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2 **A Statistically Optimal Analysis of Systematic Differences between Aeolus**

3 **HLOS Winds and NOAA's Global Forecast System**

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23 Key Points

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- There are speed-dependent systematic differences in the Aeolus M1-bias corrected Level-2B HLOS winds compared to short-term (6-h) FV3GFS forecasts.
 - The total least squares (TLS) regression provides a statistically optimal analysis of the differences.
 - A bias correction based on the TLS bias analysis proposed here is tested in a companion paper to optimize Aeolus wind assimilation and thus the impact of Aeolus winds on global NWP forecasts.

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34 **Abstract**

35 The European Space Agency Aeolus mission launched the first of its kind spaceborne Doppler
36 wind lidar in August 2018. To optimize assimilation of the Aeolus Level-2B (L2B) Horizontal
37 Line-of-Sight (HLOS) winds, systematic differences (referred as biases hereafter) between the
38 observations and numerical weather prediction (NWP) background winds should be removed.
39 Total least squares (TLS) regression is used to estimate speed-dependent biases between Aeolus
40 HLOS winds (L2B10) and the National Oceanic and Atmospheric Administration (NOAA)
41 Finite-Volume Cubed-Sphere Global Forecast System (FV3GFS) 6-h forecast winds. Unlike
42 ordinary least squares regression, TLS regression optimally accounts for random errors in both
43 predictors and predictands. Large well-defined, speed-dependent biases are found particularly in
44 the lower stratosphere and troposphere of the tropics and Southern Hemisphere. These large
45 biases should be corrected to increase the forecast impact of Aeolus data assimilated into global
46 NWP systems.

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48 **Key words:** Aeolus winds, Doppler wind lidar, total least squares, bias correction

49



50 1 Introduction

51 The space-borne Doppler wind lidar on board the European Space Agency (ESA) Aeolus
52 mission measures both Rayleigh (i.e., molecular) and Mie (i.e., clouds and aerosols) backscatter
53 to derive wind profiles along the sensor's Horizontal Line of Sight (HLOS) throughout the
54 troposphere and lower stratosphere [Straume-Lindner, 2018, Straume et al., 2020]. The Aeolus
55 HLOS Level-2B (L2B) winds have demonstrated positive impacts on global weather forecasts
56 [Rennie et al., 2021; Cress, 2020; Garrett et al., 2020, 2021].

57 To optimize the positive impact of Aeolus winds on weather forecasts, large systematic
58 differences (referred to as biases hereafter) between Aeolus winds and numerical weather
59 prediction (NWP) model background winds should be corrected [Daley, 1991]. Therefore, it is
60 important to identify potential biases between Aeolus winds and their NWP model background
61 counterparts [Liu et al., 2020, 2021]. The biases may come from both NWP models and Aeolus
62 winds. First, current operational global NWP models still have larger errors or uncertainty in
63 regions where conventional observations are sparse or absent, and these errors include bias
64 components as the NWP models evolve towards their own climatology in the absence of
65 observations. For example, the backgrounds from the ECMWF model
66 (<https://www.ecmwf.int/en/forecasts>) and the NOAA Finite-Volume Cubed-Sphere Global
67 Forecast System (FV3GFS) model (<https://www.gfdl.noaa.gov/fv3/>) show large systematic
68 differences in the zonal winds in the troposphere and lower stratosphere of the tropics, the
69 Southern Hemisphere (SH), and north of 70° N, with maxima on the order of 2.0, -0.5, and 0.5
70 m/s, respectively (see Figure 1).



71 Secondly, although corrections to several substantial bias sources in the Aeolus L2B
72 winds have been implemented, including corrections to the dark current signal anomalies of
73 single pixels (so-called hot pixels) on the Accumulation-Charge-Coupled Devices (ACCDs),
74 linear drift in the illumination of the Rayleigh/Mie spectrometers, and the telescope M1 mirror
75 temperature variations [Reitebuch et al., 2020; Weiler et al., 2021], uncorrected biases due to
76 potential calibration issues might remain in Aeolus L2B winds and may contribute to potential
77 biases between Aeolus and the NWP background winds. The residual biases may lead to sub-
78 optimal assimilation of Aeolus winds in NWP systems. In addition, the Aeolus L2B winds might
79 be biased towards the ECMWF model, as the M1 bias correction makes use of ECMWF 6-hour
80 forecasts [Rennie et al., 2021], which might also lead to sub-optimal assimilation of Aeolus
81 winds in other NWP systems.

82 Using ordinary least squares (OLS) to identify and estimate the speed-dependent biases in
83 the innovations of Aeolus minus NWP background winds (O-B) is subject to contamination from
84 random errors in Aeolus and/or NWP background winds [Frost and Thompson, 2000], since
85 OLS assumes no errors in the predictor or independent variable, which in this case would be
86 either the Aeolus winds, the NWP background winds, or a combination of the two. In contrast,
87 total least squares (TLS) regression takes account of errors in both dependent and independent
88 variables and generates a statistically optimal analysis of the biases [Deming, 1943; Ripley and
89 Thompson, 1987; Markovsky and Van Huffel, 2007]. For the case of Aeolus and NWP
90 background winds, the use of linear TLS regression [Ripley and Thompson, 1987] finds a best fit
91 line that is an estimate of the true (assumed linear) relationship between Aeolus and NWP
92 background winds.



93 In this study, the TLS regression approach is used to identify and estimate potential
94 biases between the Aeolus HLOS winds (L2B10) and the NOAA FV3GFS background winds.
95 The suboptimality of OLS bias estimates is demonstrated by comparison to the TLS bias
96 estimates. A bias correction based on the TLS bias analysis is proposed for the innovations of
97 Aeolus minus FV3GFS winds in order to optimize Aeolus wind assimilation with the FV3GFS
98 model and thus improve the impact of Aeolus winds on FV3GFS forecasts.

99 Section 0 describes the Aeolus L2B and FV3GFS background winds, the TLS bias
100 analysis method, and the estimation of the ratio of error variances of Aeolus winds to FV3GFS
101 background winds used in the TLS regression. Section 3 describes the variations of the TLS bias
102 estimates with height, latitude, and wind speed. Section 4 demonstrates the substantial
103 differences between the TLS and OLS bias estimates. Section 5 proposes a TLS bias correction
104 for the O-B innovations. Finally, Section 6 presents a summary of findings and conclusions.
105 Throughout this article, we will refer to the Aeolus and FV3GFS HLOS winds as the Aeolus and
106 FV3GFS winds, respectively. In discussions of winds that are not HLOS winds we will use terms
107 like u -wind, v -wind, or wind vector.

108 **2 Data and Methodology**

109 **2.1 Aeolus L2B and FV3GFS background wind data**

110 The Aeolus L2B clear-sky Rayleigh winds and cloudy-sky Mie winds are examined for
111 the period 1-7 September 2019. This one-week period provides a sufficient sample to estimate
112 the biases. The Aeolus winds were obtained from the Aeolus dataset (L2B10) re-processed by
113 ESA [Rennie et al., 2021, Weiler et al., 2021]. The reprocessing includes the M1 bias correction,



114 which removes most of the globally and vertically averaged biases of Rayleigh and Mie winds
115 [Weiler et al., 2021]. The Aeolus winds are reported at a standard set of vertical layers [de Kloe,
116 2019, 2020]. This study examines Aeolus Mie and Rayleigh winds within height ranges of 0-16
117 km and 3-22 km, respectively. These height ranges include almost all Aeolus wind observations.
118 The height is defined relative to the EGM96 geoid for the L2B winds [Tan et al. 2008].

119 Similar Aeolus data quality control procedures as recommended by ESA and ECMWF
120 [Rennie et al., 2021] were implemented to reject the following observations: HLOS L2B
121 confidence flag “invalid”; Rayleigh winds at layers below 850 hPa, L2B uncertainties greater
122 than 12 m/s, accumulation lengths less than 60 km, and atmospheric pressure within 20 hPa of
123 topographic surface pressure; Mie winds with L2B uncertainties greater than 5 m/s and
124 accumulation lengths less than 5 km.

125 The winds from Aeolus and collocated FV3GFS backgrounds are obtained from a data
126 assimilation experiment (hereafter the BASE experiment) where the Aeolus winds are monitored
127 and the Aeolus wind observation operator (H_i) is applied to the FV3GFS background (\mathbf{x}^b) to
128 obtain the value of FV3GFS background wind ($y_i^b = H_i(\mathbf{x}^b)$) corresponding to each Aeolus
129 observation (y_i^o). This experiment employs the FV3GFS data assimilation system, called Global
130 Statistical Interpolation [GSI, Kleist et al. 2009], configured for the 4DEnVar algorithm with 64
131 vertical levels, and horizontal resolutions of C384 (~25 km) for the deterministic analysis and
132 forecast and C192 (~50 km) for the 80 ensemble members [Wang and Lei, 2014].

133 When examining Aeolus wind statistics, we stratify the Aeolus data by orbital phase,
134 either ascending when the spacecraft is moving northward or descending when the spacecraft is
135 moving southward. The vertical and daily variations of global horizontal means and standard



136 deviations of the innovations of Mie winds minus FV3GFS background winds are consistent
137 throughout the period (Figs. 2 and 3). For Mie winds in ascending orbits, the biases are positive
138 above 6 km and negative below 6 km, as large as +1.8 m/s and -0.5 m/s, respectively. The biases
139 are smaller and positive at most levels in the descending orbits. The standard deviations are
140 smallest (about 4 m/s) from 2 to 8 km elevation and increase to only about 5 m/s at the highest
141 levels. For Rayleigh winds in descending orbits, the biases are as positive as +1.2 m/s above 10
142 km, and as negative as -1.2 m/s below 8 km. The positive biases in ascending orbits are smaller.
143 The standard deviations are smallest (again about 4 m/s) from 6 to 12 km elevation and increase
144 to about 7 m/s at the highest levels. The results indicate that the biases vary substantially with
145 height for both Mie and Rayleigh winds, the standard deviations vary from 4 m/s to somewhat
146 larger values at higher elevations, and that both mean and standard deviations remain stable in
147 time throughout the period.

148 The mean differences of Mie and Rayleigh winds minus FV3GFS winds vary
149 considerably with latitude (Figure 4). Mie winds have biases as large as +1.5 m/s in the upper
150 troposphere and Rayleigh winds have biases as large as +2.0 m/s in the tropical upper
151 troposphere. Both Mie and Rayleigh winds show negative biases as large as -1.0 m/s in the
152 lowest layers.

153 **2.2 TLS Linear Regression**

154 In this section, we review the TLS regression method [Ripley and Thompson, 1987] in
155 the context of estimating potential speed-dependent biases between Aeolus winds and FV3GFS
156 background winds. The TLS estimate for each collocated pair of Aeolus and FV3GFS winds (y_i^o ,
157 y_i^b) is defined by



158
$$y_i^o = \hat{y}_i^o + \varepsilon_i^o \quad \text{and} \quad y_i^b = \hat{y}_i^b + \varepsilon_i^b \quad (i=1, N) \quad (1)$$

159 where \hat{y}_i^o and \hat{y}_i^b are the TLS estimates of the true Aeolus and FV3GFS winds, and ε_i^o and ε_i^b
 160 are random errors, and N is the number of Aeolus/FV3GFS collocations in the sample. The
 161 sample might be defined by a vertical layer or a latitude band. In OLS regression, since it is
 162 assumed that there are no errors in the predictor, the predictor can be used directly to estimate the
 163 predictand. The situation is a little more complicated in TLS regression where $(\hat{y}_i^b, \hat{y}_i^o)$, the most
 164 probable true state, is the point on the regression line that is closest in a statistical sense to the
 165 point (y_i^b, y_i^o) .

166 Here we assume that ε_i^o and ε_i^b are independent and that the random error variance ratio
 167 $\delta = (\sigma^o / \sigma^b)^2 = E[\varepsilon_i^o \varepsilon_i^o] / E[\varepsilon_i^b \varepsilon_i^b]$ is known. Also, we assume the true relationship between the
 168 Aeolus and FV3GFS winds is described by a linear function:

169
$$\hat{y}_i^o = c_0 + c_1 \hat{y}_i^b \quad (i=1, N) \quad (2)$$

170 where c_0 is an offset or constant bias and c_1 is a speed-dependent bias coefficient.

171 The TLS regression finds an optimal estimate of the \hat{y}_i^b , c_0 and c_1 by minimizing the
 172 cost function

173
$$J = \sum_{i=1}^N \left((\varepsilon_i^o / \sigma^o)^2 + (\varepsilon_i^b / \sigma^b)^2 \right)$$

 174
$$= \frac{1}{(\sigma^o)^2} \sum_{i=1}^N \left((y_i^o - c_0 - c_1 \hat{y}_i^b)^2 + \delta (y_i^b - \hat{y}_i^b)^2 \right)$$

175 To determine the \hat{y}_i^b , set the derivative of J with respect to \hat{y}_i^b to zero, to obtain

176
$$\hat{y}_i^b = (c_1 (y_i^o - c_0) + \delta y_i^b) / (c_1^2 + \delta) \quad (i=1, N) \quad (3)$$



177 Eq. (3) thereby reduces the problem to a minimization in terms of c_0 and c_1 . A similar equation
178 holds even if the error variances vary with i , but then there is no closed form solution for c_0 and
179 c_1 , as there is in the current case, which is known as the Deming problem [Ripley and
180 Thompson, 1987]. When the coefficients c_0 and c_1 are obtained, the TLS estimate for the new or
181 within-sample observation is given by Eq. (3). Finally, the estimate of the bias for the k th
182 observation, either for a new or within-sample observation, is given by

$$183 \quad \hat{d}_k = \hat{y}_k^o - \hat{y}_k^b = c_0 + (c_1 - 1)\hat{y}_k^b \quad (4)$$

184 We will refer to c_0 and $(c_1 - 1)$ as the constant and speed-dependent bias coefficients,
185 respectively, hereafter.

186 Note that the error variance ratio δ is a crucial parameter in the TLS bias analysis. If
187 $\sigma^o = 0$ or $\sigma^b = 0$, then the TLS solution is equivalent to the OLS regression of the O-B on the
188 Aeolus winds or on the FV3GFS winds, respectively.

189 **2.3 Estimation of the random error variance ratio**

190 The random error variance ratio $\delta = (\sigma^o/\sigma^b)^2$ used in the TLS bias analysis is estimated
191 from the O-B innovations from the BASE experiment using the Hollingsworth-Lonnberg (HL)
192 method [Hollingsworth and Lonnberg, 1986]. It is assumed that there is no correlation between
193 the random errors in Aeolus and FV3GFS winds and no horizontal correlation in the random
194 errors in Aeolus winds at 90 km distance and beyond. For more details, see Hollingsworth and
195 Lonnberg [1986] and Garrett et al. [2021].

196 The random error variance ratio δ is estimated at the middle height of each vertical range
197 bin using the Aeolus samples for 1-7 September 2019, separately for Mie and Rayleigh winds.



198 Figure 5 shows that the vertical profiles of the square root of δ varies in the range of 1.2-1.6 and
199 2-3 for Mie winds versus FV3GFS winds and Rayleigh winds versus FV3GFS winds,
200 respectively.

201 **3 The TLS Bias Estimates**

202 The statistical relationship between Aeolus and FV3GFS winds is illustrated by the
203 density plots of collocated Aeolus and FV3GFS winds in a single layer shown in Figure 6. There
204 is a strong correlation of 0.93 between Mie and FV3GFS winds, and of 0.94 between Rayleigh
205 and FV3GFS winds. The TLS analyses of the FV3GFS winds versus Aeolus winds indicate that
206 the innovations (Aeolus minus FV3GFS winds) are positive and increase with wind speed. In
207 terms of Eq. (4), for Figure 6a, the innovation solution is $0.53 \text{ m/s} + 0.06$ times the background
208 solution, while for Figure 6b, the innovation solution is $1.04 \text{ m/s} + 0.04$ times the background
209 solution.

210 **3.1 Variation of Biases with Height**

211 The variation of the TLS solution with height and orbital phase is described here. The
212 TLS samples are over all latitudes. The vertical distribution of the TLS constant and speed-
213 dependent bias analysis coefficients for the innovation in terms of the background in Eq. (4) is
214 shown in Figure 7. The speed-dependent bias coefficient ($c_1 - 1$) varies substantially with height
215 and orbital phase. For Mie winds, the coefficient is quite large at most heights, ranging from 3 to
216 6%, with maxima at 3 km and 12-16 km. The coefficient for Rayleigh winds is smaller and
217 ranges from 1 to 3% in ascending orbits and 1 to 5% in descending orbits, with maxima around
218 the 3.5 and 16 km.



219 The constant bias coefficient c_0 for both Mie and Rayleigh winds also shows large
220 variations on height and orbit with its value as large as +/- 1.0 m/s. In general, the constant bias
221 coefficient is positive in upper layers and negative in layers close to the Earth surface, consistent
222 with the patterns seen in the global horizontal average of innovations in Figures 2 and 3.

223 The vertical distribution of the average TLS bias estimates as function of Aeolus wind is
224 shown in Figure 8. The average TLS biases vary substantially with height. Since the TLS biases
225 are in part dependent on speed, at most heights the biases increase substantially as the magnitude
226 of Aeolus wind speed increases. The biases at high Aeolus wind speeds are considerably larger
227 for Mie winds than for Rayleigh winds, as large as +2.5 m/s and -2.0 m/s for Mie winds, and
228 +1.5 m/s and -2.0 m/s for Rayleigh winds. There are clear speed-dependent biases in the vertical
229 average of these biases (Figure 9). The results suggest that both vertically varying and vertically
230 averaged speed-dependent biases remain in the Aeolus winds (L2B10).

231 **3.2 Variation of Biases with Latitude**

232 The variation of the TLS solution with latitude and orbital phase is described here. The
233 TLS samples are over all heights for 10-degree latitude bands. In general, the coefficients
234 obtained are large and vary considerably with latitude and orbital phase, with maxima found in
235 the tropics (Figure 10). For example, the speed-dependent bias coefficient ($c_1 - 1$) for Mie
236 winds in the tropics can be quite large, ranging from 0% to a maximum of 11%. The coefficient
237 ($c_1 - 1$) is smaller for Rayleigh winds, ranging from -1% to 5%, with maxima found in the
238 tropics and at northern high latitudes. The constant bias coefficient c_0 for Mie winds also varies
239 considerably with latitude and orbit, ranging from -1.0 m/s to +1.6 m/s. The coefficient c_0 is
240 smaller for Rayleigh winds.



241 The latitudinal distribution of the average TLS bias as a function of Aeolus wind is
242 shown in Figure 11. For Mie winds, the average TLS bias increases considerably at most
243 latitudes as the magnitude of Aeolus wind speed increases, particularly in the tropics and SH,
244 with maxima of about ± 2.5 m/s. For Rayleigh winds, the average biases are much smaller and
245 are consistent with the fact that the M1 bias correction removes most globally and vertically
246 averaged biases of Rayleigh winds [Weiler et al., 2021].

247 **3.3 Discussion**

248 The results presented in this section indicate that the speed-dependent bias coefficient is
249 quite large, with $(c_1 - 1)$ reaching up to $\sim 10\%$ and 5% for Mie and Rayleigh winds,
250 respectively, particularly in the lower stratosphere and lower troposphere of the tropics. This
251 suggests that there exist large speed-dependent biases in FV3GFS background winds and/or in
252 the Aeolus winds. Given that there exist large uncertainties in the FV3GFS (and ECMWF)
253 background winds in the tropics (see Figure 1), it is likely that the FV3GFS may be a significant
254 source of the large biases and this will require further investigation. In any case, these large
255 speed-dependent biases should be corrected to optimize Aeolus wind assimilation and the impact
256 of Aeolus winds on NWP forecasts.

257 **4 Comparison to OLS Regressions**

258 As a comparison to the TLS bias estimate results, we conducted parallel OLS regressions
259 using three different predictors of the biases in O-B. These predictors are the FV3GFS winds, the
260 Aeolus winds, and their average. The first two of these OLS regressions are equivalent to OLS
261 regressing Aeolus on FV3GFS winds and OLS regressing FV3GFS on Aeolus winds. As



262 examples, the regression lines of these two cases are added to Figure 6. The TLS speed-
263 dependent coefficient ($c_1 - 1$) (in Eq. 4) = 6% and 4% for Mie and Rayleigh winds,
264 respectively. However, the OLS regression of Aeolus winds on FV3GFS winds produces
265 considerably smaller bias estimates, with ($c_1 - 1$) estimated as 1% and 2% for Mie and
266 Rayleigh winds, respectively; thus, this OLS regression considerably underestimates the biases.

267 On the other hand, the OLS regression of the FV3GFS winds on Aeolus winds exhibits
268 much larger bias estimates relative to the TLS bias analysis, with ($c_1 - 1$) estimated as 18% and
269 15% for Mie and Rayleigh winds, respectively. This indicates that the speed-dependent biases
270 are considerably overestimated by the OLS regression on Aeolus winds.

271 The vertical distributions of the average biases as a function of Aeolus winds are shown
272 in Figure 12 for the descending orbits for three methods: The top panels are for OLS regression
273 using FV3GFS winds as a predictor, the middle panels, which repeat the bottom two panels of
274 Figure 8 are for TLS regression, and the bottom panels are for OLS regression using the average
275 of FV3GFS and Aeolus as a predictor (bottom). The average bias estimates in the top panels are
276 about 0.5-1.0 m/s smaller in magnitude in most layers than the middle panels. This confirms that,
277 on average, the biases are considerably underestimated by OLS regression using FV3GFS winds
278 as a predictor.

279 The average biases in the bottom panel are about 0.5-1.5 m/s in magnitude larger than the
280 middle panel in most layers, particularly for Rayleigh winds, indicating the biases are
281 overestimated by OLS regression using the average of Aeolus and FV3GFS winds as a predictor.
282 The bias estimates of OLS regression using Aeolus winds only as a predictor (not shown) are
283 even larger (than the bottom panel).



284 5 A TLS Bias Correction

285 In this section, a TLS bias correction for O-B is proposed to optimize Aeolus wind data
286 assimilation. For each assimilation cycle, the bias coefficients are computed by TLS regression
287 for the O-B in the week before the cycle (i.e., for the previous 28 cycles). One week provides a
288 large enough sample for the regression. As shown by Ripley and Thompson [1987], the TLS
289 solution only involves solving a quadratic equation with coefficients given by sample sums.
290 Therefore, an efficient approach is to calculate and save these sums for every cycle and
291 accumulate them over the 28 cycles. Because the findings in this study show substantial variation
292 of the bias coefficients with latitude, vertical layer, and orbital phase, the bias coefficients are
293 calculated from the winds in 19 discrete bins of latitude (centered every 10° between 90° S to 90°
294 N) for each vertical range/layer and for ascending and descending orbits separately. For each of
295 the O-B innovations in the assimilation cycle, values of c_0 and c_1 are linearly interpolated to the
296 latitude of the Aeolus observation. Subsequently, the TLS estimated bias, calculated using Eq.
297 (4), is subtracted from the O-B. Note that the bias correction is determined by the TLS analysis
298 solution for \hat{y}_k^b that in turn is determined from the observation and background wind, y_k^o and y_k^b ,
299 following Eq. (3).

300 The proposed scheme is applied to the O-B innovations of the BASE experiment. The
301 vertical distribution of the average remaining biases as a function of Aeolus wind is shown in
302 Figure 13, which is in the same format and for the same sample of observations as Figure 8. A
303 comparison of these two figures reveals that most of the biases are removed by the proposed TLS
304 bias correction. The latitudinal variations of the biases are also corrected (Figure 14). In addition,
305 the biases in the vertical average are also mostly removed, as shown in Figure 9.



306 **6 Summary and Conclusions**

307 In this study a TLS regression is used to optimally estimate speed-dependent biases
308 between Aeolus L2B Horizontal Line-of-Sight winds and short-term (6-h) forecasts of NOAA's
309 FV3GFS. The winds for 1-7 September 2019 are analyzed. Clear speed-dependent biases for
310 both Mie and Rayleigh winds are found, particularly in the lower troposphere and stratosphere of
311 the tropics and Southern Hemisphere. The largest biases are about 10% and 5% of FV3GFS wind
312 speed, as large as +/- 2.5 m/s and +/- 1.5 m/s at high FV3GFS wind speed, for Mie and Rayleigh
313 winds, respectively.

314 It is found that the biases are considerably underestimated by the OLS regression of the
315 innovations of Aeolus winds minus FV3GFS background winds on FV3GFS winds; but are
316 overestimated by the OLS regression, both on Aeolus winds only, and on the average of Aeolus
317 and FV3GFS winds.

318 The biases should be fully corrected to optimize Aeolus wind assimilation and to improve
319 the impact of Aeolus winds on FV3GFS global forecasts. The proposed TLS bias correction can
320 remove most of the biases before assimilation. In a companion paper, Garrett et al. [2021]
321 demonstrate that the application of this TLS bias correction to the Aeolus minus FV3GFS
322 background (O-B) winds considerably enhances the positive impact of Aeolus winds on NOAA
323 FV3GFS global and tropical cyclone forecasts. It is expected that the application of this
324 additional bias correction to the O-B innovations of Aeolus winds can improve and enhance
325 Aeolus data impacts on the analysis and forecast skill of other NWP systems as well.

326 Note that the proposed TLS approach presented here might be applied to other types of
327 observations that have errors typically characterized as a percentage of the observed value,



328 including quantities related to the concentrations or mass fractions of chemical species or
329 hydrometeors, or quantities like radio occultation refractivity and bending angle.

330

331 **Acknowledgments**

332 This work was supported by the NOAA/NESDIS Office of Projects, Planning, and
333 Acquisition (OPPA) Technology Maturation Program (TMP), managed by Patricia Weir and Dr.
334 Nai-Yu Wang, through the Cooperative Institute for Satellites and Earth System Studies
335 (CISESS) at the University of Maryland (Grant NA14NES4320003 and NA19NES4320002).
336 The authors would like to acknowledge Dr. Michael Rennie (ECMWF) and Dr. Lars Isaksen
337 (KNMI) for their comments and suggestions on the assimilation of Aeolus observations, and Dr.
338 William McCarty with NASA/GMAO for providing earlier versions of the GSI with Aeolus
339 ingest and observation operator capability. The Aeolus L2B BUFR data were provided by
340 ECMWF. The scientific results and conclusions, as well as any views or opinions expressed
341 herein, are those of the author(s) and do not necessarily reflect those of NOAA or the U.S.
342 Department of Commerce.

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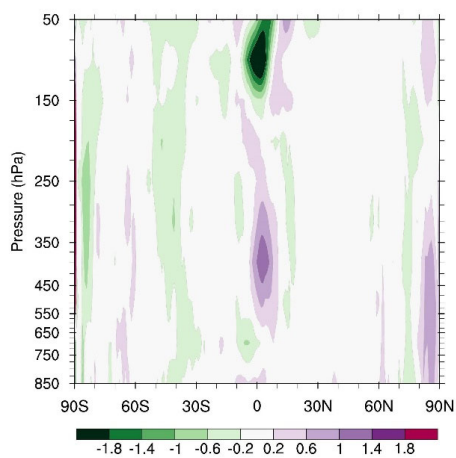
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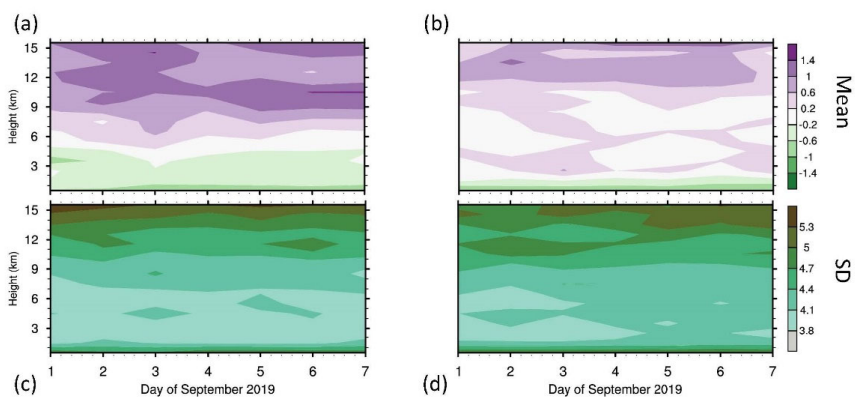
413 **8 Figures**



414

415 Figure 1. Latitudinal and height distributions of zonal mean difference of ECMWF minus FV3GFS

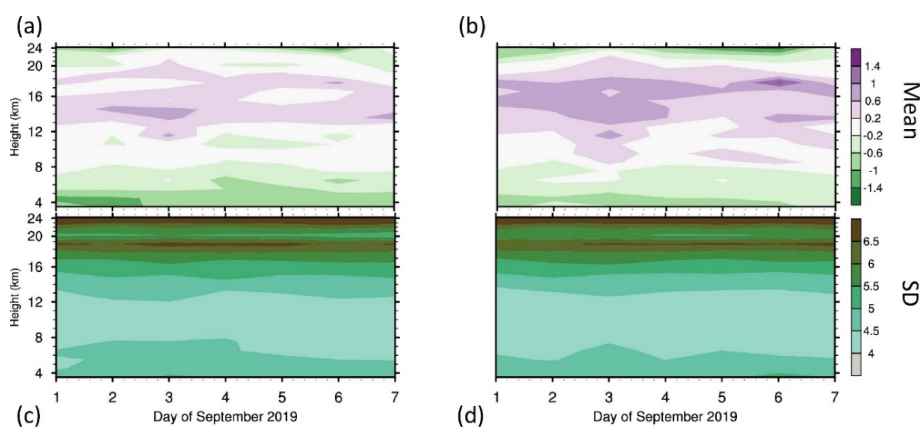
416 background zonal wind (m/s) for 1-7 September 2019.



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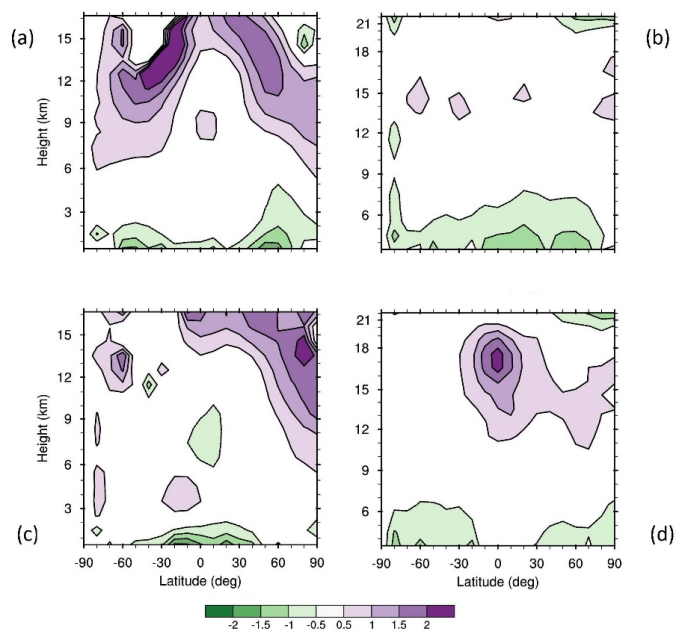
418 Figure 2. Vertical and daily variations of global horizontal means (a, b) and
419 the innovations of Mie winds minus FV3GFS background winds (m/s) in ascending (a, c) and descending
420 (b, d) orbits.

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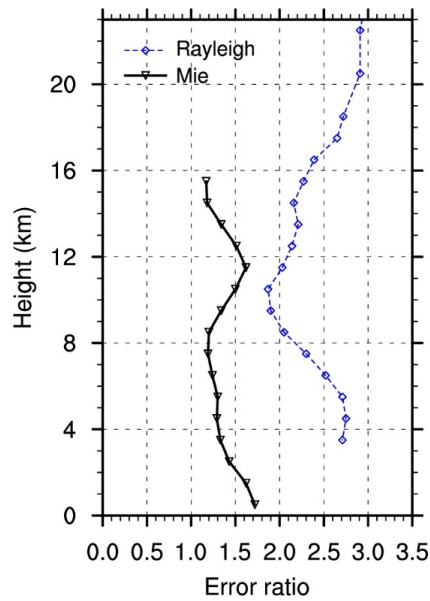
423 Figure 3. As in Fig. 2 but for Rayleigh winds.



424

425 Figure 4. Latitudinal and height distributions of mean differences (color scale, m/s) of Mie minus
426 FV3GFS winds (a, c) and Rayleigh minus FV3GFS winds (b, d) in ascending (a, b) and
427 descending (c, d) orbits for 1-7 September 2019.

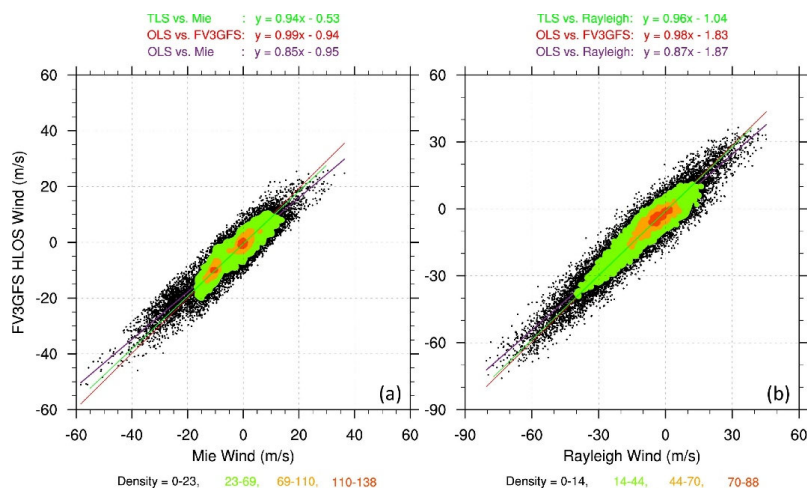
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430 Figure 5. Vertical variation of the square root of the ratio of random error variance in Aeolus winds
431 versus FV3GFS background winds for Mie (solid black) and Rayleigh (dashed blue) winds. Results are
432 based on global O-B innovations of Aeolus minus FV3GFS winds from the Aeolus BASE experiment
433 using Hollingsworth-Lonnberg method. The symbols are plotted at averaged height in each vertical layer.

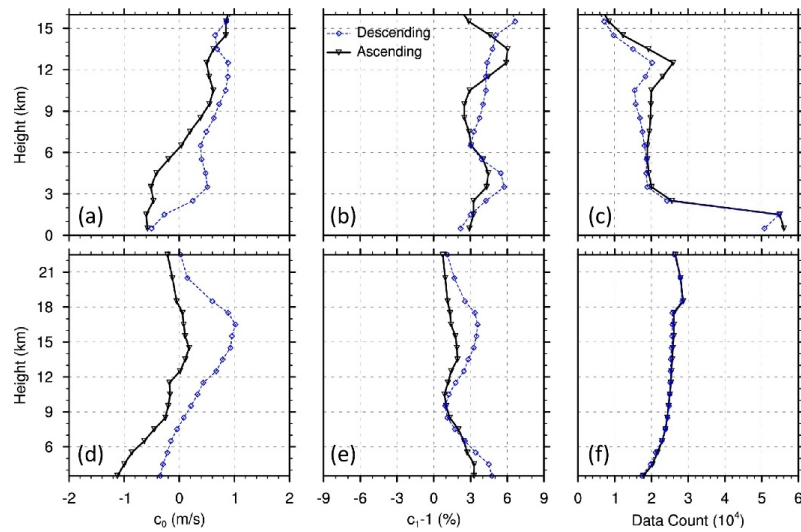
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436 Figure 6. Density plots of global collocated Mie and FV3GFS winds at ~3.5 km altitude (a), and Rayleigh
437 and FV3GFS winds at ~16.5 km altitude (b) in descending orbits. The TLS analysis line (green), the OLS
438 regression line of FV3GFS winds on Aeolus winds (purple), and the OLS regression line of Aeolus winds
439 on FV3GFS winds (transformed and plotted as a function of Aeolus winds in red) are shown, with
440 corresponding regression coefficients displayed above each panel.

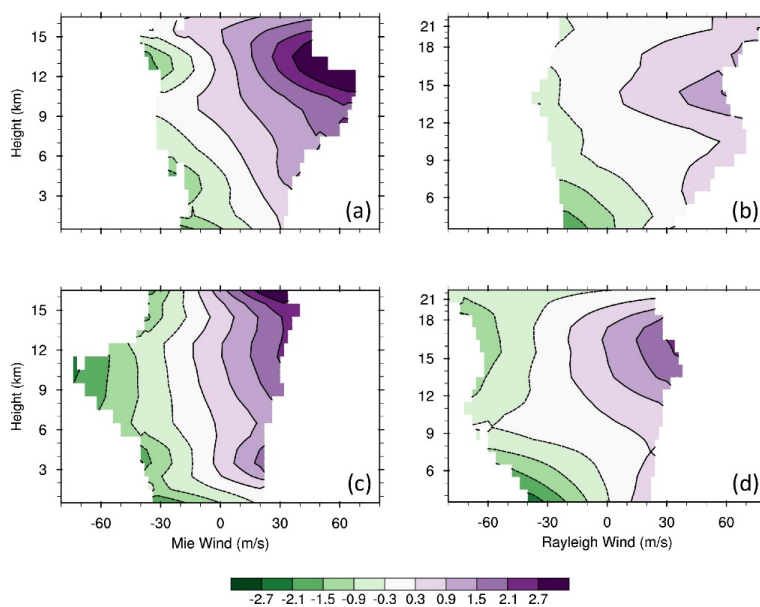
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444 Figure 7. Vertical variations of TLS bias coefficients for Mie versus FV3GFS winds (a, b, c), and
445 Rayleigh versus FV3GFS winds (d, e, f). Each point plotted represents a separate TLS analysis for all
446 observations in each layer for all latitudes and for either ascending (black) or descending (blue) orbits.
447 The symbols are plotted at the average height of the observations in each layer.

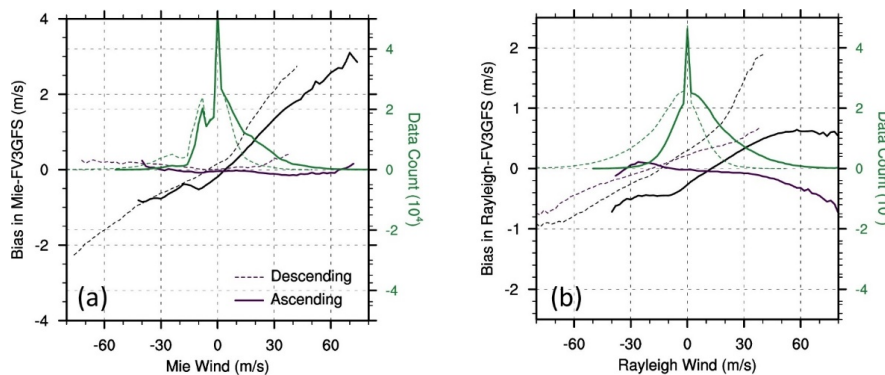
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451 Figure 8. Vertical distributions of average TLS estimated biases (color scale, m/s) for Mie versus
452 FV3GFS winds (a, c) and Rayleigh versus FV3GFS winds (b, d) as a function of observed Aeolus winds
453 (m/s) in ascending (a, b) and descending (c, d) orbits for all latitudes, obtained from the TLS fits
454 displayed in Figure 7.

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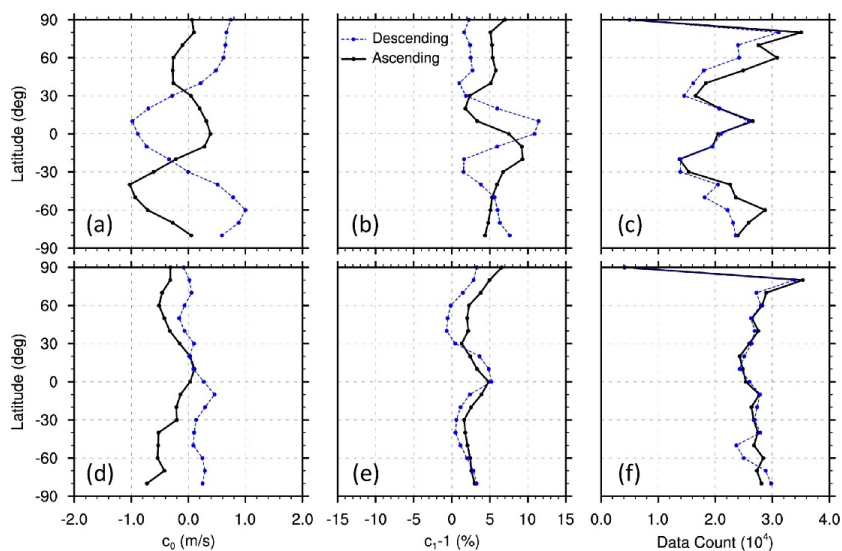
456

457 Figure 9. TLS estimated biases (m/s) before (black lines) and after (purple lines) TLS bias correction for
458 Mie versus FV3GFS winds (a) and Rayleigh versus FV3GFS winds (b) as a function of the observed



459 Aeolus winds (m/s), vertically averaged for all latitudes of Aeolus winds. The green lines report the
460 number of observations in each 2 m/s bin.

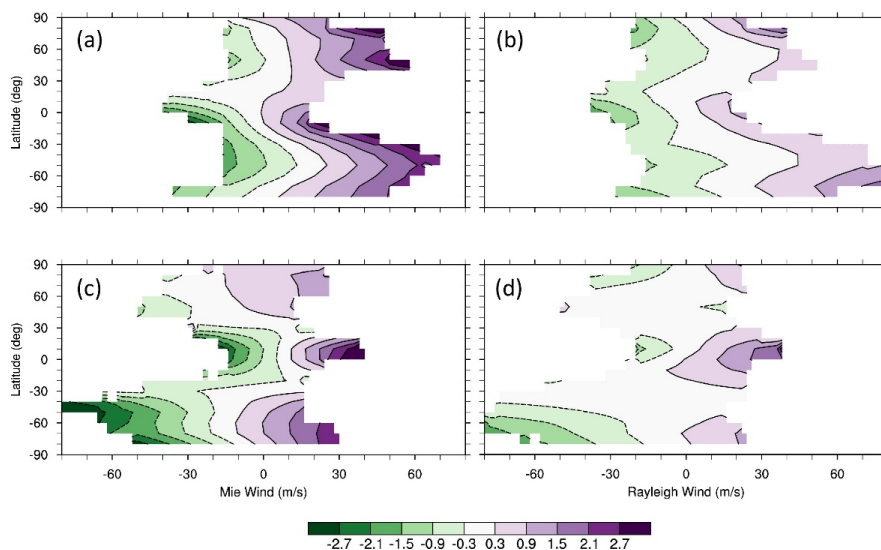
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463 Figure 10. Latitudinal variation of TLS bias coefficients for Mie versus FV3GFS winds (a, b, c) and for
464 Rayleigh versus FV3GFS winds (d, e, f). Each point plotted represents a separate TLS analysis for all
465 observations in all vertical layers in a 10° latitude band for either ascending (black) or descending (blue)
466 orbits. The latitude bands are centered every 10° from 90°S to 90°N. The symbols are plotted at the center
467 in each latitude band. The vertical layers are 0-16 km for Mie winds and 3-22 km for Rayleigh winds.

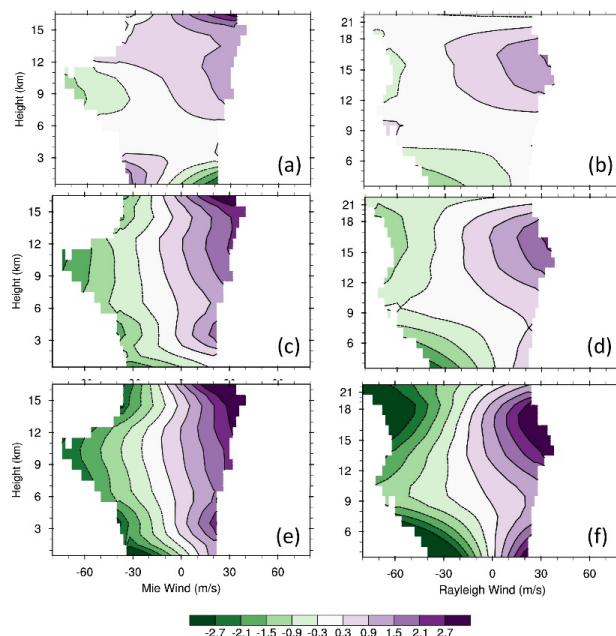
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470 Figure 11. Latitudinal distributions of average TLS estimated biases (color scale, m/s) for Mie versus
471 FV3GFS winds (a, c) and Rayleigh versus FV3GFS winds (b, d) as a function of Aeolus wind in
472 ascending (a, b) and descending (c, d) orbits for all latitudes, obtained from the TLS fits displayed in
473 Figure 10.

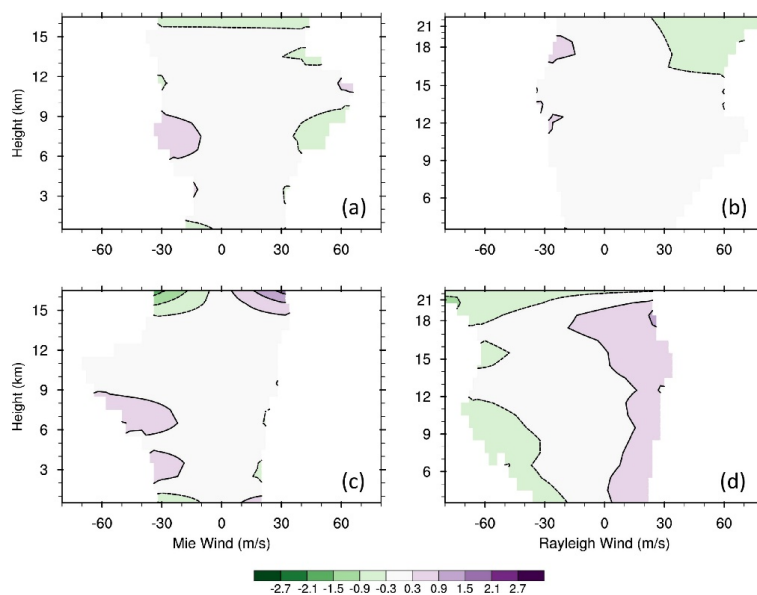
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476 Figure 12. Vertical distributions of average bias estimates (color scale, m/s) in Mie versus FV3GFS winds
477 (a, c, e) and Rayleigh versus FV3GFS winds (b, d, f) as a function of Aeolus winds using one of three
478 methods for descending orbits for all latitudes. The methods are OLS using FV3GFS winds as a predictor
479 (a, b), TLS (c, d, same as the bottom panels of Figure 8), and OLS using the average of Aeolus and
480 FV3GFS as a predictor (e, f).

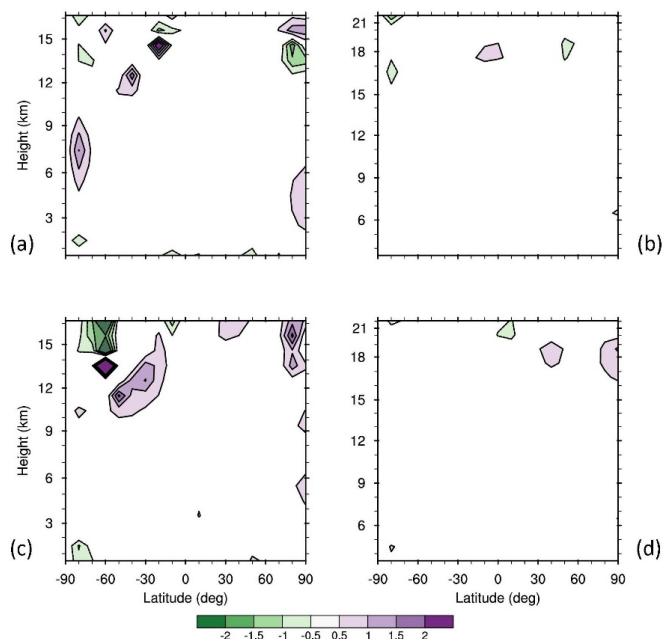
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483 Figure 13. As in Figure 8 but for the mean innovation (O-B) after the TLS bias correction is applied. For
484 each 6-h cycle during 1-7 September 2019, the TLS bias correction is calculated from the 28 preceding
485 cycles.

486



487

488 Figure 14. As in Figure 4 but after the TLS bias correction is applied. Note that the remaining
489 bias in several bins are due to small sample size, and the TLS bias correction is not applied in
490 these bins in Aeolus wind assimilation.