

Consistency test of precipitating ice cloud retrieval properties obtained from the observations of different instruments operating at Dome-C (Antarctica)

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Abstract.

Selected case studies of precipitating ice clouds at Dome-C (Antarctic Plateau) ~~are~~ were used to test a new approach for the estimation of ice cloud reflectivity at 24 GHz (12.37 mm ~~of~~ wavelength) using ground-based far infrared spectral measurements from the REFIR-PAD Fourier transform spectroradiometer and backscattering/depolarization lidar profiles. The resulting re-
5 flectivity ~~is~~ was evaluated with the direct reflectivity measurements provided by a co-located micro rain radar (MRR) operating at 24 GHz, ~~which is~~ that was able to detect falling crystals with large particle size, typically above ~~500~~ 600 μm .

To obtain the 24 GHz reflectivity, we used the particle effective diameter and the cloud optical depth retrieved from the far infrared spectral radiances provided by REFIR-PAD and the tropospheric co-located backscattering lidar to calculate the modal radius and the intercept of the particle size distribution. ~~From these~~ These parameters were found spanning in the wide ranges
10 between 570–2400 μm and 10^{-2} – 10^4 cm^{-5} , respectively. The retrieved effective sizes and optical depths mostly varied in the ranges 70–250 μm and 0.1–5, respectively. From these parameters, the theoretical reflectivity at 24 GHz ~~is~~ was obtained by integrating the size distribution over different ~~microwave~~ cross sections for various habit crystals provided by Eriksson et al. (2018) databases. From the comparison with the radar reflectivity measurements, we found that the hexagonal column-like habits ~~and the plates/,~~ the columnar crystal aggregates ~~show~~ and the 5/6 branches bullet rosettes showed the best agreement
15 with the MRR observations. The ~~presence of (hexagonal) columns is confirmed both by the presence of 22° solar halos, detected by the HALO-CAMERA, and~~ dispersion coefficient of the crystal particle size distribution was assumed in the range 0–2 according to the temperature dependence found in previous works. The retrieved values of intercept and slope were found in good agreement with these works. The presence of the estimated habits was confirmed by the crystal images taken by the ICE-CAMERA, operating in proximity of REFIR-PAD and the MRR, in particular, the occurrence of hexagonal column-like
20 ice crystals was confirmed by the presence of 22° solar halos, detected by the HALO-CAMERA. The average crystal lengths obtained from the retrieved size distribution ~~are~~ were also compared to ~~the ones~~ those estimated from the ICE-CAMERA im-

ages. The agreement between the two results ~~confirms~~confirmed that the retrieved parameters of the particle size distributions correctly ~~reproduce~~reproduced the observations.

1 Introduction

25 The importance of clouds in the global climate is shown by many studies and is strongly related to their role in modulating the incoming solar radiation in the shortwave (0.2-5 μm) broadband and the outgoing emission from the Earth in the longwave (5-100 μm) ~~bands.~~The cloud effect can be either broadband. Clouds can be responsible either of a net cooling if they are enough thick to reflect most of the incoming radiation back to space or a net warming if they absorb more radiation than they reflect; therefore they acting as regulators of the Earth Radiation Budget (ERB) (Kiehl and Trenberth, 1997; Solomon, 2007).
30 The ~~effect~~impact of clouds on the ERB is still not completely assessed; for example, recent studies demonstrated that small ice crystals and optical depth greater than 10 or large particles and optical depths less than 10 can yield to a net cooling as low as -40 W m^{-2} or a net warming as high as $+20 \text{ W m}^{-2}$ (Baran, 2009). Therefore, more accurate statistics of the cloud optical and microphysical properties are needed to better characterize their radiative effect; this is especially true for ice clouds, which represent the greatest challenge because of the extremely inhomogeneous composition of crystal sizes and habits. Ice cloud
35 properties in the polar regions are the least well known and improved characterizations of these properties are much needed.

A realistic parameterization of the Antarctic ice clouds has ~~proven~~been shown to improve the performance of the Global Circulation Models (GCMs) (Lubin et al., 1998). The radiative forcing caused by these clouds, defined as the differences between the total flux in the presence of cloud and one in clear sky condition (Intrieri et al., 2002), influences the Surface Radiation Budget (SRB) and thereby the surface temperature (Stone et al., 1990), which is ~~a relevant aspect~~an important
40 component of the Antarctic environment.

Mixed phase clouds greatly impact the SRB (Lawson and Gettelman, 2014; Korolev et al., 2017), since the atmospheric radiation balance is very sensitive to the distribution of cloud phase as pointed out in Shupe et al. (2008). These clouds represent a three-phase system consisting of water vapour, ice crystals, and supercooled water droplets at temperatures between 0°C and -40°C in which the glaciation process is the result of the ice growth at the expense of the liquid droplets, also known as the
45 Wegener–Bergeron–Findeisen (WBF) mechanism (Korolev and Isaac, 2003). Mixed-phase clouds are very common in polar regions (Turner et al., 2003; Cossich et al., 2021) but they also occur at lower latitudes as discussed in Costa et al. (2017).

The uncertainties in the cloud radiative properties represent the main contributor to the biases in the radiative fluxes both at the top of the atmosphere and at the surface (~~Rossow et al., 1995~~)(Rossow et al., 1995; Sun et al., 2022). These uncertainties are mostly due to the lack of spectrally resolved measurements in the Far InfraRed (FIR) both from ground-based sites and
50 from airborne instruments, as well as to the scarceness of in-situ measurements of size and habit distributions of the ice crystals.

The representation of the radiative properties of cirrus clouds is ~~tricky~~problematic because of the presence of myriad of different crystal habits and sizes (Baran, 2009). This inhomogeneity is strongly related to the supersaturation condition (Korolev et al., 2017), ~~which~~that depends on the atmospheric temperature, humidity, and vertical wind (Keller and Hallett, 1982). These clouds are also sensitive to the aerosol concentration and composition, which act as ice nucleation particles and

55 cloud condensation nuclei (Fan et al., 2017). The complexity of the habit crystals is well described in detail in Bailey and Hallett (2009), where the single crystals and polycrystalline regimes (columnar and plate-like) are shown as a function of the ice supersaturation and temperature.

It is clear that the FIR portion of the spectrum plays an important role in the longwave radiative budget since even in clear sky conditions more than 50% of the entire flux comes from this spectral region; the contribution can exceed 60% ~~at poles in~~
60 ~~polar regions~~ because of the extremely dry conditions and the low temperatures. Furthermore, ~~the~~ FIR spectrum is strongly modulated by the clouds and, in particular, shows an important feedback from cirrus clouds (Harries et al., 2008) since this region is very sensitive to the ~~microphysics~~ ~~the optical properties and, particularly, to the particle sizes~~ (Yang et al., 2003a; Baran, 2007).

Different studies pointed out that the total downwelling radiative flux in the internal regions of Antarctica, including Dome-
65 C, varies from 50 to 220 W m⁻² (Bromwich et al., 2013; Di Natale et al., 2020) because of the cloud forcing. In particular, the FIR component (below 667 cm⁻¹) reaches the 75% of the total flux for ~~thinner~~ ~~optically thin~~ clouds and reduces to 55% for the ~~thicker ones~~ ~~optically thick clouds~~, since the longwave radiative fluxes (LRF) strongly depend on the Ice/Liquid Water Content (IWC/LWC) ~~inside of~~ the cloud (Di Natale et al., 2020).

The study of the downwelling FIR spectrum by means of ground-based, zenith-looking observations is extremely important
70 in order to assess the emission component of the ERB providing the complementary component of the spectral radiance at the top of the atmosphere (TOA). These kind of measurements need to be performed from extremely dry sites, such as high mountains or polar regions, ~~due to the opacity because of the opacity due to sensitivity~~ of the atmosphere ~~to water vapor~~ (Turner and Mlawer, 2010) so there are difficult constraints on where these observations can be made. On the other hand, ~~they allow the~~ ~~measurements can be used~~ to detect the signal coming from the upper part the atmosphere, where clouds occur, with a greater
75 contrast with respect to the nadir-looking observations, since the background signal comes from ~~the~~ cold space and not from the emitting surface.

During last two decades, measurements of the downwelling longwave radiation, including in the FIR, have been used to study the cirrus cloud radiative properties both at mid-latitudes (Palchetti et al., 2016; Di Natale et al., 2021; Maestri et al., 2014) and in polar regions, in particular in Arctic (Garrett and Zhao, 2013; Intrieri et al., 2002; Ritter et al., 2005) and Antarctica
80 (~~Maesh et al., 2001a, b; Palchetti et al., 2015; Di Natale et al., 2017; Rowe et al., 2019; Rathke et al., 2002; Maestri et al., 2019~~)
~~(Maesh et al., 2001a, b; Palchetti et al., 2015; Di Natale et al., 2017; Rowe et al., 2019; Rathke et al., 2002; Maestri et al., 2019; Bellisario~~

Since December 2008, several instruments have been installed at Dome-C and operated continuously ~~in order~~ to characterize the microphysical properties of ice clouds over Antarctica. Starting in 2018, the FIRCLOUDS (Far InfraRed closure experi-
85 ment for Antarctic CLOUDS) project, funded by the Italian National Program for the Antarctic Research (PNRA), has been providing statistics of the radiative properties of the Antarctic clouds ~~in order~~ to evaluate the current parameterizations of ice and mixed phase clouds through the intercomparison of the retrieval products obtained from different kind of measurements.

This paper describes a new approach to compare the clouds radiative and physical properties retrieved from spectral FIR measurements against microwave radar observations using data from 14 days of selected observations of precipitating ice

90 clouds observed between 2019-2020 at Dome-C. Section 2 presents and describes the instruments operating at Dome-C, and section 3 discusses the methodology used to compare the 24 GHz radar reflectivity observations with those retrieved from the FIR radiance spectra. The results are discussed in section 4, with a detailed comparison from four selected days. Finally, in section 5 the conclusions [and future perspective](#) are drawn.

2 Instruments and observations

95 2.1 REFIR-PAD Fourier spectroradiometer and tropospheric backscattering/depolarization lidar

The Radiation in Far InfraRed - Prototype for Applications and Development (REFIR-PAD) (Bianchini et al., 2019) is a Fourier transform spectroradiometer (FTS) ~~which~~that detects the spectral radiance emitted by the atmosphere in the broad band between $100\text{-}1500\text{ cm}^{-1}$ ($6\text{-}100\text{ }\mu\text{m}$) with a spectral resolution of 0.4 cm^{-1} . REFIR-PAD was installed inside the PHYSICS shelter at Concordia base at Dome-C, where it views the atmosphere through a 1.5 m chimney. It was installed in
100 December 2011, and has operated continuously in unattended mode since, providing spectral radiances every ~ 12 minutes. The radiance calibration is performed for each scene measurement through two black bodies stabilized in temperature, one hot and one cold, forming the calibration unit, while the thermal background is stabilized by means of a reference black body at room temperature. The interferometer is in Mach-Zehender configuration with two inputs and two outputs, which enables the best performance. The total field of view (FOV) is equal to 115 mrad, with a internal beam divergence of about 0.00087 sr
105 and a throughput of about $0.0035\text{ cm}^2\text{ sr}$. The complete instrument specifications and description are thoroughly described in Bianchini et al. (2006, 2019) and Palchetti et al. (2015).

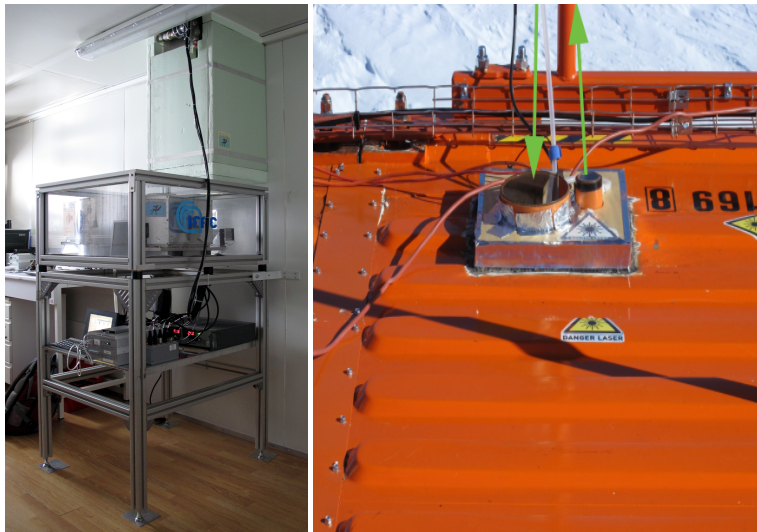


Figure 1. Left side: REFIR-PAD Fourier transform spectroradiometer inside the PHYSICS shelter with the 1.5 m chimney connecting the instrument with outside. Right side: output windows of the tropospheric lidar on the roof of the shelter.

The backscattering/depolarization tropospheric lidar is collocated inside the PHYSICS shelter. It was installed in 2008, and has operated in unattended mode providing the backscattering and depolarization signal profiles with a temporal frequency of 10 minutes. The instrument uses the spectral channel at 532 nm of wavelength to provide the backscattering signal and the depolarization. Fig. 1 shows the REFIR-PAD Fourier transform spectroradiometer inside the PHYSICS shelter and the aperture of [the](#) tropospheric lidar on the roof.

2.2 Micro Rain Radar (MRR)

The Micro Rain Radar-2 (MRR, Metek GmbH, Germany), a profiling Doppler radar, has been operating at Concordia station at Dome-C since December 2018. It was installed on the roof of the PHYSICS shelter in a zenith-looking observation geometry [providing one measurement every minute](#). It operates at 24 GHz, measuring Doppler power spectra in 64 bins over 32 vertical range bins that ~~for Concordia installation,~~ were set to a width of 40 meters. MRR has a compact design being composed of a dish with a diameter of ~60 cm and a small enclosure containing ~~transmitting both a transmitting and~~ a receiving apparatus. It is characterized by low power consumption and high robustness, making it suitable for deployment in remote regions for long-term unattended measurements. In fact, [the](#) MRR is a quite popular instrument for precipitation measurements in Antarctica, in spite of the relatively low sensitivity (Bracci et al., 2022). The post-processing MRR procedure by Maahn and Kollias (2012) that partially improves the sensitivity of the system and removes spectra aliasing has been adopted.

An automatic data transfer system provides daily measurements directly to the storage server at the National Institute of Optics (CNR-INO) in Florence.

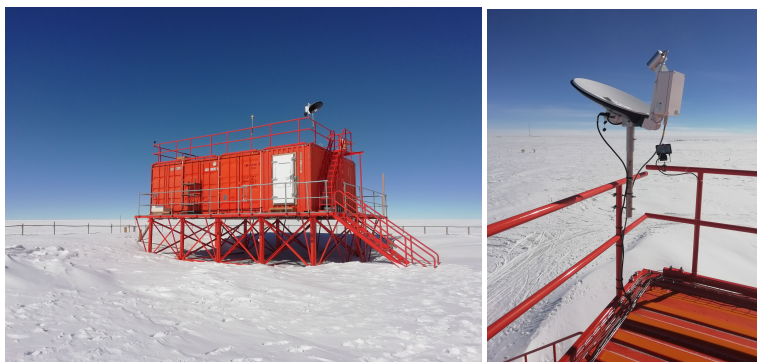


Figure 2. Left side: PHYSICS shelter at Concordia station. Right side: Micro Rain Radar (MRR) installed in 2018 on the roof of the shelter.

Fig. 2 shows on the left side the PHYSICS shelter at Concordia station, where REFIR-PAD spectroradiometer and the tropospheric lidar are installed; on the right side the MRR, which is installed on the roof.

2.3 ICE- and HALO-CAMERA

The ICE-CAMERA (Del Guasta, 2022) is an optical imager mounted on the roof of the PHYSICS shelter. It is able to routinely image falling ice crystals by freezing them on a screen, rapidly photographing them, and then sublimating the deposited

particles by heating the screen in a regular cycle. Sublimation of the ice particles occurs without melting on the ICE-CAMERA surface, as its temperature is kept below -5 °C also during the heating of the plate.

The photographs are analyzed to sort and classify the precipitating ice crystals depending on their habit and sizes and they are hourly provided unless work of maintenance or cleaning are needed causing a lack of data. A MATLAB software routine performs the automatic processing of the images: it subtracts the background, enlarges and reduces the binary image, deletes the edge objects, eliminates the single grains, creates and enlarges the grains bounding boxes, and finally sorts the grains depending on the increasing size for graphic use. In the last step, the software calculates the contour and the skeletonization of the remaining grains.

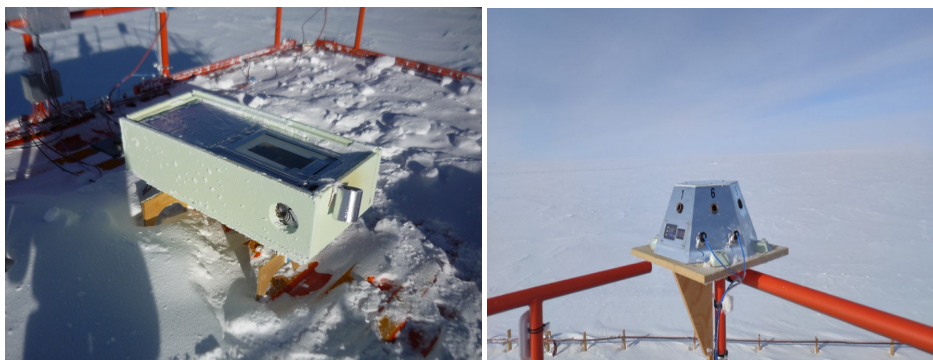


Figure 3. Left side: ICE-CAMERA mounted on the roof of the PHYSICS shelter. Right side: HALO-CAMERA installed on the handrail at the edge of the shelter.

HALO-CAMERA is a sky imager equipped of a sun-tracker installed on the shelter roof used for monitoring the solar and lunar halos generated by the floating ice crystals. These halos occur because the scattering phase function at visible wavelength of particular wavelengths of hexagonal ice crystals habits has two peaks at 22° and 46° scattering angles. Fig. 3 shows the two imagers deployed on the roof of the PHYSICS shelter at Concordia station.

In the work by Lawson et al. (2006), the images of ice crystals were recorded at the South Pole (Antarctica) by using two ground-based cloud particle imagers (CPIs) jointly with the LaMP (French Laboratoire de Meteorologie Physique) polar nephelometer, which measured the ice crystal phase function. In that work, it was found that the phase function shows showed the peak at 22° when column-like and plate-like habits occur, while is-was smoother in case of rosette-like shape. We know that the presence of the peaks in the phase scattering function at visible wavelengths does not depend on the particular crystal habit but on the roughness of the crystal surface (Yang et al., 2013); the fact that Lawson et al. (2006) did not measure halos in the presence of bullet rosettes is-was probably related to a rougher crystal surface occurring during the formation of these particular crystals. In summary, we will use fact, as shown in Forster and Mayer (2022), the smooth crystal fraction (SCF) of the solid bullet rosettes tends to be minimum with respect to the other habits, that means the rough component is the most frequent. In summary, since the plate-like crystal were not detected by the ICE-CAMERA during the precipitating event, we

used the evidence of halo-halos formation as a good indicator of the occurrence of column-like crystals-hexagonal ice crystals columns in the Antarctic environment.

3 Methodology

The REFIR-PAD retrieved cloud products are-were used to derive an estimation for the equivalent reflectivity $Z_e Z_e$, which can be compared with those obtained from MRR spectra. We used the cloud parameters, such as the ice optical depth (OD_i) at visible wavelengths and the ice effective diameter (D_{ei}), to derive the intercept (N_o) and the modal radius L_m of the particle size distribution (PSD). The PSD (denoted as $n(L)$ in the formulas) was assumed as Γ -like distribution (Platnick et al., 2017; Matrosov et al., 1994; Turner, 2005) with exponent μ and the width associated to L_m defined as $\sigma = 1/(3 + \mu) = 0.1$, assuming $\mu = 7$ (Platnick et al., 2017; Matrosov et al., 1994; Turner, 2005). Thus, the expression of the size distribution results.
 160 The Γ size distribution is expressed as:

$$n(L) = N_o L^\mu e^{-(3+\mu) \frac{L}{L_m}} \quad (1)$$

and the mode of the distribution given by $(\frac{\mu}{3+\mu})L_m$ where L is the length of assumed crystal in the given size bin and the mode is given by $\mu/(3 + \mu)L_m$. Then, we define the effective diameter following Yang et al. (2005):

$$D_{ei} = \frac{3 \int_{L_{\min}}^{L_{\max}} V(L)n(L)dL}{2 \int_{L_{\min}}^{L_{\max}} A(L)n(L)dL} \quad (2)$$

165 where V and A denote the particle volume and projected area, respectively. According to the measurements performed by Heymsfield et al. (2013, 2002) and the range of cloud temperature found at Dome-C from our analysis, between -50 and -25 °C, we assumed the μ coefficient of the PSD spanning between 0 and 2. As long as the effective diameter is defined as in Eq. (2), the spectral radiance detected by REFIR-PAD turns out to be insensitive to the detailed shape of the size distribution (Wyser and Yang, 1998), in particular to the dispersion coefficient μ . We also verified this assertion by performing simulations
 170 of the downwelling spectral radiance for different values of D_e and optical depth by assuming different values of μ between 0 and 7 to generate the crystal infrared optical properties. Therefore, the results of the cloud properties retrieval can not be affected by the choice of μ .

Once the PSD is-was defined, the effective MRR reflectivity is-was obtained by integrating the backscattering cross sections at 24 GHz (12.37 mm) tabulated in the database provided by Eriksson et al. (2018) over the PSD for different assumed crystal
 175 habits.

Figure 4 shows the backscattering and absorption cross sections contribution as a function of the particle dimension (L), for two different length L , for a normalized particle size distribution with $L_m \sim 1000 \mu\text{m}$ and $L_m = 2300$ respectively, corresponding to effective diameters-an effective diameter D_e equal to 100 and 300-120 μm , as we can see from shown in Fig. 5. The case $L_m = 1000 \mu\text{m}$ corresponds approximately to the average found from our retrieval analysis.

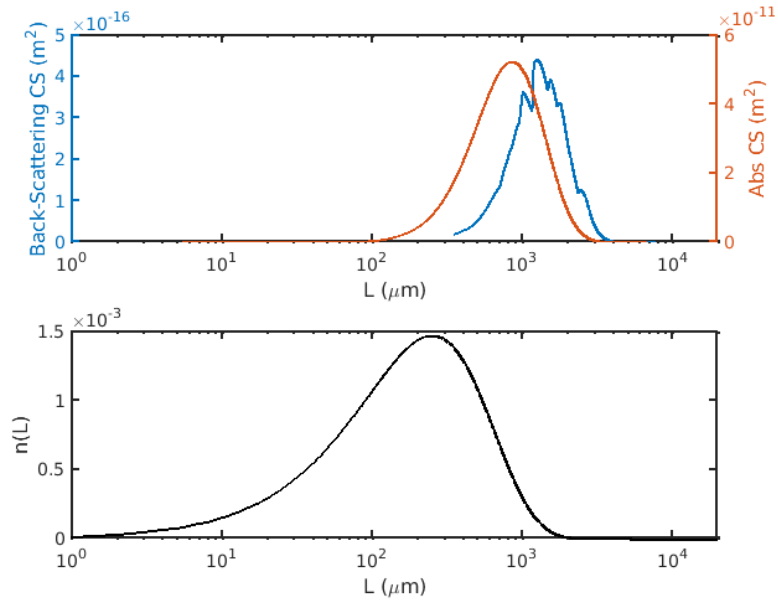


Figure 4. Left side: normalized PSD with $L_m = 1000 \mu\text{m}$ (lower panel) and the relative backscattering cross section at 24 GHz and absorption cross sections at 400 cm^{-1} as a function of particle dimensions (upper panel). Right side: same as left side but for a PSD defined by $L_m = 2300$.

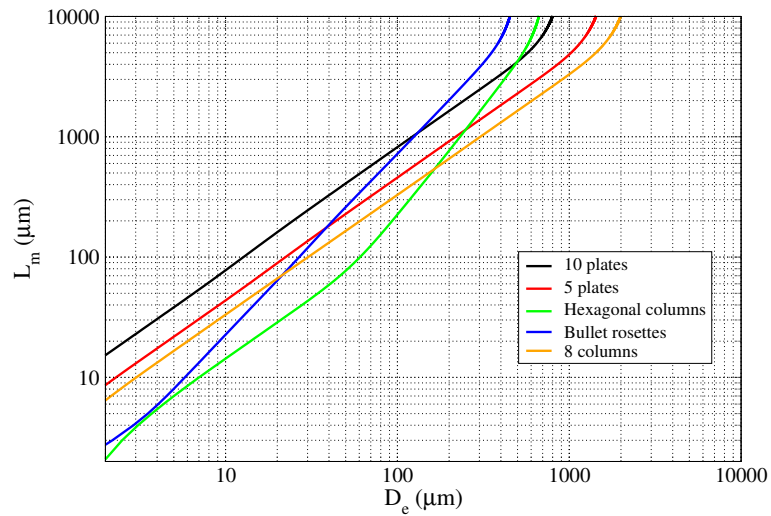


Figure 5. Relationship between the effective diameter (D_{ei}) and the modal radius (L_m) of the particle size distribution for the various ice crystal habits.

180 The results are-were obtained using the single particle optical properties of the large plate aggregates at 24 GHz for the backscattering and at 400 cm^{-1} for the absorption cross sections. The figure Fig. 4 shows that the largest crystals of the assumed PSDs (lower panelspanel) provide the biggest contribution to the total backscattering cross section (representative of the MRR measurement). A similar result is-was obtained for the absorption cross section at 400 cm^{-1} (assumed as the key parameter of the REFIR-PAD measurements at FIR), which, however, presents a peak slightly shifted towards the smaller
 185 dimensions. A considerable overlap between the two curves (mostly between 600–2000 μm) suggests that it is-was possible to obtain information on a large part of the PSD from FIR spectral measurements.

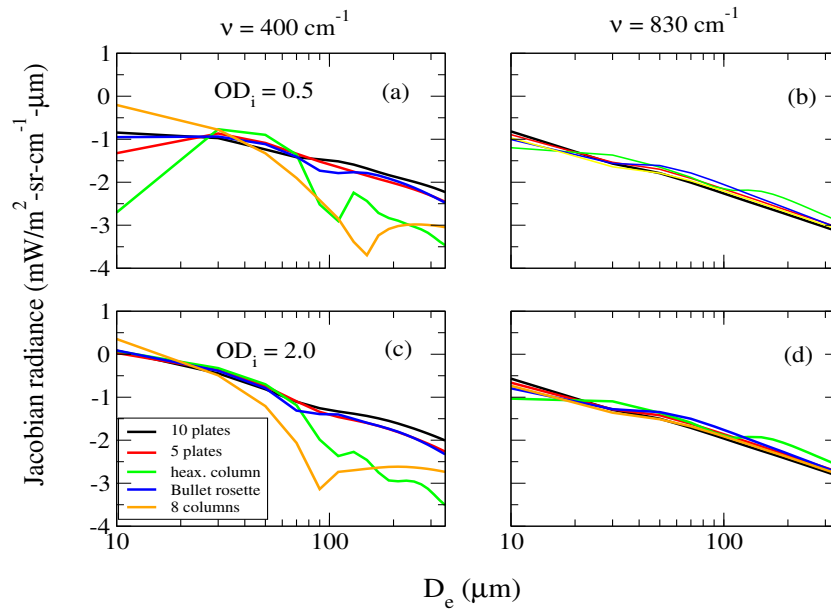


Figure 6. Absolute values of the downwelling spectral radiance derivatives with respect to the effective diameter simulated for two precipitating ice clouds with optical depth 0.5 (upper panels) and 2 (lower panels), at wavenumbers (ν) 400 cm^{-1} (panels a and c) and 830 cm^{-1} (panels b and d) for five different crystal habits.

The MRR signal represents an indicator of the presence of large ice particles, while the infrared downwelling spectral radiance (R_ν) measured by REFIR-PAD shows more sensitivity to changes in smaller particles. On the left side of In Fig. 6 we can see that the absolute values of the downwelling spectral radiance derivatives calculated with respect to D_{ei} for values of
 190 OD_i equal to 0.5 and 2 (upper and lower panels) at 400 cm^{-1} (panels a and c) of wavenumber ν are more intense than at 830 cm^{-1} (panels b and d), as much as one order of magnitude. The simulations are-were generated by placing an ice cloud close to the ground and the top at 5 km a.s.l., which is-was representative of the precipitating ice clouds we observed. From panels a and c of Fig. 6 we can also notice that for D_{ei} larger than $100\text{ }\mu\text{m}$ the derivatives calculated for the 10 plates aggregate habit shows the highest sensitivity. The color map on the right side of Fig. 7 shows that there is a good sensitivity in the FIR region
 195 (400 cm^{-1}) for D_{ei} as high as about $300\text{ }\mu\text{m}$ for optical depth lower than 6. All this suggests-suggested to us that 10 plates

aggregate could be the more suitable habit for retrieving atmospheric scenarios with large ice particles up to $300 \mu\text{m}$ for OD_i lower than 6.

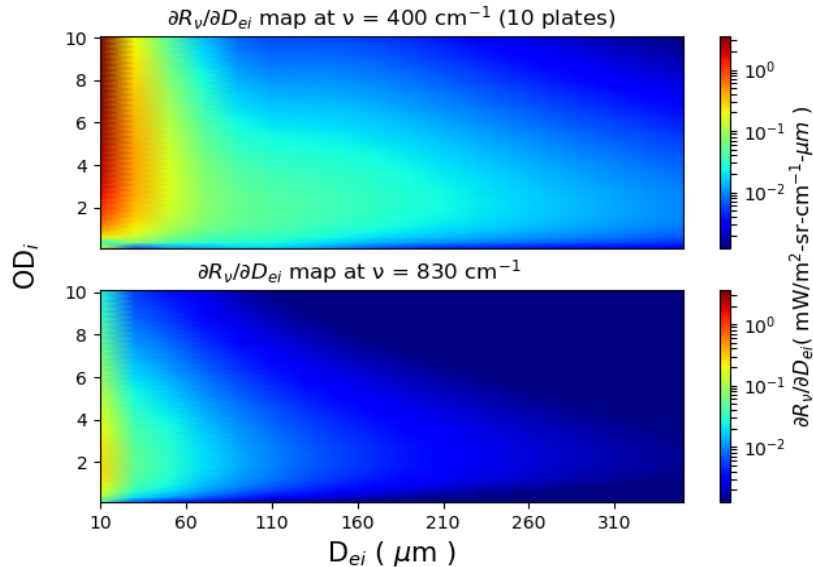


Figure 7. Left side: absolute values Color map of the downwelling spectral radiance derivatives with respect to the effective diameter simulated for two precipitating ice clouds with optical depth 0.5 (upper panels) and 2 (lower panels), at wavenumbers (ν) 400 (panels a and e) and 830 (panels b and d) for five different crystal habits. Right side: same derivatives of the left side Fig. 6 but only for 10 plates aggregate and for multiple optical depth values ranging between 0.1 and 10.

In this work, we assumed that plate-like and droxtal-like crystals were not present, since at temperatures below -20°C , the prevalent regime is columnar because the ice supersaturation and the crystal growth rate are generally higher as pointed out in Bailey and Hallett (2009). Moreover, at these temperatures, plates and droxtals show a low growth rate (Bailey and Hallett, 2009) and then have smaller sizes, below 60 and $100 \mu\text{m}$, respectively (Yang et al., 2013; Lawson et al., 2006). Also, their occurrence is mostly found during diamond dust events and they were rarely observed in the ICE-CAMERA photographs during the precipitation events detected with the MRR. In the next section, we will show the low dependence on the habit type of the particle size distribution when the maximum crystal length stays in the range between $600 \mu\text{m}$ and $1800-2000 \mu\text{m}$. This peculiarity, and the fact that for the 10 plate aggregates the downwelling spectral radiance is much more sensitive to the D_{ei} at the largest values above $100 \mu\text{m}$ with respect to the other habits, will be were exploited to retrieve the effective diameter of the larger particles as discussed in the next section.

The average absorption/extinction efficiencies ($\langle Q_{a,ei} \rangle_\nu$), the single scattering albedo ($\langle \omega_i \rangle_\nu$), and the asymmetry factor ($\langle g_i \rangle_\nu$) at the wavenumber ν used to simulate the spectral radiances in the presence of ice clouds were calculated by assuming the PSD ($n(L)$) in Eq. (1). Thus, the $\langle Q_{a,ei} \rangle_\nu$ are given by (Yang et al., 2005):

$$\langle Q_{a,ei} \rangle_\nu = \frac{\int_{L_{min}}^{L_{max}} Q_{a,ei,\nu}(L)A(L)n(L)dL}{\int_{L_{min}}^{L_{max}} A(L)n(L)dL} \quad (3)$$

$$\langle g_i \rangle_\nu = \frac{\int_{L_{min}}^{L_{max}} g_i(L)Q_{si,\nu}(L)A(L)n(L)dL}{\int_{L_{min}}^{L_{max}} Q_{si,\nu}(L)A(L)n(L)dL} \quad (4)$$

$$\langle \omega_i \rangle_\nu = 1 - \frac{\langle Q_{ai} \rangle_\nu}{\langle Q_{ei} \rangle_\nu} \quad (5)$$

where $Q_{si,\nu} = Q_{ei,\nu} - Q_{ai,\nu}$ is the scattering efficiency, L_{min} and L_{max} denote the maximum length database limits equal to 2 and 10000 μm , respectively, and $A(L)$ is the projected area of the crystal.

3.1 Retrieval of the particle size distributions from REFIR-PAD spectral radiances

To simulate the downwelling spectral radiance of the atmosphere in the presence of ice clouds, the optical depth of the ice at the infrared wavenumbers is was obtained through the relationship (Yang et al., 2003a):

$$OD_{i,\nu} = \frac{3 \cdot \text{IWP}}{D_{ei}\rho_i} \frac{\langle Q_{ei} \rangle_\nu}{2} = OD_i \frac{\langle Q_{ei} \rangle_\nu}{2} \quad (6)$$

where $\rho_i = 917 \text{ Kg m}^{-3}$ is the ice density and $\langle Q_{ei} \rangle_\nu$ the average extinction efficiency at the wavenumber ν . The optical coefficients as a function of L are were taken from the database provided by Yang et al. (2013). From Eq. (6), by setting $\langle Q_{ei} \rangle_\nu = 2$ since this factor can be assumed constant because of the large size parameters ($\frac{\pi D_e}{\lambda}$), usually greater than 20 at the typical visible wavelengths, the OD_i is was obtained as follows:

$$OD_i = \frac{3\text{IWP}}{\rho_i D_{ei}} \quad (7)$$

Now we show that within the particle size range of MRR sensitivity, the PSD has in general a very low variability with respect to the crystal habit assumed in the range 600–2000 μm . The modal radius L_m of the PSD in Eq. (1) can be directly derived from the D_{ei} as shown on the left side of Fig. 5, while the intercept N_o can be obtained by using the expression of the ice water path (IWP):

$$\text{IWP} = \Delta z \cdot \text{IWC} = \Delta z \cdot \rho_i \int_{L_{min}}^{L_{max}} V(L)n(L)dL \quad (8)$$

230 with $\Delta z = z_t - z_b$ the cloud thickness, the IWC is denoted the average Ice Water Content along the cloud layer, and z_t and z_b denote the cloud top and bottom heights (CTH, CBH), respectively, which can be that were estimated from the lidar signal by applying the polar threshold (PT) algorithm (Van Tricht et al., 2013). Thus, by replacing Eq. (1) in Eq. (8) and using Eq. (7) yieldsto:

$$N_o(L_m) = \frac{OD_i \cdot D_{ei}}{3\Delta z \cdot C(L_m)} \quad (9)$$

235 expressed in $[m^{-3}mm^{-8}]$ and the volume factor $C(L_m)$ is given by:

$$C(L_m) = \int_{L_{min}}^{L_{max}} V(L) L^7 e^{-10 \frac{L}{L_m}} dL \quad (10)$$

with $V(L)$ defined as the volume of the crystals as used a function of length as in Eq. (2). This result is was obtained by assuming the optical depth and the effective diameter constant in the cloud in Eq. (9) and equal to average values.

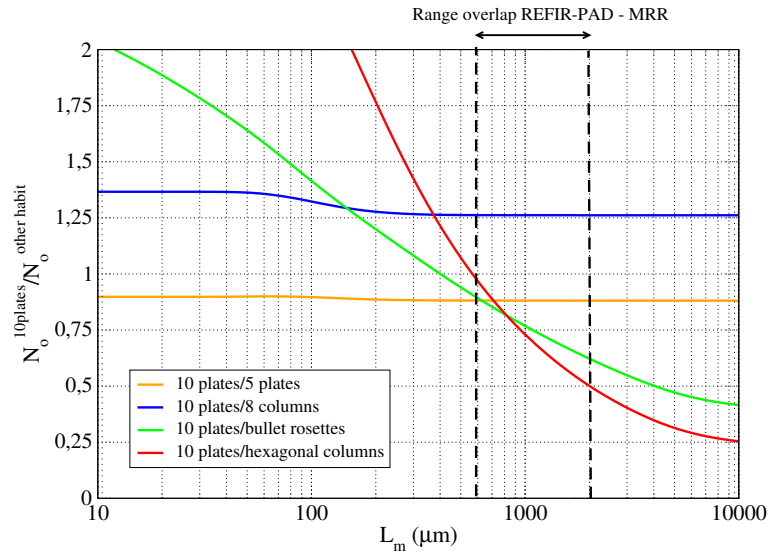


Figure 8. Curves of the ratio between the intercept (N_o) calculated from Eq. (9) for 10 plates aggregates with respect to those of the other habits of Fig. 6 and 5 as a function of L_m .

Fig. 8 shows the curves of the ratio between the intercept (N_o) calculated from Eq. (9) for 10 plates aggregates with respect to those of the other habits of Fig. 6 and 5 as a function of L_m . We can see that in Note that the range of L_m between 500 about 600 and 2000 μm , where the sensitivity of REFIR-PAD and MRR overlaps, the ratios are close to 1 showing a similar behaviour mostly overlaps, represents the interval where the ratio is minimized, reaching a maximum deviation of about 50% for the hexagonal columns.

The retrieval of the cloud properties was performed by using the Simultaneous Atmospheric and Cloud Retrieval (SACR) (Di Natale et al., 2020), which is ~~a~~ composed of a forward model (FM) and a retrieval code based on ~~the~~ an optimal estimation (OE) approach. The downwelling spectral radiance ~~is~~ was simulated in the spectral band between 200–980 cm^{-1} (10–50 μm) through the FM as a function of the atmospheric profiles and the cloud parameters, such as the optical depth and the effective diameter. By using the entire band we can retrieve ~~all~~ a number of the atmospheric variables, since the infrared spectrum shows strong sensitivity to water vapour in the spectral region between 230–600 cm^{-1} (16–43 μm), to the temperature in the band centered at 667 cm^{-1} (15 μm), to the cloud optical depth in the atmospheric window, between 820–980 cm^{-1} (10–12 μm), and to the particle size below 600 cm^{-1} (above 16 μm).

When liquid supercooled water exists overhead, the retrieval algorithm switches to the mixed-phase clouds retrieval (Di Natale et al., 2021; Turner et al., 2003), where the ice fraction (γ) ~~is~~ was also retrieved together with the effective diameter of the water droplets (D_{ew}) in suspension. The ice fraction is defined as (Yang et al., 2003b):

$$\gamma = \frac{\text{IWP}}{\text{IWP} + \text{LWP}} \quad (11)$$

where LWP is the Liquid Water Path and, in case of only-ice phase, LWP = 0 and γ ~~is~~ was set to 1. In the presence of liquid content D_{ew} ~~is~~ was calculated as follows:

$$D_{ew} = 2 \frac{\int_{R_{\min}}^{R_{\max}} R^3 n(R) dR}{\int_{R_{\min}}^{R_{\max}} R^2 n(R) dR} \quad (12)$$

where R is the radius of the droplets and the size distribution $n(R)$ is still a Γ -function like for the ice. The liquid water optical depth (OD_w) ~~is~~ was derived from Eq. (7) by using the parameters for water (LWP, D_{ew}) and the density $\rho_w = 1000 \text{ kg m}^{-3}$.

Since the profiles of water vapour and temperature ~~are~~ were retrieved simultaneously with the cloud parameters, the final state vector used in the retrieval is given by (Di Natale et al., 2021):

$$\mathbf{x} = (D_{ei}, \text{OD}_i, \mathbf{U}, \mathbf{T}, \Omega, \beta) \quad (13)$$

for the only-ice case and, by defining the total optical depth $\text{OD} = \text{OD}_i + \text{OD}_w$, becomes:

$$\mathbf{x} = (D_{ei}, D_{ew}, \text{OD}, \gamma, \mathbf{U}, \mathbf{T}, \Omega, \beta) \quad (14)$$

in for the case of mixed phase clouds, where \mathbf{U} and \mathbf{T} represent the vectors which contain the profile fitted levels of water vapour and temperature (7 for water vapour and 4 for temperature) at fixed pressure levels; Ω is the internal solid angle of the beam divergence which determines the formulation of the Instrument Line Shape (ILS) and it ~~is also fitted in order~~ was

270 also fitted to take into account the effect of self-apodization; finally, β is a scale factor on the frequency grid introduced to compensate for possible drift of the REFIR-PAD laser reference and for the shift due to the internal finite aperture (Bianchini et al., 2019; Di Natale et al., 2021).

SACR uses a Levenberg-Marquardt iterative algorithm to minimize the cost function (Rodgers, 2000):

$$\chi^2 = (\mathbf{y} - \mathbf{FM}(\mathbf{x}))^T \mathbf{S}_y^{-1} (\mathbf{y} - \mathbf{FM}(\mathbf{x})) + (\mathbf{x} - \mathbf{x}_a)^T \mathbf{S}_a^{-1} (\mathbf{x} - \mathbf{x}_a) \quad (15)$$

275 with \mathbf{y} and \mathbf{x}_a being vectors of the measurements and a priori parameters, respectively. \mathbf{S}_y denotes the Variance-Covariance Matrices (VCM) of the measurements and contains the REFIR-PAD spectral noise, which is given by the square sum of the Noise Equivalent to Signal Ratio (NESR) and the calibration error (Bianchini et al., 2019). The NESR is calculated from the standard deviation of the four uncalibrated spectra provided during each REFIR-PAD measurement; the calibration error is due to the uncertainty on the temperature of the three black bodies (hot, cold, and reference) used for the radiance calibration
 280 procedure. The \mathbf{S}_a matrix represents the VCM of the a priori errors associated to the a priori state vector \mathbf{x}_a .

The a priori cloud parameters were set to large values equal to 100 μm for the effective diameters and 3 for the optical depth, with a priori error equal to 100%, in order to avoid constraining the retrieval algorithm. We calculated the a priori thermodynamic profiles by interpolating those provided by the daily radiosondes launched at Concordia station routinely made by the Italian meteo Climatological Antarctic Observatory staff. We assumed an a priori error equal to 50% for water vapor
 285 profiles and 1% for temperature profiles with a correlation length equal to 2 km to regularize above 9 m of height (Di Natale et al., 2020) and below 5 km. For heights above 5 km where sensitivity both to water vapour and temperature is-was very low and the information comes mainly from the a priori, a more stringent correlation length equal to 5 km is-was used to regularize the solution. Note that below 9 m, the levels of the a priori profiles are-were considered completely uncorrelated and the radiative contribution is-was mostly given by the temperature and humidity internal to the instrument.

290 The cost function in Eq. ~~(15)~~ 15 is minimized through the OE and the Levenberg-Marquardt iterative formula given by:

$$\mathbf{x}_{i+1} = \mathbf{x}_i + [\mathbf{K}_i^T \mathbf{S}_y^{-1} \mathbf{K}_i + \gamma_i \mathbf{D}_i + \mathbf{S}_a^{-1}]^{-1} [\mathbf{K}_i^T \mathbf{S}_y^{-1} (\mathbf{y} - \mathbf{FM}(\mathbf{x}_i)) - \mathbf{S}_a^{-1} (\mathbf{x}_i - \mathbf{x}_a)] \quad (16)$$

where γ_i is the damping factor at the iteration i , \mathbf{K}_i denotes the Jacobian matrix of \mathbf{FM} and \mathbf{D}_i is a diagonal matrix as described in Di Natale et al. (2020). The convergence is reached when variations on χ^2 are less than 1 ‰. The error of the retrieved parameters is-was obtained with the relationship:

295
$$\mathbf{S}_x = (\mathbf{K}^T \mathbf{S}_y^{-1} \mathbf{K} + \mathbf{S}_a^{-1})^{-1} \quad (17)$$

We considered the retrievals good unless we-have-there-was a reduced $\chi_{red}^2 = \frac{\chi^2}{N-M} < 3$, with N number of spectral channels used and M number of retrieved parameters, as done in Di Natale et al. (2020).

The results of Fig. 9 show, as similarly done in Maestri et al. (2019), the retrievals performed with the different habits averaging the differences between the REFIR-PAD radiances and the simulated spectra in 28 microwindows reported in Turner

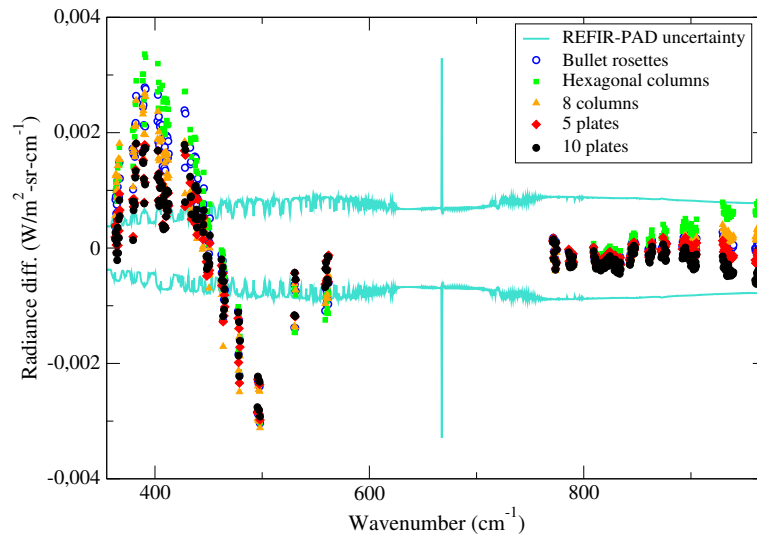


Figure 9. Comparison with respect of the averaged REFIR-PAD instrumental uncertainty (turquoise curves) of the mean differences between the measurements and the simulated spectra calculated in 28 selected microwindows reported in (Turner et al., 2003) for various ice crystal habits.

300 et al. (2003), chosen between 360 and 970 cm^{-1} . We found that the aggregates of 10 plates show the best agreement with the measurements, with the lowest χ_{red}^2 .

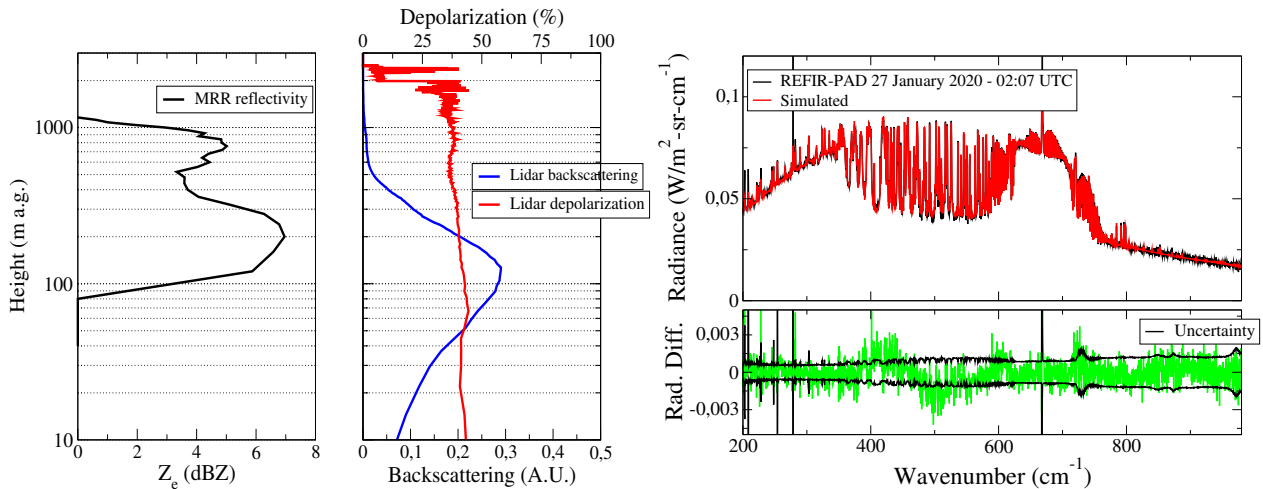


Figure 10. Left panel: reflectivity profiles provided by the MRR on the day 27 January 2020 at 02:07 UTC. Middle panel: backscattering (blue curve) and depolarization (red curve) lidar profiles. Right upper panel: comparison of a REFIR-PAD measurement (black curve) at 808:24 UTC on 10 December 2020 with the simulated spectra at the last iteration (red curve). Right lower panel: comparison of the differences between the measured and the simulated spectrum (green curve) with the instrumental noise (black curve).

The left panel of Fig. 10 shows an example of the measurement of vertical reflectivity provided by the MRR on 27 January 2020 at 02:07 UTC, together with the lidar and REFIR-PAD measurements. The middle panel shows the lidar backscattering signal in arbitrary units (blue curve) and the depolarization (red curve). When the depolarization is higher than 15% the cloud is classified as ice cloud as described in Cossich et al. (2021). The right upper panel reports the REFIR-PAD measurement (black curve) in comparison with the simulated spectrum (red curve); the right lower panel shows the differences (green) in comparison with the instrumental uncertainty (black). The plot shows a very good agreement between the measurement and the simulation; the retrieval provides $D_{ei} = (121 \pm 4) \mu\text{m}$, $L_m = (994 \pm 33) \mu\text{m}$, $OD_i = (1.270 \pm 0.004)$, and $\chi_{red}^2=1.3$.

A direct retrieval of the optical extinction or ice fraction from the lidar measurements was not possible due to the high noise of the signal above the cloud top heights, which does not allow the application of a retrieval algorithm such as the Klett method. These lidar measurements represent qualitative data, which allow identifying the occurrence of clouds and assessing their position and the presence of ice and supercooled water.

4 Results and discussion

Fig. 11 shows the scatter-plots of L_m - N_o and the OD_i - D_{ei} retrieved from REFIR-PAD (black circles). From these parameters, L_m and N_o values were obtained and they allowed to obtain the PSD from Eq. (1), expressed in $\text{m}^{-3}\text{mm}^{-1}$. These values were which was used to derive the effective reflectivity Z_e at 24 GHz for the comparison with the MRR: the green circles in Fig. 11 denote the points detected by the MRR with reflectivity higher than -5 dBZ. We can see that the modal radius L_m of the maximum crystal length distribution varies mostly between 600–2000 μm . D_{ei} retrieved with REFIR-PAD mostly ranged between 20–250 μm ; the intercept N_o mostly stays in the range 10^4 – $10^{10} \text{m}^{-3}\text{mm}^{-8}$, but those detected also by the MRR stayed above 70 μm .

The retrieved ODs from REFIR-PAD measurements. Right panel: scatter plot between spectra over all the analysed data spanned mostly in the ice optical depth (OD_i) broad range between 0.1 and 5, as we can see from Fig. 11. In Fig. 12 is shown the variability in the REFIR-PAD spectra because of the optical depth during the day 23 July 2019.

The average crystal length can be calculated through the retrieved PSD as:

$$L_{av}^{\text{REFIR}} = \frac{\int_{L_{min}}^{L_{max}} L \cdot n(L) dL}{\int_{L_{min}}^{L_{max}} n(L) dL} \quad (18)$$

This value was used for the comparison with the crystal size estimated from the ICE-CAMERA measurements. The uncertainty is was calculated by propagating the retrieval error in Eq. (18) and the one coming from the error in evaluating the CTH

Left panel: scatter plot between the intercept N_o and the modal radius L_m of the particle size distributions retrieved from

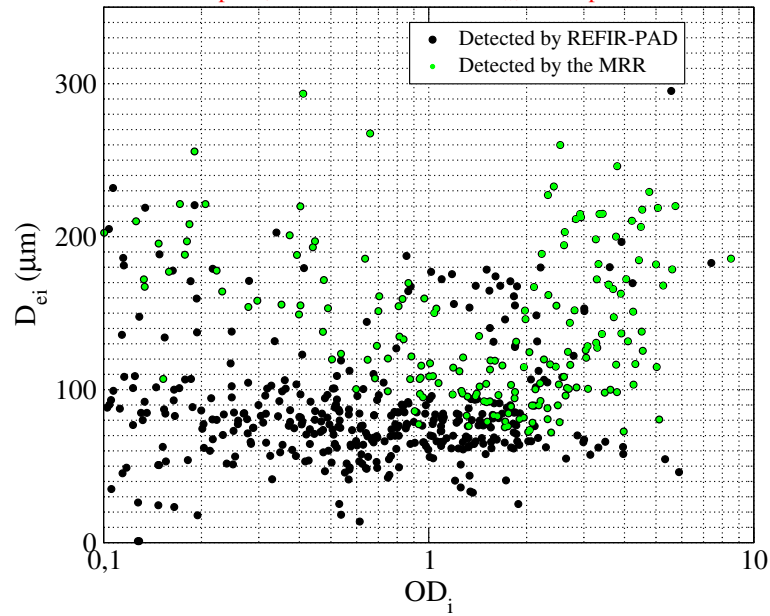


Figure 11. Variability of the retrieved ice optical depth (OD_i) as a function of the effective diameter (D_{ei}). The green circles denote the values detected also by the MRR.

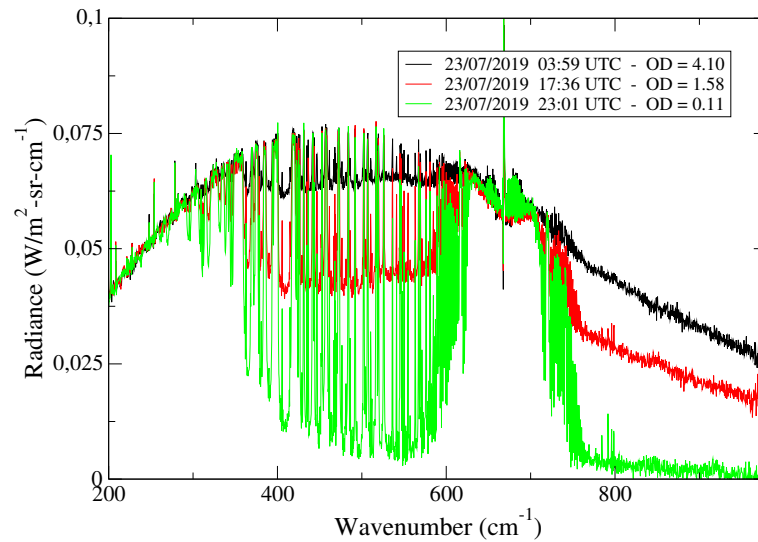


Figure 12. Variability of the ice effective diameter (D_{ei}). The green circles denote the points cloudy spectra detected by MRR-REFIR-PAD during the day 23 July 2019.

with the PT algorithm, which can be as large as 500 m in the worst cases. The CBH is-was considered not affected by error
 330 since it is-was always very close to the ground because we are-were treating precipitating events. If we indicate:

$$f_{l+1+l+1,\mu}(L_m) = \int_{L_{min}}^{L_{max}} L^{7+l\mu+l} e^{-10\frac{L}{L_m} - (\mu+3)\frac{L}{L_m}} dL \quad \text{with } l = 0, 1 \quad (19)$$

the uncertainty $\Delta L_{av}^{\text{REFIR,ret}}$ due to the retrieval error turns out to be:

$$\Delta L_{av,\mu}^{\text{REFIR}} = \sqrt{\left| \frac{\partial L_{av}^{\text{REFIR,ret}}}{\partial f_1} \right|^2 \Delta f_1^2 + \left| \frac{\partial L_{av}^{\text{REFIR,ret}}}{\partial f_2} \right|^2 \Delta f_2^2} \sqrt{\left| \frac{\partial L_{av}^{\text{REFIR,ret}}}{\partial f_{1,\mu}} \right|^2 \Delta f_{1,\mu}^2 + \left| \frac{\partial L_{av}^{\text{REFIR,ret}}}{\partial f_{2,\mu}} \right|^2 \Delta f_{2,\mu}^2} \quad (20)$$

with

$$335 \quad \Delta f_{l+1+l+1,\mu} = \frac{10\Delta L_m}{L_m^2} \int_{L_{min}}^{L_{max}} L^{8+l\mu+1+l} e^{-10\frac{L}{L_m} - (\mu+3)\frac{L}{L_m}} dL \quad \text{with } l = 0, 1 \quad (21)$$

where ΔL_m denote the retrieval error of L_m .

The uncertainty $\Delta L_{av}^{\text{REFIR,CTH}}$ due to the CTH error is-was calculated by repeating the retrieval for each measurement increasing and decreasing this latter by 500 m; the maximum deviation from the original value of L_{av}^{REFIR} is-was considered its associated uncertainty. The total uncertainty is-was finally calculated as follows:

$$340 \quad \Delta L_{av,\mu}^{\text{REFIR}} = \sqrt{|\Delta L_{av}^{\text{REFIR,ret}}|^2 + |\Delta L_{av}^{\text{REFIR,CTH}}|^2} \sqrt{|\Delta L_{av,\mu}^{\text{REFIR}}|^2 + |\Delta L_{av}^{\text{REFIR,CTH}}|^2} \quad (22)$$

where $\mu = 0, 1, 2$ in our analysis.

4.1 Derivation of the equivalent radar reflectivity at 24 GHz

We can calculate the effective reflectivity at the MRR wavelength $\lambda = 12.37$ mm (24 GHz) by using the PSD retrieved from REFIR-PAD in the following formula (Eriksson et al., 2018; Tinel et al., 2005):

$$345 \quad Z_e^{\text{REFIR}} = \frac{\lambda^4}{\pi^5 K_w^2} \int_{L_{min}}^{L_{max}} \sigma_{\lambda,h}(L, T_{cld}) n(L) dL \quad (23)$$

where $K_w^2 = 0.92$ is the dielectric constant of water and $\sigma_{\lambda,h}(L, T_{cld})$ is the backscattering cross section in [m²] for the habit h at wavelength λ , T_{cld} in [K] is the cloud temperature, and L in [mm] as provided by the Eriksson et al. (2018) microwaves

scattering database, which we name for simplicity EMD (for Eriksson Microwave Database). We set L_{max} equal to 10 mm as for the FIR properties and Z_e is expressed in $[\text{mm}^6\text{m}^{-3}]$.

350 The backscattering cross sections are tabulated for 34 different habits, including liquid spheres and spherical graupel, and 17 of them are classified as single crystals, 3 habits represent heavily rimed particles, and the remaining habits are aggregates of different types, including snow and hail. Even though the particle sizes vary considerably among the habits, and the maximum length of 10 and 20 mm are typical values for the largest single crystal and aggregate particles, respectively, we limited the integral in Eq. (23) up to a cut-off value equal to 10 mm, corresponding to the maximum crystal length of the Yang et al. (2013) 355 FIR database. The EMD is compiled with a broad coverage in frequency (1–886 GHz) for 3 values of temperature (190, 230 and 270 K), so that the final value can be obtained by interpolating. The temperature T_{cl} was calculated from the temperature profiles retrieved with SACR and the bounding heights CBH and CTH of the precipitating clouds.

The Z_e measured by the MRR was averaged along the vertical path in order to ~~provided~~ provide a parameter to compare with those retrieved from REFIR-PAD observations, which in turn represents an average over the cloud thickness:

$$360 \quad Z_e^{\text{MRR}} = \frac{\int_{z_b}^{z_t} Z_e(z) dz}{\Delta z} \quad (24)$$

where z is the height.

Table 1. ~~Summary of the parameters obtained~~ Crystal habits used from ~~the comparison of the REFIR-PAD~~ Eriksson et al. (2018) database and ~~MRR reflectivity~~ their corresponding index in Fig. 13.

<u>Index</u>	<u>Habit name</u>
<u>1</u>	
Long Columns <u>2</u>	
<u>3</u>	
<u>4</u>	
<u>5</u>	
Block Columns <u>253-10.31</u> <u>6</u>	
Short Columns <u>176-5.71</u> <u>7</u>	
<u>AGGREGATES</u> <u>8</u>	Large Block Aggregate <u>136-1.62-0.31</u> Large Column Aggregate <u>17-0.87-0.17</u> Large Plate Aggregate <u>123-1.24-0.2</u>
5-Bullet Rosette <u>72-1.382</u> <u>9</u>	
6-Bullet Rosette <u>89-1.586</u> <u>10</u>	
Flat-3-Bullet Rosette <u>18-1.273</u> <u>11</u>	
Flat-4-Bullet Rosette <u>25-0.985</u> <u>12</u>	
<u>13</u>	
<u>14</u>	
<u>15</u>	
<u>16</u>	

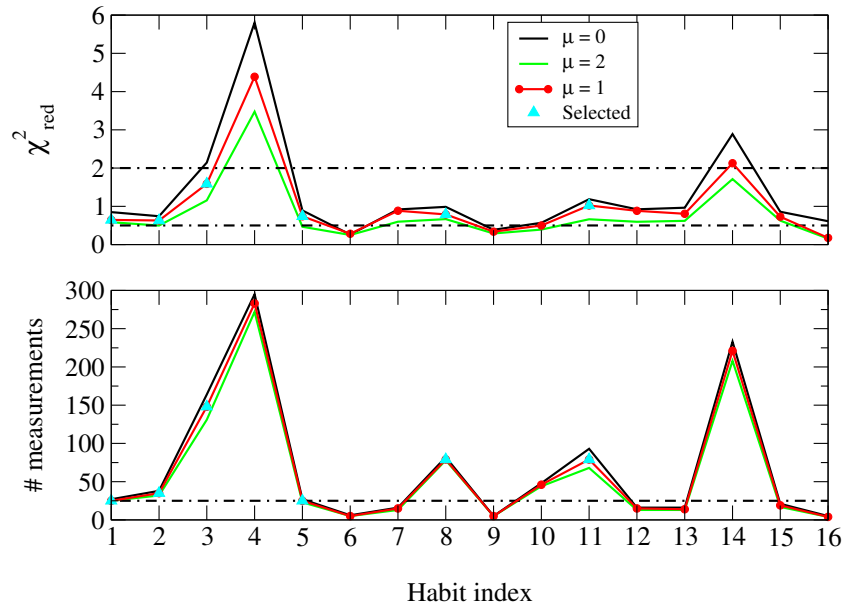


Figure 13. Upper panel: reduced χ_{red}^2 calculated from the Z_e retrieved from REFIR-PAD and those measured by the MRR by assuming $\mu = 0, 1, 2$ (green, blue, red curves). Lower panel: number of measurements above the -5 dBZ threshold assumed for the analysis.

Only MRR Z_e values above -5 dBZ were analyzed and included in the analysis, since below this value the results are were not considered sufficiently reliable (Maahn and Kollias, 2012; Souverijns et al., 2017). In Table 1, we show results for all column-like, aggregates-like, and bullet rosette-like habits in EMD: the Fig. 13, in the upper panel were reported the reduced χ_{red}^2 obtained from the Z_e retrieved from REFIR-PAD and those measured by the MRR by assuming $\mu = 0, 1, 2$ (green, blue, red curves) and considering their respective retrieval errors; in the lower panel are shown the total number of measurements (N) available considering the cut off at -5 dBZ. On the x-axis we reported the habit index explained in Table 1. To select the best habits we adopted the criteria of having the χ_{red}^2 close to 1 and maximise the number of observations of REFIR-PAD measurements in coincidence with MRR which provide $Z_e > -5$ dBZ, the reduced χ_{red}^2 , calculated considering the total error obtained for Z_e^{MRR} and $Z_e^{REFIR-PAD}$, and the correlation index r^2 between the MRR-observed and REFIR-PAD derived reflectivity measurements by assuming some thresholds (dashed black lines in Fig. 13): we required that N had to be greater than 25 and χ_{red}^2 had to stay between 0.5 and 2, since when it decreases too much usually indicates that the associated error is overestimated. The selected cases that complied the criteria were identified with cyan triangles. From Fig. 13 we can see that there is no much difference by varying μ in the range 0–2 for the selected cases, so that we assumed as average value $\mu = 1$ for the next considerations.

We see that the habits which maximize the number of points and r^2 , and also minimize the χ_{red}^2 , are the long columns and the thin columns for the column-like habits, the large block and large plate aggregates for aggregate-like habits, and The habits that showed best accordance with the radar measurements were the 5/6 bullet rosette for bullet rosette-like habits. However,

Scatter-plots of the Z_e measured by the MRR and those retrieved from REFIR-PAD obtained by using the habits from Eriksson et al. (2018) database which provide the best accordance: long columns, block columns aggregate and 5 bullet rosette:

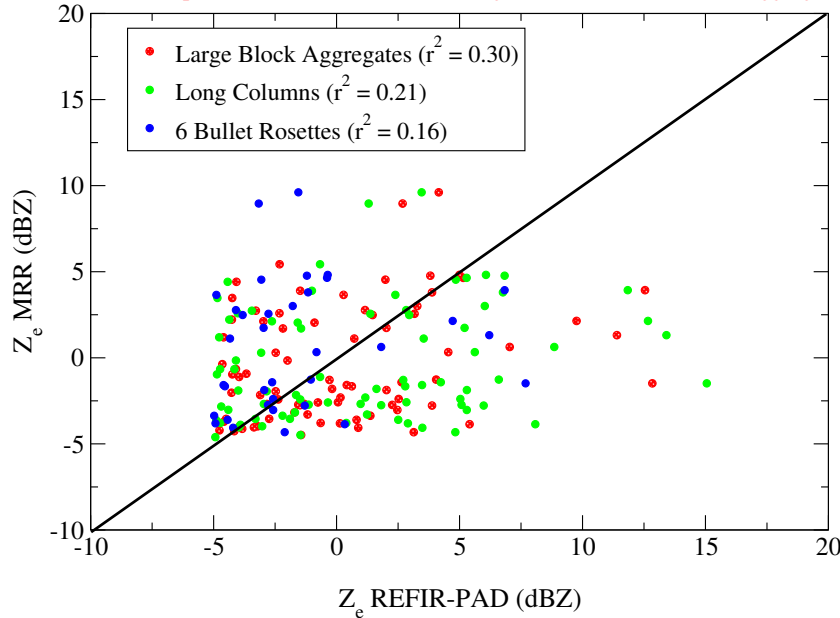


Figure 14. Scatter-plots of the Z_e measured by the MRR and those retrieved from REFIR-PAD by assuming $\mu = 1$ and by using the habits from Eriksson et al. (2018) database that provided the best accordance: long columns, large plates aggregates and 6 branches bullet rosettes.

the habits which maximize the number of points are the branches bullet rosettes, the thin and long columns and the aggregates. Figure 8 columns/large block aggregates. Fig. 14 shows the comparison of the MRR measured reflectivity with those obtained from REFIR-PAD by using some of the habits from EMD that provide the best match.

Finally, it in Table 1 that provided the best agreement. The high occurrence of hexagonal columns, aggregates and bullet rosettes was confirmed by the ICE-CAMERA photographs. In particular, the high occurrence of hexagonal columns was corroborated by the presence of 22° halos detected by the co-located HALO-CAMERA sky images as shown in previous studies at South Pole by Lawson et al. (2006). It also should be noted that while the correlation coefficient turns turned out to be moderate (maximum ~ 0.403), this is was mostly due to the difficulty to retrieve of retrieving with good accuracy the shape of the PSD from the FIR observations, and in particular the intercept N_o , for large particle sizes, and mostly because of the need of increasing the number of measurements for improving the statistical distribution. However, the results indicate that in the particle size range between around about 600 and 2000 μm , the retrieval algorithm is was able to estimate the intercept with a correct order of magnitude as suggested by Fig. 14 assuming the dispersion coefficient μ in the range 0–2, as shown in Fig. 14. The distributions of the retrieved N_o converted in cm^{-5} and the slope $\Lambda = (3 + \mu)/L_m$ in cm^{-1} as a function of the retrieved cloud temperature (T_{cloud}), were found in very good accordance with those found in Heymsfield et al. (2013, 2002) and Wolf et al. (2019) and they were shown in Fig 15, left and right panels, respectively. Note that N_o varied mostly between

395 10^{-2} – 10^4 cm^{-5} , while Λ mostly between 20–200 cm^{-1} . The average relative error found for N_o was equal to 20%, which was comparable to the systematic error due to the assumption of a specific habit in the retrieval as shown in Fig. 8.

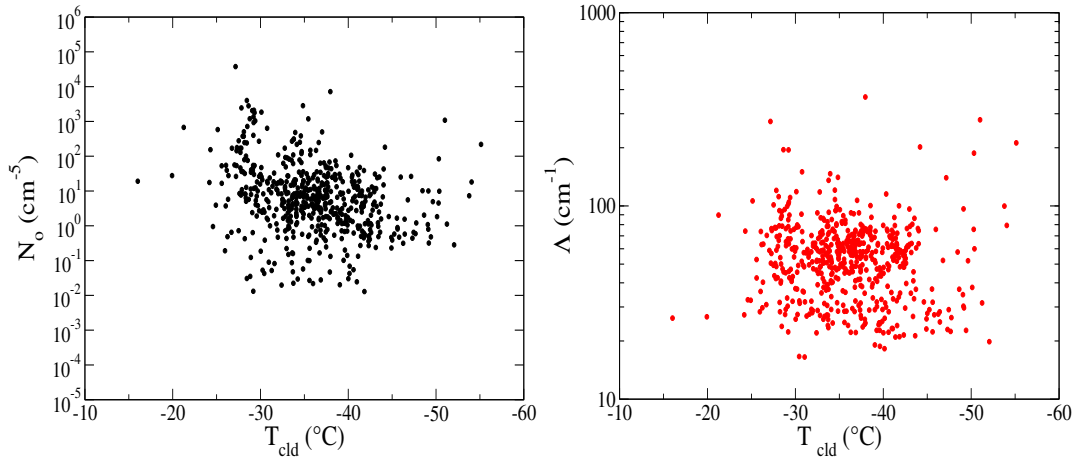


Figure 15. Left and right panels: intercept N_o and slope Λ as a function of the cloud retrieved temperature (T_{cld}).

4.2 Assessment of particle size and habit from ICE- and HALO-CAMERA

An average length of the ice crystals falling on the ICE-CAMERA screen can be defined by the area of the bounding box (A_{box}) containing the crystal itself as shown in Figs. 20 and 25 (red boxes). This parameter represents the diameter of the crystal with the projected area equal to the bounding box and it ~~is~~ was calculated in μm (1 image pixel = 7 μm) by averaging
 400 ~~all-over-over all of~~ the acquired crystals at the i -th scanning through the formula:

$$L_{\text{av}}^{\text{ICE-CAMERA}} = \frac{14}{N_c} \sum_{i=1}^{N_c} \sqrt{\frac{A_{\text{box},i}}{\pi}} \quad (25)$$

where N_c is the number of crystals acquired at the i -th scanning. The corresponding uncertainty is given by:

$$\Delta L_{\text{av}}^{\text{ICE-CAMERA}} = \frac{7\Delta A_{\text{box}}}{N_c\sqrt{\pi}} \sqrt{\sum_{i=1}^{N_c} \frac{1}{A_{\text{box},i}}} \quad (26)$$

where $\Delta A_{\text{box}} = \Delta A_{\text{box},i} \simeq 5$ pixel $\forall i$ is the uncertainty in pixel associated to each bounding box.

405 4.3 Selected days for case studies

We selected four days ~~on-in~~ 2020 among all analysed data, specifically 23/24 February and 21/24 April, when most of the measurements from the different instruments were simultaneously available, ~~in-order~~ to be able to operate a ~~specifie~~ comparison

with the retrieved particle sizes. From the retrieved temperature profiles we assessed the average in-cloud temperatures by weighting the profiles with the corresponding backscattering lidar signal. The temperature varied between $-20\text{ }^{\circ}\text{C}$ and $-40\text{ }^{\circ}\text{C}$ and on average was found to be $-28\text{ }^{\circ}\text{C}$. Specifically for the cases discussed hereafter, the average temperatures turned out to be $-30\text{ }^{\circ}\text{C}$ during the days 23/02, 24/02 and 23/04, while during the day 21/04 equal to $-25\text{ }^{\circ}\text{C}$.

In Fig. 16 we show the plot of four retrieved temperature profiles (colored lines on the left panel) at the date reported in the label. We can see the inversion of the temperature typical of the Antarctic Plateau at around 750 m above the ground, while the ground peak corresponds to the internal temperature of the REFIR-PAD instrument, since it was treated as a separated environment in the retrieval procedure as already mentioned. We can also see that only on the 21/04/2020 the inversion of the temperature reached the $-6\text{ }^{\circ}\text{C}$ at around 1000 m. On the right panel, we have also reported the backscattering lidar profiles which show that the precipitating clouds occurred for these cases below 500 m.

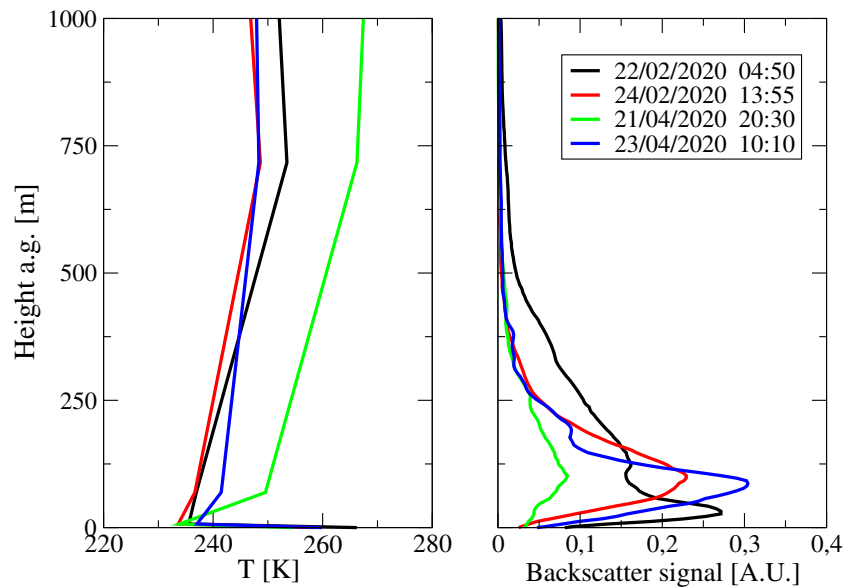


Figure 16. Left panel: retrieved temperature profiles during the selected days of measurement. Right panel: backscattering lidar signal in arbitrary units for the analysed measurements.

4.3.1 Days 23 and 24 February 2020

The MRR reflectivity time-height cross-section for the selected days 23 and 24 February 2020 are shown on the left side upper panel of Fig. 17. The data are were not continuous because of the filtering procedure due to the sensitivity of the MRR to the largest particles. The corresponding color map of the backscattering and depolarization lidar signals are also shown on the right of the same figure Fig. 17. The depolarization lidar shows that precipitation starts from the passage of ice clouds. The figure between 02:00–04:00 UTC, when larger ice crystals formed as detected by the MRR signal, which reached a few dBZ above 0. Then the precipitations continued but with smallest particles, in fact the MRR signal decreases rapidly. On 24 February

425 an intense precipitation started at 07:00 UTC and finished at about 22:00 UTC; this was composed of larger crystals as clear from the MRR signal in the upper panel of Fig. 18, in particular the signal reached about 3 dBZ at 11:30, 14:30 and 18:30 UTC. Fig. 18 also shows the comparison of the average crystal length (L_{av}) retrieved from REFIR-PAD infrared spectra (red diamonds) with those obtained from the ICE-CAMERA (blue dots). Continuous MRR measurements and ICE-CAMERA data were available ~~for the majority most of the time~~ of both days as shown in Fig. 17.

430 Mixed-phase clouds ~~did appear~~ passed above the site on 23 February between ~~8–9 UTC and 12–13 UTC, where the presence of supercooled water is~~ 08:00–09:00 UTC and 12:00–13:00 UTC, when their occurrence was detected by the lidar depolarization signal at around 200 m above the ground ~~-(indicated with black arrows) and, in particular, the supercooled water formed layers of 100 m and 300 m of thickness on the 23 and 24 February, respectively. The average retrieved precipitable water vapor (PWV) was found equal to 1.33 and 0.98 mm on the days 23 and 24 February, respectively, while the average cloud~~
435 temperatures about -40 and -39 °C. The average temperature of the water layers was found equal to -31 °C, which is acceptable since supercooled water can exist down to -40 °C.

In the first mixed-phase cloud time slot, the retrieval provided an average ice fraction γ equal to 0.47 with LWP equal to 0.62 g/m², while in the second time slot values were found equal to 0.56 and 1.5 g/m².

The lower panels in ~~Fig. 17~~ Figs. 17 and 18 indicate that the values of the average crystal lengths retrieved from REFIR-PAD and those estimated from ICE-CAMERA ~~are varied between 700–1200 μm and 700–1000 μm , respectively, and they were mostly~~ in very good agreement for most of the cases, particularly on day 23 February.

~~Ice crystal pictures taken~~

Figs. 19 and 20 show the photographs took by the ICE-CAMERA in Fig. 20 indicates that the majority of the ice particles were at 04:10 UTC and 08:10 UTC on the days 23 and 24 February 2020, respectively. These times were selected because were
445 close to the strong precipitations detected both by the lidar and the radar, as we can note from Figs. 17 and 18, when the sun was still rised and generating the halos. In Fig. 21 is also shown the photograph at the 18:03 UTC of the 24 February right before the intense precipitation detected by the lidar and radar (Fig. 18), where we can see the presence of columns aggregates (or clusters) and rimmed rosettes beside the hexagonal columns. The crystal habits were automatically catalogued by the internal algorithm, and labeled with the green labels. The solid column crystal are represented by hexagonal columns (label hexpri) or bullet (label bullet), which are columns with a tip at one end; aggregates (irrgra, clusters) were also found, together with bullet rosettes (rosette) or rimmed rosettes (rimros). In general, some elements needed to be discarded since represent volatile material (label fiberr) produced by the main building of the station.

Ice crystal shown in Fig. 19 on the day 23 February indicate that almost only column-like crystals with some complex aggregates. This is crystals were present. On the contrary, the photograph in Fig. 20 on the day 24 February, shows also a little
455 component of bullet rosettes. The prevalence of hexagonal columns was confirmed by the presence of distinct detection of well distinguishable solar halos in the HALO-CAMERA images at the same times as shown in Fig. 22 for the both mentioned days. In fact, the right panel shows that the phase functions of the smooth columns, aggregate and bullet rosettes ($\sigma_r = 0$) present a strong scattering peak at 22 °, which is responsible for the most intense halos, while for the roughest particles ($\sigma_r = 0.50$) the function is smoother without the peaks; the parameter σ_r reported in Fig. 22 indicates the degree of roughness with

460 larger values denoting rougher particle surfaces, in particular, values 0 (smooth surface), 0.03 (moderate roughness) and 0.50 (severe roughness) were assumed as described in Yang et al. (2013). Since, as found by Forster and Mayer (2022), plate-like and hexagonal column-like crystal have a SCF higher than solid bullet rosettes and columns aggregates, as also confirmed by the measurements performed by Lawson et al. (2006) at South Pole, the presence of the 22 ° confirmed the high occurrence of hexagonal columns.

465 ~~Furthermore, the ICE-CAMERA crystal photographs and the halos recorded by the HALO-CAMERA sky images confirm the best agreement found for columns-like and aggregate-like habits shown in Table 1.~~

4.3.2 Days 21 and 23 April 2020

During 21 ~~and 23 April~~ April 2020, ~~some measurements~~ strong precipitations occurred between 08:00–15:00 UTC and between 17:00–24:00 UTC as we can see from the lidar signal on the lower panel of Fig. 23, while the radar reflectivity reached 5 dBZ.
470 The larger particles formed between 18:00–21:00 UTC as detected by the MRR in the upper panel of Fig. 23. On 24 April, an intense precipitation detected by the backscattering lidar started at 03:00 UTC and continued until 15:00 UTC, while the MRR detected the Doppler signal from 05:30 UTC up to 11:00 UTC showing a strong reflectivity signal around 10:00 UTC.

Some photographs from ICE-CAMERA were available for the comparison as shown in the lower panels of Fig. 24, 25 and 26. Unfortunately, on the 23rd 23rd, only a single ice scan measurement was ~~made~~ actually provided by the ICE-CAMERA at 03:03 UTC and it did not overlap in time with the radar data. However, the comparison ~~for~~ of the 21 April shows a good agreement with the retrieved L_{av} . The MRR reflectivity shows high signal values, up to 8 dBZ, between ~~the~~ 19:00 and 21:00–21:00 UTC ~~for the on~~ 21 April and between the 06:00 and 11:00–11:00 UTC on 23 April. ~~Fig. 25 shows photographs of of ice crystals from the ICE-CAMERA on both days, which most of the ice is column-like crystals and rosettes with some complex aggregates. Also on~~ Also during 21 April, a mixed-phase cloud with supercooled water occurred between ~~17~~ 19:00 and 20:00 UTC at
480 ~~about 1500 and 400~~ 200 m above the ground.

The average retrieved precipitable water vapor (PWV) was found as higher as 2.46 mm for the day 21 April and 1.33 mm on 23 April, while the average cloud temperature was equal to about -33 and -38 °C, respectively. The average temperature of the water layer occurred during the REFIR-PAD and MRR measurements was found equal to -23 °C and it was placed between 200 and 500 m above the ground. In this case γ was found on average equal to 0.58 and LWP equal to 9.5 g/m².

485 From ICE-CAMERA photograph in Fig. 25 we can see that on day 21 April at 19:03 UTC, in the middle of the second precipitation when mixed clouds passed, mostly columnar habits with a minor component of rosettes was present. On 24 April at 03:03 UTC, when the precipitation started and 1 hour and half before the MRR signal was detected, the falling ice crystals were mostly rosettes, as clear from ICE-CAMERA photograph shown in Fig. 26. Unfortunately, for these days the HALO-CAMERA images were not available.

490 5 Conclusions and future perspectives

We presented a new approach to test the consistency of the retrieved ice cloud optical and microphysical properties during precipitating events at Dome-C, Antarctica, obtained from two separated portions of the atmospheric spectrum: in the microwave (24 GHz) the observations were provided by the Micro Rain Radar (MRR) while in the FIR, between ~~200-1000~~200-980 cm^{-1} , the downwelling spectral radiance measurements were performed with the REFIR-PAD Fourier spectroradiometer.

495 The MRR was installed at Dome-C in 2018 and it has been operating in continuous and unattended mode since then. At the same location, the REFIR-PAD and the tropospheric backscattering lidar have been operating continuously since 2011 and 2008, respectively.

Cloud retrieval properties and the parameters of the particle size distributions were obtained from the synergistic use of the far infrared REFIR-PAD radiance spectra and the backscattering/depolarization lidar profiles.

500 The average crystal sizes of the precipitating particles were inferred from the photographs taken by the ICE-CAMERA, also installed at Dome-C. Furthermore, sky images provided by an HALO-CAMERA ~~are~~were used to detect the solar ~~and lunar~~ halos generated by the ice crystals, allowed us to identify and discriminate ~~some type of the hexagonal columns~~ crystal habits responsible for the halos formation.

It is known that the sensitivity of the MRR is limited to the bigger falling particles (a priori estimated around 1 mm), due to the large wavelength (12.37 mm) at which the MRR operates. For this reason, we restricted our study to a set of measurements, for now, over the first 2 years (2019–2020) of the radar measurements when the REFIR-PAD processed data were already consolidated. ~~For~~We exploited the fact that for large ice particles with ~~sizes around 1 mm, the backscattering component of the infrared spectral radiance due to the ground emission is negligible. Furthermore, the dominant absorption component turns out to be independent of the crystal habit~~ effective diameters greater than 80 μm and lower than 250 μm the intercept of the particle size distribution shows a low dependence on the habit type. We modelled the cloud with the aggregate-like crystal habit composed of 10 plates to simulate the radiative transfer and fit the radiance spectra with the Simultaneous Atmospheric and Cloud Retrieval (SACR) code, since for this type of habit the far infrared spectral radiance exhibits higher sensitivity. By analysing the depolarization of the backscattered lidar signal, we were able to ~~assume that only ice was present~~discriminate the presence of only ice or the supercooled water, and to determine the top of the precipitating ice cloud through the Polar
515 Threshold (PT) algorithm.

The retrieval procedure provided the cloud particle effective diameter and optical depth from which we could derive the intercept and the modal radius of the particle size distribution for each observation, which were found spanning in wide ranges between 570–2400 μm and 10^{-2} – 10^4 cm^{-5} , respectively, and found in good agreement with the findings of Heymsfield et al. (2013, 2002). These were used to calculate the effective reflectivity at 24 GHz through the scattering databases
520 of Eriksson et al. (2018), which was then compared with MRR observations. The retrieved particle size distribution was also used to assess the mean length of the ice crystals and was compared with those inferred from the ICE-CAMERA images.

We found the best agreement between the reflectivity derived from the REFIR-PAD retrievals and the MRR observations when hexagonal column-like (long columns and thin columns) ice crystals habits and aggregates-like (8-columns and large

block aggregate) and 5/6 branches bullet rosettes were used in the calculation of the reflectivity at 24 GHz. These habits show
525 ~~a the~~ maximum number of observations with $\chi_{\text{red}}^2 \simeq 1$ and the correlation coefficient ~~$r^2 \geq 0.3$~~ $0.1 < r^2 < 0.3$. Even though the
bullet ~~rosette (5-bullet rosette) habits show a correlation coefficient of 0.37 with rosettes~~ (5/6 branches bullet rosettes) showed
low chi square, the number of observations in accordance with the data ~~is much was~~ lower with respect to the other habits.
The differences arising in the ~~column and aggregates comparison of the reflectivity~~ were mostly due to the difficulty to retrieve
the intercept parameter of the size distribution from FIR spectra in the presence of large particles and the low amount of radar
530 data available at the stage of this work. The high occurrence of hexagonal columns and aggregates was confirmed by the
ICE-CAMERA photographs. In particular, the presence of hexagonal columns was confirmed by the 22° halos detected by the
co-located HALO-CAMERA sky images as shown in ~~previous studies~~ the work by Forster and Mayer (2022) and corroborated
by previous measurements at South Pole performed by Lawson et al. (2006). The agreement of both the retrieved parameters
of the size distribution ~~confirms that they confirmed that the retrieval products~~ correctly reproduced the data.

535 ~~Furthermore, we found agreement in the ice crystal lengths between those derived from the REFIR-PAD retrievals and values~~
~~derived from the~~ The ICE-CAMERA images matrices data were also used to compare the length of the ice crystals with those
retrieved by REFIR-PAD finding a good agreement. These results ~~suggest~~ suggested, based upon the four days of data shown
here, that the MRR has sensitivity to ice crystals as small as about 600 μm of ice crystal length.

Because of the very low sensitivity of the MRR to the smallest particles, a drastic reduction of the data to be processed was
540 necessary, partially limiting the impact of our study. However, as the instruments are all running operationally in an unattended
mode allows us the opportunity to collect a larger dataset, which can be used in future studies for confirming the results
presented in this work and supporting further considerations with wider statistics.

We are confident that by extending the analysis of at least five more years the results would gain in quality and reliability.
Furthermore, still within future perspective, the possibility of collect more retrieval of effective size of the precipitating crystals
545 together with the Doppler velocity provided by the MRR, could allow to derive a new analytic relationship between the particle
fall velocity and diameters, which is still missing for ice crystals as far as we know. This relationship could be used to directly
estimate the size distribution from the radar power spectra.

Author contributions.

GDN conceptualized and designed the methodology and prepared the manuscript. DT conceptualized and designed the
550 methodology. GDN, LP, GB and MDG installed and ran the instruments in Antarctica. AB, LB, LF and GDN prepared and
performed MRR data analysis. GDN performed the REFIR-PAD, LiDAR and ICE-CAMERA data analysis. TM, WC and MM
have contributed to design the methodology and the data analysis. GDN was responsible for the FIRCLOUDS project. All
authors revised the manuscript.

Competing interests. The authors declare that they have no conflict of interest.

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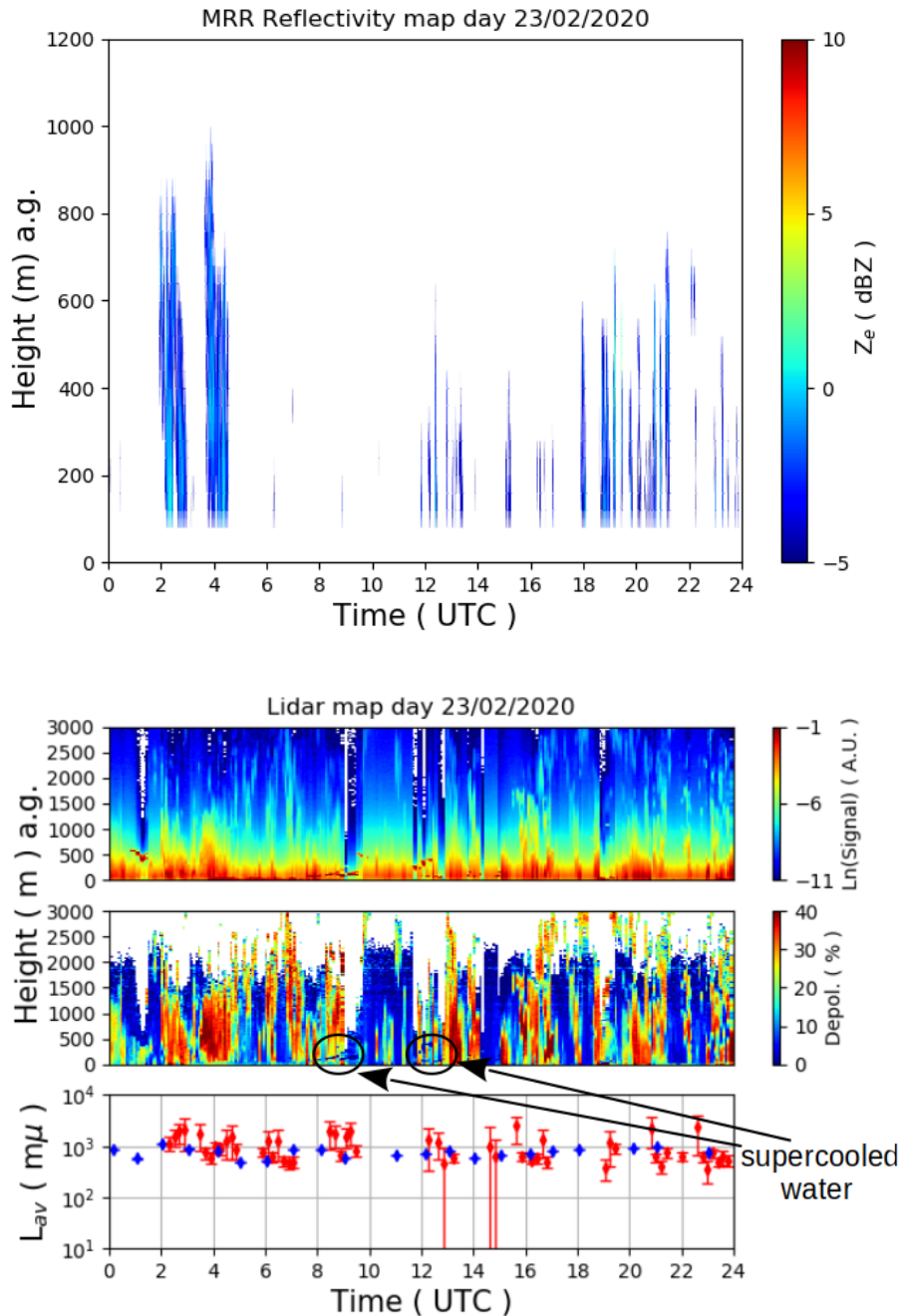


Figure 17. Left-side Upper figure: vertical profiles of reflectivity Z_e in dBZ obtained by the MRR as a function of the UTC time in hours of the days 23 and 24 February 2020. Right-side Lower figure: in the first the upper and second upper middle panels are shown the backscattering and depolarization signals detected by the tropospheric lidar and in the lower panels is shown panel the comparison of the average crystals length of the ice crystals (L_{av}) retrieved from REFIR-PAD spectra (red diamonds) with those estimated from the ICE-CAMERA (blue dots).

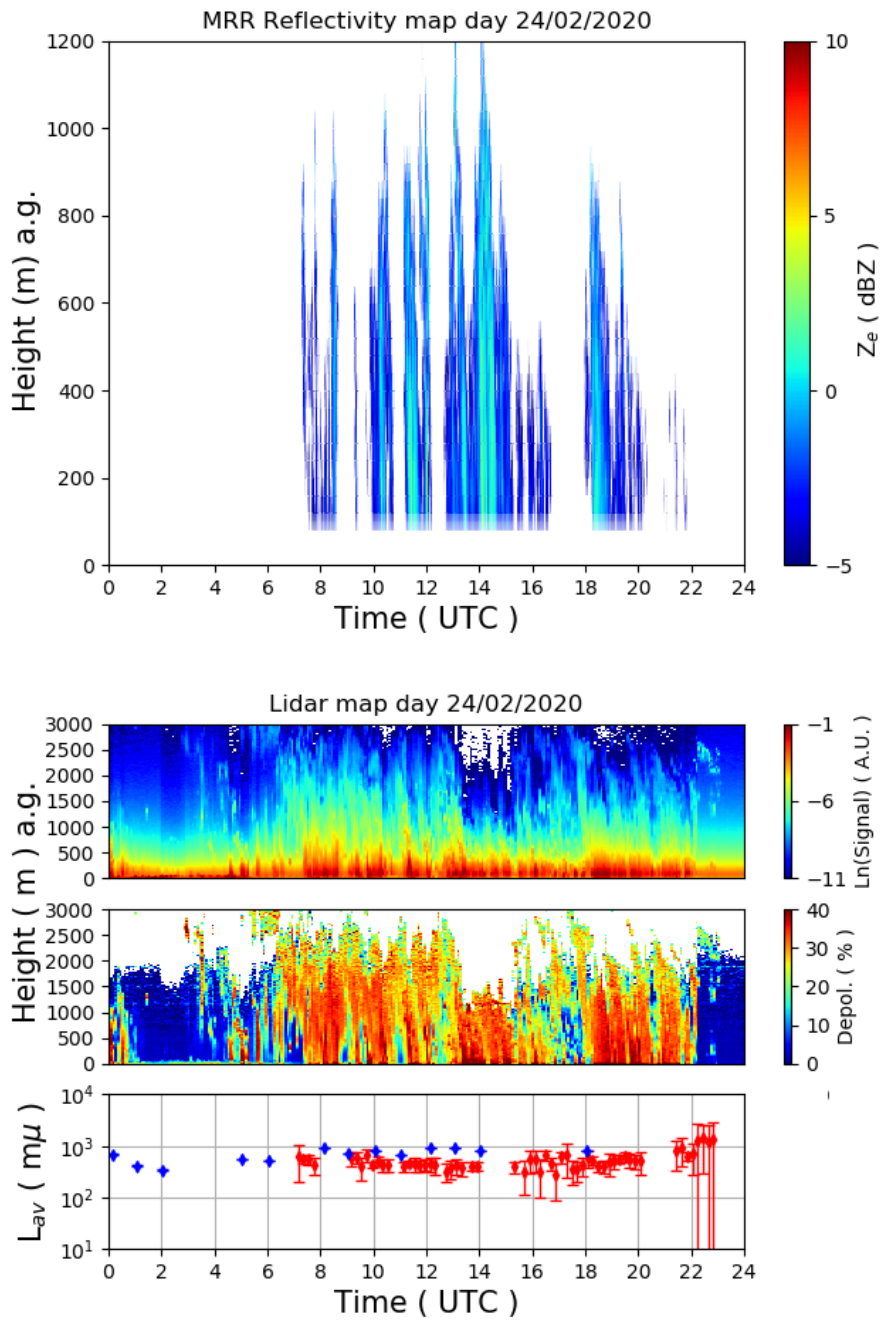


Figure 18. [As in Fig. 17 but for the day 24 February 2020.](#)

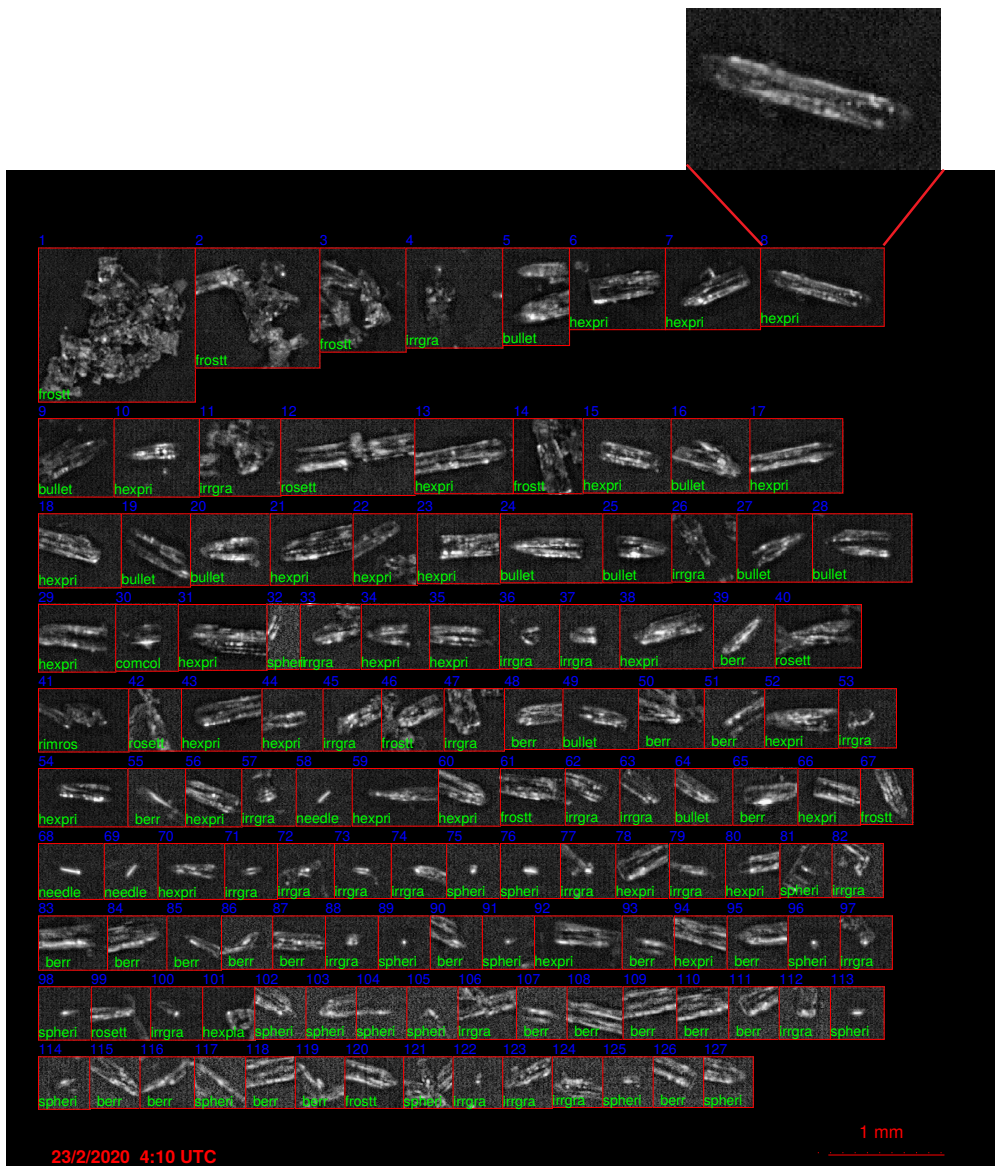


Figure 19. ICE-CAMERA photographs for the days 23 February (left side) and 24 February 2020 (right side) at 04:10 UTC. The photograph indicates the presence of mostly hexagonal columns.

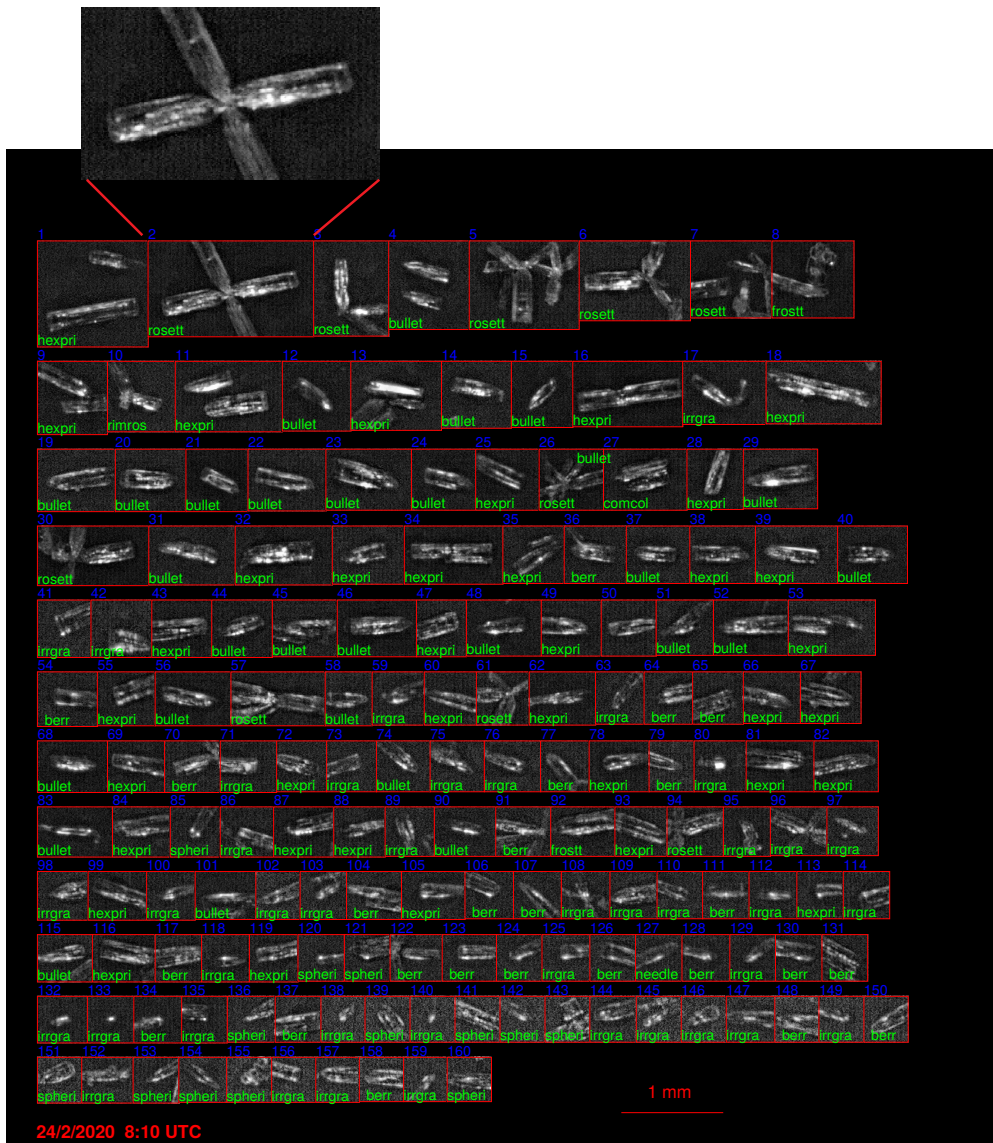


Figure 20. As Fig. 19 but for the day 24 February 2020 at 08:10 UTC. The photograph indicates a large amount of hexagonal columns with a small amount of bullet rosettes is also present. In the upper part the zoom of a single bullet rosette crystal.

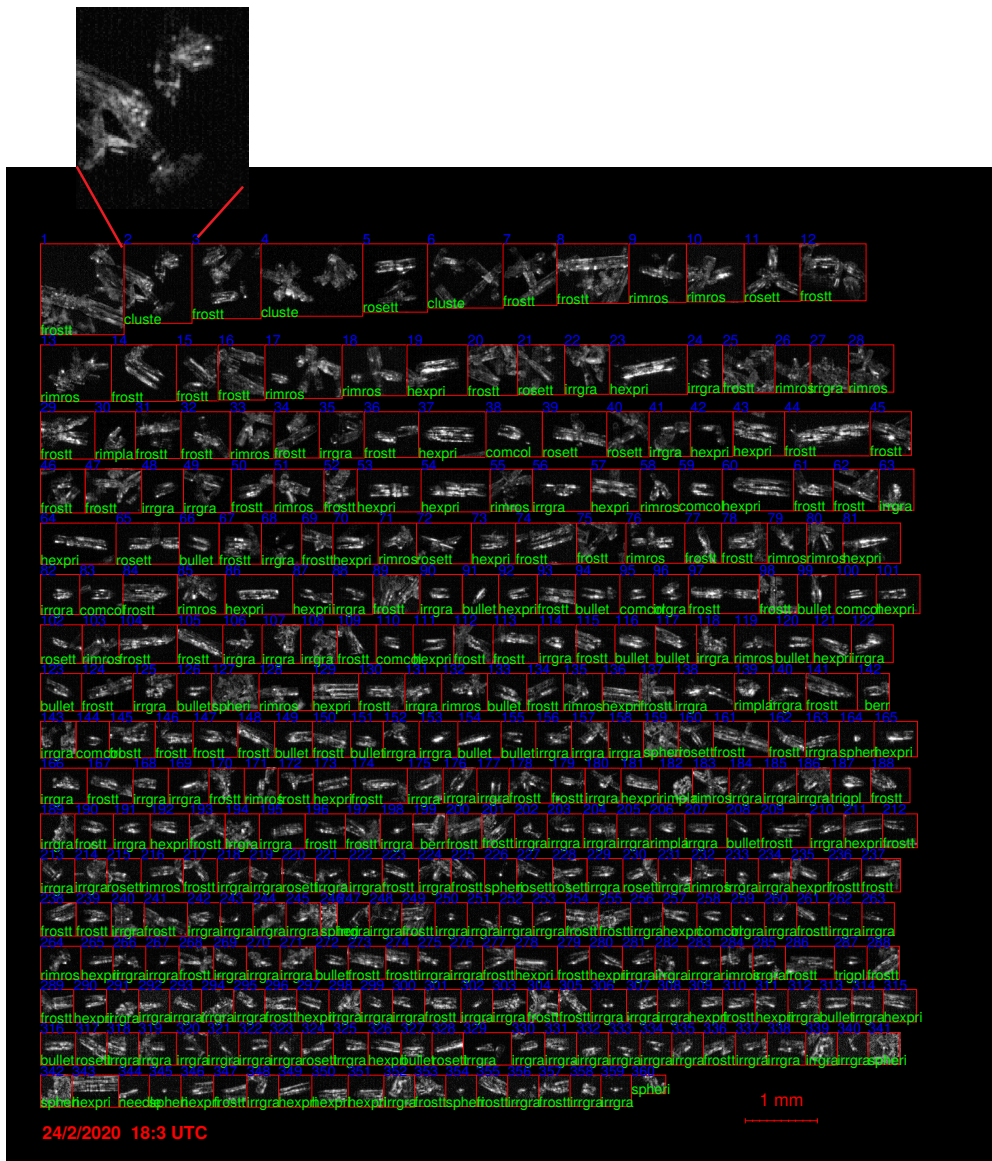


Figure 21. As Fig. 20 still for the day 24 February 2020 but at 18:03 UTC. The photograph indicates a large amount of hexagonal columns and aggregates (or cluster) with a small amount of rimmed rosettes. In the upper part the zoom of an aggregate.

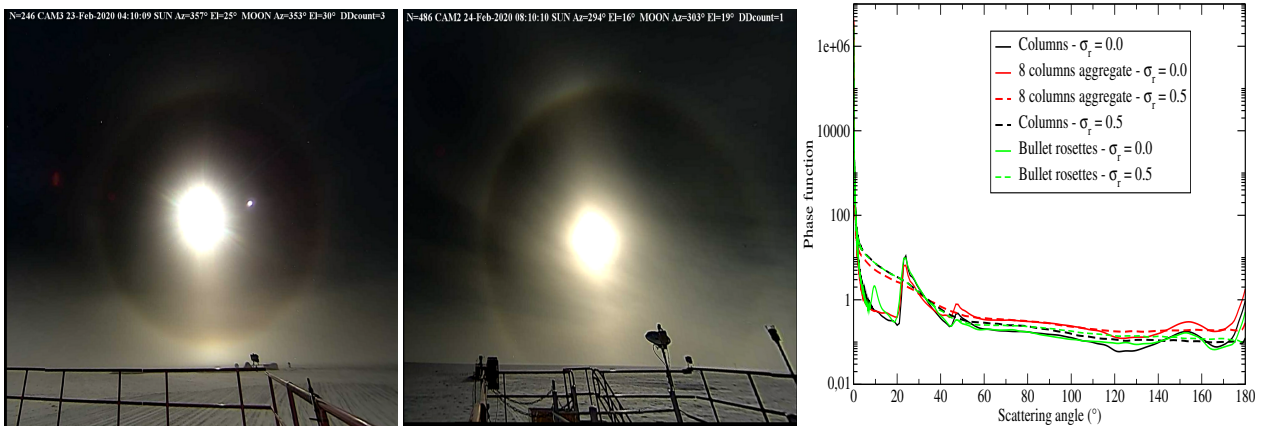


Figure 22. HALO-CAMERA images for the days 23 ~~February~~ (left side) and 24 ~~February 2020~~ (middle) February 2020. On the right side panel the simulated phase functions at 532 nm for the three habits considered with roughness $\sigma_r = 0$ (smooth crystal surface) and $\sigma_r = 0.5$ (severe rough crystal surface).

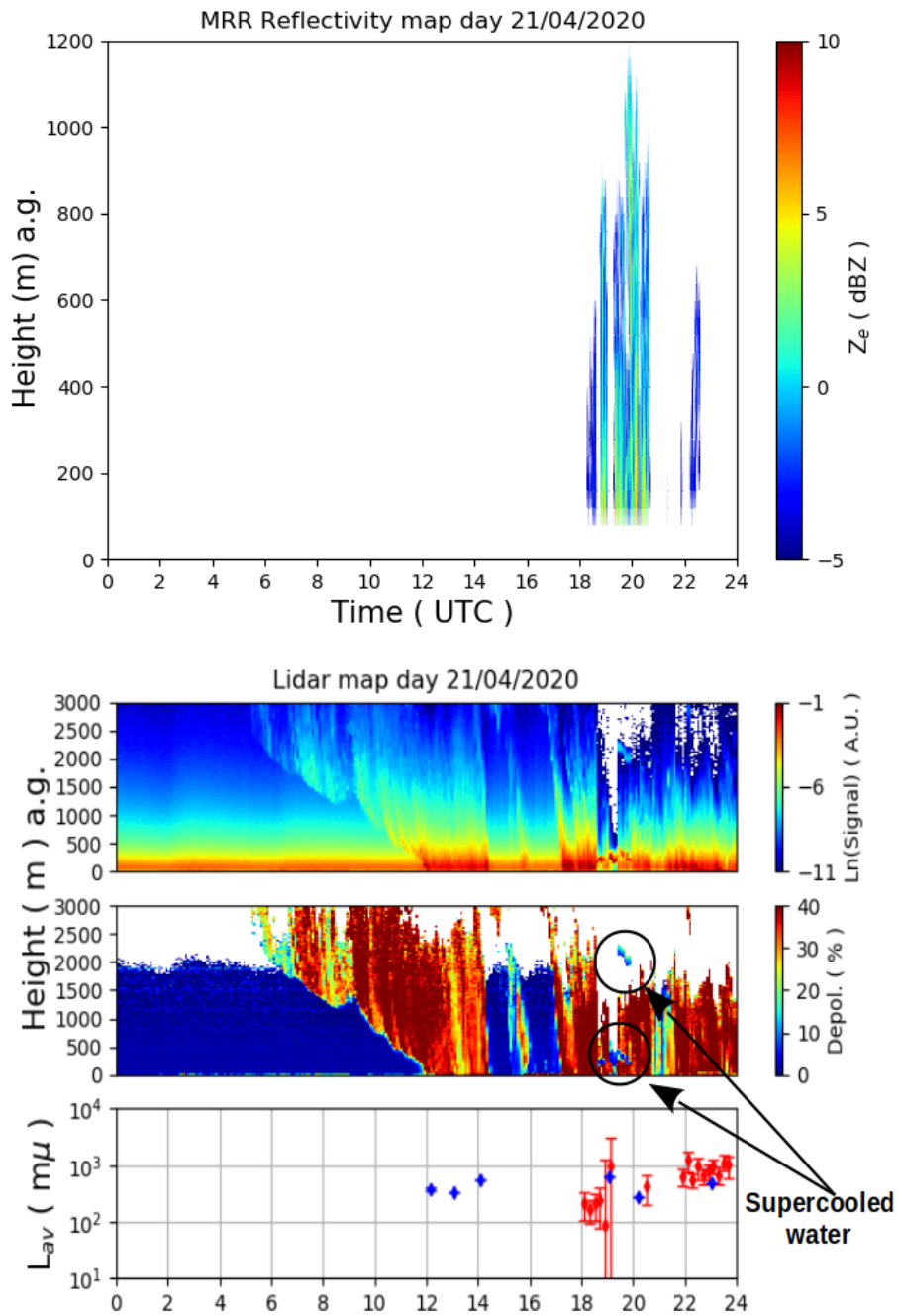


Figure 23. [As for Fig. 17 but for the days 21 and 23 April 2020.](#)

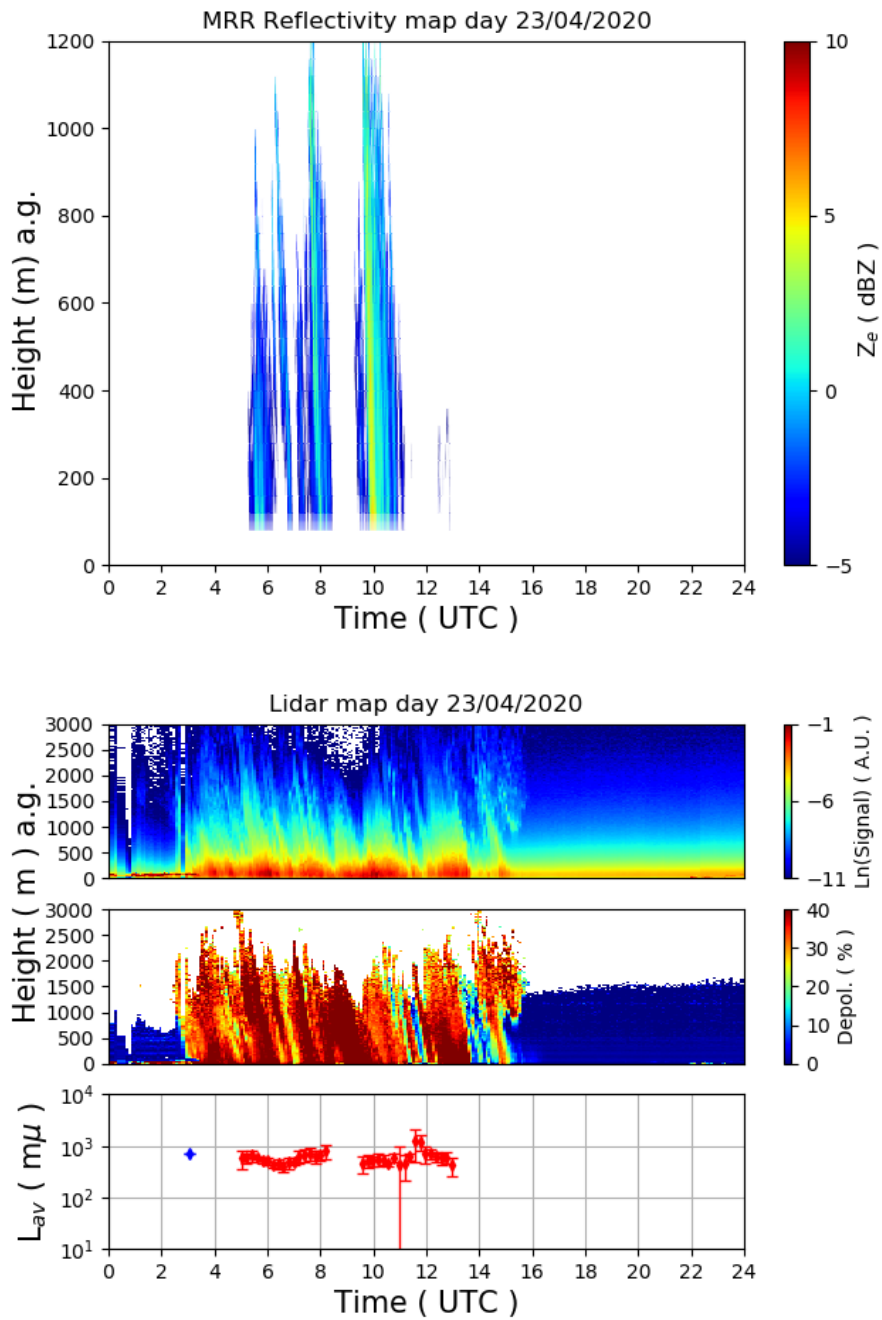


Figure 24. As for Fig. 17 but for the days 21 and 23 April 2020.

IceCamera INO-CNR 21/4/2020 19:3 UTC N°=85

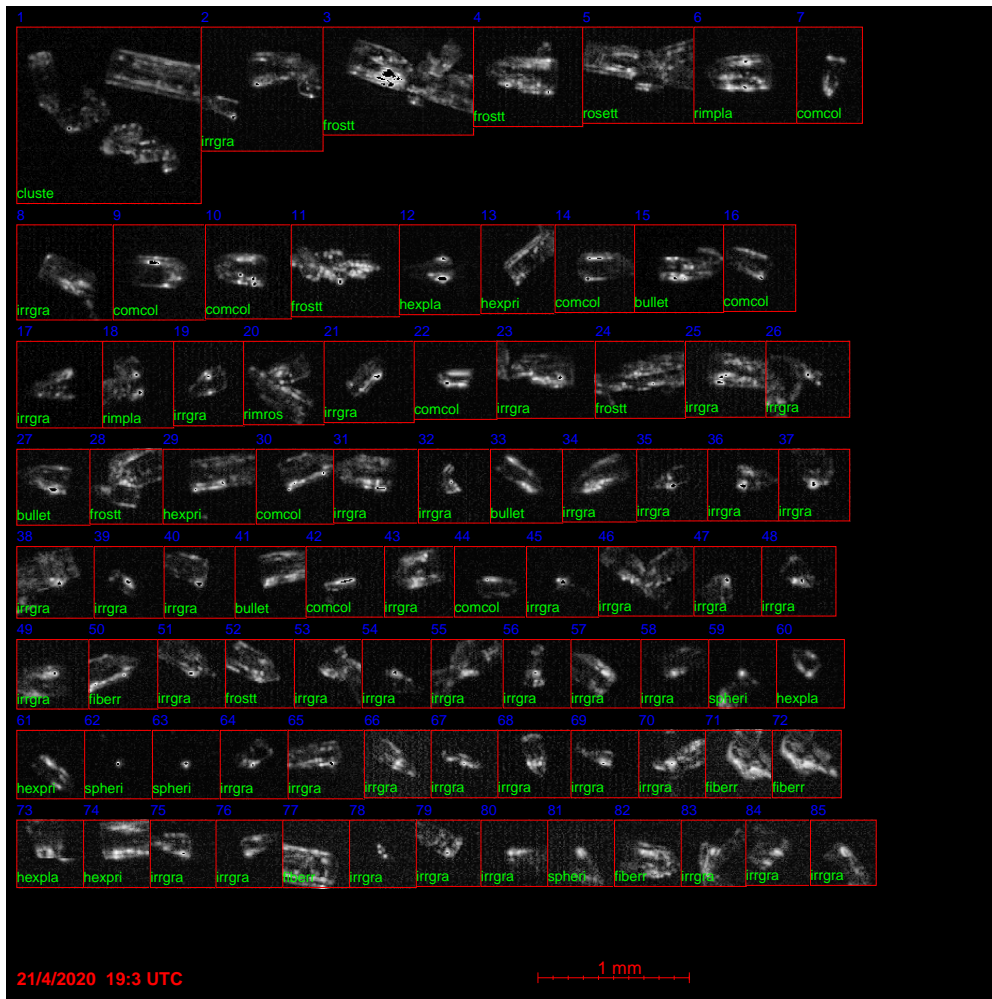


Figure 25. As for Fig. 20 but for the days-day 21 and 23-April 2020-2020 at 19:03 UTC. At this time also complex aggregates of crystals are present.

IceCamera INO-CNR 23/4/2020 3:3 UTC N°=100

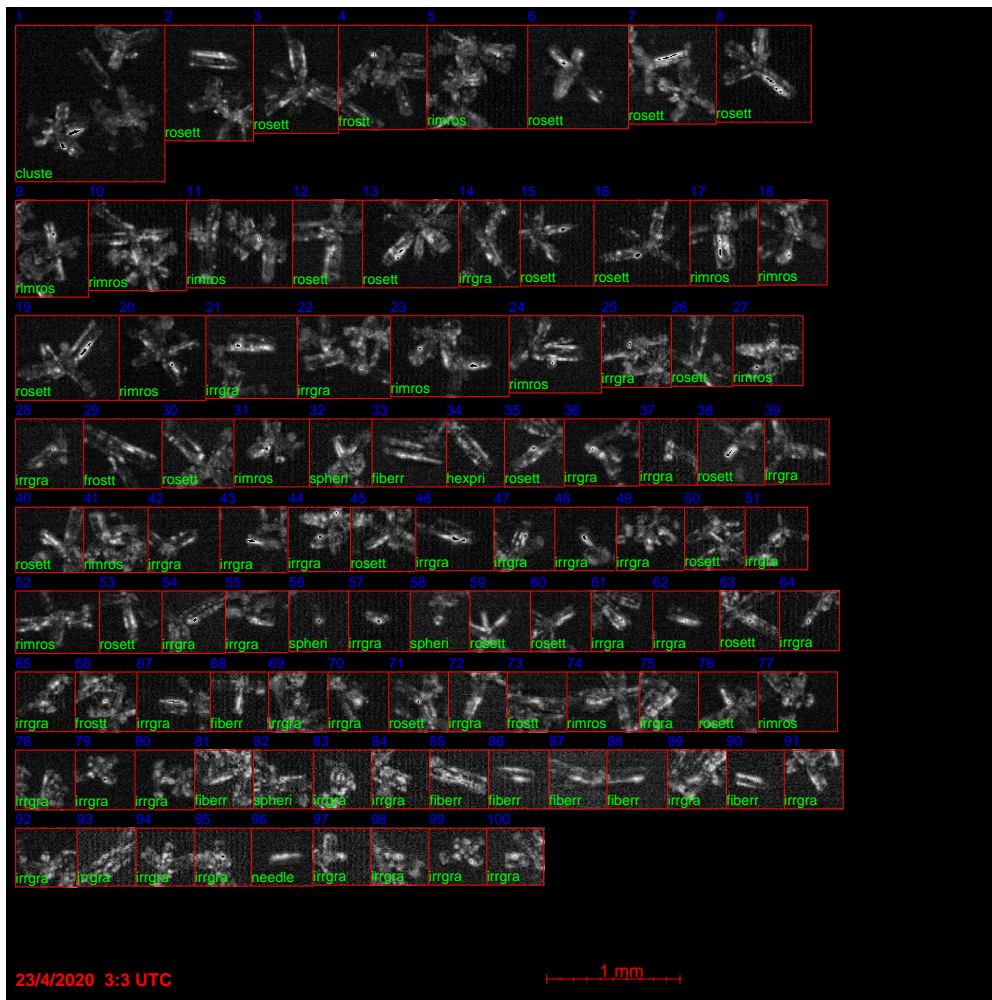


Figure 26. As for Fig. 20 but for the day 23 April 2020 at 03:03 UTC. At this time crystals aggregates and bullet rosettes are present.