

1                   **Improving thermodynamic profile retrievals from microwave**  
2                   **radiometers by including Radio Acoustic Sounding System (RASS)**  
3                   **observations**

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44 **Abstract**

45           Thermodynamic profiles are often retrieved from the multi-wavelength brightness  
46 temperature observations made by microwave radiometers (MWRs) using regression methods  
47 (linear, quadratic approaches), artificial intelligence (neural networks), or physical-iterative  
48 methods. Regression and neural network methods are tuned to mean conditions derived from  
49 a climatological dataset of thermodynamic profiles collected nearby. In contrast, physical-  
50 iterative retrievals use a radiative transfer model starting from a climatologically reasonable  
51 profile of temperature and water vapor, with the model running iteratively until the derived  
52 brightness temperatures match those observed by the MWR within a specified uncertainty.

53           In this study, a physical-iterative approach is used to retrieve temperature and humidity  
54 profiles from data collected during XPIA (eXperimental Planetary boundary layer Instrument  
55 Assessment), a field campaign held from March to May 2015 at NOAA's Boulder Atmospheric  
56 Observatory (BAO) facility. During the campaign, several passive and active remote sensing  
57 instruments as well as in-situ platforms were deployed and evaluated to determine their  
58 suitability for the verification and validation of meteorological processes. Among the deployed  
59 remote sensing instruments were a multi-channel MWR, as well as two radio acoustic sounding  
60 systems (RASS), associated with 915-MHz and 449-MHz wind profiling radars.

61           In this study the physical-iterative approach is tested with different observational  
62 inputs: first using data from surface sensors and the MWR in different configurations, and then  
63 including data from the RASS into the retrieval with the MWR data. These temperature  
64 retrievals are assessed against co-located radiosonde profiles. Results show that the  
65 combination of the MWR and RASS observations in the retrieval allows for a more accurate

66 characterization of low-level temperature inversions, and that these retrieved temperature  
67 profiles match the radiosonde observations better than the temperature profiles retrieved from  
68 only the MWR in the layer between the surface and 3 km above ground level (AGL). Specifically,  
69 in this layer of the atmosphere, both root mean square errors and standard deviations of the  
70 difference between radiosonde and retrievals that combine MWR and RASS are improved by  
71 mostly 10-20% compared to the configuration that does not include RASS observations.  
72 Pearson correlation coefficients are also improved.

73           A comparison of the temperature physical retrievals to the manufacturer-provided neural  
74 network retrievals is provided in Appendix A.

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88 **1. Introduction**

89 Monitoring the state of the atmosphere for process understanding and for model  
90 verification and validation requires observations from a variety of instruments, each one having  
91 its set of advantages and disadvantages. Using several diverse instruments allows one to  
92 monitor different aspects of the atmosphere, while combining them in an optimized synergetic  
93 approach can improve the accuracy of the information available on the state of the  
94 atmosphere.

95 During the eXperimental Planetary boundary layer Instrumentation Assessment (XPIA)  
96 campaign, a U.S. Department of Energy sponsored experiment held at the Boulder Atmospheric  
97 Observatory (BAO) in Spring 2015, several instruments were deployed (Lundquist et al., 2017)  
98 with the goal of assessing their capability for measuring atmospheric boundary layer  
99 meteorological variables. XPIA investigated novel measurement approaches, and quantified  
100 uncertainties associated with these measurement methods. While the main interest of the XPIA  
101 campaign was on wind and turbulence, measurements of other important atmospheric  
102 variables were also collected, including temperature and humidity. Among the deployed  
103 instruments were two identical microwave radiometers (MWRs) and two radio acoustic  
104 sounding systems (RASS), as well as radiosondes launches.

105 MWRs are passive sensors, sensitive to atmospheric temperature, humidity and liquid  
106 water path (LWP), that allow for a high temporal observation of the state of the atmosphere,  
107 with some advantages and limitations. In order to estimate profiles of temperature and  
108 humidity from the observed brightness temperatures ( $T_b$ ), several methods could be applied  
109 such as regressions, neural network retrievals, or physical retrieval methodologies which can

110 include additional information about the atmospheric state in the retrieval process (e.g., Maahn  
111 et al. 2020). Microwave radiative transfer models (e.g., Rosenkranz, 1998; Clough et al. 2005)  
112 are commonly used to train statistical retrievals, or as forward models used within physical  
113 retrieval methods. Advantages of MWRs include their compact design, the relatively high  
114 temporal resolution of the measurements (2-3 minutes), the possibility to observe the vertical  
115 structure of both temperature and moisture through the lower part of the troposphere during  
116 both clear and cloudy conditions, and their capability to operate in a standalone mode.  
117 Disadvantages include limited accuracy in the presence of rain, rather coarse vertical  
118 resolution, and the necessity to have a site-specific climatology for retrievals. Other  
119 disadvantages include the challenges related to performing accurate calibrations (Küchler et al.,  
120 2016, and references within), radio frequency interference (RFI), and the low accuracy on the  
121 retrieved LWP especially for values of LWP less than  $20 \text{ g m}^{-2}$  (Turner 2007).

122 RASS, in comparison, are active instruments that emit a longitudinal acoustic wave  
123 upward, causing a local compression and rarefaction of the ambient air. These density  
124 variations are tracked by the Doppler radar associated with the RASS, and the speed of the  
125 propagating sound wave is measured. The speed of sound is related to the virtual temperature  
126 ( $T_v$ ) (North et al., 1973), and therefore, RASS are used to remotely measure vertical profiles of  
127 virtual temperature in the boundary layer. Being an active instrument, the RASS is in general  
128 more accurate than a passive instrument (Bianco et al., 2017), but they also come with their  
129 own disadvantages. The main limitations of RASS for temperature measurements are the low  
130 temporal resolution (typically a 5-min averaged RASS profile is measured once or twice per  
131 hour), their limited altitude coverage, and the noise “pollution” that impacts local communities.

132 Adachi and Hashiguchi (2019) have shown that RASS could use parametric speakers to take  
133 advantage of their high directivity and very low side lobes. Nevertheless, the maximum height  
134 reached by the RASS is limited by sound attenuation, which is a function of both radar  
135 frequency and atmospheric conditions (May and Wilczak, 1993) such as temperature, humidity,  
136 and the advection of the propagating sound wave out of the radar's field-of-view. Therefore,  
137 data availability is usually limited to the lowest several kilometers, depending on the frequency  
138 of the radar. In addition, wintertime coverage is usually lower than that in summer, due to  
139 increased attenuation of the acoustic signal in cooler and drier environments.

140         To get a better picture of the state of the temperature and moisture structure of the  
141 atmosphere, it makes sense to try to combine the information obtained by both MWR and  
142 RASS. Integration of different instruments has been and still is a topic of ongoing scientific  
143 interest (Han and Westwater 1995; Stankov et al. 1996; Bianco et al., 2005; Engelbart et al.,  
144 2009; Cimini et al., 2020; Turner and Löhnert, 2021, to name some). In this study, the focus is  
145 on the combination of the MWR and RASS observations in the retrievals to improve the  
146 accuracy of the temperature profiles in the lowest 3 km compared to physical retrieval  
147 approaches that do not include the information from RASS measurements. Some studies have  
148 used analyses from numerical weather prediction (NWP) models as an additional constraint in  
149 these variational retrievals (e.g., Hewison 2007; Cimini et al. 2006, 2011; Martinet et al. 2020);  
150 however, we have elected not to include model data in this study because we wanted to  
151 evaluate the impact of the RASS profiles on the retrievals from a purely observational  
152 perspective.

153 This paper is organized as follows: Section 2 summarizes the experimental dataset;  
154 Section 3 introduces the principles of the physical retrieval approaches used to obtain vertical  
155 profiles of the desired variables; Section 4 produces statistical analysis of the comparison  
156 between the different retrieval approaches and radiosonde measurement; finally, conclusions  
157 are presented in Section 5.

158

## 159 **2. XPIA dataset**

160 The data used in our analysis were collected during the XPIA experiment, held in Spring  
161 2015 (March-May) at NOAA's BAO site, in Erie, Colorado (Lat.: 40.0451 N, Lon.: 105.0057 W, El.:  
162 1584 m MSL). XPIA was the last experiment conducted at this facility, as after almost 40 years  
163 of operations the BAO 300-m tower was demolished at the end of 2016 (Wolfe and Lataitis,  
164 2018). XPIA was designed to assess the capability of different remote sensing instruments for  
165 quantifying boundary layer structure, and was a preliminary study as many of these same  
166 instruments were later deployed, among other campaigns, for the second Wind Forecast  
167 Improvement Project WFIP2 (Shaw et al., 2019; Wilczak et al., 2019) which investigated flows in  
168 complex terrain for wind energy applications, where they were for example used to study cold  
169 air pools (Adler et al., 2021) and gap flow characteristics (Neiman et al., 2019; Banta et al.,  
170 2020). The list of the deployed instruments included active and passive remote-sensing devices,  
171 and in-situ instruments mounted on the BAO tower. Data collected during XPIA are publicly  
172 available at <https://a2e.energy.gov/projects/xpia>. A detailed description of the XPIA  
173 experiment can be found in Lundquist et al. (2017), while a specific look at the accuracy of the  
174 instruments used in this study can be found in Bianco et al. (2017).



175

176 **2.1 MWR measurements**

177 Two identical MWRs (Radiometrics MP-3000A) managed by NOAA (MWR-NOAA) and by  
178 the University of Colorado (MWR-CU), were deployed next to each other at the visitor center  
179 ~600 m south of the BAO tower (see Lundquist et al., 2017 for a detailed map of the study  
180 area). Prior to the experiment, both MWRs were thoroughly serviced (sensor cleaning, radome  
181 replacement, etc.) and calibrated using an external liquid nitrogen target and an internal  
182 ambient target. MWRs are passive devices which record the natural microwave emission in the  
183 water vapor and oxygen absorption bands from the atmosphere, providing measurements of  
184 the brightness temperatures. Both MWRs have 35-channels spanning a range of frequencies,  
185 with 21 channels in the lower (22-30 GHz) K-band frequency band, of which 8 channels were  
186 used during XPIA: 22.234, 22.5, 23.034, 23.834, 25, 26.234, 28 and 30 GHz; and 14 channels in  
187 the higher (51-59 GHz) V-band frequency band, of which all were used in XPIA: 51.248, 51.76,  
188 52.28, 52.804, 53.336, 53.848, 54.4, 54.94, 55.5, 56.02, 56.66, 57.288, 57.964 and 58.8 GHz.  
189 Frequencies in the K-band are more sensitive to water vapor and cloud liquid water, while  
190 frequencies in the V-band are sensitive to atmospheric temperature due to the absorption of  
191 atmospheric oxygen (Cadeddu et al., 2013). V-band frequencies or channels can also be divided  
192 in two categories: the opaque channels, 56.66 GHz and higher, that are more informative in the  
193 layer of the atmosphere from the surface to ~1 km AGL, and the transparent channels, 51-56  
194 GHz, that are more informative above 1 km AGL. Both MWRs observed at the zenith and at 15-  
195 and 165-degree elevation angles in the north-south plane (referred to as oblique elevation  
196 scans and used as their average hereafter; note zenith views have a 90-degree elevation angle).

197 However, when MWRs are deployed in locations with unobstructed views, oblique scans can be  
198 performed down to 5 degrees elevation angles and may provide better temperature profile  
199 accuracy in the lowest 0-1 or even 0-2 km AGL layers (Crewell and Löhnert, 2007).

200 In addition, each MWR was provided with a separate surface sensor to measure  
201 pressure, temperature, and relative humidity at the installation level that was ~2.5 m AGL.  
202 Vertical profiles of temperature (T), water vapor density (WVD), and relative humidity (RH)  
203 were retrieved in real-time during XPIA every 2-3 minutes using a neural network (NN)  
204 approach provided by the manufacturer of the radiometer (Solheim et al. 1998a, and 1998b;  
205 Ware et al., 2003). Although the physical retrieval configurations used in this study do not  
206 exactly match the NN retrieval configurations, a comparison of both physical and neural  
207 network retrievals to the radiosonde temperature data is presented in Appendix A.

208 Both MWRs nominally operated from 9 March to 7 May 2015, although the MWR-NOAA  
209 was unavailable between 5-27 April 2015. For the overlapping dates, temperature profiles  
210 retrieved from the two MWRs showed very good agreement with less than 0.5 °C bias and  
211 0.994 correlation (Bianco et al., 2017). For this reason, and because the MWR-CU was available  
212 for a longer time period, only the MWR-CU (hereafter simply called MWR) is used.

213

## 214 **2.2 WPR-RASS measurements**

215 Two NOAA wind profiling radars (WPRs), operating at frequencies of 915-MHz and 449-  
216 MHz, were deployed at the visitor center (same location as the MWR) during XPIA. These  
217 systems are primarily designed to measure the vertical profile of the horizontal wind vector, but  
218 co-located RASS also enable the observation of profiles of virtual temperature in the lower

219 atmosphere, with different resolutions and height coverages depending on the WPR. Thus, the  
220 RASS associated with the 915-MHz WPR (hereafter referred to as RASS 915) measured virtual  
221 temperature from 120 to 1618 m with a vertical resolution of 62 m, and the 449 MHz RASS  
222 (hereafter referred to as RASS 449) sampled the boundary layer from 217 to 2001 m with a  
223 vertical resolution of 105 m. The maximum height reached by the RASS is a function of both  
224 radar frequency and atmospheric conditions (May and Wilczak, 1993), and is usually lower for  
225 RASS 915 data, as will be shown later in the analysis.

226 The RASS data were processed using a radio frequency interference (RFI)-removal  
227 algorithm (performed on the RASS spectra), a consensus algorithm (Strauch et al. 1984)  
228 performed on the moment data using a 60% consensus threshold, a Weber-Wuertz outlier  
229 removal algorithm (Weber et al., 1993) performed on the consensus averages, and a RASS  
230 range-correction algorithm (Görsdorf and Lehmann, 2000) using an average relative humidity  
231 setting of 50% determined from the available observations.

232

### 233 **2.3 BAO data**

234 The BAO 300-m tower was built in 1977 to study the planetary boundary layer (Kaimal  
235 and Gaynor 1983). During XPIA, measurements were collected at the surface (2 m) and at six  
236 higher levels (50, 100, 150, 200, 250 and 300 m AGL). Each tower level was equipped with 2  
237 sonic anemometers on orthogonal booms, and one sensor based on a Sensiron SHT75 solid-  
238 state sensor to measure temperature and relative humidity with a time resolution of 1 s, and  
239 averaged over five minutes. The more accurate temperature and water vapor observations

240 (Horst et al., 2016) at the BAO tower 2 m AGL level are used in the physical retrieval in place of  
241 the less accurate MWR surface sensor.

242

## 243 **2.4 Radiosonde measurements**

244 Between 9 March and 7 May 2015, while the MWR was operational, radiosondes were  
245 launched by the National Center for Atmospheric Research (NCAR) assisted by several students  
246 from the University of Colorado over three selected periods, one each in March, April, and May.  
247 All radiosondes were Vaisala model RS92. There was a total of 59 launches, mostly four times  
248 per day, around 1400, 1800, 2200, and 0200 UTC (0800, 1200, 1600 and 2000 local standard  
249 time, LST). The first 35 launches, between 9-19 March, were done from the visitor center, while  
250 11 launches between 15-22 April, and 13 launches between 1-4 May, were done from the  
251 water tank site, ~1000 meters away from the visitor center (see Lundquist et al., 2017 for a  
252 detailed map of the study area). The radiosonde measurements included temperature, dew  
253 point temperature, and relative humidity to altitudes usually higher than 10 km AGL, with  
254 measurements every few seconds. As a first step, for additional verification, the radiosonde  
255 data from the 59 launches taken between 9 March and 4 May 2015 were compared to the BAO  
256 tower measurements, up to 300 m AGL. These observed data sets match very well, with a  
257 correlation coefficient of 0.99 and a standard deviation of ~0.7 °C. However, one radiosonde  
258 profile showed a large bias (> 5 °C) against all seven levels of BAO temperature measurements  
259 and all available Tv measurements from the RASS 915 (eight measurements up to 600 m AGL)  
260 and from the RASS 449 (nine measurements up to 1100 m AGL), therefore this particular  
261 radiosonde profile was excluded from the statistical analysis. Moreover, while accurate RASS

262 data can be collected during rain, MWR data could be potentially deteriorated due to water  
263 deposition on the radome. Therefore, six profiles (three for March 13, and one each on May 1,  
264 3 and 4) were eliminated from the statistical evaluation. These restrictions lowered the number  
265 of total radiosonde launches used in this study to 52.

266

### 267 **3. Physical retrievals**

268 One way to combine the active and passive instruments would be to use the RASS  
269 observations up to their maximum available height, and stitch them with the profiles obtained  
270 from a physical-iterative method using MWR data. To do this, the moisture contribution to the  
271 RASS virtual temperatures could be removed by using either the relative humidity measured by  
272 the MWR or by a climatology of the moisture term. However, merging these different profiles  
273 could result in artificial jumps at the connecting heights.

274 Alternatively, a physical retrieval (PR) iterative approach can be used to retrieve vertical  
275 profiles of thermodynamic properties from the MWR and RASS observations in a synergistic  
276 manner (e.g., Maahn et al 2020; Turner and Löhnert 2021). In this case, an optimal estimation-  
277 based physical retrieval is initialized with a climatologically reasonable profile of temperature  
278 and water vapor, and is iteratively repeated until the computed brightness temperatures match  
279 those observed by the MWR within the uncertainty of the observed brightness temperatures  
280 and the RASS virtual temperatures within their uncertainties (Rodgers, 2000; Turner and  
281 Löhnert, 2014; Cimini et al. 2018; Maahn et al. 2020).

282

#### 283 **3.1 Iterative retrieval technique**

284 For this study, the PR uses the *TROPoe* retrieval algorithm (formerly *AERIOe*, Turner and  
285 Löhnert 2014; Turner and Blumberg 2019; Turner and Löhnert 2021). This algorithm is able to  
286 use radiance data from microwave radiometers, infrared spectrometers, and other  
287 observations as input. The microwave radiative transfer model, MonoRTM (Clough et al., 2005),  
288 serves as the forward model, which is fully functional for the microwave region and was  
289 intensively evaluated previously on MWR measurements (Payne et al. 2008; 2011).

290 We start with the state vector  $\mathbf{X}_a = [\mathbf{T}, \mathbf{Q}, \text{LWP}]^T$ , where superscript T denotes transpose,  
291 and vectors and matrices are shown in bold.  $\mathbf{T}$  (K) and  $\mathbf{Q}$  ( $\text{g kg}^{-1}$ ) are temperature and water  
292 vapor mixing ratio profiles at 55 vertical levels from the surface up to 17 km, with the distance  
293 between the levels increasing geometrically with height. LWP is the liquid water path in ( $\text{g m}^{-2}$ )  
294 that measures the integrated content of liquid water in the entire vertical column above the  
295 MWR, and is a scalar. For this study,  $\mathbf{X}_a$  has dimensions equal to  $111 \times 1$  (two vectors  $\mathbf{T}$  and  $\mathbf{Q}$   
296 with 55 levels each, and LWP). The retrieval framework of Turner and Blumberg (2019) is used,  
297 but only using MWR data (no spectral infrared). Here, we demonstrate the extension of the  
298 retrieval to include RASS profiles of  $\mathbf{T}_v$ , and the resulting impact this has on the retrieved  
299 temperature profiles and information content.

300 The observation vector  $\mathbf{Y}$  includes temperature and water vapor mixing ratio measured  
301 at the surface in-situ, and spectral  $\mathbf{T}_b$  measured by the MWR. The MonoRTM model  $\mathbf{F}$  is used as  
302 the forward model from the current state vector  $\mathbf{X}$ , and is then compared to the observation  
303 vector  $\mathbf{Y}$ , iterating until the difference between  $\mathbf{F}(\mathbf{X})$  and  $\mathbf{Y}$  is small within a specified uncertainty  
304 (Eq 1).

305

$$X_{n+1} = X_n + (S_a^{-1} + K^T S_\varepsilon^{-1} K)^{-1} K^T S_\varepsilon^{-1} [Y - F(X_n) + K(X_n - X_a)] \quad (1)$$

307 with

$$308 \quad X_a = \begin{bmatrix} T \\ Q \\ LWP \end{bmatrix} \quad S_a = \begin{bmatrix} \sigma_{TT}^2 & \sigma_{TQ}^2 & 0 \\ \sigma_{QT}^2 & \sigma_{QQ}^2 & 0 \\ 0 & 0 & \sigma_{LWP}^2 \end{bmatrix} \quad K_{ij} = \frac{\partial F_i}{\partial X_j}$$

309 where i and j in the  $K_{ij}$  definition mark channel and vertical level, respectively. The superscripts

310 T and -1 in (1) indicate the transpose and inverse matrix, respectively. The observation vector  $Y$

311 and the covariance matrix of the observed data,  $S_\varepsilon$ , depending on the configuration used, are

312 equal to:

$$313 \quad Y_1 = \begin{bmatrix} T_{sfc} \\ Q_{sfc} \\ T\mathbf{b}_{zenith} \end{bmatrix} \quad S_{\varepsilon_1} = \begin{bmatrix} \sigma_{Tsfc}^2 & 0 & 0 \\ 0 & \sigma_{Qsfc}^2 & 0 \\ 0 & 0 & \sigma_{T\mathbf{b}_{zenith}}^2 \end{bmatrix}$$

$$314 \quad Y_2 = \begin{bmatrix} T_{sfc} \\ Q_{sfc} \\ T\mathbf{b}_{zenith+oblique} \end{bmatrix} \quad S_{\varepsilon_2} = \begin{bmatrix} \sigma_{Tsfc}^2 & 0 & 0 \\ 0 & \sigma_{Qsfc}^2 & 0 \\ 0 & 0 & \sigma_{T\mathbf{b}_{zenith+oblique}}^2 \end{bmatrix}$$

$$315 \quad Y_3 = \begin{bmatrix} T_{sfc} \\ Q_{sfc} \\ T\mathbf{b}_{zenith+oblique} \\ T\mathbf{v}_{RASS915} \end{bmatrix} \quad S_{\varepsilon_3} = \begin{bmatrix} \sigma_{Tsfc}^2 & 0 & 0 & 0 \\ 0 & \sigma_{Qsfc}^2 & 0 & 0 \\ 0 & 0 & \sigma_{T\mathbf{b}_{zenith+oblique}}^2 & 0 \\ 0 & 0 & 0 & \sigma_{T\mathbf{v}_{RASS915}}^2 \end{bmatrix}$$

$$316 \quad Y_4 = \begin{bmatrix} T_{sfc} \\ Q_{sfc} \\ T\mathbf{b}_{zenith+oblique} \\ T\mathbf{v}_{RASS449} \end{bmatrix} \quad S_{\varepsilon_4} = \begin{bmatrix} \sigma_{Tsfc}^2 & 0 & 0 & 0 \\ 0 & \sigma_{Qsfc}^2 & 0 & 0 \\ 0 & 0 & \sigma_{T\mathbf{b}_{zenith+oblique}}^2 & 0 \\ 0 & 0 & 0 & \sigma_{T\mathbf{v}_{RASS449}}^2 \end{bmatrix}$$

317 Note that the 2-m surface-level observations of temperature and water vapor mixing  
318 ratio ( $T_{sfc}$  and  $Q_{sfc}$ , respectively) are included as part of the observation vector  $\mathbf{Y}$ , and thus the  
319 uncertainties (0.5 K for temperature and less than  $0.4 \text{ g kg}^{-1}$  for mixing ratio) in these  
320 observations are included in  $\mathbf{S}_\epsilon$ .

321 The mean state vector of the climatological estimates, or a “prior” vector  $\mathbf{X}_a$ , is a key  
322 component in the optimal estimation framework and it is the first guess of the state vector  $\mathbf{X}$ ,  
323  $\mathbf{X}_1$  in Eq. (1). It provides a constraint on the ill-posed inversion problem. The prior is calculated  
324 independently for each month of the year from climatological sounding profiles (using 10 years  
325 of data) in the Denver area. The covariance matrix,  $\mathbf{S}_a$ , of the “prior” vector includes not only  
326 temperature or water vapor variances but also the covariances between them. Using around  
327 3,000 radiosondes launched by the NWS in Denver, each radiosonde profile is interpolated to  
328 the vertical levels used in the retrieval, after which the covariance of temperature and  
329 temperature, temperature and humidity, and humidity and humidity is computed for different  
330 levels. LWP is arbitrarily assigned in  $\mathbf{X}_a$ , with large values chosen for its uncertainty in  $\mathbf{S}_a$ , so that  
331 it does not impact (constrain) the retrieval.

332 Four configurations are chosen for the observational vector  $\mathbf{Y}$  ( $\mathbf{Y}_1$ ,  $\mathbf{Y}_2$ ,  $\mathbf{Y}_3$ , and  $\mathbf{Y}_4$ ). In each  
333 of these, the surface observations are obtained by the 2-m BAO *in-situ* measurements of  
334 temperature and humidity. The MWR provides  $\mathbf{Tb}$  measurements from 22 channels from the  
335 zenith scan for the zenith only configuration ( $\mathbf{Y}_1$ ), while when using the zenith plus oblique  $\mathbf{Tb}$   
336 inputs ( $\mathbf{Y}_2$ ,  $\mathbf{Y}_3$ , and  $\mathbf{Y}_4$ ) the same 22 channels were used from the zenith scans together with only  
337 the four opaque channels (56.66, 57.288, 57.964 and 58.8 GHz) from the oblique scans. Using  
338 additional measurements from the co-located radar systems with RASS, the observational



339 vector is further expanded with either RASS 915 ( $\mathbf{Y}_3$ ) or RASS 449 ( $\mathbf{Y}_4$ ) virtual temperature  
 340 observations. The covariance matrix of the observed data,  $\mathbf{S}_\epsilon$ , depends on the chosen  $\mathbf{Y}_i$  as seen  
 341 in the matrix  $\mathbf{S}_{\epsilon i}$  (with  $i = 1:4$ ) descriptions, with increasing dimensions from  $\mathbf{Y}_1$  to  $\mathbf{Y}_2$  and  
 342 additional increasing dimensions to  $\mathbf{Y}_3$  or  $\mathbf{Y}_4$  through the multi-level measurements of the RASS  
 343 (Turner and Blumberg, 2019). Table 1 summarizes the observational information included in  
 344 these four different configurations of the PR.  
 345

	$T_{sfc}$	$Q_{sfc}$	$Tb_{zenith}$	$Tb_{oblique}$	$TV_{RASS915}$	$TV_{RASS449}$
$\mathbf{Y}_1 = MWRz$	X	X	X			
$\mathbf{Y}_2 = MWRzo$	X	X	X	X		
$\mathbf{Y}_3 = MWRzo915$	X	X	X	X	X	
$\mathbf{Y}_4 = MWRzo449$	X	X	X	X		X

346 Table 1. Four PR configurations corresponding to the four observational  $\mathbf{Y}_i$  vectors in Eq. (1).

347

348 The uncertainty in the MWR Tb observations was set to the standard deviation from a  
 349 detrended time-series analysis for each channel during cloud-free periods. The method to  
 350 detect those cloud-free periods is described in detail in Section 3.2. The derived uncertainties  
 351 ranged from 0.3 K to 0.4 K in the 22 to 30 GHz channels, and 0.4 to 0.8 K in the 52 to 60 GHz

352 channels. We assumed that there was no correlated error between the different MWR  
353 channels.

354 For the RASS, co-located RASS and radiosonde profiles were compared and the standard  
355 deviation of the differences in  $T_v$  were determined as a function of the radar's signal-to-noise  
356 ratio (SNR). This relationship resulted in uncertainties that ranged from 0.8 K at high SNR values  
357 to 1.5 K at low SNR values. Again, we assumed that there was no correlated error between  
358 different RASS heights. Following these assumptions, the covariance matrix  $\mathbf{S}_\epsilon$  is diagonal.

359 The Jacobian matrix,  $\mathbf{K}$ , is computed using finite differences by perturbing the elements  
360 of  $\mathbf{X}$  and rerunning the forward model. It has dimensions  $m \times 111$ , where  $m$  is the length of the  
361 vector  $\mathbf{Y}_i$ , therefore its dimension increases correspondingly with the inclusion of more  
362 observational data.  $\mathbf{K}$  makes the "connection" between the state vector and the observational  
363 data and should be calculated at every iteration.

364

### 365 **3.2 Bias-correction of MWR observations using radiosondes or climatology**

366 Observational errors propagate through retrieval into the derived profiles (i.e. the bias  
367 of the observed data will contribute to a bias in the retrievals). For that, retrieval uncertainties  
368 in Eq. (1) from  $\mathbf{Y} = \mathbf{Y}_1$  or  $\mathbf{Y}_2$  derive only from uncertainties in surface and MWR data, while  
369 retrieval uncertainties from  $\mathbf{Y} = \mathbf{Y}_3$  or  $\mathbf{Y}_4$  come from uncertainties in the surface, MWR, and RASS  
370 measurements.

371 The bias of the retrieval depends on both the absolute accuracy of the forward model  
372 and on any observational systematic offset, of which the systematic error in the MWR  
373 observations could potentially be reduced through application of an MWR  $T_b$  bias-correction

374 procedure. In this study, two different approaches were used for the bias-correction: the first is  
375 based on a comparison to the radiosondes, while the second uses climatological profiles. The  
376 first method could be used for a field campaign where occasional co-located radiosonde  
377 launches are taken, while the second would be used for deployments without any supporting  
378 radiosonde observations.

379 For both approaches, the first step is to identify clear-sky periods during which the bias  
380 can be estimated (to eliminate uncertainties associated with clouds) and subsequently the bias  
381 can be removed from the observed MWR Tbs. One method to identify clear-sky times is to use  
382 a time-series of Tb observations in the 30 GHz liquid water sensitive channel of the MWR.

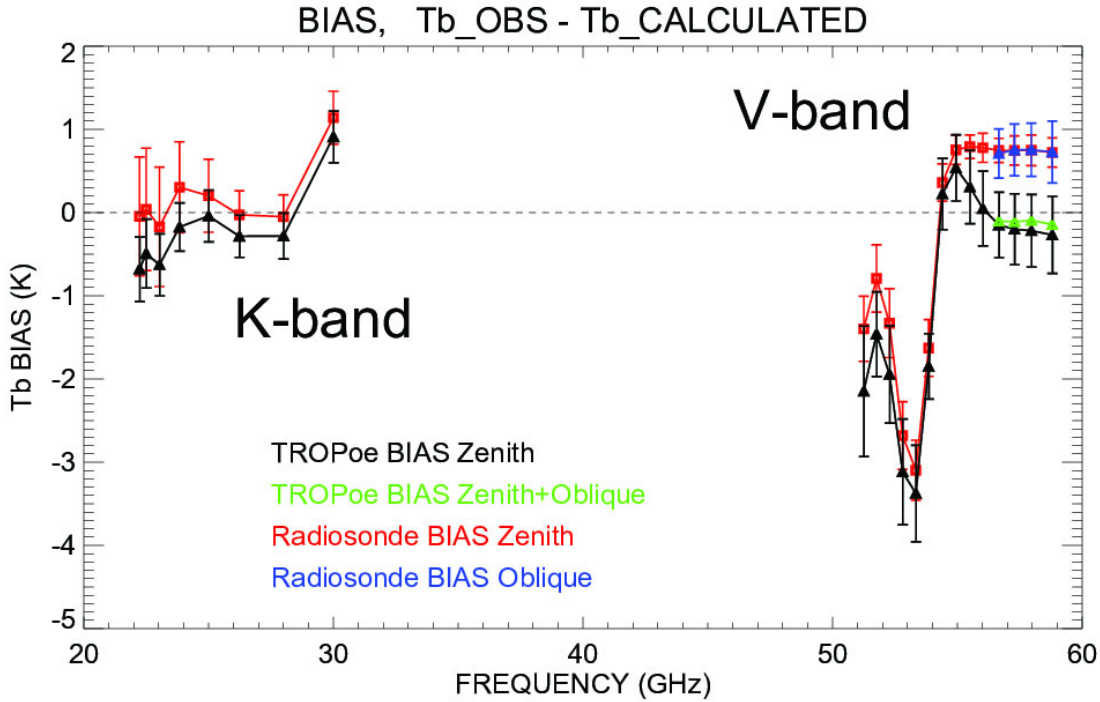
383 The standard deviation of the MWR Tb in the 30 GHz channel is calculated over a time  
384 frame of one hour centered at the radiosonde launch time. The data from the zenith scan and  
385 the averaged oblique scans are reviewed separately. Liquid-cloud free periods were identified  
386 by cases where the temporal standard deviation was small ( $< 0.4$  K), and more than 35  
387 radiosonde profiles were classified as being launched in clear skies. The usage of the standard  
388 deviation from the time-series from the oblique scans, with the same 0.4 K restriction, reduces  
389 the number of the clear-sky radiosonde profiles to 18. For those chosen 18 radiosonde profiles,  
390 the Tb is calculated from radiosonde temperature profiles through MonoRTM at each of the  
391 MWR channels. The mean difference between these calculated radiosonde Tbs and measured  
392 MWR Tbs forms the Tb bias with which the MWR Tb data can be corrected. This bias-correction  
393 method will be referred to as 'radiosonde BC'.

394 While this radiosonde BC method can be employed for the XPIA dataset, for other  
395 campaigns this approach would not be possible if co-located radiosonde observations were not

396 available. For this situation, an alternative method for correcting the MWR Tb biases is  
397 presented. There are often spectral features in the observed minus computed brightness  
398 temperature residuals that could not be explained by any physically realistic atmospheric  
399 profiles, and can only result because of a calibration error in the observations. This alternative  
400 bias-correction method is aimed purely to remove this unphysical spectral signature. In this  
401 method, to choose clear-sky periods, the 30 GHz channel MWR Tb data are used on a daily  
402 basis. The standard deviation of the MWR Tb is calculated as the average of standard deviations  
403 in a one-hour sliding window through all data points of a day. Four clear-sky days were  
404 identified using a threshold of 0.4 K on the standard deviation: March 10 and 30, and April 13  
405 and 29, 2015. The Tb bias is then computed for each of the 22 channels as the averaged  
406 difference between the observed Tb from the MWR zenith observations and the forward model  
407 calculated Tbs at zenith using the TROPoe-retrieved profiles ( $Y_1$ ) of those selected clear-sky  
408 days. This method identified spectral calibration errors in the MWR observations that could not  
409 be explained by physically realistic atmospheric profiles. This bias-correction technique, which  
410 accounts for those unphysical spectral calibration features, will be referred to as 'TROPoe BC'.

411 Fig. 1 shows the Tb biases found for all 22 MWR channels from both bias-correction  
412 approaches. The biases calculated with the radiosonde BC scheme are shown for all channels  
413 used in our analysis: 22 channels of the zenith scan, in red, and four V-band opaque channels of  
414 the oblique scans, in blue. The black and green triangles represent the biases calculated using  
415 the TROPoe BC approach for zenith and for zenith+oblique scans, respectively. All biases are  
416 presented with associated uncertainties (error bars representing the standard deviation over all

417 radiosondes for radiosonde BC, and mean observation Tb vector uncertainties for chosen four  
 418 clear-sky days for TROPoe BC).



419 *Fig. 1. Tb biases derived from the radiosonde BC method (and TROPoe BC method) in all*  
 420 *22 MWR channels of the zenith scan in red (and in black), and in the four opaque channels of*  
 421 *the oblique scans in blue (and in green).*

422

423 The biases from the two bias-correction schemes are within the uncertainties of each  
 424 other for most of the channels except at the higher frequencies in the V-band. Biases in the  
 425 most opaque channels are significantly affected by the accuracy of the boundary layer  
 426 temperature profiles. When TROPoe BC is used, a monthly average prior temperature profile is  
 427 used in the PR, and thus differences between this prior profile and the actual temperature

428 profile can result in a spectral bias in the more opaque MWR channels. On the contrary, the  
429 radiosonde BC uses a direct measurement of the temperature profile (from the radiosonde),  
430 and thus is more accurate. It is also important to note that, in both approaches, the biases in  
431 the opaque channels for zenith and for oblique scans (for radiosonde BC these are red and blue,  
432 respectively; and for the TROPoe BC these are black and green, respectively) are very similar to  
433 each other. This supports the assumption that the true bias is nearly independent of the scene,  
434 or that the sensitivity to the scene (e.g., zenith or off-zenith) is small.

435 The bias-correction methods were applied by removing the corresponding calculated  
436 biases from the MWR Tb observations before the retrievals were performed. Later in Section 4,  
437 differences in the retrieved temperature profiles will be shown when using the two bias-  
438 correction approaches. These differences will be more evident in the temperature profiles  
439 exhibiting near-ground temperature inversions.

440 However, the final goal of this study is not to assess the sensitivity to different bias-  
441 correction approaches but to verify that the inclusion of RASS observations does improve  
442 retrieved temperature profiles, independently of the bias-correction method used.

443

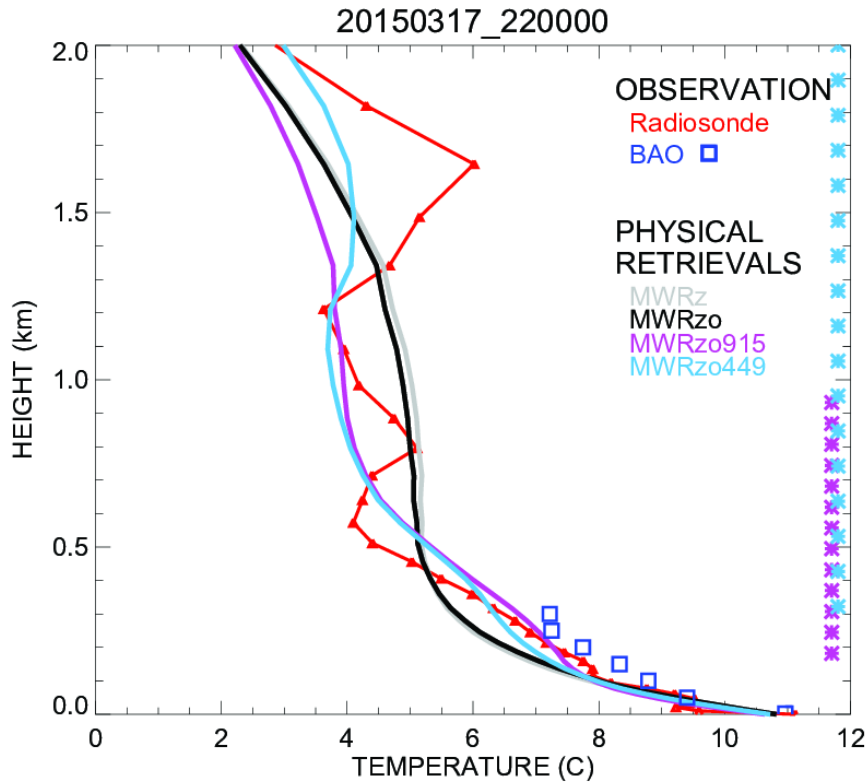
### 444 **3.3 Analysis of physical retrieval characteristics**

445 The retrieved profiles of the four different PR configurations presented in Table 1  
446 (MWRz, MWRzo, MWRzo915, MWRzo449) were compared to the radiosonde profiles. To  
447 compare radiosonde observations against the PR profiles, all radiosonde profiles were  
448 interpolated vertically to the same PR heights, and PR profiles were averaged in the time  
449 window between 15 minutes before and 15 minutes after each radiosonde launch. Since the

450 radiosonde ascends quite quickly in the lowest kilometers of the atmosphere (~15-20 min to  
451 reach 5 km), the 30-minute temporal window is estimated to be representative of the same  
452 volume of the atmosphere measured by the radiosonde. BAO tower temperature and mixing  
453 ratio data at the seven available levels were used as an additional validation dataset, without  
454 any vertical interpolation, averaged in the time window between 15 minutes before and 15  
455 minutes after each radiosonde launch.

456         As an example of the different temperature retrievals and their relative performance,  
457 data obtained on 17 March 2015 at 2200 UTC are presented in Fig. 2. Temperature profiles up  
458 to 2 km AGL retrieved from the four PR configurations (MWRz, MWRzo, MWRzo915,  
459 MWRzo449, using the radiosonde BC) are compared to the radiosonde data in red and to the  
460 BAO measurements in blue squares. Note that all four of the PRs match the BAO observations  
461 reasonably well near the ground. The MWRz and MWRzo profiles are very smooth and depart  
462 quite substantially from the radiosonde measurements, being unable to reproduce the more  
463 detailed structure of the atmospheric temperature profile measured by the radiosonde, while  
464 the MWRzo449 profile (in light-blue) demonstrates a better agreement with both the  
465 radiosonde and BAO measurements (blue squares). The MWRzo915 profile (in purple) also tries  
466 to follow the elevated temperature inversion observed by the radiosonde, successfully only in  
467 the lower part of the atmosphere (below 1 km AGL) where RASS 915 measurements are  
468 available. This behavior will be also addressed in the following section and in the statistical  
469 analysis presented later in the manuscript.

470



471

472 *Fig. 2. Temperature profiles obtained by the four PR configurations, after applying the*  
 473 *radiosonde BC on the MWR Tbs: MWRz in gray, MWRzo in black, MWRzo915 in purple, and*  
 474 *MWRzo449 in light-blue. These retrievals are compared to radiosonde measurements, in red,*  
 475 *and BAO tower observations, in blue squares. The heights with available RASS virtual*  
 476 *temperature measurements (RASS 915 in purple and RASS 449 in light-blue) are marked by the*  
 477 *asterisks on the right Y-axis.*

478

479 An asset of TROPoe is that several characteristics of the PRs can be obtained from two  
 480 matrices, the averaging kernel, **Akernel**, and the posterior covariance matrix, **Sop** (Masiello et  
 481 al., 2012; Turner and Löhnert, 2014, Turner and Bloomberg, 2019), calculated as:

482



483 
$$\mathbf{Akernel} = \mathbf{B}^{-1} \mathbf{K}^T \mathbf{S}_\varepsilon^{-1} \mathbf{K} \quad (2)$$

484 and:

485 
$$\mathbf{Sop} = \mathbf{B}^{-1} \quad (3)$$

486 where:

487 
$$\mathbf{B} = \mathbf{S}_a^{-1} + \mathbf{K}^T \mathbf{S}_\varepsilon^{-1} \mathbf{K}$$

488

489 All matrices, **Akernel**, **Sop**, and **B**, have dimensions 111 x 111 in our configuration. While  
 490 the top left corner of the **Akernel** matrix (1:55, 1:55) is devoted to temperature, called further  
 491 in the text **ATkernel**, the next (56:110, 56:110) elements are devoted to the water vapor mixing  
 492 ratio, called **AQkernel**.

493 The **Akernel** provides useful information about the calculated retrievals, such as vertical  
 494 resolution and degrees of freedom for signal at each level. The rows of the **Akernel** provide the  
 495 smoothing functions (Rodgers, 2000) that could be applied to the radiosonde profiles (Eq. 4) to  
 496 minimize the vertical representativeness error in the comparison between the various retrievals  
 497 and the radiosonde profiles due to very different vertical resolutions of these profiles (Turner  
 498 and Löhnert, 2014).

499 Smoothed radiosonde observed profiles can be computed using the averaging kernel,  
 500 as:

501 
$$\mathbf{X}_{smoothed\_radiosonde} = \mathbf{Akernel} (\mathbf{X}_{radiosonde} - \mathbf{X}_a) + \mathbf{X}_a \quad (4)$$

502 The **Akernel** in Eq. (2) depends on the retrieval parameters (e.g., which datasets are  
 503 used in the **Y** vector, the values assumed in the observation covariance matrix **S<sub>ε</sub>**, and the

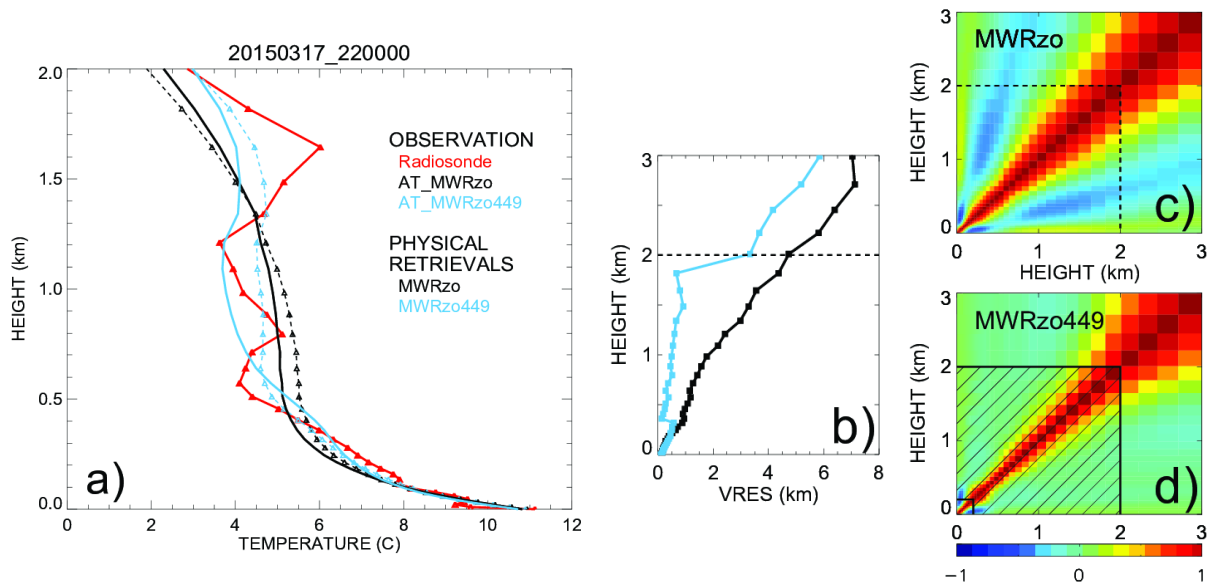
504 sensitivity of the forward model), so for our four PR configurations it is possible to calculate  
505 four different kernels from Eq. (2).

506 For each of the four **Akernels**, a smoothed radiosonde profile can be computed for each  
507 radiosonde profile using Eq. (4). In the presence of temperature inversions or other particular  
508 structures in the atmosphere, these smoothed profiles can be quite different from each other  
509 and also from the original unsmoothed radiosonde profile. Consequently, while comparison of  
510 the retrievals to the relative **Akernel**-smoothed radiosonde profiles can be used to minimize the  
511 vertical representativeness effects due to the different vertical resolutions of these profiles, we  
512 note that a statistical comparison between the four configurations of the observational vector  
513 would not be fair if each of their retrieved profiles is compared to a different **Akernel**-smoothed  
514 radiosonde profile. Therefore, in the statistical analysis presented later in the manuscript  
515 (section 4.2), mean bias, root mean square error (RMSE), and Pearson correlation coefficients  
516 will be computed between the various TROPoe retrieval configurations and the unsmoothed  
517 radiosonde profiles, just interpolated to the same vertical levels of the retrieved profiles.

518 The **ATkernel** can help understand the differences in the retrieved temperature profiles  
519 obtained by the configurations using additional RASS data, shown in the example of Fig. 2.  
520 Figure 3a includes the temperature profiles of the radiosonde (unsmoothed and **ATkernel**'s  
521 smoothed) and PRs of MWRzo and MWRzo449 for the same example as in Fig. 2. Due to the  
522 inclusion of RASS measurements, the **ATkernel**-smoothed radiosonde profile of the MWRzo449  
523 configuration (dashed light-blue line) is closer to the original radiosonde data (in red) compared  
524 to the black dashed profile of the MWRzo's **ATkernel**-smoothed radiosonde profile.  
525 Additionally, the rows of the **ATkernel** provide a measure of the retrieval smoothing as a

526 function of altitude, so the full-width half maximum (FWHM) of each **ATkernel** row estimates  
 527 the vertical resolution of the retrieved solution at each vertical level (Maddy and Barnet, 2008;  
 528 Merrelli and Turner, 2012). Plots of this vertical resolution as a function of the height for the  
 529 MWRzo PR and for the MWRzo449 PR are included in Fig. 3b. This plot shows that the  
 530 additional observations from the RASS 449 significantly improve the vertical resolution of the  
 531 retrievals.

532 The posterior covariance matrix, **Sop**, provides a measure of the uncertainty of the  
 533 retrievals while the square root of the diagonal of this matrix is used to specify the 1- $\sigma$  errors in  
 534 the profiles of temperature or mixing ratio. Also, **Sop** shows the level-to-level dependency of  
 535 the retrievals, and in an ideal case should have all non-diagonal elements equal to zero.  
 536 Converted to a correlation matrix, it is possible to visualize these dependencies, as presented in  
 537 Fig. 3c, d. The use of additional RASS data (MWRzo449 **Sop**, Fig. 3d) reduces the off-diagonal  
 538 covariances, therefore substantially decreasing the correlations in those areas compared to the  
 539 MWRzo **Sop** (Fig. 3c).



540

541 *Fig. 3. a) observed temperature profiles from radiosonde, in red, from **AT** kernels smoothed*  
542 *radiosonde, **AT\_MWRzo** in dashed black, and **AT\_MWRzo449** in dashed light-blue; PRs from*  
543 *MWRzo PR in solid black, and from MWRzo449 PR in solid light-blue. b) vertical resolution*  
544 *(VRES) as a function of the height for the MWRzo PR (black), and for the MWRzo449 PR (light-*  
545 *blue). c) and d) 3 x 3 km (37 x 37 levels) **Sop** matrices, converted to correlation matrices, for the*  
546 *MWRzo PR (c), and for the MWRzo449 PR (d). Dashed lines on plots b)-d) mark 2 km AGL.*  
547 *Hatched area on panel d marks the RASS measurement heights.*

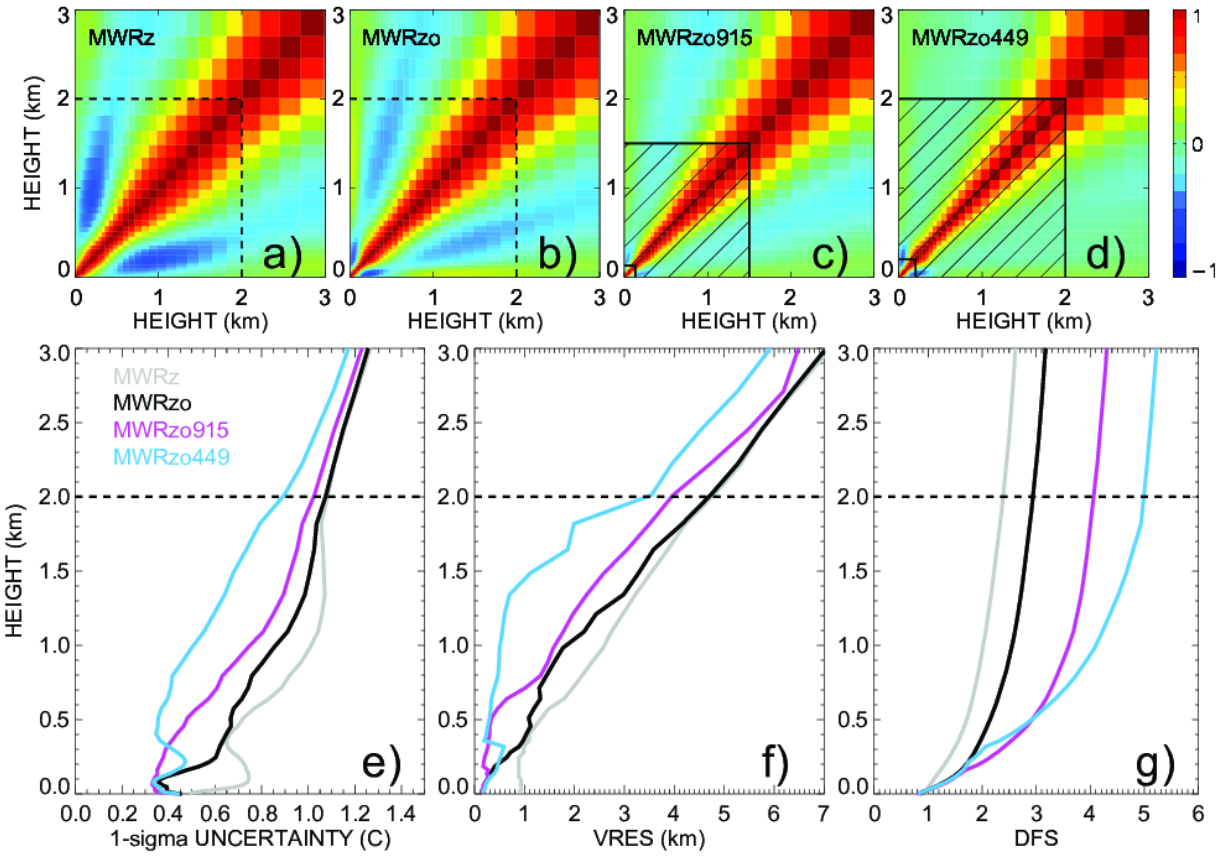
548

549       To understand the level-to-level correlations among the 4 different retrieval  
550 configurations in Table 1, the **Sop** matrices were averaged over all radiosonde events, and  
551 converted to correlation matrices (Fig. 4). A clearly visible narrowing of the spread around the  
552 main diagonal and correlation reduction in the off-diagonal elements result by adding  
553 additional observations, from MWR zenith only (Fig. 4a), to MWR zenith-oblique (Fig. 4b), to  
554 the larger impact obtained by the usage of the RASS 915 (Fig. 4c), concluding with the RASS 449  
555 (Fig. 4d) data. The mean retrieval uncertainty profile for each of the PR configurations is  
556 presented in Fig. 4e. The uncertainty of the MWRzo449 retrieval up to 1 km AGL is around 0.5  
557 °C while the other retrievals have higher uncertainties of up to 1 °C. The higher accuracy of the  
558 MWRzo449 retrievals is because that configuration has more observational information  
559 compared to the other retrieval configurations.

560       Other statistically important features to analyze in the PRs, besides their uncertainty,  
561 are the vertical resolution already introduced in the example of Fig. 3b, and the degree of  
562 freedom for signal (DFS). These two features, derived from the **A** kernels of each PR

563 configuration, averaged over all radiosonde events, are shown in Fig 4f and 4g. The vertical  
564 resolution (Fig. 4f) shows the width of the atmosphere layer used for each retrieval height,  
565 computed as the full-width half-maximum value of the averaging kernel. The cumulative DFS  
566 profile (Fig. 4g) is a measure of the number of independent pieces of information in the  
567 observations below the specified height. For example, at the 1 km AGL level the vertical  
568 resolution of MWRzo449 is 0.5 km (i.e. information is from +/- 0.5 km around the retrieval  
569 height is considered in the retrieval), while all other retrievals use the information from more  
570 than +/- 1.5 km. Also, the DFS, as a cumulative measure, shows an increase in pieces of  
571 information from MWRz to MWRzo for the whole profile and from MWRzo to MWRzo915 and  
572 to MWRzo449 above ~0.2 km where RASS data are available. The DFS of MWRzo915 is higher  
573 compared to the DFS of MWRzo449 in the 0.2-0.5 km AGL layer because RASS 915 data have  
574 denser measurements there. It is also important to note that there is no additional information  
575 added to any of the retrievals above 2km AGL, i.e. the slope of the cumulative DFS profiles are  
576 equal. Despite that, the statistical analysis of the PRs up to 3 km AGL, shown in Section 4, will  
577 prove that the retrieval improvements obtained by including the RASS are found even above  
578 the height of the RASS measurements availability.

579



580

581 Fig. 4. Top row: The mean **Sops**, displayed as correlation matrices, for (a) MWRz, (b) MWRzo, (c)  
 582 MWRzo915, and (d) MWRzo449, averaged over all radiosonde events. Hatched area on panels  
 583 c) and d) marks the RASS maximum measurement heights. Bottom panels: (e) one-sigma  
 584 uncertainty derived from the posterior covariance matrix in °C, (f) vertical resolution (VRES) in  
 585 km, and (g) cumulative Degree of Freedom (DFS) as a function of height for temperature,  
 586 averaged over all radiosonde events (MWRz is in gray, MWRzo is in black, MWRzo915 is in  
 587 purple, and MWRzo449 is in light-blue). Dashed lines mark 2 km AGL on all panels.

588

589 The improvements from MWRz (in gray) to MWRzo (in black), to MWRzo915 (in purple),  
 590 and finally to MWRzo449 (in light-blue) are visible in all three panels (Fig 4e-g), whereas

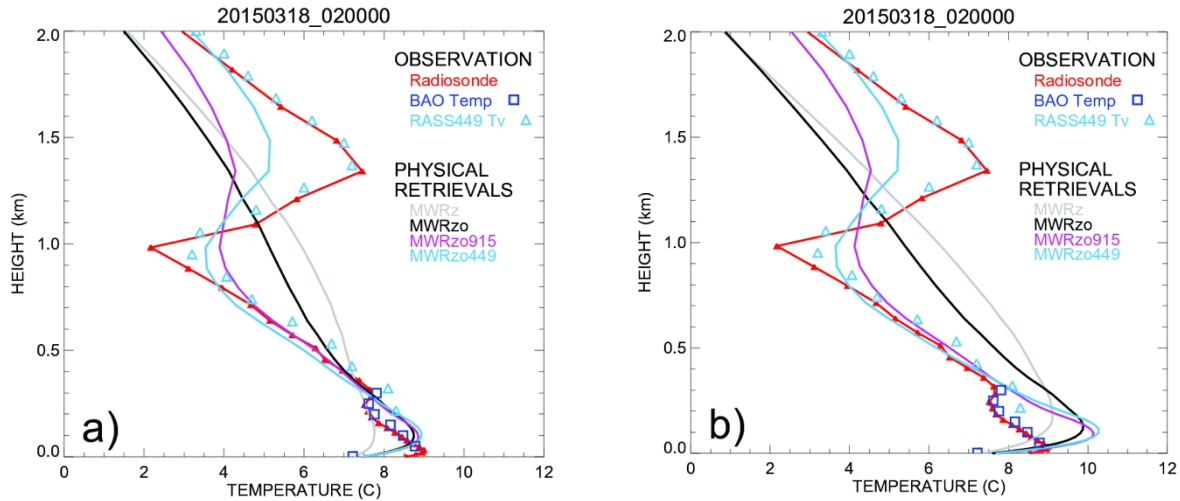
591 MWRzo449 has the lowest  $1-\sigma$  uncertainty and highest DFS compared to the other PRs,  
592 particularly below 2 km AGL, where RASS 449 measurements are available. Finally, it is  
593 interesting that below 200 m AGL the MWRzo915 has slightly smaller lowest  $1-\sigma$  uncertainty  
594 and vertical resolution relative to the MWRzo449, as could be expected due to the first  
595 available height of the RASS 915 being lower (120 m AGL) than the first available height for the  
596 RASS 449 (217 m AGL) and due to the finer vertical resolution of the 915-MHz RASS. This  
597 suggests that if additional observations were available in the lowest several 100 m of the  
598 atmosphere where RASS measurements are not available, improvements might be even better  
599 closer to the surface, where temperature inversions, if present, are sometimes difficult to  
600 retrieve correctly.

601

## 602 **4. Results**

### 603 **4.1 Statistical analysis of physical retrievals up to 3km AGL**

604 Several cases were found during XPIA when the temperature profile exhibited  
605 inversions, with the lowest happening in the surface layer. Figure 5 shows one of the most  
606 complex cases, with several temperature inversions visible in the temperature profile from the  
607 radiosonde (red line), in the temperature measurements from the BAO tower (blue squares),  
608 and in the virtual temperature measured by the RASS 449 (light blue triangles). Note that the  
609 virtual temperature profile is in close agreement with the temperature measured by  
610 radiosonde.



611

612 *Fig. 5. As in Fig. 2 but for 18 March 2015 at 0200 UTC. The RASS 449 virtual temperature is*  
 613 *included as light blue triangles. a) shows the PRs obtained after applying the radiosonde BC, and*  
 614 *b) shows the PRs obtained after applying the TROPoe BC on the MWR Tbs.*

615

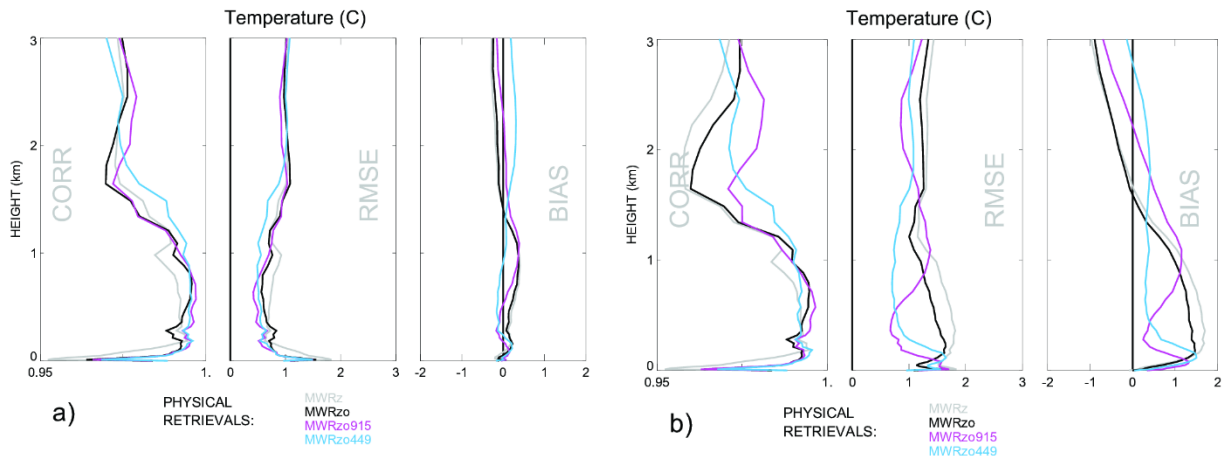
616 Figure 5 also illustrates the difference in the temperature profiles, especially between 0-  
 617 300m AGL, for the two different bias-correction schemes, which show noticeable differences in  
 618 the biases of the opaque channels (especially important for the near-ground retrievals)  
 619 presented in Fig. 1. As expected, the radiosonde BC method yielded a retrieved profile closer to  
 620 the radiosonde temperature profile than when using TROPoe BC, for which the inversion in the  
 621 temperature profile close to the surface is too accentuated (particularly the black, purple, and  
 622 cyan lines, all of which used oblique scan data).

623

624 The relative statistical behavior (Pearson correlation, RMSE, and bias) of the PRs for  
 625 both temperature and mixing ratio against radiosondes is shown in Figure 6, using both bias-  
 correction approaches. PRs obtained after applying the radiosonde BC (Fig. 6a) present overall



626 smaller RMSE and bias (the latter almost equal to zero up to 3 km AGL) and slightly higher  
 627 correlations compared to the statistics of the PRs obtained after applying the TROPoe BC (Fig.  
 628 6b). This could be expected since for the comparison in Fig. 6a a subset of the radiosondes was  
 629 already used for the Tb bias correction. Also, the different retrievals show a narrower  
 630 distribution for the panels in Fig. 6a. Nevertheless, the results obtained when applying either  
 631 bias-correction methods (in Fig. 6a, b) consistently show the improvement obtained when the  
 632 RASS observations are used, with relatively smaller bias and RMSE in the 3 km layer AGL. The  
 633 correlation is mainly improved above 1 km, when RASS observations are included.

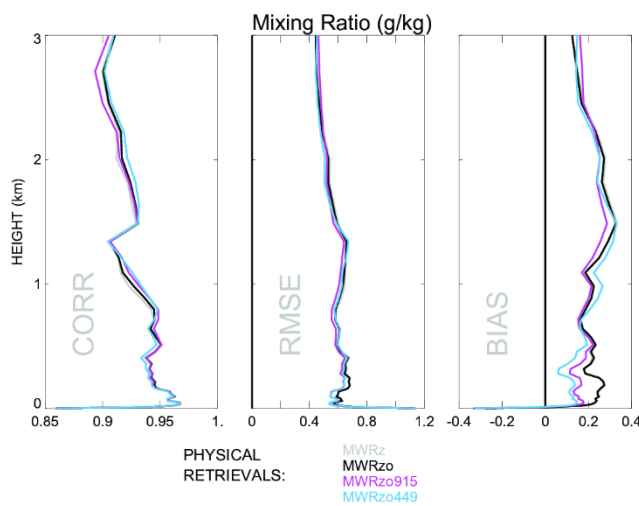


634 *Fig. 6. Pearson correlation, RMSE, and mean bias for temperature profiles of MWRz in gray,*  
 635 *MWRzo in black, MWRzo915 in purple, and MWRzo449 in light-blue for the radiosonde BC bias-*  
 636 *correction method in a) and TROPoe BC method in b).*

637

638 Besides temperature profiles, the PRs also provide water vapor mixing ratio profiles. It is  
 639 understandable that the different configurations of PRs are not noticeably different from each  
 640 other in relation to moisture, because the Tv observations from the RASS are dominated by the  
 641 ambient temperature (not moisture), and thus have little impact on the water vapor retrievals.

642 We found that the **AQKernels** are almost identical for all four PR configurations (not shown).  
 643 Detailed statistical evaluation of the PRs mixing ratio profiles are presented in Fig. 7, also  
 644 averaged over all radiosonde events, and show very similar correlations, RMSEs, and biases for  
 645 all PRs, implying that the impact of including RASS observations in the retrieval is minimal on  
 646 this variable. Finally, it is noted that Fig. 7 shows the mixing ratio of the data from TROPoe BC.  
 647 The radiosonde BC mixing ratio results are almost identical.

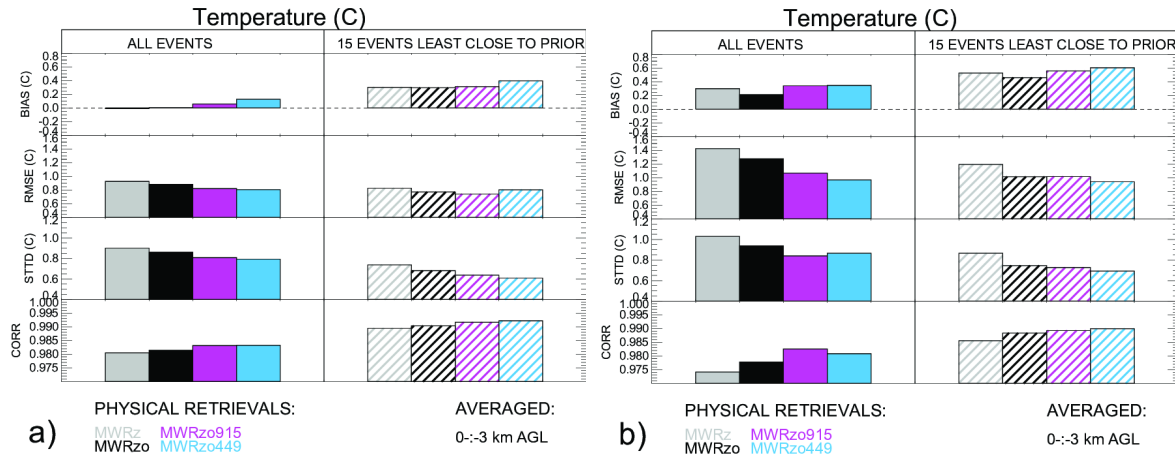


649  
 650  
 651  
 652  
 653  
 654  
 655 *Fig. 7. Same as the panels in Fig. 6b, but for mixing ratio, when using the TROPoe BC method on*  
 656 *the MWR Tbs.*

657  
 658 **4.2 Statistics for the profiles least close to the climatology**

659 Physical retrievals use climatological data as a constraint in the retrieval. Statistically,  
 660 the averaged profiles of both temperature and moisture variables are very close to the  
 661 climatological averages. However, the most interesting and difficult profiles to retrieve are the  
 662 cases furthest from climatology (Löhnert and Maier, 2012). To check the behavior of the  
 663 retrieved data in such “extreme” cases, the RMSE was first calculated for each radiosonde

664 profile relative to the prior profiles for 37 vertical levels from the surface up to 3 km AGL, and  
 665 then the 15 cases with the largest 0-3 km layer averaged RMSEs compared to the prior were  
 666 selected.



667 *Fig. 8. From top to bottom: biases (retrievals minus radiosonde), RMSEs, standard deviations of*  
 668 *the difference between retrievals and radiosonde, and Pearson correlations for the four PR*  
 669 *configurations, averaged from the surface to 3 km AGL, and over all radiosonde data (solid*  
 670 *boxes), and over the 15 extreme cases (hatched boxes). The data in panels a) use radiosonde BC,*  
 671 *and in b) TROPoe BC on the MWR Tbs.*

672 Figure 8 shows the temperature statistical analysis for the entire radiosonde data set  
 673 (solid boxes) and for the fifteen events far from the climatological mean (hatched boxes) for  
 674 bias, RMSE, standard deviation of the differences between retrievals and radiosonde data, and  
 675 Pearson correlation, calculated as the weighted averaged over the 37 vertical heights up to 3  
 676 km AGL<sup>1</sup>.

<sup>1</sup> The vertical grid used in the PRs is not uniform, with more frequent levels closer to the surface. If a simple average of the data from all levels is used, the near-surface layer will be weighted more compared to the upper levels of the retrievals. To avoid this, a vertical average over the lowest 3 km AGL is performed using weights at each vertical level determined by the distance between the levels.

677 Differences in the statistics when using the entire radiosonde data set or the fifteen  
678 extreme profiles are noticeable for all statistical estimators. The PRs that include RASS  
679 observations show better performance compared to the strictly MWR-only PR profiles (i.e.,  
680 MWRz and MWRzo) for almost all statistical comparisons. This improvement is larger for the  
681 PRs using the TROPoe BC (Fig. 8b) compared to the PRs using the radiosonde BC (Fig. 8a). Three  
682 statistical estimators, RMSE, standard deviation, and Pearson correlation show overall better  
683 values for the 15 extreme cases compared to the whole radiosonde dataset, for all PR  
684 configurations and both BC approaches. This is due to the fact that for this dataset the monthly  
685 averaged radiosonde profiles (for March and May particularly) depart quite substantially from  
686 the monthly prior profiles. For example, the averaged radiosonde profile in March is warmer by  
687  $\sim 7$  °C compared to the March prior (and in May by  $\sim 5$  °C) in the first 3 km AGL. Consequently,  
688 the extreme cases (mostly found in March) have the warmest radiosonde temperature profiles,  
689 but are overall closer to the monthly averaged radiosonde profiles.

690 Table 2 includes the same data as in Figure 8 but as a percentage of the improvement,  
691 compared to the MWRz retrievals.

692

693

694

695

696

697

0-3 km AGL	ALL EVENTS					15 EVENTS LEAST CLOSE TO THE PRIOR			
RADIOSONDE BIAS-CORRECTION									
	MWRz	MWRzo	MWRzo RASS915	MWRzo RASS449		MWRz	MWRzo	MWRzo RASS915	MWRzo RASS449
RMSE	0%	5%	11%	13%		0%	7%	10%	3%
STTD	0%	4%	10%	12%		0%	8%	14%	17%
CORR	0%	0.1%	0.3%	0.3%		0%	0.1%	0.2%	0.3%
TROPoe BIAS-CORRECTION									
RMSE	0%	10%	25%	32%		0%	15%	15%	21%
STTD	0%	9%	18%	16%		0%	14%	16%	20%
CORR	0%	0.4%	0.9%	0.7%		0%	0.3%	0.4%	0.4%

698

699 *Table 2. Retrieval improvements for different RASS/MWR configurations as a percentage*

700 *compared to MWRz.*

701

702 The results presented in Table 2 show improvements in all statistical estimations when  
703 including RASS observations, with improvements in RMSE between 10 and 20 %, demonstrating  
704 the positive impact derived by the inclusion of the active measurements, regardless of the bias-  
705 correction method used, but larger for the TROPoe BC data because there is more room for  
706 improvement when this BC method is used. Improvements in the Pearson correlation

707 coefficients are small because correlation, determined during XPIA by the overall temperature  
708 structure with height and diurnal cycle, is already good, leaving little room for improvement.

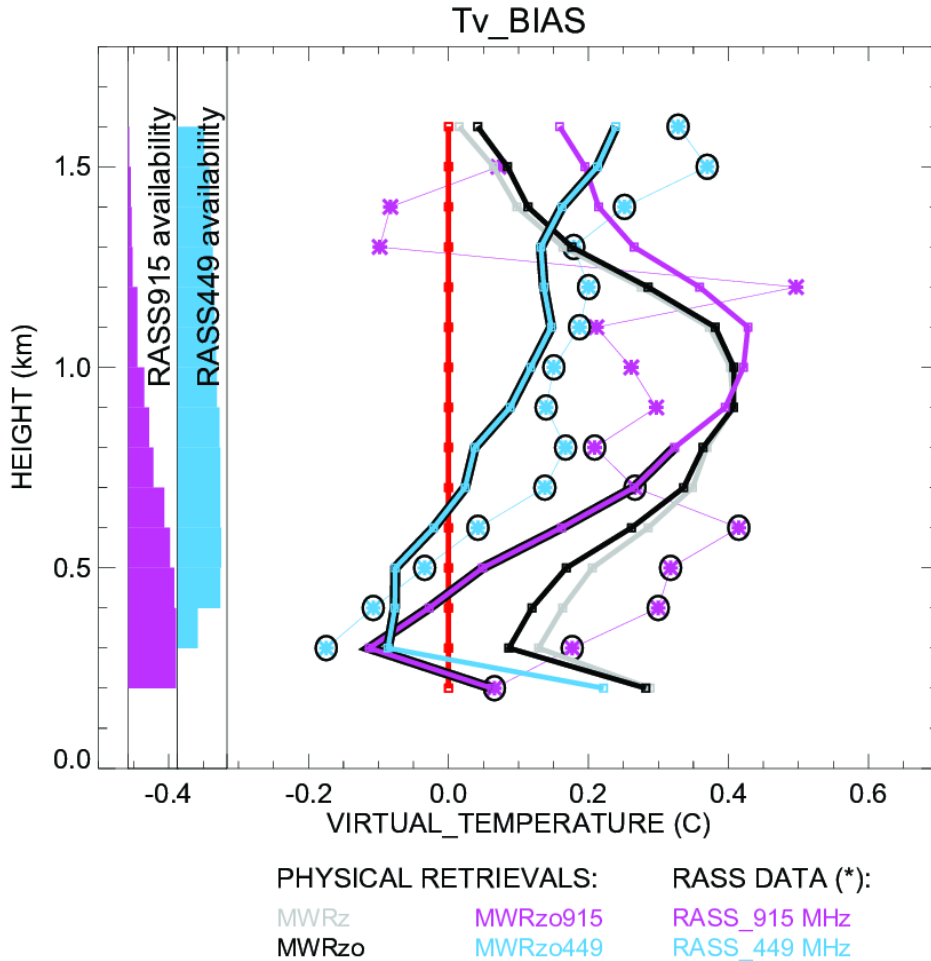
709

### 710 **4.3 Virtual temperature profile statistics**

711 Using the physical retrieval outputs, “retrieved virtual temperature profiles” can also be  
712 calculated. In this section the direct comparison of these retrieved virtual temperature profiles  
713 and RASS virtual temperature profiles to the original radiosonde is shown. With this comparison  
714 we want to show how the biases of the retrieved profiles relate to the original RASS Tv biases.

715 Figure 9 shows Tv retrieved profile biases compared to the original radiosonde data.

716 These Tv profiles and RASS 915 and RASS 449 Tv bias data are interpolated onto a regular  
717 vertical grid, going from 200 m to 1.6 km with a 100 m resolution, for easy comparison.



718

719 *Fig. 9. Bias of virtual temperature for all PR configurations compared to the original radiosonde*  
 720 *measurements. A zero bias is denoted by the red line. RASS data biases are marked by asterisks*  
 721 *and by additional circles for the RASS data with more than 50% availability, according to the*  
 722 *availability bar charts on the left.*

723 *All PRs profiles are derived after applying the radiosonde BC method.*

724

725 While RASS 449 data are available at almost all heights up to 1.6 km, the RASS 915 data  
 726 availability decreases considerably with height, lowering to 50% availability around 800 m AGL.

727 The PRs that include RASS data, MWRzo915 and MWRzo449, are also marked with additional  
728 black lines at the heights with at least 50% of relative RASS data availability. In agreement with  
729 Fig. 6a, this figure clearly shows the superiority of the MWRzo449 and MWRzo915 (in the layer  
730 with > 50% RASS data availability) compared to the MWRz and MWRzo configurations, which  
731 do not include RASS data. For MWRzo449, RASS 449 data were almost always available,  
732 therefore it is easy to identify a similarity between the Tv bias profiles of the RASS 449 and the  
733 PRs including it. Thus, for the MWRzo449 the Tv bias is more uniform through the heights  
734 compared to all other PRs that do not include RASS data. Moreover, it is noted a roughly  
735 constant offset between the MWRzo449 Tv and RASS 449 Tv biases profiles, with their  
736 averaged difference equal to  $\sim 0.08$  °C (when the radiosonde BC is used), and to  $\sim 0.32$  °C (when  
737 the TROPoe BC is used, not shown), over the  $\sim 1.3$  km (0.3-1.6 km) atmospheric layer where  
738 more than 50% of the RASS 449 measurements are available, uniformly distributed through the  
739 heights. The inclusion of the RASS into the PRs does reduce the values of the biases in the  
740 retrievals even below the values of the RASS biases, because of the combined information from  
741 RASS and MWR.

742

## 743 **5. Conclusions**

744 In this study, data collected during the XPIA field campaign were used to test different  
745 configurations of a physical-iterative retrieval (PR) approach in the determination of  
746 temperature and humidity profiles from data collected by microwave radiometers, surface  
747 sensors, and RASS measurements. The accuracy of several PR configurations was tested: two  
748 configurations made use only of surface observations and MWR observed brightness



749 temperature (zenith only, MWRz; and zenith plus oblique, MWRzo); while two others included  
750 the active virtual temperature profile observations available from co-located RASS (one, RASS  
751 915, associated with a 915-MHz; and the other, RASS 449, associated with a 449-MHz wind  
752 profiling radar). Radiosonde launches were used for verification of the retrieved profiles. In  
753 Appendix A, the performance of MWRz and MWRzo retrieved profiles and Neural Network  
754 retrieved profiles against the radiosondes was evaluated.

755         To remove any observational systematic error in the MWR Tb observations, two bias-  
756 correction procedures were tested. The first one takes advantage of the many radiosondes  
757 launched during XPIA, and the second one uses climatological profiles. As expected, the  
758 radiosonde bias-correction method gives retrieved profiles closer to the radiosonde  
759 temperature profiles than when using the climatological based method. Nevertheless, our  
760 results show that regardless of the bias-correction method used, the inclusion of the  
761 observations from the active RASS instruments in the PR approach improves the accuracy of the  
762 temperature profiles by around 10-20% compared to the PR configuration using only surface  
763 observations and MWR observed brightness temperature from the zenith scan. Of the PRs  
764 configurations tested, generally better statistical agreement is found with the radiosonde  
765 observations when the RASS 449 is used together with the surface observations and brightness  
766 temperature from the zenith and averaged oblique MWR observations.

767         The **AKernel** and the posterior covariance matrices for temperature are used to derive  
768 the one-sigma uncertainty, vertical resolution, and cumulative degree of freedom as a function  
769 of height for the different PRs, and the level-to-level correlated uncertainty of the retrievals.  
770 Results show that the inclusion of the active instruments improves all of the above-mentioned

771 variables in the 0-3km layer, including at heights between 2-3km that are above the maximum  
772 RASS height. Thus, the positive impact of the RASS observations extends into the atmosphere  
773 above the height of measurements themselves.

774 Furthermore, 15 cases when temperature profiles from the radiosonde observations  
775 were the furthest away from the mean climatological average were selected, and the statistical  
776 comparison was reproduced over this subset of cases. These are the cases usually the most  
777 difficult to retrieve and the most important to forecast; therefore, it is essential to improve the  
778 retrievals in these situations. Even for this subset of selected cases the inclusion of active  
779 sensor observations in the PRs is found to be beneficial.

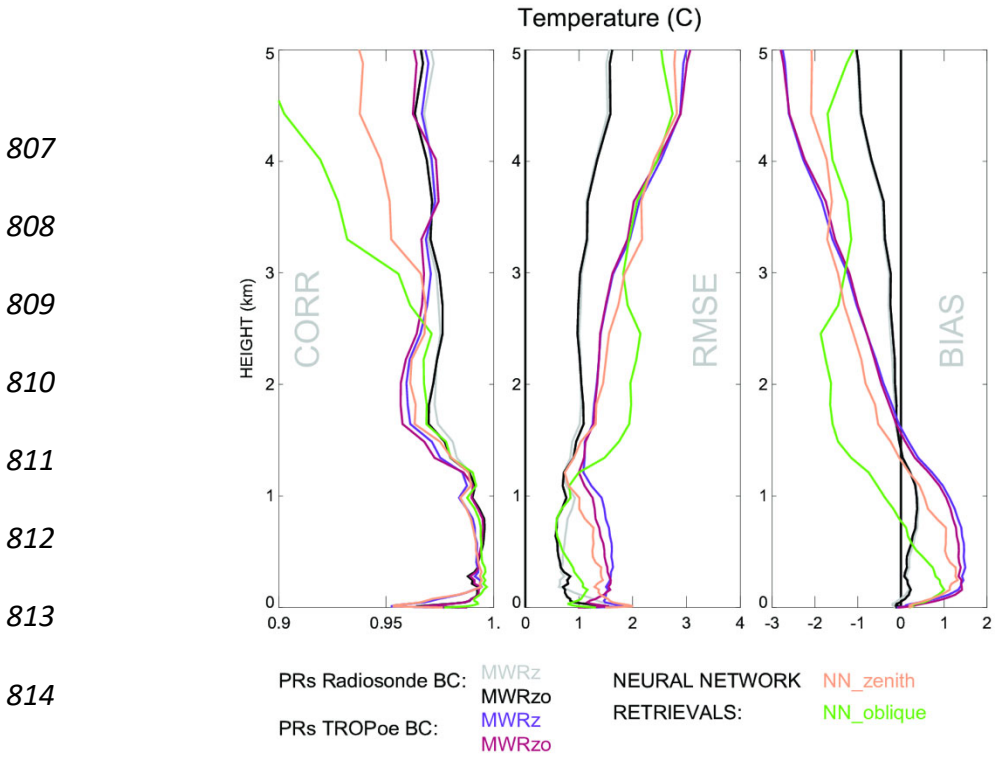
780 Finally, the impact of the inclusion of RASS measurements on the retrieved humidity  
781 profiles was considered, but the inclusion of RASS observations did not produce significantly  
782 better results, compared to the configurations that do not include them. This was not a surprise  
783 as RASS measures virtual temperature, effectively adding very little extra information to the  
784 water vapor retrieval. In this case a better option would be to consider adding other active  
785 remote sensors such as water vapor differential absorption lidars (DIALs) to the PRs. Turner and  
786 Löhnert (2021) showed that including the partial profile of water vapor observed by the DIAL  
787 substantially increases the information content in the combined water vapor retrievals.  
788 Consequently, to improve both temperature and humidity retrievals a synergy between MWR,  
789 RASS, and DIAL systems would likely be necessary.

790

791 **Appendix A**

792           The neural network (NN) retrievals developed by the vendor explicitly for XPIA use a  
793 training dataset based on a 5-year climatology of profiles from radiosondes launched at the  
794 Denver International Airport, 35 miles south-east from the XPIA site. NN-based MWR vertical  
795 retrieval profiles were obtained using the zenith or an average of two oblique elevation scans,  
796 15- and 165-degrees (not including the zenith), all with 58 levels extending from the surface up  
797 to 10 km, with nominal vertical grid depending on the height (every 50 m from the surface to  
798 500 m, every 100 m from 500 m to 2 km, and every 250 m from 2 to 10 km, AGL).

799           Fig. 1A shows composite NN vertical profiles of temperature (separately for the zenith  
800 and averaged obliques) calculated for radiosonde launch times, and the corresponding PR  
801 profiles already introduced in Fig. 6a, b. For a proper comparison, only MWRz and MWRzo  
802 profiles are used, without including RASS measurements. It has to be noted that since the “NN  
803 oblique” retrieval provided by the manufacturer of the radiometer does not include the zenith,  
804 this configuration cannot be considered exactly equivalent to the MWRzo PR.



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816 *Fig. 1A. Pearson correlation, RMSE, and mean bias for temperature profiles for MWRz in grey*  
 817 *(and purple) and MWRzo in black (and maroon) when the radiosonde BC (and the TROPoe BC)*  
 818 *method is applied. Included in this figure are the NN temperature profiles, from the zenith scan*  
 819 *(in beige), and from the averaged oblique scans (in green).*

820

821 Another difference to point out is that, while the MWR Tb data have been bias-  
 822 corrected before being used in the PR configurations, as discussed in Section 3.2, the NN  
 823 retrievals use the uncorrected Tb, since it was non-trivial to reprocess those retrievals. Martinet  
 824 et al. (2015) showed that when it is possible to bias-correct the MWR Tb before applying the  
 825 NN retrieval technique, the NN retrievals are not impacted below 1 km AGL, but a clear  
 826 improvement of NN retrievals in terms of RMSE and bias are observed between 1 and 3 km

827 altitude. As is visible in Fig. 1A, this is the layer of the atmosphere where the NN profiles (beige  
828 and green lines) have larger bias and RMSE, compared to the PR profiles.

829         When the radiosonde BC method is used, the MWRz and MWRzo PRs (gray and black  
830 lines) present better statistics through the entire profiles shown in Fig. 1A, with larger values of  
831 the correlation coefficient, and smaller values of RMSE and bias. The oblique only NN profiles  
832 (in green) show comparable statistics to the PRs employing the radiosonde BC method up to 1  
833 km AGL, with degraded performances above this height. Above 1 km AGL, the zenith NN  
834 profiles (in beige) do better than the oblique NN in terms of RMSE and bias. When the TROPoe  
835 BC method is used, the MWRz and MWRzo PRs (purple and maroon lines) perform better than  
836 the NN profiles only in terms of RMSE and bias, and only between 1.5 and 3 km AGL.

837         The better performance obtained by the MWRz and MWRzo PRs that use the  
838 radiosonde BC approach demonstrate the importance of having an accurate and reliable  
839 method for bias correcting the MWR.

840

#### 841 **Data availability**

842         All data are publicly accessible at the DOE Atmosphere to Electrons Data Archive and  
843 Portal, found at <https://a2e.energy.gov/projects/xpia> (Lundquist et al., 2016).

844

#### 845 **Author contribution**

846         Irina Djalalova completed the primary analysis using the XPIA dataset. Daniel Gottas  
847 contributed to the post-processing of the RASS data. Dave Turner modified the TROPoe

848 algorithm to include the RASS data as input. All authors contributed to the analysis of the  
849 results. Irina Djalalova prepared the manuscript with contributions from all co-authors.

850

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858

### 859 **Competing interests**

860 The authors declare no competing interests.

861

### 862 **References**

863 Adachi, A. and H. Hashiguchi: Application of parametric speakers to radio acoustic sounding  
864 system. **ATMOS MEAS TECH**, **12**, 5699–5715, [https://doi.org/10.5194/amt-12-5699-](https://doi.org/10.5194/amt-12-5699-2019)  
865 [2019](https://doi.org/10.5194/amt-12-5699-2019), 2019.

866 Adler, B., J. M. Wilczak, L. Bianco, I. Djalalova, J. B. Duncan Jr., D. D. Turner: Observational case  
867 study of a persistent cold air pool and gap flow in the Columbia River Basin. **J APPL**  
868 **METEOROL CLIM**, **60**, 1071-1090, <https://doi.org/10.1175/JAMC-D-21-0013.1>, 2021.

869 Banta, R. M., and coauthors: Characterizing NWP model errors using Doppler lidar  
870 measurements of recurrent regional diurnal flows: Marine-air intrusions into the  
871 Columbia River Basin. **MON WEATHER REV**, **148**, 927-953,  
872 <https://doi.org/10.1175/MWR-D-19-0188.1>, 2020.

873 Bianco L., D. Cimini, F. S. Marzano, and R. Ware: Combining microwave radiometer and wind  
874 profiler radar measurements for high-resolution atmospheric humidity profiling, **J**  
875 **ATMOS OCEAN TECH**, **22**, 949–965, <https://doi.org/10.1175/JTECH1771.1>, 2005.

876 Bianco, L., K. Friedrich, J. M. Wilczak, D. Hazen, D. Wolfe, R. Delgado, S. Oncley, and J. K.  
877 Lundquist: Assessing the accuracy of microwave radiometers and radio acoustic  
878 sounding systems for wind energy applications. **ATMOS MEAS TECH**, **10**, 1707-1721,  
879 <https://doi.org/10.5194/amt-10-1707-2017>, 2017.

880 Cadeddu, M. P., J. C. Liljegren, and D. D. Turner: The Atmospheric radiation measurement  
881 (ARM) program network of microwave radiometers: instrumentation, data, and  
882 retrievals, **ATMOS MEAS TECH**, **6**, 2359–2372, [https://doi.org/10.5194/amt-6-2359-](https://doi.org/10.5194/amt-6-2359-2013)  
883 [2013](https://doi.org/10.5194/amt-6-2359-2013), 2013.

884 Cimini, D., T. J. Hewison, L. Martin, J. Guldner, C. Gaffard, F. S. Marzano: Temperature and  
885 humidity profile retrievals from ground-based microwave radiometers during TUC,  
886 **METEOROL Z**, Vol. 15, No. 5, 45-56, [DOI: 10.1127/09411-D-2948/2006/0099](https://doi.org/10.1127/09411-D-2948/2006/0099), 2006.

887 Cimini, D., E. Campos, R. Ware, S. Albers, G. Giuliani, J. Oreamuno, P. Joe, S. E. Koch, S. Cober,  
888 and E. Westwater: Thermodynamic Atmospheric Profiling during the 2010 Winter  
889 Olympics Using Ground-based Microwave Radiometry, **IEEE T GEOSCI REMOTE**, **49**, 12,  
890 <https://doi.org/10.1109/TGRS.2011.2154337>, 2011.

891 Cimini, D., Rosenkranz, P. W., Tretyakov, M. Y., Koshelev, M. A., and Romano, F.: Uncertainty of  
892 atmospheric microwave absorption model: impact on ground-based radiometer  
893 simulations and retrievals, **ATMOS CHEM PHYS**, **18**, 15231–15259,  
894 <https://acp.copernicus.org/articles/18/15231/2018>, 2018.

895 Cimini, D., M. Haeffelin, S. Kotthaus, U. Löhnert, P. Martinet, E. O'Connor, C. Walden, M.  
896 Collaud Coen, and J. Preissler: Towards the profiling of the atmospheric boundary layer  
897 at European scale—introducing the COST Action PROBE. **Bulletin of Atmospheric**  
898 **Science and Technology**, **1**, 23–42, <https://doi.org/10.1007/s42865-020-00003-8>, 2020.

899 Clough, S.A., M. W. Shephard, E. J. Mlawer, J. S. Delamere, M. Iacono, K. E. Cady-Pereira, S.  
900 Boukabara and P. D. Brown: Atmospheric radiative transfer modeling: A summary of the  
901 AER codes, **J QUANT SPECTROSC RA**, vol 91, no. 2, pp 233-244,  
902 <https://doi.org/10.1016/j.jqsrt.2004.05.058>, 2005.

903 Crewell, S., U. Löhnert: Accuracy of Boundary Layer Temperature Profiles Retrieved With  
904 Multifrequency Multiangle Microwave Radiometry, **IEEE T GEOSCI REMOTE**, VOL. 45,  
905 NO. 7, JULY 2007, [DOI: 10.1109/TGRS.2006.888434](https://doi.org/10.1109/TGRS.2006.888434), 2007.

906 Engelbart, D., W. Monna, J. Nash: Integrated Ground-Based Remote-Sensing Stations for  
907 Atmospheric Profiling, **COST Action 720 Final Report**, EUR 24172,  
908 <https://doi.org/10.2831/10752>, 2009.

909 Görzdorf, U., and V. Lehmann: Enhanced Accuracy of RASS-Measured Temperatures Due to an  
910 Improved Range Correction. **J ATMOS OCEAN TECH**, **17 (4)**, 406–416,  
911 [https://doi.org/10.1175/1520-0426\(2000\)017<0406:EAORMT>2.0.CO;2](https://doi.org/10.1175/1520-0426(2000)017<0406:EAORMT>2.0.CO;2), 2000.



912 Han, Y., and E. R. Westwater: Remote sensing of tropospheric water vapor and cloud liquid  
913 water by integrated ground-based sensors. **J ATMOS OCEAN TECH**, **12**, 1050-1059, DOI:  
914 [https://doi.org/10.1175/1520-0426\(1995\)012<1050:RSOTWV>2.0.CO;2](https://doi.org/10.1175/1520-0426(1995)012<1050:RSOTWV>2.0.CO;2), 1995.

915 Hewison, T.: 1D-VAR Retrieval of Temperature and Humidity Profiles From a Ground-Based  
916 Microwave Radiometer, **IEEE T GEOSCI REMOTE**, **45(7)**, 2163–2168,  
917 <https://doi.org/10.1109/TGRS.2007.898091>, 2007.

918 Horst, T. W., S. R. Semmer, and I. Bogoev: Evaluation of Mechanically-Aspirated  
919 Temperature/Relative Humidity Radiation Shields, 18th Symposium on Meteorological  
920 Observation and Instrumentation, AMS Annual Meeting, New Orleans, LA, 10-15  
921 January 2016, <https://ams.confex.com/ams/96Annual/webprogram/Paper286839.html>,  
922 2016.

923 Kaimal, J. C., and J. E. Gaynor: The Boulder Atmospheric Observatory. **J CLIM APPL METEOROL**,  
924 **22**, 863–880, [https://doi.org/10.1175/1520-0450\(1983\)022<0863:TBAO>2.0.CO;2](https://doi.org/10.1175/1520-0450(1983)022<0863:TBAO>2.0.CO;2), 1983.

925 Küchler, N., D. D. Turner, U. Löhnert, and S. Crewell: Calibrating ground-based microwave  
926 radiometers: Uncertainty and drifts, **RADIO SCI**, **51**, 311–327,  
927 [doi:10.1002/2015RS005826](https://doi.org/10.1002/2015RS005826), 2016.

928 Löhnert U. and O. Maier: Operational profiling of temperature using ground-based microwave  
929 radiometry at Payerne: prospects and challenges. **ATMOS MEAS TECH**, **5**, 1121–1134,  
930 <https://doi.org/10.5194/amt-5-1121-2012>, 2012.

931 Lundquist, J. K., J. M. Wilczak, R. Ashton, L. Bianco, W. A. Brewer, A. Choukulkar, A. Clifton, M.  
932 Debnath, R. Delgado, K. Friedrich, S. Gunter, A. Hamidi, G. V. Iungo, A. Kaushik, B.  
933 Kosović, P. Langan, A. Lass, E. Lavin, J. C.-Y. Lee, K. L. McCaffrey, R. K. Newsom, D. C.

934 Noone, S. P. Oncley, P. T. Quelet, S. P. Sandberg, J. L. Schroeder, W. J. Shaw, L. Sparling,  
935 C. St. Martin, A. St. Pe, E. Strobach, K. Tay, B. J. Vanderwende, A. Weickmann, D. Wolfe,  
936 and R. Worsnop: Assessing state-of-the-art capabilities for probing the atmospheric  
937 boundary layer: the XPIA field campaign. **B AM METEOROL SOC**, **98**, 289–314,  
938 <https://doi.org/10.1175/BAMS-D-15-00151.1>, 2017.

939 Maahn, M., D. D. Turner, U. Löhnert, D. J. Posselt, K. Ebell, G. G. Mace, and J. M. Comstock:  
940 Optimal estimation retrievals and their uncertainties: What every atmospheric scientist  
941 should know. **B AM METEOROL SOC**, **101**, E1512-E1523, [https://doi.org/10.1175/BAMS-](https://doi.org/10.1175/BAMS-D-19-0027.1)  
942 [D-19-0027.1](https://doi.org/10.1175/BAMS-D-19-0027.1), 2020.

943 Maddy, E. S. and C. D. Barnett: Vertical Resolution Estimates in Version 5 of AIRS Operational  
944 Retrievals. **IEEE T GEOSCI REMOTE**, VOL. **46**, NO. 8, AUGUST 2008,  
945 <https://doi.org/10.1109/TGRS.2008.917498>, 2008.

946 Martinet, P., A. Dabas, J.-M. Donier, T. Douffet, O. Garrouste, and R. Guillot: 1D-Var  
947 temperature retrievals from microwave radiometer and convective scale model, **TELLUS**  
948 **A**, **67:1**, <https://doi.org/10.3402/tellusa.v67.27925>, 2015.

949 Martinet, P., D. Cimini, F. Burnet, B. Ménétrier, Y. Michel, and V. Unger: Improvement of  
950 numerical weather prediction model analysis during fog conditions through the  
951 assimilation of ground-based microwave radiometer observations: a 1D-Var study,  
952 **ATMOS MEAS TECH**, **13**, 6593–6611, <https://doi.org/10.5194/amt-13-6593-2020>, 2020.

953 May, P. T. and J. M. Wilczak: Diurnal and Seasonal Variations of Boundary-Layer Structure  
954 Observed with a Radar Wind Profiler and RASS. **MON WEATHER REV**, **121**, 673–682,  
955 [https://doi.org/10.1175/1520-0493\(1993\)121<0673:DASVOB>2.0.CO;2](https://doi.org/10.1175/1520-0493(1993)121<0673:DASVOB>2.0.CO;2), 1993.

956 Masiello, G., C. Serio, and P. Antonelli: Inversion for atmospheric thermodynamical parameters  
957 of IASI data in the principal components space. **Q J ROY METEOR SOC**, **138**, 103–117,  
958 <https://doi.org/10.1002/qj.909>, 2012.

959 Merrelli, A. M., and D. D. Turner: Comparing information content of upwelling far infrared and  
960 midinfrared radiance spectra for clear atmosphere profiling. **J ATMOS OCEAN TECH**, **29**,  
961 510–526, <https://doi.org/10.1175/JTECH-D-11-00113.1>, 2012.

962 Neiman, P. J., D. J. Gottas, and A. B. White: A Two-Cool-Season Wind Profiler–Based Analysis of  
963 Westward-Directed Gap Flow through the Columbia River Gorge. **MON WEATHER REV**,  
964 **147**, 4653–4680, <https://doi.org/10.1175/MWR-D-19-0026.1>, 2019.

965 North, E. M., A. M. Peterson, and H. D. Parry: RASS, a remote sensing system for measuring low-  
966 level temperature profiles. **B AM METEOROL SOC**, **54**, 912–919, 1973.

967 Payne, V. H., J. S. Delamere, K. E. Cady-Pereira, R. R. Gamache, J.-L. Moncet, E. J. Mlawer, and S.  
968 A. Clough: Air-broadened half-widths of the 22- and 183-GHz water-vapor lines. **IEEE T**  
969 **GEOSCI REMOTE**, **46**, 3601–3617, <https://doi.org/10.1109/TGRS.2008.2002435>, 2008.

970 Payne, V. H., E. J. Mlawer, K. E. Cady-Pereira, and J.-L. Moncet: Water vapor continuum  
971 absorption in the microwave. **IEEE T GEOSCI REMOTE**, **49**, 2194–2208,  
972 <https://doi.org/10.1109/TGRS.2010.2091416>, 2011.

973 Rodgers, C. D.: Inverse Methods for Atmospheric Sounding: Theory and Practice. Series on  
974 Atmospheric, Oceanic and Planetary Physics, Vol. 2, World Scientific, 238 pp, 2000.

975 Rosenkranz, P. W.: Water vapour microwave continuum absorption: A comparison of  
976 measurements and models. **RADIO SCI**, **33**, 919–928,  
977 <https://doi.org/10.1029/98RS01182>, 1998.

978 Shaw, W., and Coauthors: The Second Wind Forecast Improvement Project (WFIP 2): General  
979 Overview. **B AM METEOROL SOC**, **100(9)**, 1687–1699, [https://doi.org/10.1175/BAMS-D-](https://doi.org/10.1175/BAMS-D-18-0036.1)  
980 [18-0036.1](https://doi.org/10.1175/BAMS-D-18-0036.1), 2019.

981 Solheim, F., J. R. Godwin, J., and R. Ware: Passive ground-based remote sensing of atmospheric  
982 temperature, water vapor, and cloud liquid profiles by a frequency synthesized  
983 microwave radiometer. **METEOROL Z**, **7**, 370–376, 1998a.

984 Solheim F., J. R. Godwin, E. R. Westwater, Y. Han, S. J. Keihm, K. Marsh, R. Ware: Radiometric  
985 profiling of temperature, water vapor and cloud liquid water using various inversion  
986 methods. **RADIO SCI**, **33**, 393–404, <https://doi.org/10.1029/97RS03656>, 1998b.

987 Stankov, B. B., E. R. Westwater, and E. E. Gossard: Use of wind profiler estimates of significant  
988 moisture gradients to improve humidity profile retrieval. **J ATMOS OCEAN TECH**, **13**,  
989 1285-1290, DOI:  
990 [https://doi.org/10.1175/15200426\(1996\)013<1285:UOWPEO>2.0.CO;2](https://doi.org/10.1175/15200426(1996)013<1285:UOWPEO>2.0.CO;2), 1996.

991 Strauch, R. G., D. A. Merritt, K. P. Moran, K. B. Earnshaw, and D. V. De Kamp: The Colorado  
992 wind-profiling network. **J ATMOS OCEAN TECH**, **1**, 37–49, [https://doi.org/10.1175/1520-](https://doi.org/10.1175/1520-0426(1984)001<0037:tcwpn>2.0.co;2)  
993 [0426\(1984\)001<0037:tcwpn>2.0.co;2](https://doi.org/10.1175/1520-0426(1984)001<0037:tcwpn>2.0.co;2), 1984.

994 Turner, D. D.: Improved ground-based liquid water path retrievals using a combined infrared  
995 and microwave approach. **J GEOPHYS RES-ATMOS**, **112**, D15204,  
996 <https://doi.org/10.1029/2007JD008530>, 2007.

997 Turner, D. D., and U. Löhnert: Information content and uncertainties in thermodynamic profiles  
998 and liquid cloud properties retrieved from the ground-based Atmospheric Emitted

999 Radiance Interferometer (AERI). **J APPL METEOROL CLIM**, **53**, 752–771,  
1000 <https://doi.org/10.1175/JAMC-D-13-0126.1>, 2014.

1001 Turner, D. D., and W. G. Blumberg: Improvements to the AERIoe thermodynamic profile  
1002 retrieval algorithm. **IEEE J-STARS**, **12(5)**, 1339–1354,  
1003 <https://doi.org/10.1109/JSTARS.2018.2874968>, 2019.

1004 Turner, D. D., and U. Löhnert: Ground-based Temperature and Humidity Profiling: Combining  
1005 Active and Passive Remote Sensors. **ATMOS MEAS TECH**, **14**, 3033–3048,  
1006 <https://doi.org/10.5194/amt-2020-352>, 2021.

1007 Ware R., Solheim F., Carpenter R., and Coauthors: A multi-channel radiometric profiler of  
1008 temperature, humidity and cloud liquid. **RADIO SCI**, **38**, No. 4, 8079,  
1009 <https://doi.org/10.1029/2002RS002856>, 2003.

1010 Weber, B. L., D. B. Wuertz, D. C. Welsh, and R. Mcpeek: Quality controls for profiler  
1011 measurements of winds and RASS temperatures. **J ATMOS OCEAN TECH**, **10**, 452–464,  
1012 [https://doi.org/10.1175/1520-0426\(1993\)010<0452:gcfpmo>2.0.co;2](https://doi.org/10.1175/1520-0426(1993)010<0452:gcfpmo>2.0.co;2), 1993.

1013 Wilczak, J. M., and Coauthors: The Second Wind Forecast Improvement Project (WFIP2):  
1014 Observational Field Campaign. **B AM METEOROL SOC**, **100(9)**, 1701–1723,  
1015 <https://doi.org/10.1175/BAMS-D-18-0035.1>, 2019.

1016 Wolfe, D. E. and R. J. Latatits: Boulder Atmospheric Observatory: 1977–2016: The end of an era  
1017 and lessons learned. **B AM METEOROL SOC**, **99**, 1345–1358,  
1018 <https://doi.org/10.1175/BAMS-D-17-0054.1>, 2018.

1019