle concentration sensor: PMS5003 series data manual, https://www.aqmd.gov/docs/default-source/aq-spec/resources-page/plantower-pms5003-manual_v2-3.pdf, last access: 27 July 2021, 2016.