

1 **Improving thermodynamic profile retrievals from microwave**
2 **radiometers by including Radio Acoustic Sounding System (RASS)**
3 **observations**

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44 **Abstract**

45 Thermodynamic profiles are often retrieved from the multi-wavelength brightness
46 temperature observations made by microwave radiometers (MWRs) using regression methods
47 (linear, quadratic approaches), artificial intelligence (neural networks), or physical-iterative
48 methods. Regression and neural network methods are tuned to mean conditions derived from
49 a climatological dataset of thermodynamic profiles collected nearby. In contrast, physical-
50 iterative retrievals use a radiative transfer model starting from a climatologically reasonable
51 profile of temperature and water vapor, with the model running iteratively until the derived
52 brightness temperatures match those observed by the MWR within a specified uncertainty.

53 In this study, a physical-iterative approach is used to retrieve temperature and humidity
54 profiles from data collected during XPIA (eXperimental Planetary boundary layer Instrument
55 Assessment), a field campaign held from March to May 2015 at NOAA's Boulder Atmospheric
56 Observatory (BAO) facility. During the campaign, several passive and active remote sensing
57 instruments as well as in-situ platforms were deployed and evaluated to determine their
58 suitability for the verification and validation of meteorological processes. Among the deployed
59 remote sensing instruments were a multi-channel MWR, as well as two radio acoustic sounding
60 systems (RASS), associated with 915-MHz and 449-MHz wind profiling radars.

61 In this study the physical-iterative approach is tested with different observational
62 inputs: first using data from surface sensors and the MWR in different configurations, and then
63 including data from the RASS into the retrieval with the MWR data. These temperature
64 retrievals are assessed against co-located radiosonde profiles. Results show that the
65 combination of the MWR and RASS observations in the retrieval allows for a more accurate

66 characterization of low-level temperature inversions, and that these retrieved temperature
67 profiles match the radiosonde observations better than the temperature profiles retrieved from
68 only the MWR in the layer between the surface and 3 km above ground level (AGL). Specifically,
69 in this layer of the atmosphere, both root mean square errors and standard deviations of the
70 difference between radiosonde and retrievals that combine MWR and RASS are improved by
71 mostly 10-20% compared to the configuration that does not include RASS observations.
72 Pearson correlation coefficients are also improved.

73 A comparison of the temperature physical retrievals to the manufacturer-provided neural
74 network retrievals is provided in Appendix A.

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88 **1. Introduction**

89 Monitoring the state of the atmosphere for process understanding and for model
90 verification and validation requires observations from a variety of instruments, each one having
91 its set of advantages and disadvantages. Using several diverse instruments allows one to
92 monitor different aspects of the atmosphere, while combining them in an optimized synergetic
93 approach can improve the accuracy of the information available on the state of the
94 atmosphere.

95 During the eXperimental Planetary boundary layer Instrumentation Assessment (XPIA)
96 campaign, a U.S. Department of Energy sponsored experiment held at the Boulder Atmospheric
97 Observatory (BAO) in Spring 2015, several instruments were deployed (Lundquist et al., 2017)
98 with the goal of assessing their capability for measuring atmospheric boundary layer
99 meteorological variables. XPIA investigated novel measurement approaches, and quantified
100 uncertainties associated with these measurement methods. While the main interest of the XPIA
101 campaign was on wind and turbulence, measurements of other important atmospheric
102 variables were also collected, including temperature and humidity. Among the deployed
103 instruments were two identical microwave radiometers (MWRs) and two radio acoustic
104 sounding systems (RASS), as well as radiosondes launches.

105 MWRs are passive sensors, sensitive to atmospheric temperature and humidity content
106 that allow for a high temporal observation of the state of the atmosphere, with some
107 advantages and limitations. In order to estimate profiles of temperature and humidity from the
108 observed brightness temperatures (T_b), several methods could be applied such as regressions,
109 neural network retrievals, or physical retrieval methodologies which can include additional

110 information about the atmospheric state in the retrieval process (e.g., Maahn et al. 2020).
111 Microwave radiative transfer models (e.g., Rosenkranz, 1998; Clough et al. 2005) are commonly
112 used to train statistical retrievals, or as forward models used within physical retrieval methods.
113 Advantages of MWRs include their compact design, the relatively high temporal resolution of
114 the measurements (2-3 minutes), the possibility to observe the vertical structure of both
115 temperature and moisture through the lower part of the troposphere during both clear and
116 cloudy conditions, and their capability to operate in a standalone mode. Disadvantages include
117 limited accuracy in the presence of rain because of scattering of radiation from raindrops in the
118 atmosphere (and because water can deposit on the radome, although the instruments use a
119 hydrophobic radome and force airflow over the surface of the radome during rain to mitigate
120 this impact), rather coarse vertical resolution, and for retrievals the necessity to have a site-
121 specific climatology. Other disadvantages include the challenges related to performing accurate
122 calibrations (Küchler et al., 2016, and references within), radio frequency interference (RFI), and
123 the low accuracy on the retrieved liquid water path (LWP) especially for values of LWP less than
124 20 g m^{-2} (Turner 2007; Turner et al. 2007).

125 RASS, in comparison, are active instruments that emit a longitudinal acoustic wave
126 upward, causing a local compression and rarefaction of the ambient air. These density
127 variations are tracked by the Doppler radar associated with the RASS, and the speed of the
128 propagating sound wave is measured. The speed of sound is related to the virtual temperature
129 (T_v) (North et al., 1973), and therefore, RASS are used to remotely measure vertical profiles of
130 virtual temperature in the boundary layer. Being an active instrument, the RASS is in general
131 more accurate than a passive instrument (Bianco et al., 2017), but they also come with their

132 own disadvantages. The main limitations of RASS for temperature measurements are the low
133 temporal resolution (typically a 5-min averaged RASS profile is measured once or twice per
134 hour), their limited altitude coverage, and the noise “pollution” that impacts local communities.
135 Adachi and Hashiguchi (2019) have shown that RASS could use parametric speakers to take
136 advantage of their high directivity and very low side lobes. Nevertheless, the maximum height
137 reached by the RASS is still limited, being a function of both radar frequency and atmospheric
138 conditions (May and Wilczak, 1993). It is determined both by the attenuation of the sound,
139 which is a function of atmospheric temperature, humidity, and frequency of the sound source,
140 and the advection of the propagating sound wave out of the radar’s field-of-view. Therefore,
141 data availability is usually limited to the lowest several kilometers, depending on the frequency
142 of the radar. In addition, wintertime coverage is usually lower than that in summer, due to
143 increased attenuation of the acoustic signal in cooler and drier environments.

144 To get a better picture of the state of the temperature and moisture structure of the
145 atmosphere, it makes sense to try to combine the information obtained by both MWR and
146 RASS. Integration of different instruments has been a topic of ongoing scientific interest (Han
147 and Westwater 1995; Stankov et al. 1996; Bianco et al., 2005; Engelbart et al., 2009; Cimini et
148 al., 2020; Turner and Löhnert, 2021, to name some). In this study, the focus is on the
149 combination of the MWR and RASS observations in the retrievals to improve the accuracy of
150 the temperature profiles in the lowest 3 km compared to physical retrieval approaches that do
151 not include the information from RASS measurements. Some studies have used analyses from
152 numerical weather prediction (NWP) models as an additional constraint in these variational
153 retrievals (e.g., Hewison 2007; Cimini et al. 2005, 2011; Martinet et al. 2020); however, we have

154 elected not to include model data in this study because we wanted to evaluate the impact of
155 the RASS profiles on the retrievals from a purely observational perspective.

156 This paper is organized as follows: Section 2 summarizes the experimental dataset;
157 Section 3 introduces the principles of the physical retrieval approaches used to obtain vertical
158 profiles of the desired variables; Section 4 produces statistical analysis of the comparison
159 between the different retrieval approaches and radiosonde measurement; finally, conclusions
160 are presented in Section 5.

161

162 **2. XPIA dataset**

163 The data used in our analysis were collected during the XPIA experiment, held in Spring
164 2015 (March-May) at NOAA's BAO site, in Erie, Colorado (Lat.: 40.0451 N, Lon.: 105.0057 W, El.:
165 1584 m MSL). XPIA was the last experiment conducted at this facility, as after almost 40 years
166 of operations the BAO 300-m tower was demolished at the end of 2016 (Wolfe and Lataitis,
167 2018). XPIA was designed to assess the capability of different remote sensing instruments for
168 quantifying boundary layer structure, and was a preliminary study as many of these same
169 instruments were later deployed, among other campaigns, for the second Wind Forecast
170 Improvement Project WFIP2 (Shaw et al., 2019; Wilczak et al., 2019) which investigated flows in
171 complex terrain for wind energy applications, where they were for example used to study cold
172 air pools (Adler et al., 2021) and gap flow characteristics (Neiman et al., 2019; Banta et al.,
173 2020). The list of the deployed instruments included active and passive remote-sensing devices,
174 and in-situ instruments mounted on the BAO tower. Data collected during XPIA are publicly
175 available at <https://a2e.energy.gov/projects/xpia>. A detailed description of the XPIA

176 experiment can be found in Lundquist et al. (2017), while a specific look at the accuracy of the
177 instruments used in this study can be found in Bianco et al. (2017).

178

179 **2.1 MWR measurements**

180 Two identical MWRs (Radiometrics MP-3000A) managed by NOAA (MWR-NOAA) and by
181 the University of Colorado (MWR-CU), were deployed next to each other at the visitor center
182 ~600 m south of the BAO tower (see Lundquist et al., 2017 for a detailed map of the study
183 area). Prior to the experiment, both MWRs were thoroughly serviced (sensor cleaning, radome
184 replacement, etc.) and calibrated using an external liquid nitrogen target and an internal
185 ambient target. MWRs are passive devices which record the natural microwave emission in the
186 water vapor and oxygen absorption bands from the atmosphere, providing measurements of
187 the brightness temperatures. Both MWRs have 35-channels spanning a range of frequencies,
188 with 21 channels in the lower (22-30 GHz) K-band frequency band, of which 8 channels were
189 used during XPIA: 22.234, 22.5, 23.034, 23.834, 25, 26.234, 28 and 30 GHz; and 14 channels in
190 the higher (51-59 GHz) V-band frequency band, of which all were used in XPIA: 51.248, 51.76,
191 52.28, 52.804, 53.336, 53.848, 54.4, 54.94, 55.5, 56.02, 56.66, 57.288, 57.964 and 58.8 GHz.
192 Frequencies in the K-band are more sensitive to water vapor and cloud liquid water, while
193 frequencies in the V-band are sensitive to atmospheric temperature due to the absorption of
194 atmospheric oxygen (Cadeddu et al., 2013). V-band frequencies or channels can also be divided
195 in two categories: the opaque channels, 56.66 GHz and higher, that are more informative in the
196 layer of the atmosphere from the surface to ~1 km AGL, and the transparent channels, 51-56
197 GHz, that are more informative above 1 km AGL. Both MWRs observed at the zenith and at 15-

198 and 165-degree elevation angles in the north-south plane (referred to as oblique elevation
199 scans and used as their average hereafter; note zenith views have a 90-degree elevation angle).
200 However, when MWRs are deployed in locations with unobstructed views, oblique scans can be
201 performed down to 5 degrees elevation angles and may provide better temperature profile
202 accuracy in the lowest 0-1 or even 0-2 km AGL layers (Crewell and Löhnert, 2007).

203 In addition, each MWR was provided with a separate surface sensor to measure
204 pressure, temperature, and relative humidity at the installation level that was ~2.5 m AGL.
205 Vertical profiles of temperature (T), water vapor density (WVD), and relative humidity (RH)
206 were retrieved in real-time during XPIA every 2-3 minutes using a neural network (NN)
207 approach provided by the manufacturer of the radiometer (Solheim et al. 1998a, and 1998b;
208 Ware et al., 2003). Although the physical retrieval configurations used in this study do not
209 exactly match the NN retrieval configurations, a comparison of both physical and neural
210 network retrievals to the radiosonde temperature data is presented in Appendix A.

211 Both MWRs nominally operated from 9 March to 7 May 2015, although the MWR-NOAA
212 was unavailable between 5-27 April 2015. For the overlapping dates, temperature profiles
213 retrieved from the two MWRs showed very good agreement with less than 0.5 °C bias and
214 0.994 correlation (Bianco et al., 2017). For this reason, and because the MWR-CU was available
215 for a longer time period, only the MWR-CU (hereafter simply called MWR) is used.

216

217 **2.2 WPR-RASS measurements**

218 Two NOAA wind profiling radars (WPRs), operating at frequencies of 915-MHz and 449-
219 MHz, were deployed at the visitor center (same location as the MWR) during XPIA. These

220 systems are primarily designed to measure the vertical profile of the horizontal wind vector, but
221 co-located RASS also enable the observation of profiles of virtual temperature in the lower
222 atmosphere, with different resolutions and height coverages depending on the WPR. Thus, the
223 RASS associated with the 915-MHz WPR (hereafter referred to as RASS 915) measured virtual
224 temperature from 120 to 1618 m with a vertical resolution of 62 m, and the 449 MHz RASS
225 (hereafter referred to as RASS 449) sampled the boundary layer from 217 to 2001 m with a
226 vertical resolution of 105 m. The maximum height reached by the RASS is a function of both
227 radar frequency and atmospheric conditions (May and Wilczak, 1993), and is usually lower for
228 RASS 915 data, as will be shown later in the analysis.

229 The RASS data were processed using a radio frequency interference (RFI)-removal
230 algorithm (performed on the RASS spectra), a consensus algorithm (Strauch et al. 1984)
231 performed on the moment data using a 60% consensus threshold, a Weber-Wuertz outlier
232 removal algorithm (Weber et al., 1993) performed on the consensus averages, and a RASS
233 range-correction algorithm (Görsdorf and Lehmann, 2000) using an average relative humidity
234 setting of 50% determined from the available observations.

235

236 **2.3 BAO data**

237 The BAO 300-m tower was built in 1977 to study the planetary boundary layer (Kaimal
238 and Gaynor 1983). During XPIA, measurements were collected at the surface (2 m) and at six
239 higher levels (50, 100, 150, 200, 250 and 300 m AGL). Each tower level was equipped with 2
240 sonic anemometers on orthogonal booms, and one sensor based on a Sensiron SHT75 solid-
241 state sensor to measure temperature and relative humidity with a time resolution of 1 s, and

242 averaged over five minutes. The more accurate temperature and water vapor observations
243 (Horst et al., 2016) at the BAO tower 2 m AGL level are used in the physical retrieval in place of
244 the less accurate MWR inline surface sensor.

245

246 **2.4 Radiosonde measurements**

247 Between 9 March and 7 May 2015, while the MWR was operational, radiosondes were
248 launched by the National Center for Atmospheric Research (NCAR) assisted by several students
249 from the University of Colorado over three selected periods, one each in March, April, and May.
250 All radiosondes were Vaisala model RS92. There was a total of 59 launches, mostly four times
251 per day, around 1400, 1800, 2200, and 0200 UTC (0800, 1200, 1600 and 2000 local standard
252 time, LST). The first 35 launches, between 9-19 March, were done from the visitor center, while
253 11 launches between 15-22 April, and 13 launches between 1-4 May, were done from the
254 water tank site, ~1000 meters away from the visitor center (see Lundquist et al., 2017 for a
255 detailed map of the study area). The radiosonde measurements included temperature, dew
256 point temperature, and relative humidity to altitudes usually higher than 10 km AGL, with
257 measurements every few seconds. As a first step, for additional verification, the radiosonde
258 data from the 59 launches taken between 9 March and 4 May 2015 were compared to the BAO
259 tower measurements, up to 300 m AGL. These observed data sets match very well, with a
260 correlation coefficient of 0.99 and a standard deviation of ~0.7 °C. However, one radiosonde
261 profile showed a large bias (> 5 °C) against all seven levels of BAO temperature measurements
262 and all available Tv measurements from the RASS 915 (eight measurements up to 600 m AGL)
263 and from the RASS 449 (nine measurements up to 1100 m AGL), therefore this particular

264 radiosonde profile was excluded from the statistical analysis. Moreover, while accurate RASS
265 data can be collected during rain, MWR data could be potentially deteriorated due to water
266 deposition on the radome. Therefore, six profiles (three for March 13, and one each on May 1,
267 3 and 4) were eliminated from the statistical evaluation. These restrictions lowered the number
268 of total radiosonde launches used in this study to 52.

269

270 **3. Physical retrievals**

271 One way to combine the active and passive instruments would be to use the RASS
272 observations up to their maximum available height, and stitch them with the profiles obtained
273 from a physical-iterative method using MWR data. To do this, the moisture contribution to the
274 RASS virtual temperatures could be removed by using either the relative humidity measured by
275 the MWR or by a climatology of the moisture term. However, merging these different profiles
276 could result in artificial jumps at the connecting heights.

277 Alternatively, a physical retrieval (PR) iterative approach can be used to retrieve vertical
278 profiles of thermodynamic properties from the MWR and RASS observations in a synergistic
279 manner (e.g., Maahn et al 2020; Turner and Löhnert 2021). In this case, an optimal estimation-
280 based physical retrieval is initialized with a climatologically reasonable profile of temperature
281 and water vapor, and is iteratively repeated until the computed brightness temperatures match
282 those observed by the MWR within the uncertainty of the observed brightness temperatures
283 and the RASS virtual temperatures within their uncertainties (Rodgers, 2000; Turner and
284 Löhnert, 2014; Maahn et al. 2020).

285

286 3.1 Iterative retrieval technique

287 For this study, the PR uses the *TROPoe* retrieval algorithm (formerly *AERIOe*, Turner and
288 Löhnert 2014; Turner and Blumberg 2019; Turner and Löhnert 2021). This algorithm is able to
289 use radiance data from microwave radiometers, infrared spectrometers, and other
290 observations as input. The microwave radiative transfer model, MonoRTM (Clough et al., 2005),
291 serves as the forward model, which is fully functional for the microwave region and was
292 intensively evaluated previously on MWR measurements (Payne et al. 2008; 2011).

293 We start with the state vector $\mathbf{X}_a = [\mathbf{T}, \mathbf{Q}, \text{LWP}]^T$, where superscript T denotes transpose,
294 and vectors and matrices are shown in bold. \mathbf{T} (K) and \mathbf{Q} (g kg^{-1}) are temperature and water
295 vapor mixing ratio profiles at 55 vertical levels from the surface up to 17 km, with the distance
296 between the levels increasing geometrically with height. LWP is the liquid water path in (g m^{-2})
297 that measures the integrated content of liquid water in the entire vertical column above the
298 MWR, and is a scalar. For this study, \mathbf{X}_a has dimensions equal to 111×1 (two vectors \mathbf{T} and \mathbf{Q}
299 with 55 levels each, and LWP). The retrieval framework of Turner and Blumberg (2019) is used,
300 but only using MWR data (no spectral infrared). Here, we demonstrate the augmentation of the
301 retrieval to include RASS profiles of \mathbf{T}_v , and the resulting impact this has on the retrieved
302 temperature profiles and information content.

303 The observation vector \mathbf{Y} includes temperature and water vapor mixing ratio measured
304 at the surface in-situ, and spectral \mathbf{T}_b measured by the MWR. The MonoRTM model \mathbf{F} is used as
305 the forward model from the current state vector \mathbf{X} , and is then compared to the observation
306 vector \mathbf{Y} , iterating until the difference between $\mathbf{F}(\mathbf{X})$ and \mathbf{Y} is small within a specified uncertainty
307 (Eq 1).

308

$$X_{n+1} = X_n + (S_a^{-1} + K^T S_\varepsilon^{-1} K)^{-1} K^T S_\varepsilon^{-1} [Y - F(X_n) + K(X_n - X_a)] \quad (1)$$

310 with

$$311 \quad X_a = \begin{bmatrix} T \\ Q \\ LWP \end{bmatrix} \quad S_a = \begin{bmatrix} \sigma_{TT}^2 & \sigma_{TQ}^2 & 0 \\ \sigma_{QT}^2 & \sigma_{QQ}^2 & 0 \\ 0 & 0 & \sigma_{LWP}^2 \end{bmatrix} \quad K_{ij} = \partial F_i / \partial X_j$$

312 where i and j in the K_{ij} definition mark channel and vertical level, respectively. The superscripts

313 T and -1 in (1) indicate the transpose and inverse matrix, respectively. The observation vector Y

314 and the covariance matrix of the observed data, S_ε , depending on the configuration used, are

315 equal to:

$$316 \quad Y_1 = \begin{bmatrix} T_{sfc} \\ Q_{sfc} \\ T\mathbf{b}_{zenith} \end{bmatrix} \quad S_{\varepsilon_1} = \begin{bmatrix} \sigma_{T_{sfc}}^2 & 0 & 0 \\ 0 & \sigma_{Q_{sfc}}^2 & 0 \\ 0 & 0 & \sigma_{T\mathbf{b}_{zenith}}^2 \end{bmatrix}$$

$$317 \quad Y_2 = \begin{bmatrix} T_{sfc} \\ Q_{sfc} \\ T\mathbf{b}_{zenith+oblique} \end{bmatrix} \quad S_{\varepsilon_2} = \begin{bmatrix} \sigma_{T_{sfc}}^2 & 0 & 0 \\ 0 & \sigma_{Q_{sfc}}^2 & 0 \\ 0 & 0 & \sigma_{T\mathbf{b}_{zenith+oblique}}^2 \end{bmatrix}$$

$$318 \quad Y_3 = \begin{bmatrix} T_{sfc} \\ Q_{sfc} \\ T\mathbf{b}_{zenith+oblique} \\ T\mathbf{v}_{RASS915} \end{bmatrix} \quad S_{\varepsilon_3} = \begin{bmatrix} \sigma_{T_{sfc}}^2 & 0 & 0 & 0 \\ 0 & \sigma_{Q_{sfc}}^2 & 0 & 0 \\ 0 & 0 & \sigma_{T\mathbf{b}_{zenith+oblique}}^2 & 0 \\ 0 & 0 & 0 & \sigma_{T\mathbf{v}_{RASS915}}^2 \end{bmatrix}$$

$$\begin{aligned}
319 \quad Y_4 &= \begin{bmatrix} T_{sfc} \\ Q_{sfc} \\ \mathbf{Tb}_{zenith+oblique} \\ \mathbf{Tv}_{RASS449} \end{bmatrix} \quad S_{\varepsilon_4} = \begin{bmatrix} \sigma_{T_{sfc}}^2 & 0 & 0 & 0 \\ 0 & \sigma_{Q_{sfc}}^2 & 0 & 0 \\ 0 & 0 & \sigma_{\mathbf{Tb}_{zenith+oblique}}^2 & 0 \\ 0 & 0 & 0 & \sigma_{\mathbf{Tv}_{RASS449}}^2 \end{bmatrix}
\end{aligned}$$

320 Note that the 2-m surface-level observations of temperature and water vapor mixing
321 ratio (T_{sfc} and Q_{sfc} , respectively) are included as part of the observation vector \mathbf{Y} , and thus the
322 uncertainties (0.5 K for temperature and less than 0.4 g kg⁻¹ for mixing ratio) in these
323 observations are included in \mathbf{S}_ε .

324 The mean state vector of the climatological estimates, or a ‘‘prior’’ vector \mathbf{X}_a , is a key
325 component in the optimal estimation framework and it is the first guess of the state vector \mathbf{X} ,
326 \mathbf{X}_1 in Eq. (1). It provides a constraint on the ill-posed inversion problem. The prior is calculated
327 independently for each month of the year from climatological sounding profiles (using 10 years
328 of data) in the Denver area. The covariance matrix, \mathbf{S}_a , of the ‘‘prior’’ vector includes not only
329 temperature or water vapor variances but also the covariances between them. Using around
330 3,000 radiosondes launched by the NWS in Denver, each radiosonde profile is interpolated to
331 the vertical levels used in the retrieval, after which the covariance of temperature and
332 temperature, temperature and humidity, and humidity and humidity is computed for different
333 levels.

334 Four configurations are chosen for the observational vector \mathbf{Y} (\mathbf{Y}_1 , \mathbf{Y}_2 , \mathbf{Y}_3 , and \mathbf{Y}_4). In each
335 of these, the surface observations are obtained by the 2-m BAO *in-situ* measurements of
336 temperature and humidity. The MWR provides \mathbf{Tb} measurements from 22 channels from the
337 zenith scan for the zenith only configuration (\mathbf{Y}_1), while when using the zenith plus oblique \mathbf{Tb}

338 inputs (\mathbf{Y}_2 , \mathbf{Y}_3 , and \mathbf{Y}_4) the same 22 channels were used from the zenith scans together with only
 339 the four opaque channels (56.66, 57.288, 57.964 and 58.8 GHz) from the oblique scans. Using
 340 additional measurements from the co-located radar systems with RASS, the observational
 341 vector is further expanded with either RASS 915 (\mathbf{Y}_3) or RASS 449 (\mathbf{Y}_4) virtual temperature
 342 observations. The covariance matrix of the observed data, \mathbf{S}_e , depends on the chosen \mathbf{Y}_i as seen
 343 in the matrix \mathbf{S}_{ei} (with $i = 1:4$) descriptions, with increasing dimensions from \mathbf{Y}_1 to \mathbf{Y}_2 and
 344 additional increasing dimensions to \mathbf{Y}_3 or \mathbf{Y}_4 through the multi-level measurements of the RASS
 345 (Turner and Blumberg, 2019). Table 1 summarizes the observational information included in
 346 these four different configurations of the PR.

347

	T_{sfc}	Q_{sfc}	Tb_{zenith}	$Tb_{oblique}$	$TV_{RASS915}$	$TV_{RASS449}$
$\mathbf{Y}_1 = MWRz$	X	X	X			
$\mathbf{Y}_2 = MWRzo$	X	X	X	X		
$\mathbf{Y}_3 = MWRzo915$	X	X	X	X	X	
$\mathbf{Y}_4 = MWRzo449$	X	X	X	X		X

348 Table 1. Four PR configurations corresponding to the four observational \mathbf{Y}_i vectors in Eq. (1).

349

350 The uncertainty in the MWR Tb observations was set to the standard deviation from a
 351 detrended time-series analysis for each channel during cloud-free periods. The method to

352 detect those cloud-free periods is described in detail in Section 3.2. The derived uncertainties
353 ranged from 0.3 K to 0.4 K in the 22 to 30 GHz channels, and 0.4 to 0.8 K in the 52 to 60 GHz
354 channels. We assumed that there was no correlated error between the different MWR
355 channels.

356 For the RASS, co-located RASS and radiosonde profiles were compared and the standard
357 deviation of the differences in T_v were determined as a function of the radar's signal-to-noise
358 ratio (SNR). This relationship resulted in uncertainties that ranged from 0.8 K at high SNR values
359 to 1.5 K at low SNR values. Again, we assumed that there was no correlated error between
360 different RASS heights. Following these assumptions, the covariance matrix \mathbf{S}_ϵ is diagonal.

361 The Jacobian matrix, \mathbf{K} , is computed using finite differences by perturbing the elements
362 of \mathbf{X} and rerunning the forward model. It has dimensions $m \times 111$, where m is the length of the
363 vector \mathbf{Y}_i , therefore its dimension increases correspondingly with the inclusion of more
364 observational data. \mathbf{K} makes the "connection" between the state vector and the observational
365 data and should be calculated at every iteration.

366

367 **3.2 Bias-correction of MWR observations using radiosondes or climatology**

368 Observational errors propagate through retrieval into the derived profiles (i.e. the bias
369 of the observed data will contribute to a bias in the retrievals). For that, retrieval uncertainties
370 in Eq. (1) from $\mathbf{Y} = \mathbf{Y}_1$ or \mathbf{Y}_2 derive only from uncertainties in surface and MWR data, while
371 retrieval uncertainties from $\mathbf{Y} = \mathbf{Y}_3$ or \mathbf{Y}_4 come from uncertainties in the surface, MWR, and RASS
372 measurements.

373 The bias of the retrieval depends on both the absolute accuracy of the forward model
374 and on any observational systematic offset, of which the systematic error in the MWR
375 observations could potentially be reduced through application of a MWR Tb bias-correction
376 procedure. In this study, two different approaches were used for the bias-correction: the first is
377 based on a comparison to the radiosondes, while the second uses climatological profiles. The
378 first method could be used for a field campaign where occasional co-located radiosonde
379 launches are taken, while the second would be used for deployments without any supporting
380 radiosonde observations.

381 For both approaches, the first step is to identify clear-sky periods during which the bias
382 can be estimated (to reduce the degrees of freedom associated with clouds) and subsequently
383 the bias can be removed from the observed MWR Tbs. One method to identify clear-sky times
384 is to use a time-series of Tb observations in the 30 GHz liquid water sensitive channel of the
385 MWR.

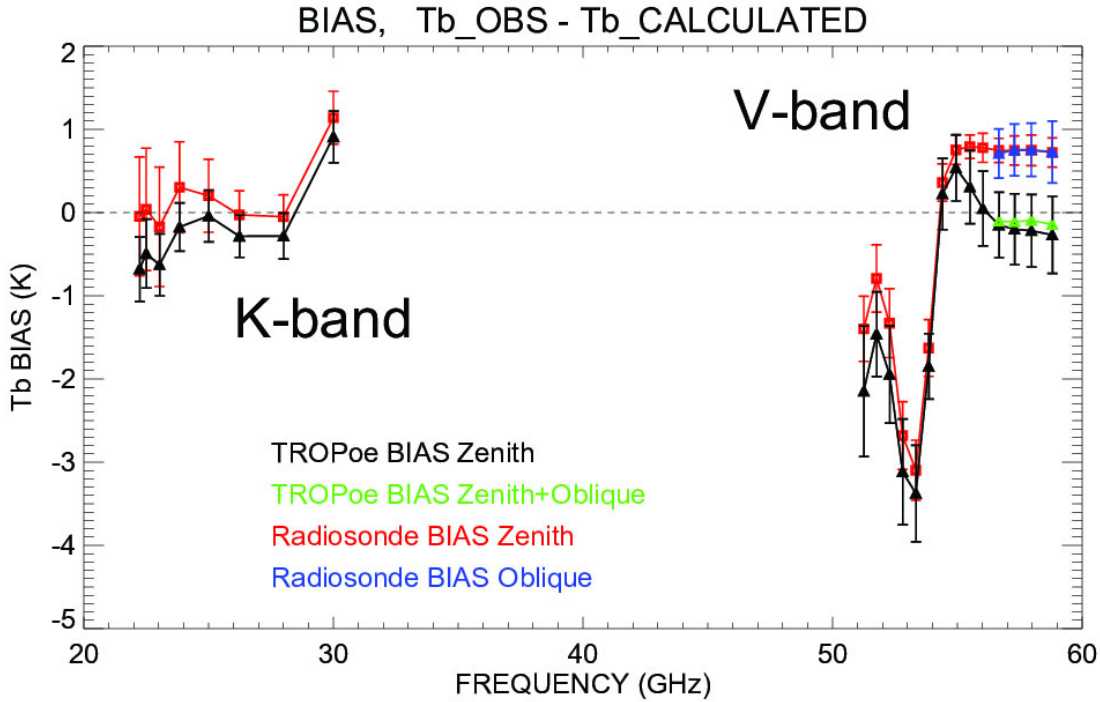
386 The standard deviation of the MWR Tb in the 30 GHz channel is calculated over a time
387 frame of one hour centered at the radiosonde launch time. The data from the zenith scan and
388 the averaged oblique scans are reviewed separately. Liquid-cloud free periods were identified
389 by cases where the temporal standard deviation was small (< 0.4 K), and more than 35
390 radiosonde profiles were classified as being launched in clear skies. The usage of the standard
391 deviation from the time-series from the oblique scans, with the same 0.4 K restriction, reduces
392 the number of the clear-sky radiosonde profiles to 18. For those chosen 18 radiosonde profiles,
393 the Tb is calculated from radiosonde temperature profiles through MonoRTM at each of the
394 MWR channels. The mean difference between these calculated radiosonde Tbs and measured

395 MWR Tbs forms the Tb bias with which the MWR Tb data can be corrected. This bias-correction
396 method will be referred to as 'radiosonde BC'.

397 While this radiosonde BC method can be employed for the XPIA dataset, for other
398 campaigns this approach would not be possible if co-located radiosonde observations were not
399 available. For this situation, an alternative method for correcting the MWR Tb biases is
400 presented. In this method, to choose clear-sky periods, the 30 GHz channel MWR Tb data are
401 used on a daily basis. The standard deviation of the MWR Tb is calculated as the average of
402 standard deviations in a one-hour sliding window through all data points of a day. Four clear-
403 sky days were identified using a threshold of 0.4 K on the standard deviation: March 10 and 30,
404 and April 13 and 29, 2015. The Tb bias is then computed for each of the 22 channels as the
405 averaged difference between the observed Tb from the MWR zenith observations and the
406 forward model calculated Tbs at zenith using the TROPoe-retrieved profiles (Y_1) of those
407 selected clear-sky days. This method identified spectral calibration errors in the MWR
408 observations that could not be explained by physically realistic atmospheric profiles. This bias-
409 correction technique will be referred to as 'TROPoe BC'.

410 Fig. 1 shows the Tb biases found for all 22 MWR channels from both bias-correction
411 approaches. The biases calculated with the radiosonde BC scheme are shown for all channels
412 used in our analysis: 22 channels of the zenith scan, in red, and four V-band opaque channels of
413 the oblique scans, in blue. The black and green triangles represent the biases calculated using
414 the TROPoe BC approach for zenith and for zenith+oblique scans, respectively. All biases are
415 presented with associated uncertainties (error bars representing the standard deviation over all

416 radiosondes for radiosonde BC, and mean observation Tb vector uncertainties for chosen four
417 clear-sky days for TROPoe BC).



418 *Fig. 1. Tb biases derived from the radiosonde BC method (and TROPoe BC method) in all*
419 *22 MWR channels of the zenith scan in red (and in black), and in the four opaque channels of*
420 *the oblique scans in blue (and in green).*

421
422 The biases from the two bias-correction schemes are within the uncertainties of each
423 other for most of the channels except at the higher frequencies in the V-band. Biases in the
424 most opaque channels are significantly affected by the accuracy of the boundary layer
425 temperature profiles. When TROPoe BC is used, a monthly average prior temperature profile is
426 used in the PR, and thus differences between this prior profile and the actual temperature

427 profile can result in a spectral bias in the more opaque MWR channels. On the contrary, the
428 radiosonde BC uses a direct measurement of the temperature profile (from the radiosonde),
429 and thus is more accurate. It is also important to note that, in both approaches, the biases in
430 the opaque channels for zenith and for oblique scans (for radiosonde BC these are red and blue,
431 respectively; and for the TROPoe BC these are black and green, respectively) are very similar to
432 each other. This supports the assumption that the true bias is nearly independent of the scene,
433 or that the sensitivity to the scene (e.g., zenith or off-zenith) is small.

434 The bias-correction methods were applied by removing the corresponding calculated
435 biases from the MWR Tb observations before the retrievals were performed. Later in Section 4,
436 differences in the retrieved temperature profiles will be shown when using the two bias-
437 correction approaches. These differences will be more evident in the temperature profiles
438 exhibiting near-ground temperature inversions.

439 However, the final goal of this study is not to assess the sensitivity to different bias-
440 correction approaches but to verify that the inclusion of RASS observations does improve
441 retrieved temperature profiles, independently of the bias-correction method used.

442

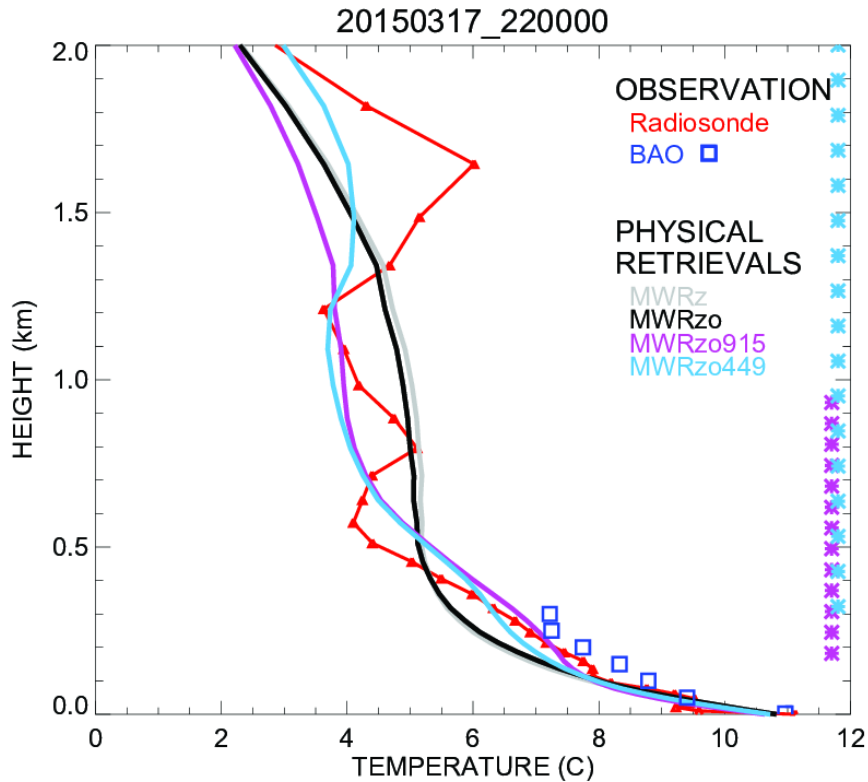
443 **3.3 Analysis of physical retrieval characteristics**

444 The retrieved profiles of the four different PR configurations presented in Table 1
445 (MWRz, MWRzo, MWRzo915, MWRzo449) were compared to the radiosonde profiles. To
446 compare radiosonde observations against the PR profiles, all radiosonde profiles were
447 interpolated vertically to the same PR heights, and PR profiles were averaged in the time
448 window between 15 minutes before and 15 minutes after each radiosonde launch. Since the

449 radiosonde ascends quite quickly in the lowest kilometers of the atmosphere (~15-20 min to
450 reach 5 km), the 30-minute temporal window is estimated to be representative of the same
451 volume of the atmosphere measured by the radiosonde. BAO tower temperature and mixing
452 ratio data at the seven available levels were used as an additional validation dataset, without
453 any vertical interpolation, averaged in the time window between 15 minutes before and 15
454 minutes after each radiosonde launch.

455 As an example of the different temperature retrievals and their relative performance,
456 data obtained on 17 March 2015 at 2200 UTC are presented in Fig. 2. Temperature profiles up
457 to 2 km AGL retrieved from the four PR configurations (MWRz, MWRzo, MWRzo915,
458 MWRzo449, using the radiosonde BC) are compared to the radiosonde data in red and to the
459 BAO measurements in blue squares. Note that all four of the PRs match the BAO observations
460 reasonably well near the ground. The MWRz and MWRzo profiles are very smooth and depart
461 quite substantially from the radiosonde measurements, being unable to reproduce the more
462 detailed structure of the atmospheric temperature profile measured by the radiosonde, while
463 the MWRzo449 profile (in light-blue) demonstrates a better agreement with both the
464 radiosonde and BAO measurements (blue squares). The MWRzo915 profile (in purple) also tries
465 to follow the elevated temperature inversion observed by the radiosonde, successfully only in
466 the lower part of the atmosphere (below 1 km AGL) where RASS 915 measurements are
467 available. This behavior will be also addressed in the following section and in the statistical
468 analysis presented later in the manuscript.

469



470

471 *Fig. 2. Temperature profiles obtained by the four PR configurations, after applying the*
 472 *radiosonde BC on the MWR Tbs: MWRz in gray, MWRzo in black, MWRzo915 in purple, and*
 473 *MWRzo449 in light-blue. These retrievals are compared to radiosonde measurements, in red,*
 474 *and BAO tower observations, in blue squares. The heights with available RASS virtual*
 475 *temperature measurements (RASS 915 in purple and RASS 449 in light-blue) are marked by the*
 476 *asterisks on the right Y-axis.*

477

478 An asset of TROPoe is that several characteristics of the PRs can be obtained from two
 479 matrices, the averaging kernel, **Akernel**, and the posterior covariance matrix, **Sop** (Masiello et
 480 al., 2012; Turner and Löhnert, 2014, Turner and Bloomberg, 2019), calculated as:

481

482
$$\mathbf{Akernel} = \mathbf{B}^{-1} \mathbf{K}^T \mathbf{S}_\varepsilon^{-1} \mathbf{K} \quad (2)$$

483 and:

484
$$\mathbf{Sop} = \mathbf{B}^{-1} \quad (3)$$

485 where:

486
$$\mathbf{B} = \mathbf{S}_a^{-1} + \mathbf{K}^T \mathbf{S}_\varepsilon^{-1} \mathbf{K}$$

487

488 All matrices, **Akernel**, **Sop**, and **B**, have dimensions 111 x 111 in our configuration. While
 489 the top left corner of the **Akernel** matrix (1:55, 1:55) is devoted to temperature, called further
 490 in the text **ATkernel**, the next (56:110, 56:110) elements are devoted to the water vapor mixing
 491 ratio, called **AQkernel**.

492 The **Akernel** provides useful information about the calculated retrievals, such as vertical
 493 resolution and degrees of freedom for signal at each level. The rows of the **Akernel** provide the
 494 smoothing functions (Rodgers, 2000) that could be applied to the radiosonde profiles (Eq. 4) to
 495 minimize the vertical representativeness error in the comparison between the various retrievals
 496 and the radiosonde profiles due to very different vertical resolutions of these profiles (Turner
 497 and Löhnert, 2014).

498 Smoothed radiosonde observed profiles can be computed using the averaging kernel,
 499 as:

500
$$\mathbf{X}_{smoothed_radiosonde} = \mathbf{Akernel} (\mathbf{X}_{radiosonde} - \mathbf{X}_a) + \mathbf{X}_a \quad (4)$$

501 The **Akernel** in Eq. (2) depends on the retrieval parameters (e.g., which datasets are
 502 used in the **Y** vector, the values assumed in the observation covariance matrix **S_ε**, and the

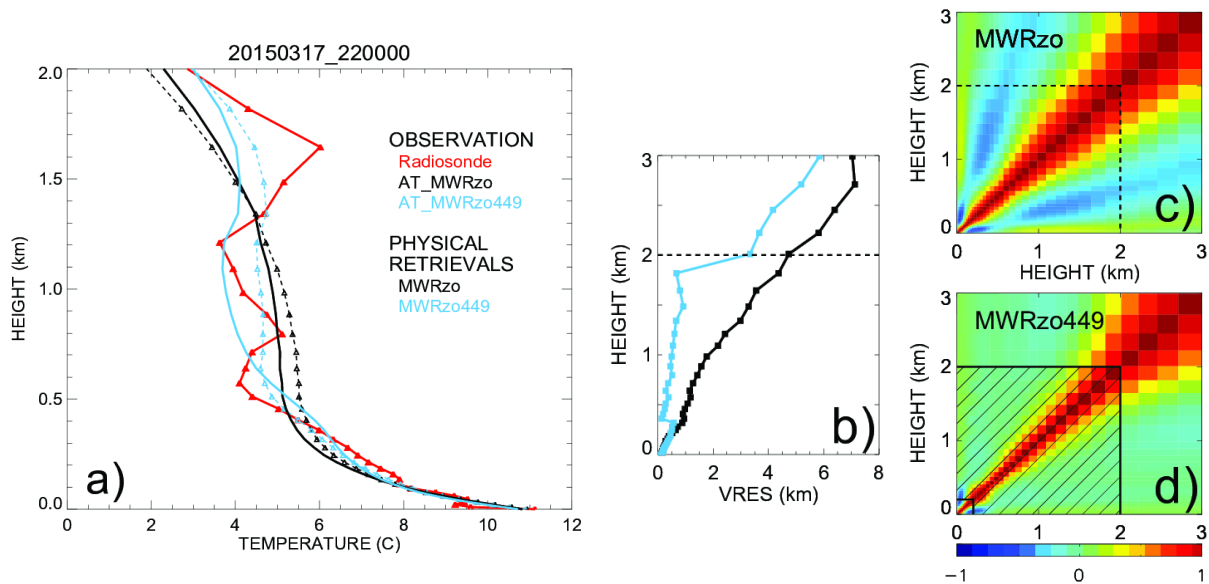
503 sensitivity of the forward model), so for our four PR configurations it is possible to calculate
504 four different kernels from Eq. (2).

505 For each of the four **Akernels**, a smoothed radiosonde profile can be computed for each
506 radiosonde profile using Eq. (4). In the presence of temperature inversions or other particular
507 structures in the atmosphere, these smoothed profiles can be quite different from each other
508 and also from the original unsmoothed radiosonde profile. Consequently, while comparison of
509 the retrievals to the relative **Akernel**-smoothed radiosonde profiles can be used to minimize the
510 vertical representativeness effects due to the different vertical resolutions of these profiles, we
511 note that a statistical comparison between the four configurations of the observational vector
512 would not be fair if each of their retrieved profiles is compared to a different **Akernel**-smoothed
513 radiosonde profile. Therefore, in the statistical analysis presented later in the manuscript
514 (section 4.2), mean bias, root mean square error (RMSE), and Pearson correlation coefficients
515 will be computed between the various TROPoe retrieval configurations and the unsmoothed
516 radiosonde profiles, just interpolated to the same vertical levels of the retrieved profiles.

517 The **ATkernel** can help understand the differences in the retrieved temperature profiles
518 obtained by the configurations using additional RASS data, shown in the example of Fig. 2.
519 Figure 3a includes the temperature profiles of the radiosonde (unsmoothed and **ATkernel**'s
520 smoothed) and PRs of MWRzo and MWRzo449 for the same example as in Fig. 2. Due to the
521 inclusion of RASS measurements, the **ATkernel**-smoothed radiosonde profile of the MWRzo449
522 configuration (dashed light-blue line) is closer to the original radiosonde data (in red) compared
523 to the black dashed profile of the MWRzo's **ATkernel**-smoothed radiosonde profile.
524 Additionally, the rows of the **ATkernel** provide a measure of the retrieval smoothing as a

525 function of altitude, so the full-width half maximum (FWHM) of each **ATkernel** row estimates
 526 the vertical resolution of the retrieved solution at each vertical level (Maddy and Barnet, 2008;
 527 Merrelli and Turner, 2012). Plots of this vertical resolution as a function of the height for the
 528 MWRzo PR and for the MWRzo449 PR are included in Fig. 3b. This plot shows that the
 529 additional observations from the RASS 449 significantly improve the vertical resolution of the
 530 retrievals.

531 The posterior covariance matrix, **Sop**, provides a measure of the uncertainty of the
 532 retrievals while the square root of the diagonal of this matrix is used to specify the 1- σ errors in
 533 the profiles of temperature or mixing ratio. Also, **Sop** shows the level-to-level dependency of
 534 the retrievals, and in an ideal case should have all non-diagonal elements equal to zero.
 535 Converted to a correlation matrix, it is possible to visualize these dependencies, as presented in
 536 Fig. 3c, d. The use of additional RASS data (MWRzo449 **Sop**, Fig. 3d) reduces the off-diagonal
 537 covariances, therefore substantially decreasing the correlations in those areas compared to the
 538 MWRzo **Sop** (Fig. 3c).



539

540 Fig. 3. a) observed temperature profiles from radiosonde, in red, from **AT** kernels smoothed
541 radiosonde, **AT_MWRzo** in dashed black, and **AT_MWRzo449** in dashed light-blue; PRs from
542 MWRzo PR in solid black, and from MWRzo449 PR in solid light-blue. b) vertical resolution
543 (VRES) as a function of the height for the MWRzo PR (black), and for the MWRzo449 PR (light-
544 blue). c) and d) 3 x 3 km (37 x 37 levels) **Sop** matrices, converted to correlation matrices, for the
545 MWRzo PR (c), and for the MWRzo449 PR (d). Dashed lines on plots b)-d) mark 2 km AGL.
546 Hatched area on panel d marks the RASS measurement heights.

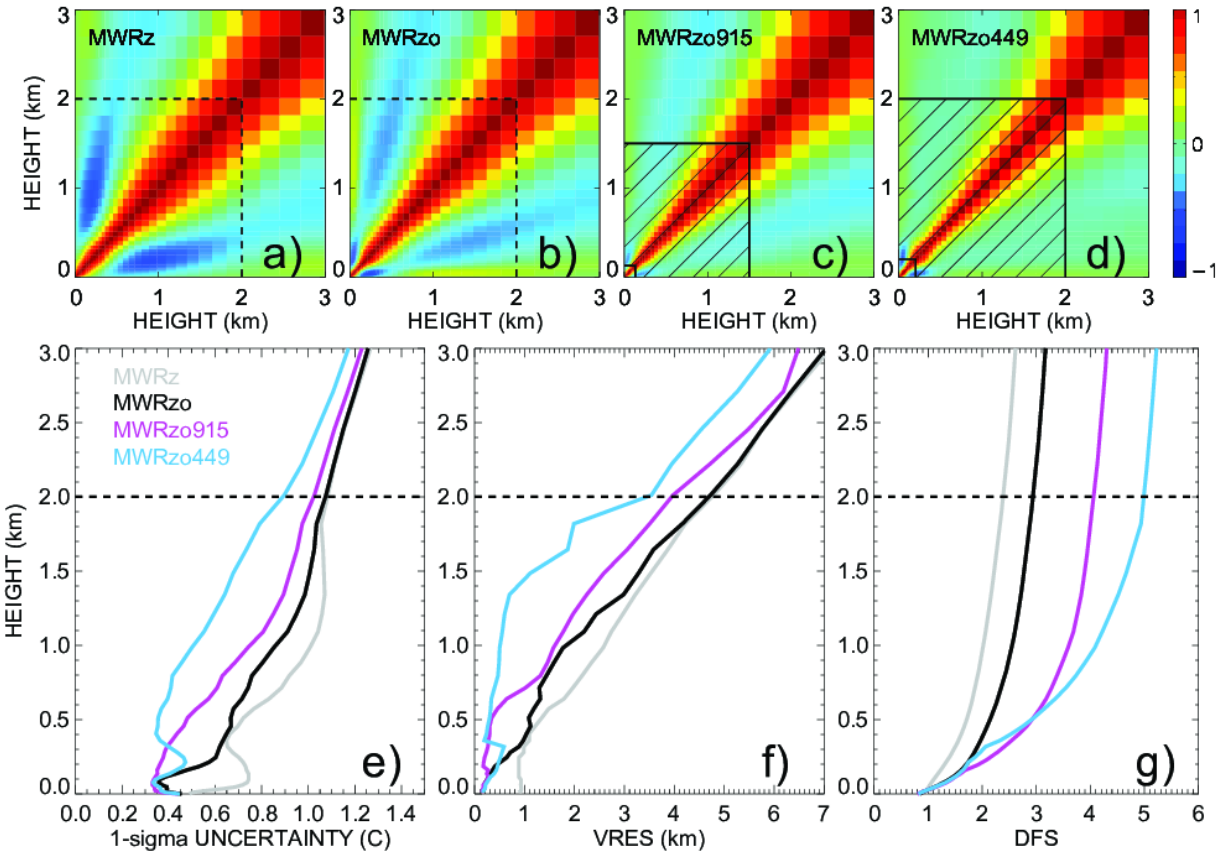
547

548 To understand the level-to-level correlations among the 4 different retrieval
549 configurations in Table 1, the **Sop** matrices were averaged over all radiosonde events, and
550 converted to correlation matrices (Fig. 4). A clearly visible narrowing of the spread around the
551 main diagonal and correlation reduction in the off-diagonal elements result by adding
552 additional observations, from MWR zenith only (Fig. 4a), to MWR zenith-oblique (Fig. 4b), to
553 the larger impact obtained by the usage of the RASS 915 (Fig. 4c), concluding with the RASS 449
554 (Fig. 4d) data. The mean retrieval uncertainty profile for each of the PR configurations is
555 presented in Fig. 4e. The uncertainty of the MWRzo449 retrieval up to 1 km AGL is around 0.5
556 °C while the other retrievals have higher uncertainties of up to 1 °C. The higher accuracy of the
557 MWRzo449 retrievals is because that configuration has more observational information
558 compared to the other retrieval configurations.

559 Other statistically important features to analyze in the PRs, besides their uncertainty,
560 are the vertical resolution already introduced in the example of Fig. 3b, and the degree of
561 freedom for signal (DFS). These two features, derived from the **A** kernels of each PR

562 configuration, averaged over all radiosonde events, are shown in Fig 4f and 4g. The vertical
563 resolution (Fig. 4f) shows the width of the atmosphere layer used for each retrieval height,
564 computed as the full-width half-maximum value of the averaging kernel. The cumulative DFS
565 profile (Fig. 4g) is a measure of the number of independent pieces of information in the
566 observations below the specified height. For example, at the 1 km AGL level the vertical
567 resolution of MWRzo449 is 0.5 km (i.e. information is from +/- 0.5 km around the retrieval
568 height is considered in the retrieval), while all other retrievals use the information from more
569 than +/- 1.5 km. Also, the DFS, as a cumulative measure, shows an increase in pieces of
570 information from MWRz to MWRzo for the whole profile and from MWRzo to MWRzo915 and
571 to MWRzo449 above ~0.2 km where RASS data are available. The DFS of MWRzo915 is higher
572 compared to the DFS of MWRzo449 in the 0.2-0.5 km AGL layer because RASS 915 data have
573 denser measurements there. It is also important to note that there is no additional information
574 added to any of the retrievals above 2km AGL, i.e. the slope of the cumulative DFS profiles are
575 equal. Despite that, the statistical analysis of the PRs up to 3 km AGL, shown in Section 4, will
576 prove that the retrieval improvements obtained by including the RASS are found even above
577 the height of the RASS measurements availability.

578



579
 580 Fig. 4. Top row: The mean **Sops**, displayed as correlation matrices, for (a) MWRz, (b) MWRzo, (c)
 581 MWRzo915, and (d) MWRzo449, averaged over all radiosonde events. Hatched area on panels
 582 c) and d) marks the RASS maximum measurement heights. Bottom panels: (e) one-sigma
 583 uncertainty derived from the posterior covariance matrix in °C, (f) vertical resolution (VRES) in
 584 km, and (g) cumulative Degree of Freedom (DFS) as a function of height for temperature,
 585 averaged over all radiosonde events (MWRz is in gray, MWRzo is in black, MWRzo915 is in
 586 purple, and MWRzo449 is in light-blue). Dashed lines mark 2 km AGL on all panels.

587
 588 The improvements from MWRz (in gray) to MWRzo (in black), to MWRzo915 (in purple),
 589 and finally to MWRzo449 (in light-blue) are visible in all three panels (Fig 4e-g), whereas

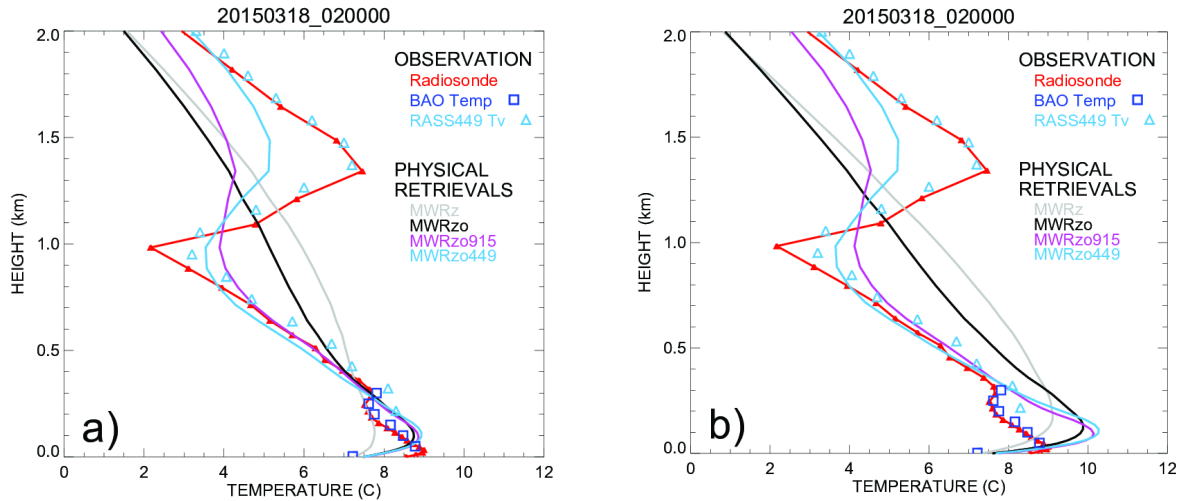
590 MWRzo449 has the lowest $1-\sigma$ uncertainty and highest DFS compared to the other PRs,
591 particularly below 2 km AGL, where RASS 449 measurements are available. Finally, it is
592 interesting that below 200 m AGL the MWRzo915 has slightly smaller lowest $1-\sigma$ uncertainty
593 and vertical resolution relative to the MWRzo449, as could be expected due to the first
594 available height of the RASS 915 being lower (120 m AGL) than the first available height for the
595 RASS 449 (217 m AGL) and due to the finer vertical resolution of the 915-MHz RASS. This
596 suggests that if additional observations were available in the lowest several 100 m of the
597 atmosphere where RASS measurements are not available, improvements might be even better
598 closer to the surface, where temperature inversions, if present, are sometimes difficult to
599 retrieve correctly.

600

601 **4. Results**

602 **4.1 Statistical analysis of physical retrievals up to 3km AGL**

603 Several cases were found during XPIA when the temperature profile exhibited
604 inversions, with the lowest happening in the surface layer. Figure 5 shows one of the most
605 complex cases, with several temperature inversions visible in the temperature profile from the
606 radiosonde (red line), in the temperature measurements from the BAO tower (blue squares),
607 and in the virtual temperature measured by the RASS 449 (light blue triangles). Note that the
608 virtual temperature profile is in close agreement with the temperature measured by
609 radiosonde.



610

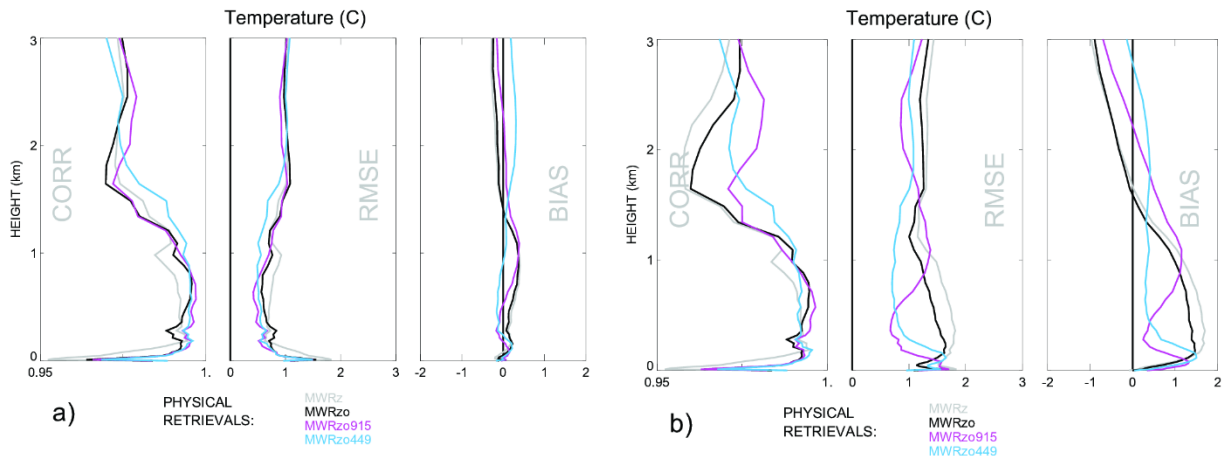
611 *Fig. 5. As in Fig. 2 but for 18 March 2015 at 0200 UTC. The RASS 449 virtual temperature is*
 612 *included as light blue triangles. a) shows the PRs obtained after applying the radiosonde BC, and*
 613 *b) shows the PRs obtained after applying the TROPoe BC on the MWR Tbs.*

614

615 Figure 5 also illustrates the difference in the temperature profiles, especially between 0-
 616 300m AGL, for the two different bias-correction schemes, which show noticeable differences in
 617 the biases of the opaque channels (especially important for the near-ground retrievals)
 618 presented in Fig. 1. As expected, the radiosonde BC method yielded a retrieved profile closer to
 619 the radiosonde temperature profile than when using TROPoe BC, for which the inversion in the
 620 temperature profile close to the surface is too accentuated (particularly the black, purple, and
 621 cyan lines, all of which used oblique scan data).

622 The relative statistical behavior (Pearson correlation, RMSE, and bias) of the PRs for
 623 both temperature and mixing ratio against radiosondes is shown in Figure 6, using both bias-
 624 correction approaches. PRs obtained after applying the radiosonde BC (Fig. 6a) present overall

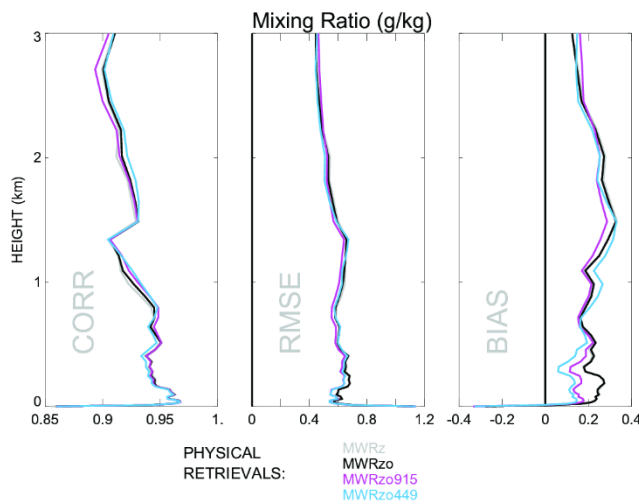
625 smaller RMSE and bias (the latter almost equal to zero up to 3 km AGL) and slightly higher
 626 correlations compared to the statistics of the PRs obtained after applying the TROPoe BC (Fig.
 627 6b). This could be expected since for the comparison in Fig. 6a a subset of the radiosondes were
 628 already used for the Tb bias correction. Also, the different retrievals show a narrower
 629 distribution for the panels in Fig. 6a. Nevertheless, the results obtained when applying either
 630 bias-correction methods (in Fig. 6a, b) consistently show the improvement obtained when the
 631 RASS observations are used, with relatively smaller bias and RMSE in the 3 km layer AGL. The
 632 correlation is mainly improved above 1 km, when RASS observations are included.



633 *Fig. 6. Pearson correlation, RMSE, and mean bias for temperature profiles of MWRz in gray,*
 634 *MWRzo in black, MWRzo915 in purple, and MWRzo449 in light-blue for the radiosonde BC bias-*
 635 *correction method in a) and TROPoe BC method in b).*

636
 637 Besides temperature profiles, the PRs also provide water vapor mixing ratio profiles. It is
 638 understandable that the different configurations of PRs are not noticeably different from each
 639 other in relation to moisture, because the Tv observations from the RASS are dominated by the
 640 ambient temperature (not moisture), and thus have little impact on the water vapor retrievals.

641 We found that the **AQKernels** are almost identical for all four PR configurations (not shown).
 642 Detailed statistical evaluation of the PRs mixing ratio profiles are presented in Fig. 7, also
 643 averaged over all radiosonde events, and show very similar correlations, RMSEs, and biases for
 644 all PRs, implying that the impact of including RASS observations in the retrieval is minimal on
 645 this variable. Finally, it is noted that Fig. 7 shows the mixing ratio of the data from TROPoe BC.
 646 The radiosonde BC mixing ratio results are almost identical.

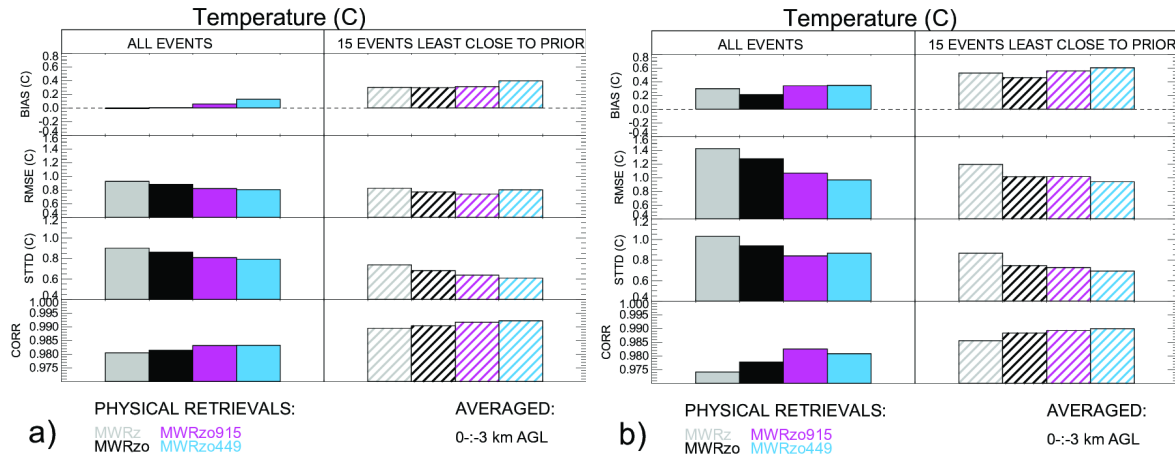


653
 654 *Fig. 7. Same as the panels in Fig. 6b, but for mixing ratio, when using the TROPoe BC method on*
 655 *the MWR Tbs.*

657 **4.2 Statistics for the profiles least close to the climatology**

658 Physical retrievals use climatological data as a constraint in the retrieval. Statistically,
 659 the averaged profiles of both temperature and moisture variables are very close to the
 660 climatological averages. However, the most interesting and difficult profiles to retrieve are the
 661 cases furthest from climatology (Löhnert and Maier, 2012). To check the behavior of the
 662 retrieved data in such “extreme” cases, the RMSE was first calculated for each radiosonde

663 profile relative to the prior profiles for 37 vertical levels from the surface up to 3 km AGL, and
 664 then the 15 cases with the largest 0-3 km layer averaged RMSEs compared to the prior were
 665 selected.



666 *Fig. 8. From top to bottom: biases (retrievals minus radiosonde), RMSEs, standard deviations of*
 667 *the difference between retrievals and radiosonde, and Pearson correlations for the four PR*
 668 *configurations, averaged from the surface to 3 km AGL, and over all radiosonde data (solid*
 669 *boxes), and over the 15 extreme cases (hatched boxes). The data in panels a) use radiosonde BC,*
 670 *and in b) TROPoe BC on the MWR Tbs.*

671 Figure 8 shows the temperature statistical analysis for the entire radiosonde data set
 672 (solid boxes) and for the fifteen events far from the climatological mean (hatched boxes) for
 673 bias, RMSE, standard deviation of the differences between retrievals and radiosonde data, and
 674 Pearson correlation, calculated as the weighted averaged over the 37 vertical heights up to 3
 675 km AGL¹.

¹ The vertical grid used in the PRs is not uniform, with more frequent levels closer to the surface. If a simple average of the data from all levels is used, the near-surface layer will be weighted more compared to the upper levels of the retrievals. To avoid this, a vertical average over the lowest 3 km AGL is performed using weights at each vertical level determined by the distance between the levels.

676 Differences in the statistics when using the entire radiosonde data set or the fifteen
677 extreme profiles are noticeable for all statistical estimators. The PRs that include RASS
678 observations show better performance compared to the strictly MWR-only PR profiles (i.e.,
679 MWRz and MWRzo) for almost all statistical comparisons. This improvement is larger for the
680 PRs using the TROPoe BC (Fig. 8b) compared to the PRs using the radiosonde BC (Fig. 8a). Three
681 statistical estimators, RMSE, standard deviation, and Pearson correlation show overall better
682 values for the 15 extreme cases compared to the whole radiosonde dataset, for all PR
683 configurations and both BC approaches. This is due to the fact that for this dataset the monthly
684 averaged radiosonde profiles (for March and May particularly) depart quite substantially from
685 the monthly prior profiles. For example, the averaged radiosonde profile in March is warmer by
686 ~ 7 °C compared to the March prior (and in May by ~ 5 °C) in the first 3 km AGL. Consequently,
687 the extreme cases (mostly found in March) have the warmest radiosonde temperature profiles,
688 but are overall closer to the monthly averaged radiosonde profiles.

689 Table 2 includes the same data as in Figure 8 but as a percentage of the improvement,
690 compared to the MWRz retrievals.

691

692

693

694

695

696

0-3 km AGL	ALL EVENTS					15 EVENTS LEAST CLOSE TO THE PRIOR			
RADIOSONDE BIAS-CORRECTION									
	MWRz	MWRzo	MWRzo RASS915	MWRzo RASS449		MWRz	MWRzo	MWRzo RASS915	MWRzo RASS449
RMSE	0%	5%	11%	13%		0%	7%	10%	3%
STTD	0%	4%	10%	12%		0%	8%	14%	17%
CORR	0%	0.1%	0.3%	0.3%		0%	0.1%	0.2%	0.3%
TROPoe BIAS-CORRECTION									
RMSE	0%	10%	25%	32%		0%	15%	15%	21%
STTD	0%	9%	18%	16%		0%	14%	16%	20%
CORR	0%	0.4%	0.9%	0.7%		0%	0.3%	0.4%	0.4%

697

698 *Table 2. Retrieval improvements for different RASS/MWR configurations as a percentage*

699 *compared to MWRz.*

700

701 The results presented in Table 2 show improvements in all statistical estimations when
702 including RASS observations, with improvements in RMSE between 10 and 20 %, demonstrating
703 the positive impact derived by the inclusion of the active measurements, regardless of the bias-
704 correction method used, but larger for the TROPoe BC data because there is more room for
705 improvement when this BC method is used. Improvements in the Pearson correlation

706 coefficients are small because correlation, determined during XPIA by the overall temperature
707 structure with height and diurnal cycle, is already good, leaving little room for improvement.

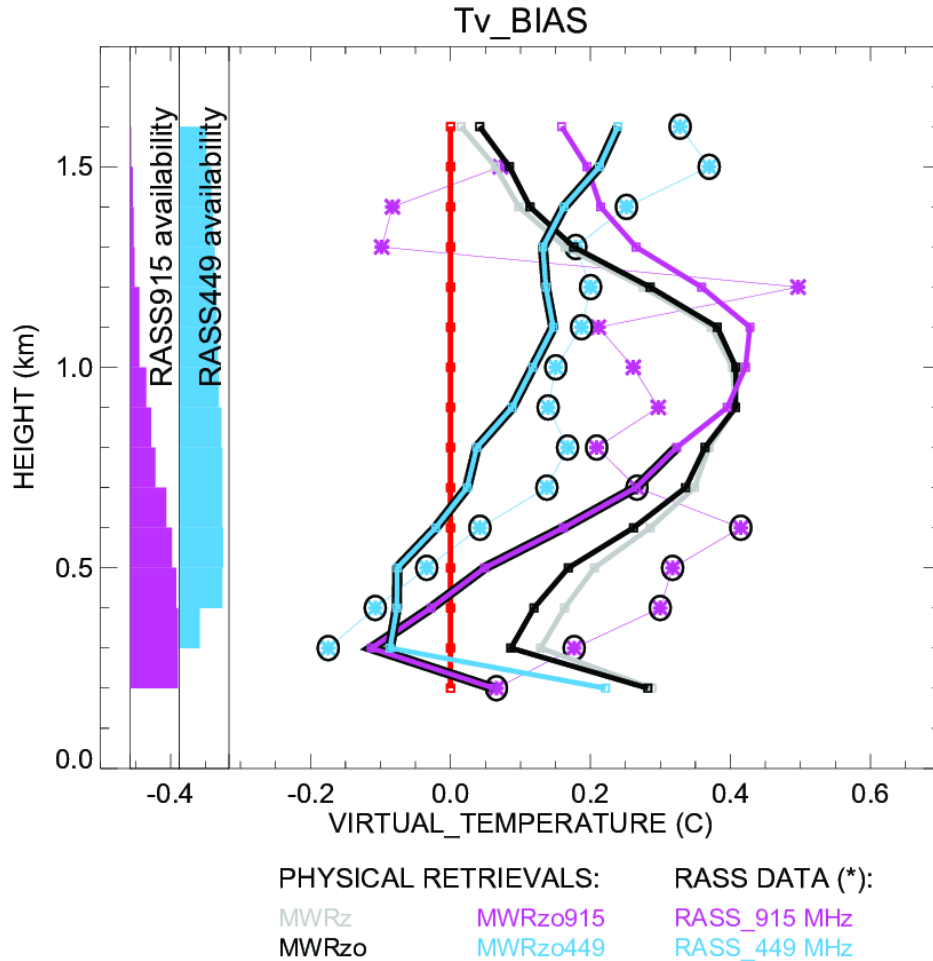
708

709 **4.3 Virtual temperature profile statistics**

710 Using the physical retrieval outputs, “retrieved virtual temperature profiles” can also be
711 calculated. In this section the direct comparison of these retrieved virtual temperature profiles
712 and RASS virtual temperature profiles to the original radiosonde is shown. With this comparison
713 we want to show how the biases of the retrieved profiles relate to the original RASS Tv biases.

714 Figure 9 shows Tv retrieved profile biases compared to the original radiosonde data as
715 solid lines, and RASS 915 and RASS 449 Tv bias as asterisks. RASS data are interpolated on a
716 regular vertical grid, going from 200 m to 1.6 km with a 100 m range, for easy comparison.

717 A zero bias is denoted by the red line. On the left side of the figure the bar charts of the
718 RASS measurement availability are shown as a function of height. The widest part of these
719 charts corresponds to 100% data availability. Heights with RASS availability greater than 50%
720 are marked with additional circles over the asterisks.



721

722 *Fig. 9. Bias of virtual temperature for all PR configurations compared to the original radiosonde*
 723 *measurements. RASS data are marked by asterisks and by additional circles for the RASS data*
 724 *with more than 50% availability, according to the availability bar charts on the left.*

725 *All PRs profiles are derived after applying the radiosonde BC method.*

726

727 While RASS 449 data are available at almost all heights up to 1.6 km, the RASS 915 data
 728 availability decreases considerably with height, lowering to 50% availability around 800 m AGL.

729 The PRs that include RASS data, MWRzo915 and MWRzo449, are also marked with additional

730 black lines at the heights with at least 50% of relative RASS data availability. In agreement with
731 Fig. 6a, this figure clearly shows the superiority of the MWRzo449 and MWRzo915 (in the layer
732 with > 50% RASS data availability) compared to the MWRz and MWRzo configurations, which
733 do not include RASS data. For MWRzo449, RASS 449 data were almost always available,
734 therefore it is easy to identify a similarity between the Tv bias profiles of the RASS 449 and the
735 PRs including it. Thus, for the MWRzo449 the Tv bias is more uniform through the heights
736 compared to all other PRs that do not include RASS data. Moreover, it is noted a roughly
737 constant offset between the MWRzo449 Tv and RASS 449 Tv biases profiles, with their
738 averaged difference equal to ~ 0.08 °C (when the radiosonde BC is used), and to ~ 0.32 °C (when
739 the TROPoe BC is used, not shown), over the ~ 1.3 km (0.3-1.6 km) atmospheric layer where
740 more than 50% of the RASS 449 measurements are available, uniformly distributed through the
741 heights. The inclusion of the RASS into the PRs does reduce the values of the biases in the
742 retrievals even below the values of the RASS biases.

743

744 5. Conclusions

745 In this study, data collected during the XPIA field campaign were used to test different
746 configurations of a physical-iterative retrieval (PR) approach in the determination of
747 temperature and humidity profiles from data collected by microwave radiometers, surface
748 sensors, and RASS measurements. The accuracy of several PR configurations was tested: two
749 configurations made use only of surface observations and MWR observed brightness
750 temperature (zenith only, MWRz; and zenith plus oblique, MWRzo); while two others included
751 the active virtual temperature profile observations available from co-located RASS (one, RASS

752 915, associated with a 915-MHz; and the other, RASS 449, associated with a 449-MHz wind
753 profiling radar). Radiosonde launches were used for verification of the retrieved profiles. In
754 Appendix A, the performance of MWRz and MWRzo retrieved profiles and Neural Network
755 retrieved profiles against the radiosondes was evaluated.

756 To remove any observational systematic error in the MWR Tb observations, two bias-
757 correction procedures were tested. The first one takes advantage of the many radiosondes
758 launched during XPIA, and the second one uses climatological profiles. As expected, the
759 radiosonde bias-correction method gives retrieved profiles closer to the radiosonde
760 temperature profiles than when using the climatological based method. Nevertheless, our
761 results show that regardless of the bias-correction method used, the inclusion of the
762 observations from the active RASS instruments in the PR approach improves the accuracy of the
763 temperature profiles by around 10-20% compared to the PR configuration using only surface
764 observations and MWR observed brightness temperature from the zenith scan. Of the PRs
765 configurations tested, generally better statistical agreement is found with the radiosonde
766 observations when the RASS 449 is used together with the surface observations and brightness
767 temperature from the zenith and averaged oblique MWR observations.

768 The **AKernel** and the posterior covariance matrices for temperature are used to derive
769 the one-sigma uncertainty, vertical resolution, and cumulative degree of freedom as a function
770 of height for the different PRs, and the level-to-level correlated uncertainty of the retrievals.
771 Results show that the inclusion of the active instruments improves all of the above-mentioned
772 variables in the 0-3km layer, including at heights between 2-3km that are above the maximum

773 RASS height. Thus, the positive impact of the RASS observations extends into the atmosphere
774 above the height of measurements themselves.

775 Furthermore, 15 cases when temperature profiles from the radiosonde observations
776 were the furthest away from the mean climatological average were selected, and the statistical
777 comparison was reproduced over this subset of cases. These are the cases usually the most
778 difficult to retrieve and the most important to forecast; therefore, it is essential to improve the
779 retrievals in these situations. Even for this subset of selected cases the inclusion of active
780 sensor observations in the PRs is found to be beneficial.

781 Finally, the impact of the inclusion of RASS measurements on the retrieved humidity
782 profiles was considered, but the inclusion of RASS observations did not produce significantly
783 better results, compared to the configurations that do not include them. This was not a surprise
784 as RASS measures virtual temperature, effectively adding very little extra information to the
785 water vapor retrieval. In this case a better option would be to consider adding other active
786 remote sensors such as water vapor differential absorption lidars (DIALs) to the PRs. Turner and
787 Löhnert (2021) showed that including the partial profile of water vapor observed by the DIAL
788 substantially increases the information content in the combined water vapor retrievals.
789 Consequently, to improve both temperature and humidity retrievals a synergy between MWR,
790 RASS, and DIAL systems would likely be necessary.

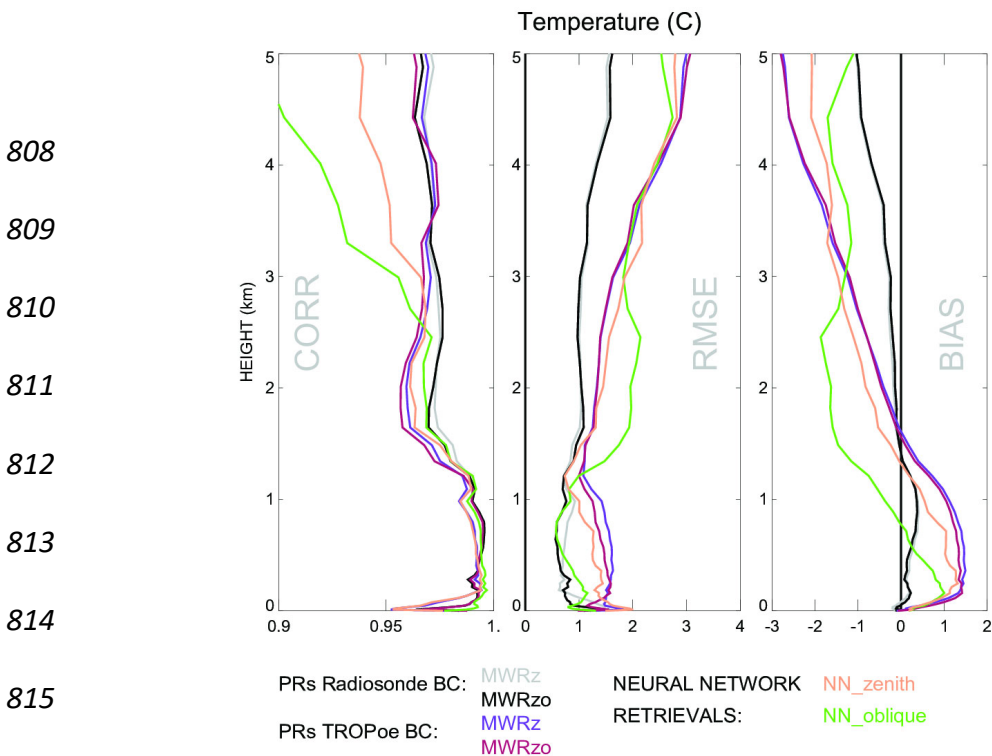
791

792 **Appendix A**

793 The neural network (NN) retrievals developed by the vendor explicitly for XPIA use a
794 training dataset based on a 5-year climatology of profiles from radiosondes launched at the

795 Denver International Airport, 35 miles south-east from the XPIA site. NN-based MWR vertical
 796 retrieval profiles were obtained using the zenith or an average of two oblique elevation scans,
 797 15- and 165-degrees (not including the zenith), all with 58 levels extending from the surface up
 798 to 10 km, with nominal vertical grid depending on the height (every 50 m from the surface to
 799 500 m, every 100 m from 500 m to 2 km, and every 250 m from 2 to 10 km, AGL).

800 Fig. 1A shows composite NN vertical profiles of temperature (separately for the zenith
 801 and averaged obliques) calculated for radiosonde launch times, and the corresponding PR
 802 profiles already introduced in Fig. 6a, b. For a proper comparison, only MWRz and MWRzo
 803 profiles are used, without including RASS measurements. It has to be noted that since the “NN
 804 oblique” retrieval provided by the manufacturer of the radiometer does not include the zenith,
 805 this configuration cannot be considered exactly equivalent to the MWRzo PR.



816 *Fig. 1A. Pearson correlation, RMSE, and mean bias for temperature profiles for MWRz in grey*
817 *(and purple) and MWRzo in black (and maroon) when the radiosonde BC (and the TROPoe BC)*
818 *method is applied. Included in this figure are the NN temperature profiles, from the zenith scan*
819 *(in beige), and from the averaged oblique scans (in green).*

820

821 Another difference to point out is that, while the MWR Tb data have been bias-
822 corrected before being used in the PR configurations, as discussed in Section 3.2, the NN
823 retrievals use the uncorrected Tb, since it was non-trivial to reprocess those retrievals. Martinet
824 et al. (2015) showed that when it is possible to bias-correct the MWR Tb before applying the
825 NN retrieval technique, the NN retrievals are not impacted below 1 km AGL, but a clear
826 improvement of NN retrievals in terms of RMSE and bias are observed between 1 and 3 km
827 altitude. As is visible in Fig. 1A, this is the layer of the atmosphere where the NN profiles (beige
828 and green lines) have larger bias and RMSE, compared to the PR profiles.

829 When the radiosonde BC method is used, the MWRz and MWRzo PRs (gray and black
830 lines) present better statistics through the entire profiles shown in Fig. 1A, with larger values of
831 the correlation coefficient, and smaller values of RMSE and bias. The oblique only NN profiles
832 (in green) show comparable statistics to the PRs employing the radiosonde BC method up to 1
833 km AGL, with degraded performances above this height. Above 1 km AGL, the zenith NN
834 profiles (in beige) do better than the oblique NN in terms of RMSE and bias. When the TROPoe
835 BC method is used, the MWRz and MWRzo PRs (purple and maroon lines) perform better than
836 the NN profiles only in terms of RMSE and bias, and above around 1.5 km AGL.

837 The better performance obtained by the MWRz and MWRzo PRs that use the
838 radiosonde BC approach demonstrate the importance of having an accurate and reliable
839 method for bias correcting the MWR.

840

841 **Data availability**

842 All data are publicly accessible at the DOE Atmosphere to Electrons Data Archive and
843 Portal, found at <https://a2e.energy.gov/projects/xpia> (Lundquist et al., 2016).

844

845 **Author contribution**

846 Irina Djalalova completed the primary analysis using the XPIA dataset. Daniel Gotta
847 contributed to the post-processing of the RASS data. Dave Turner modified the TROPoe
848 algorithm to include the RASS data as input. All authors contributed to the analysis of the
849 results. Irina Djalalova prepared the manuscript with contributions from all co-authors.

850

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858

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860

861 **References**

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