

1 **W-band S/Z Relationships for Rimed Snow Particles: Observational Evidence from**  
2 **Combined Airborne and Ground-based Observations**

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## 13 Abstract

14 Values of undercatch-corrected liquid-equivalent snowfall rate (S) at a ground site and  
15 microwave reflectivity (Z) retrieved using an airborne W-band radar were acquired during  
16 overflights. The temperature at the ground site was between -6 and -15 °C. At flight level, within  
17 clouds containing ice and supercooled liquid water, the temperature was approximately 7 °C  
18 colder. Additionally, airborne measurements of snow particle imagery were acquired. The  
19 images demonstrate that most of the snow particles were rimed, at least a flight level. A  
20 relatively small set of S/Z pairs (4) are available from the overflights. Important distinctions  
21 between these measurements and those of Pokharel and Vali (2011), who ~~also reported W-band~~  
22 S/Z pairs [and an S/Z relationship](#) for rimed snow particles, are 1) the fewer number of S/Z pairs,  
23 2) the method used to acquire S, and 3) the altitude, relative to ground, of the [W-band Z](#)  
24 retrievals. [This analysis corroborates that the S/Z relationship reported in Pokharel and Vali](#)  
25 [\(2011\) yields an S - in scenarios with snowfall produced by riming - substantially larger than that](#)  
26 [derived using an S/Z relationship developed for unrimed snow particles.](#)  
27 ~~This analysis indicates that the S/Z relationship reported in Pokharel and Vali (2011) yields an S,~~  
28 ~~in scenarios with snowfall produced by riming, that is substantially larger than that derived using~~  
29 ~~an S/Z relationship developed for unrimed snow particles.~~

30

## 31 1 - Introduction

32 Improvement of methods used to measure snowfall and rainfall are an ongoing focus of  
33 meteorological research. The various methods are ground-based instruments that evaluate the  
34 mass of precipitation that falls into or onto a collector (precipitation gauges) (Brock and  
35 Richardson 2001), ground-based radars (Wilson and Brandes 1979), and airborne and space-  
36 borne radars (Matrosov 2007; Kulie and Bennartz 2009; Geerts et al. 2010; Skofronick-Jackson  
37 et al. 2017). An objective of these approaches, whether used to make observations independent  
38 of other methods (e.g., Kulie and Bennartz 2009), or as a component of multiple observations  
39 (e.g., Cocks et al. 2016), is estimation of precipitation rate and accumulated ~~ion~~ precipitation  
40 amount.

41 Many studies have investigated using radar for evaluating rainfall (for a review see  
42 Wilson and Brandes 1979). There are two approaches. The first is research, both observational  
43 and computational, that probes the relationship between rainfall rate (R) and radar-measured  
44 values of range-corrected backscattered microwave power. The latter is commonly reported as an  
45 equivalent radar reflectivity factor ( $Z_e$ ). The second is operational in the sense that precipitation  
46 gauges are used to calibrate measurements acquired using weather surveillance radars.  
47 Complications associated with converting  $Z_e$  to R, or converting a radar reflectivity factor<sup>1</sup> (Z) to  
48 R, can be grouped in four categories: 1) Inaccuracy in quantification of Z, 2) variation of the  
49 R/Z relationship stemming from precipitation processes (e.g., coalescence and break up), 3)  
50 difference between the volume of a radar range gate versus the much smaller volume of

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<sup>1</sup> Radars are calibrated to report  $Z_e$  (Smith 1984). Herein, radar reflectivities are reported as  $Z = Z_e$  and as  $\text{dBZ} = 10\log_{10}(Z_e)$ .

51 atmosphere sampled as precipitation falls to a gauge, and 4) vertical displacement between a  
52 radar range gate and a calibrating gauge, especially at far ranges.

53 For situations with snowfall, methods employing either gauge or radar are associated  
54 with complications beyond that incurred in rainfall (Matrosov 2007; Martinaitis et al. 2015;  
55 Cocks et al. 2016). Problems associated with gauge measurements are wind-induced snow  
56 particle undercatch, gauge capping, delayed registration, and blowing snow aliasing as snowfall.  
57 Moreover, in a situation with snow particles more~~most~~ abundant within a radar range gate,  
58 compared to rain drops, and where a measurement of Z is used to infer R via a R/Z relationship,  
59 the resultant precipitation rate will likely be inaccurate. This is because hydrometeor shape,  
60 density, and dielectric properties are all variable for snow particles while relatively invariant for  
61 rain drops. Additionally, a snow particle's terminal fall speed varies with size (as is the case for  
62 drops) and with particle shape and particle density. Going forward, we refer to the latter two  
63 properties as shape and density.

64 The goals of this paper are as follows: 1) to describe measurements of undercatch-  
65 corrected liquid-equivalent snowfall rate (S, mm h<sup>-1</sup>) and how these were paired with W-band  
66 measurements of reflectivity (Z, mm<sup>6</sup> m<sup>-3</sup>); 2) to contrast the S/Z pairs against S/Z relationships  
67 commonly applied in radar retrievals of S; and 3) to investigate why the S/Z pairs deviate from  
68 predictions of some S/Z relationships.

69 In calculations of paired values of S and Z, density is an important parameter. Density is  
70 commonly estimated using empirical data (e.g., Pokharel and Vali 2011, [PV11]). For graupel, a  
71 snow particle that grows via collection of supercooled cloud droplets in a process commonly  
72 referred to as riming, paired observations of particle mass and particle size have been used to  
73 estimate density. There is considerable uncertainty in this approach. Based on data collected at

74 two northwestern US surface sites (Zikmunda and Vali 1972; Locatelli and Hobbs 1974), density  
 75 values differ by at least a factor of two at particle sizes smaller than 2000  $\mu\text{m}$  (PV11; their Fig.  
 76 4). Given that the density of rime ice varies with droplet impact speed, droplet size, and  
 77 temperature (Macklin 1962), it is not surprising that the density-size relationships analyzed by  
 78 PV11 are so varied.

79 [Table 1 and the](#) ~~he~~ following ~~introductory~~ paragraphs overview W-band S/Z relationships  
 80 ~~being~~ applied in instances [with snow particles grown](#) ~~of snowfall where mass is acquired~~ by  
 81 vapor deposition (crystal), by collection of crystals (aggregate [snowflake](#)), and by riming (rimed  
 82 crystal and graupel). Henceforth, the latter two snow particle types are collectively referred to as  
 83 rimed snow particles.

84 In a computational study, Hiley et al. (2011) considered a variety of snow particle types  
 85 (column, plate, bullet rosette, sector plate, dendrite, and aggregate [snowflake](#)), employed a  
 86 parameterized ice particle size distribution (PSD) function (Field et al. 2005), accounted for a  
 87 range of temperature (-5 to -15  $^{\circ}\text{C}$ ) via the Field et al. parameterization, and developed a range of  
 88 S/Z relationships for snow particles. Except for the aggregate [snowflakes \(henceforth,](#)  
 89 [aggregates\)](#)s, the modeled particle types were vapor-grown crystals. Hiley et al.'s upper- and  
 90 lower-limit relationships are  $S = 0.21 \cdot Z^{0.77}$  and  $S = 0.024 \cdot Z^{0.91}$ , [respectively.](#) ~~Matrosov (2007)~~  
 91 developed an S/Z relationship for aggregates. In that work, parameterized PSDs from Braham  
 92 (1990) were employed, and a range of particle aspect ratios were factored into the calculations.  
 93 For aggregates, the S/Z relationship is  $S = 0.056 \cdot Z^{1.25}$  (Matrosov 2007). It should be noted that  
 94 Hiley et al. (2011) and Matrosov (2007) employed similar, but not identical, computational  
 95 methods. [Computational research was also conducted by](#) Kulie and Bennartz (2009) [who](#)  
 96 ~~developed~~ [adopted](#) ~~an S/Z relationship for what they referred to as a “snow particle” type. The~~

97 wavelength-dependent density derived by Surussavadee and Staelin (2007) ( $200 \text{ kg m}^{-3}$  at  $\lambda =$   
 98  $3.2 \text{ mm}$ ), modeled the ~~was adopted, the~~ snow particles ~~were modeled~~ as spheres, and applied  
 99 PSDs based on the Field et al. ~~parameterization was applied~~. The resultant S/Z ~~relationship~~  
 100 ~~developed for this particle type~~ is  $S = 0.52 \cdot Z^{0.83}$  (Surussavadee and Staelin 2007; Kulie and  
 101 Bennartz 2009; henceforth, SSKB). Variance in the calculations discussed in this paragraph  
 102 originate from changes in density, shape, fall speed, PSD, and particle size as these changes are  
 103 propagated through the cloud-microphysical and microwave-scattering calculations.

104 In a hybrid approach (computational and an analysis of measurements airborne  
 105 observations), PV11 concluded that most of the snow particles they imaged were rimed snow  
 106 particles. Values of S were calculated using a density-size function ( $\rho_1$ , discussed below), a fall  
 107 speed-size function, ~~a~~ measured PSDs and measured particle images, and a determination of  
 108 particle volumes. It was assumed that a prolate spheroid approximated particle shape and that  
 109 shape is was the basis for determining a particle's sphere-equivalent volume and the particle's  
 110 sphere-equivalent size. The sphere-equivalent size was applied in the two functions. Values of Z  
 111 were calculated using a measured PSD, sphere-equivalent sizes, the  $\rho_1$  function, and Mie Theory.  
 112 PV11 presented calculations of Z, obtained using two density-size relationships (their Eqs. 1 and  
 113 2) and compared their calculated reflectivities to measurements of Z from a W-band radar. That  
 114 led to their conclusion that "...the lower density assumption...yielded closer correspondence to  
 115 observed reflectivities." Their recommendation for S as a function of measured Z - hereafter the  
 116  $S(\rho_1)/Z$  best-fit line - is  $S = 0.39 \cdot Z^{0.58}$ . Values of Z that were paired with the calculated values of  
 117 S (i.e., the S/Z pairs from PV11 that we present in Sect. 4), and that were used to determine the  
 118  $S(\rho_1)/Z$  best-fit line, came from the WCR. In addition to variance in their values of S, coming  
 119 from a dependence on density, PV11 state that a value of S derived via their best-fit line is

120 uncertain by a factor-of-ten. That uncertainty is evident in the variance of S/Z data pairs about  
121 the  $S(\rho_1)/Z$  line in Fig. 11 of PV11. Those investigators, and Geerts et al. (2010), attributed the  
122 variance to use of two-dimensional snow particle images in calculations of S and to actual  
123 variations of density, shape, and particle size not accounted for in the calculations.

124 ~~Another set of hybrid-type~~ ~~iso-relevant are~~ S/Z relationships ~~was developed~~ ~~reported~~ by  
125 Falconi et al. (2018; their Table 2). These ~~are based on~~ ~~were developed using~~ measurements from  
126 a video disdrometer, weighing precipitation gauge, microwave radiometer, and a vertically-  
127 pointing W-band radar. All these systems were operated at the ground. The data set was stratified  
128 into intervals of lightly-rimed, moderately-rimed, and heavily-rimed snow. A proxy for snow  
129 particle riming - radiometer measurements of liquid water path – was the basis for the  
130 stratifications (von Lerber et al. 2017). The S/Z relationships are  $S = 0.10 \cdot Z^{1.0}$  (lightly-rimed),  $S$   
131  $= 0.079 \cdot Z^{1.3}$  (moderately-rimed), and  $S = 0.060 \cdot Z^{1.4}$  (heavily-rimed).

132 Our focus is on surface measurements of S and on pairing of those measurements with  
133 airborne measurements of Z. We also analyze airborne measurements of snow particle imagery.  
134 The latter demonstrates that the particles observed at flight level were rimed. The ~~imagery is the~~  
135 ~~se measurements are the~~ basis for our assertion that our data set is relevant to ongoing  
136 investigations of using Z to evaluate S in situations where precipitation is produced by riming.

137 Section 2 describes the setting of our study, the instruments we deployed, and recordings  
138 we obtained using two data acquisition systems. One of the data systems was operated at a  
139 ground site and the other on an aircraft. Section 3 is an analysis of the recordings; this section  
140 also considers recordings from two additional, but ancillary, ground sites. Our findings are  
141 discussed in Sect. 4 and summarized in Sect. 5. An Appendix (Sect. 6) explains how we

142 averaged recordings of near-surface W-band reflectivities and surface-based recordings of  
143 snowfall.



144 Table 1 – W-band S/Z relationships from the literature, snow particle type, and values of minimum relative S difference

<u>Reference</u>	<u>Abbreviation used for reference</u>	<u>S/Z relationship</u>	<u>Snow Particle Type</u>	<u>Minimum relative S difference on December 15 2016<sup>a</sup></u>	<u>Minimum relative S difference on January 3 2017<sup>a</sup></u>
<u>Hiley et al. (2011)</u>	-	<u><math>S=0.21 \cdot Z^{0.77}</math></u>	<u>Upper-limit S/Z relationship for vapor-grown crystals</u>	<u>0.7</u>	<u>1.0</u>
<u>Matrosov (2007)</u>	-	<u><math>S=0.056 \cdot Z^{1.2}</math></u>	<u>Aggregates</u>	<u>1.4</u>	<u>8.5<sup>b</sup></u>
<u>Surussavadee and Staelin (2007) and Kulie and Bennartz (2009)</u>	<u>SSKB</u>	<u><math>S=0.52 \cdot Z^{0.83}</math></u>	<u>Spherical snow particles with density = 200 kg m<sup>-3</sup></u>	<u>0.3</u>	<u>0.2<sup>c</sup></u>
<u>Pokharel and Vali (2011)</u>	<u>PV11</u>	<u><math>S=0.39 \cdot Z^{0.58}</math></u>	<u>Rimed snow particles assuming the lower of two density-size relationships</u>	<u>0.3</u>	<u>0.0<sup>d</sup></u>
<u>Falconi et al. (2018)</u>	-	<u><math>S=0.060 \cdot Z^{1.4}</math></u>	<u>Snow particles classified as heavily rimed</u>	<u>0.6<sup>e</sup></u>	<u>8.5</u>

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146 <sup>a</sup> Minimum relative S difference is defined as the minimum of  $|(S_{HP}-S)|/S$  where  $S_{HP}$  is a measurement of undercatch-corrected liquid-equivalent snowfall rate (Table 6) and S is a snowfall rate on an S/Z relationship line evaluated at one of the attenuation-corrected reflectivities (Sect. 4).

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148 <sup>b</sup> Attenuation-corrected Z on this day (0.6 mm<sup>6</sup> m<sup>-3</sup>) is smaller than the lower-limit Z (1 mm<sup>6</sup> m<sup>-3</sup>) advised for this S/Z relationship (Matrosov 2007).

149  
150 <sup>c</sup> Maximum relative S difference on this day is 0.4.

151 <sup>d</sup> Maximum relative S difference on this day is 0.7.

152 <sup>e</sup> Maximum relative S difference on this day is 0.9.

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## 154 **2 - Site, Aircraft, and Instruments**

### 155 **2.1 - Site**

156 Analyzed herein are aircraft and ground data from 14/15 December 2016 and from 3  
157 January 2017. The ground data were acquired in a forest/prairie ecotone on the eastern slope of  
158 the Medicine Bow Mountains in southeast Wyoming (Figs. 1a-b). No ground-based observers  
159 were deployed during the two snowfall events analyzed.

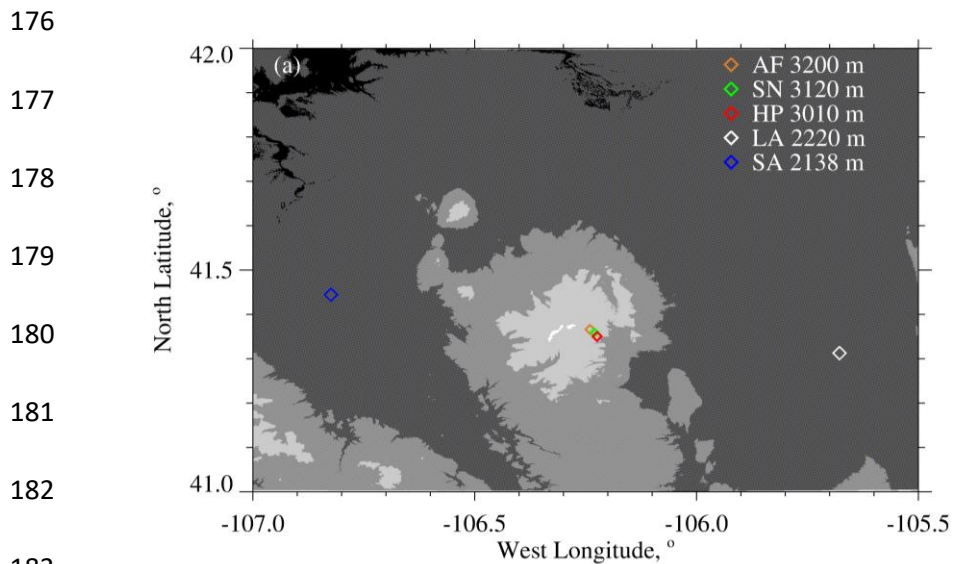
160 At one of three ground sites (HP in Figs. 1a-b) a hotplate precipitation gauge (Rasmussen  
161 et al. 2011; Zelasko et al. 2018), a GPS receiver, and a data acquisition system were deployed.  
162 Once per second, the data system ingested a hotplate-generated data string, combined that with  
163 time-of-day from the GPS receiver [Coordinated Universal Time (UTC)], and recorded the  
164 merged hotplate/UTC data string. The absolute accuracy of the time stamp is no worse than 2 s.

165 Overflights of the hotplate were done by the University of Wyoming King Air (WKA) on  
166 14/15 December 2016 and on 3 January 2017. The flights were conducted in preparation for the  
167 SNOWIE field project (Tessendorf et al. 2019) and were flown from the Laramie, WY Airport  
168 (LA in Fig. 1a). Data acquisition on the WKA was also synchronized with UTC, but with much  
169 better accuracy than at the hotplate.

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171           Measurements of horizontal wind (speed and direction), temperature, relative humidity,  
172 and pressure from the US-GLE AmeriFlux tower (AF in Figs. 1a-b) are also components the  
173 analysis. The AmeriFlux data were provided to us as 30-minute averages (AmeriFlux 2021;  
174 Marlow et al. 2023).

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192 Figure 1 – (a) Southeast Wyoming, airport at Saratoga, WY (SA), airport at Laramie, WY (LA),

193 and the ground sites: AF = US-GLE AmeriFlux tower, SN = Brooklyn Lake SNOTEL, and HP =

194 hotplate. Altitudes of the airports and ground sites are in the legend. Altitude thresholds for the

195 digital elevation map are 1500, 2000, 2500, 3000, and 3500 meters. (b) Close up of the AF, SN,

196 and HP ground sites (from © Google Earth).

197

## 198 **2.2 - University of Wyoming King Air (WKA)**

199           The following WKA measurements were analyzed: aircraft position, temperature, snow  
200 particle imagery, and three moments of the cloud droplet size distribution function. A Cloud  
201 Droplet Probe (CDP; Faber et al. 2018) was the basis for the droplet size distribution  
202 measurements and the derived moments. The latter are droplet concentration (N), cloud liquid  
203 water content (LWC), and mean droplet diameter ( $\langle D \rangle$ ). Snow particle imagery was obtained  
204 using a precipitation particle imaging probe (2DP; Korolev et al. 2011) and a cloud particle  
205 imaging probe (2DS; Lawson et al. 2006). These acquired two-dimensional images of particles  
206 between 200 to 6400  $\mu\text{m}$  (2DP) and between 10 to 1280  $\mu\text{m}$  (2DS).

## 207 **2.3 – The W-band Wyoming Cloud Radar (WCR)**

208           Retrievals from the up-looking and down-looking antennas of the WCR, operated on the  
209 WKA, were also analyzed. For this we used Level 2 WCR data<sup>2</sup> with reflectivities recorded as  
210  $dBZ = 10 \cdot \log_{10}(Z)$ . The reflectivities were converted from dBZ to Z prior to processing.  
211 Additionally, values of the vertical-component Doppler velocity retrieved from below the WKA  
212 using the WCR's down-looking antenna were analyzed. The Doppler velocities were corrected  
213 for aircraft motion as described in Haimov and Rodi (2013). We use  $V_D$  to symbolize the  
214 corrected vertical-component Doppler velocity and adopt the convention that  $V_D > 0$  indicates  
215 upward hydrometeor motion.

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<sup>2</sup> [http://flights.uwyo.edu/uwka/wcr/projects/snowie17/PROCESSED\\_DATA/](http://flights.uwyo.edu/uwka/wcr/projects/snowie17/PROCESSED_DATA/)

217           The Level 2 WCR sampling was different on the two flight days and this difference is  
218 shown in Table [24](#). Ground-based calibrations of the WCR's up-looking antenna and correlations  
219 between in-flight retrievals acquired using the WCR's up-looking and down-looking antennas  
220 were used to estimate the precision and absolute accuracy of the WCR-derived values of dBZ.  
221 These are  $\pm 1.0$  dBZ and  $\pm 2.5$  dBZ, respectively (PV11).

222

223 Table 2+ – Level 2 WCR sampling and the WKA overflight time

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Date	Level 2 WCR Vertical Sampling, m	Level 2 WCR Along-track Sampling, s	Overflight Time, UTC
14/15 December 2016	23	0.23	00:00:38 (15 December 2016)
3 January 2017	30	0.36	20:32:03

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226

## 227 **2.4 - Hotplate Gauge**

228 Algorithms used to process hotplate measurements are described in Rasmussen et al.  
229 (2011), Boudala et al. (2014), and Zelasko et al. (2018). Henceforth, these are referred to as R11,  
230 B14, and Z18, respectively. This section describes how hotplate measurements acquired at the  
231 HP site were analyzed. The hotplate deployed at the HP site is described in Wolfe and Snider  
232 (2012), Z18, and in Marlow et al. (2023).

233 Five measurements fundamental to the steady state energy budget of the hotplate's  
234 temperature-controlled up-viewing plate are output by the hotplate microprocessor as one-minute  
235 running averages (Z18). These averages were merged with the GPS time and recorded at 1 Hz by  
236 the data acquisition system (Sect. 2.1). With these measurements, calibration data (Marlow et al.  
237 2023), and the algorithm developed by Z18, we calculated  $S$  in two steps. First, the five hotplate  
238 measurements (electrical power supplied to the plate, ambient temperature, wind speed,  
239 downwelling shortwave flux, and downwelling longwave flux) were input to Eq. 3 in Z18. The  
240 output of that equation is a provisional liquid-equivalent precipitation rate. Second, the snow  
241 particle catch efficiency, described in the next paragraph, was used to calculate  $S$  as the ratio of  
242 the provisional rate and the catch efficiency.

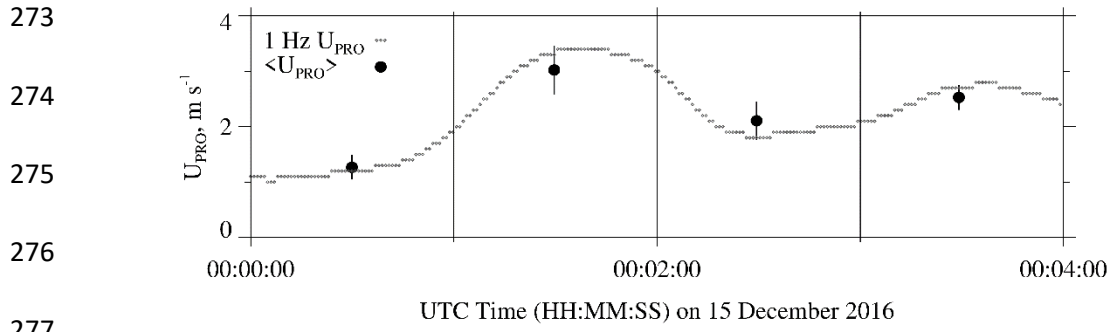
243 Marlow et al. (2023; their Fig. 3b) report the relationship between snow particle catch  
244 efficiency and wind speed that was applied in the calculation of  $S$ . There are three bases for this  
245 relationship. First is the catch efficiencies R11 derived using measurements obtained from a  
246 weighing gauge, operated within a double fence intercomparison reference shield, and collocated  
247 measurements from an unshielded hotplate gauge. These paired measurements are symbolized  
248 SRG (shielded reference gauge) and UHG (unshielded hotplate gauge). R11 plotted hotplate  
249 catch efficiencies (i.e., UHG/SRG) versus wind speeds measured at 10 m AGL (their Fig. 8).



250 Second is Marlow et al.'s adjustment of R11's 10 m AGL wind speeds to 2 m AGL. The basis  
251 for the adjustment is surface boundary layer parameters derived for R11's site (Kochendorfer et  
252 al. 2018) and an equation from Panofsky and Dutton (1984; their Eq. 6.7). The adjustment was  
253 made because the hotplate-derived wind speeds, both here and in Marlow et al. (2023), were  
254 acquired at approximately 2 m above the snowpack surface. Third is Marlow et al.'s comparison  
255 of SNOTEL-derived liquid-equivalent depth changes and hotplate-derived time-integrated  
256 accumulations. The interval for the comparisons is 24 hours. Based on the comparison, which  
257 has 57 paired values acquired at the sites labeled HP and SN in Fig. 1, the average fractional  
258 absolute relative difference is 0.30. Marlow et al. also provided an estimate of the error in a  
259 SNOTEL measurement (2.4 mm). At accumulation = 10 mm the error corresponds to a relative  
260 error = 0.24. This indicates that SNOTEL contributed significantly to the SNOTEL/hotplate  
261 variance and especially so for the smaller accumulations in Fig. 9a of Marlow et al. (2023).  
262 Because of this, we do not limit the following estimate of hotplate precision to a subset of the 57  
263 paired measurements. Based on our assessment of the average fractional absolute relative  
264 difference, the hotplate precision applied in this analysis was taken to be 0.3.

265 The hotplate-derived wind speeds acquired at ~ 2 m, and discussed in the previous  
266 paragraph, are henceforth symbolized  $U_{\text{PRO}}$ . The basis for these is a steady state energy budget of  
267 the hotplate's temperature-controlled down-viewing plate and a proprietary algorithm (R11 and  
268 Z18). The  $U_{\text{PRO}}$  are reported by a hotplate as one-minute running averages (Z18) and we  
269 recorded these at 1 Hz. Examples are the gray dots in Fig. 2. Additionally, we calculated and  
270 analyzed one-minute-averaged values of  $U_{\text{PRO}}$  and the corresponding standard deviations.  
271 Examples of these are the black circles and the short vertical line segments in Fig. 2.

272



279 Figure 2 – Hotplate wind speed measurements ( $U_{PRO}$ ) 00:00:00 to 00:04:00 on 15 December

280 2016. Gray dots are the one-minute running-average  $U_{PRO}$  recorded at 1 Hz. Black circles are the

281 one-minute-averaged  $U_{PRO}$  ( $\pm 1$  standard deviation).

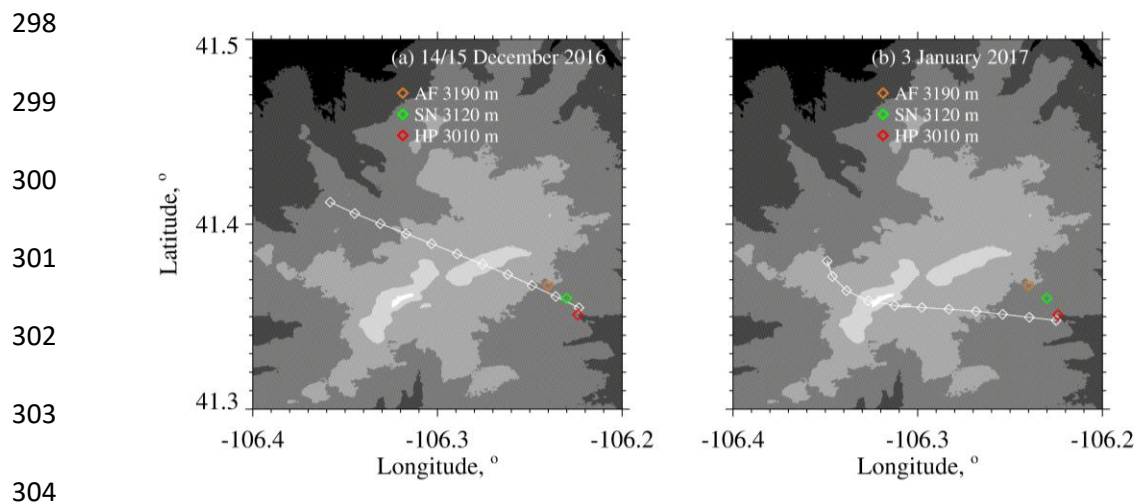
## 283 3 - Analysis

### 284 3.1 - WKA Overflight Time

285 The focus of our analysis is the two WKA flight segments shown in Figs. 3a-b. The maps  
286 shown in the figures have the three ground sites (AF, SN, and HP) and the WKA flight tracks  
287 (white line). The beginning-to-end time interval for the flight tracks is 100 s and these are  
288 divided into ten 10-second intervals. The 10 s intervals are indicated with white diamonds.  
289 Except for the turn evident in Fig. 3b, the flight tracks are straight, and the track direction is  
290 approximately upwind to downwind.

291 Times that the WKA was closest to the HP site were evaluated by finding the point on the  
292 flight track where the horizontal position of the WKA was closest to the hotplate's coordinates.  
293 These times are symbolized  $t_0$  and are referred to as overflight times. In Figs. 3a-b the downwind  
294 end of the flight tracks end at the overflight time. The latitude/longitude position of the aircraft  
295 was within 390 m of the hotplate at the overflight times. Table 2+ has the overflight times on the  
296 two flight days.

297



305 Figure 3 – (a) WKA flight track on 14/15 December 2016 for time interval = overflight time -  
 306 100 s to the overflight time. (b) WKA flight track on 3 January 2017 for time interval =  
 307 overflight time - 100 s to the overflight time. The white diamonds on the tracks are separated, in  
 308 time, by 10 s. Altitude thresholds for the digital elevation maps are 2600, 2800, 3000, 3200,  
 309 3400, and 3600 meters. Altitudes of the ground sites are in the legend.

310

### 311 3.2 – Effect of Attenuation on WCR Reflectivities

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313 The presence of molecular oxygen, water vapor, cloud water, and snow particles within  
314 the WCR's transmission path will contribute to an attenuation of microwave intensity and will  
315 therefore negatively bias the retrieved reflectivities (Matrosov 2007; Hiley et al. 2011; Kneifel et  
316 al. 2015). Models of attenuation, radar remote sensing, and in situ measurements were used to  
317 calculate this bias. For oxygen, an attenuation coefficient from Ulaby et al. (1981; their Fig. 5.6),  
318 and temperature (T) and pressure (P) measurements from the AF (Table 32), were used. For  
319 vapor, an attenuation coefficient (Ulaby et al. 1981; their Eq. 5.22), and T, P, and relative  
320 humidity (RH) measurements from the AF (Table 32), were used. Concentrations of oxygen and  
321 water vapor and the oxygen and vapor path lengths are provided in Table 43. The latter is the  
322 vertical distance between the HP and the WKA. It was assumed that concentrations were  
323 uniform over this path length.

324 Attenuation by cloud water was derived using the WKA-measured T (Table 32), the  
325 WKA-measured LWC, path length (Table 43), and an attenuation formula (Liebe et al. 1989;  
326 Vali and Haimov 2001). The LWC applied in the formula is the maximum of CDP  
327 measurements acquired between  $t_0 - 10$  s and  $t_0$ . This interval coincides with the interval the  
328 WCR's down-looking antenna was used to acquire reflectivities over the HP (Sect. 3.5). The  
329 path length for cloud water was derived as the vertical distance between cloud base [derived  
330 thermodynamically using AF measurements (Table 32)] and flight level. LWC was assumed  
331 uniform, at the maximum value, over the path length.

332 Snow particle mass concentration is typically reported as an ice water content (IWC,  $\text{g m}^{-3}$ )  
333 (Liu and Illingworth 2000). The contribution of IWC to attenuation was calculated using

334 measurements in Nemanich et. al (1988), who reported an attenuation coefficient equal to 0.9  
 335 dB/km per unit of IWC. Also used were retrievals of IWC acquired using the down-pointing  
 336 WCR antenna. There are several steps in the calculation. First, all profiles of dBZ acquired  
 337 between  $t_0 - 10$  s and  $t_0$  were selected. Second, a maximum dBZ was selected at each of the  
 338 down-beam range gates (Table 2+). Third, the dBZ maxima were increased by the overall two-  
 339 way attenuation in the final column of Table 43. Fourth, the profile of attenuation-corrected dBZ  
 340 was converted to a profile of attenuation-corrected Z. Fifth, a Z-to-IWC parameterization was  
 341 applied ( $IWC = 0.10 \cdot Z^{0.51}$ ; PV11; their Table 3). Sixth, the IWC profile was integrated, and the  
 342 derived ice water path was divided by the snow particle path length (Table 43). This calculation  
 343 produced a time- and range-averaged maximum IWC (Table 43). This IWC is the value applied  
 344 in the attenuation calculation.

345 Two-way attenuations ( $\Delta dB$ ), summed over contributions from the four components, are  
 346 presented in the final column of Table 43. Attenuation by snow and attenuation by liquid were  
 347 the most important components ( $> 50$  %) on December 15 and January 3, respectively. Vapor  
 348 contributed 32 % to the overall on December 15, and the combination of vapor and snow  
 349 contributed 45 % on January 3. Equation 1 shows how an attenuation-corrected reflectivity ( $Z'$ )  
 350 was derived using an uncorrected reflectivity ( $Z$ ) and the  $\Delta dB$  .

351

$$352 \quad Z' = 10^{\left[ \frac{10 \cdot \log_{10}(Z) + \Delta dB}{10} \right]} \quad (1)$$

353 Table 32 – Atmospheric state averages

354

Date	WKA <sup>a</sup> Track Altitude, m	WKA <sup>a</sup> T, °C	AF <sup>b</sup> T, °C	AF <sup>b</sup> RH, %	WKA <sup>a, c</sup> Track Vector	WKA <sup>a, c</sup> Wind Vector	AF <sup>b, c</sup> Wind Vector
14/15 December 2016	4546	-13.9	-6.3	86	310 / 130	274 / 32	250 / 8.5
3 January 2017	4196	-21.7	-14.6	77	280 / 120	265 / 27	260 / 5.4

355

356

357 <sup>a</sup> Altitude, temperature, track vector, and horizontal wind vector data obtained by averaging 1 Hz  
 358 WKA measurements. The averaging interval is 60 s and the interval starts at the overflight time,  
 359 minus 60 s, and ends at the overflight time.

360

361 <sup>b</sup> Temperature (T), relative humidity (RH), and horizontal wind vector data from sensors on the  
 362 US-GLE AmeriFlux tower (Sect. 2.1). The wind sensor was deployed at 26 m AGL (3223 m  
 363 MSL) and the T/RH sensor was deployed at 23 m AGL (3220 m MSL). The AF measurements  
 364 correspond to 30-minute averages closest to the overpass time. In the AF data set, time stamps on  
 365 the relevant AF recordings are 00:00 UTC (15 December 2016) and 20:30 UTC (3 January  
 366 2017).

367

368 <sup>c</sup> Vectors are presented in the following format: Direction of motion (degree relative to true  
 369 north) / speed (m s<sup>-1</sup>).

370 Table 43 – Attenuating component concentration, one-way pathlength, and the overall two-way attenuation

Date	Conc. Oxygen, kg m <sup>-3</sup>	Conc. Vapor, kg m <sup>-3</sup>	Maximum LWC, g m <sup>-3</sup>	Maximum IWC, g m <sup>-3</sup>	One-way Pathlength <sup>a</sup> Oxygen, Vapor, and Snow, km	One-way Pathlength <sup>b</sup> Cloud Water, km	Overall Two-way Attenuation, ΔdB
15 December 2016	0.21	2.7x10 <sup>-3</sup>	0.01	0.27	1.54	1.09	1.41 <sup>c</sup>
3 January 2017	0.21	1.3x10 <sup>-3</sup>	0.08	0.09	1.19	0.59	1.01 <sup>d</sup>

371

372 <sup>a</sup> Vertical distance between HP and WKA

373

374 <sup>b</sup> Vertical distance between cloud base [derived thermodynamically using AF measurements (Table 32)] and WKA

375

376 <sup>c</sup> One-way attenuation coefficients are 0.03 dB/km for oxygen (Ulaby et al. 1981), 0.14 dB/km for vapor (Ulaby et al. 1981), 0.056  
 377 dB/km for cloud water (Liebe et al. 1989; Vali and Haimov 2001), and 0.24 dB/km for snow particles (Nemarich et. al 1988).

378

379 <sup>d</sup> One-way attenuation coefficients are 0.03 dB/km for oxygen (Ulaby et al. 1981), 0.073 dB/km for vapor (Ulaby et al. 1981), 0.49  
 380 dB/km for cloud water (Liebe et al. 1989; Vali and Haimov 2001), and 0.077 dB/km for snow particles (Nemarich et. al 1988).

381



### 382 3.3 - Correction of Doppler Velocity

383 We accounted for bias in  $V_D$  (Sect. 2.3) due to deviation of the down-looking WCR  
384 antenna from vertical. This was done by applying the correction described in Zaremba et al.  
385 (2022) (their Eq. A4). The west-to-east and south-to-north particle velocities used in the  
386 correction were assumed to be equal to component wind velocities. The latter were expressed as  
387 linear functions of altitude using the information in the penultimate and last columns of Table 32.  
388 The component velocities as functions of altitude and the linear equations relating velocity and  
389 altitude are provided in the Appendix.

### 390 3.4 - Hotplate Measurement of Wind Speed

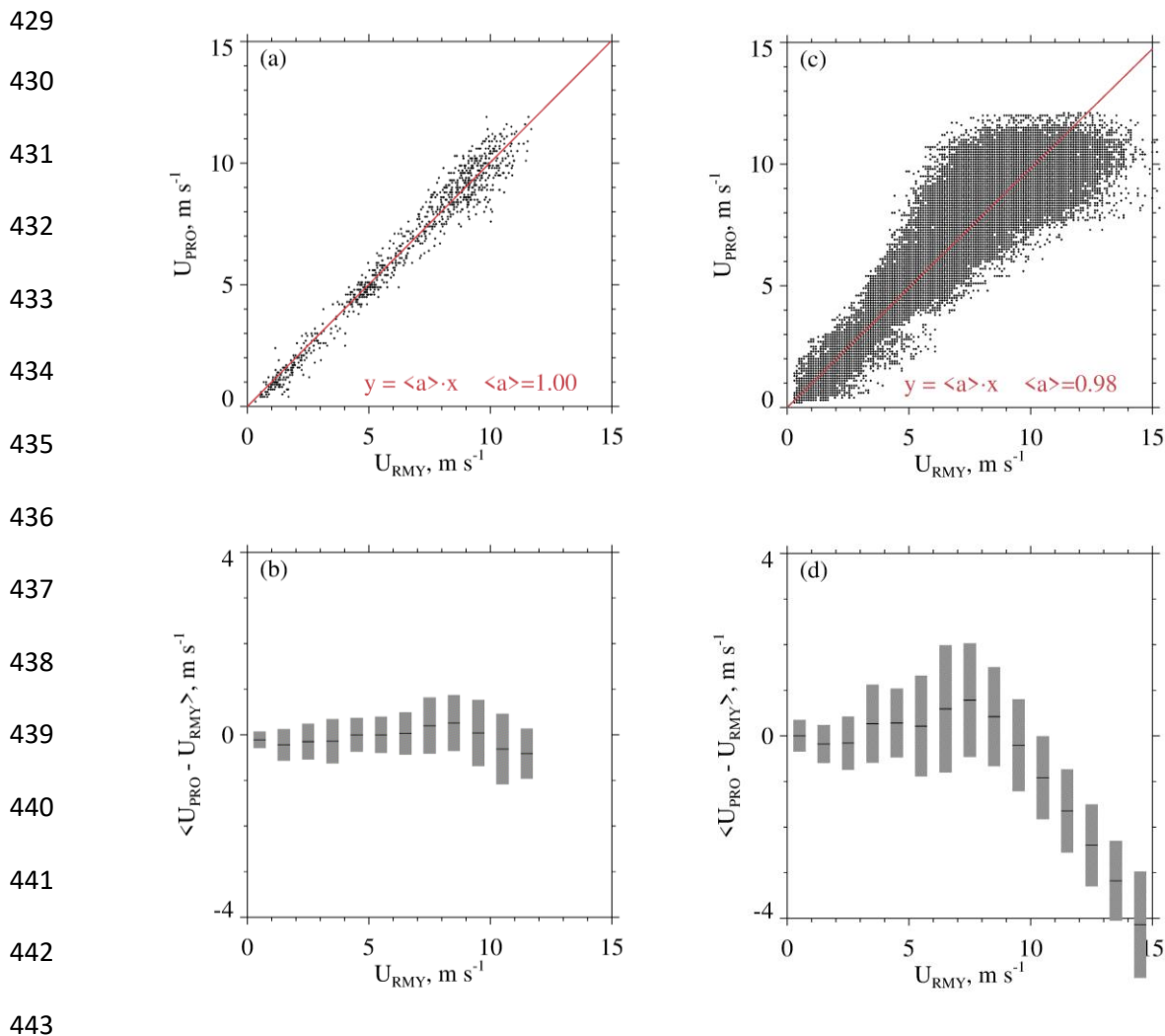
391 Here we compare the hotplate-derived wind speed to wind speed derived using an  
392 R.M.Young rotating anemometer (R.M.Young 2001). The second of these is symbolized  $U_{RMY}$   
393 and the basis for the first ( $U_{PRO}$ ) is a proprietary algorithm (Sect. 2.4). We are doing this  
394 comparison because B14 showed that  $U_{PRO}$  can be high-biased, relative to a conventional  
395 anemometer, and because  $U_{PRO}$  is the primary determinant of the rate that the up-viewing plate  
396 dissipates sensible heat energy. Diagnosis of that heat transfer rate is our basis for calculating the  
397 liquid-equivalent snowfall rate (Z18). The  $U_{PRO}$  also determines the snow particle catch  
398 efficiency and the latter was used in calculations of the undercatch-corrected liquid-equivalent  
399 snowfall rate (Sect. 2.4).

400 The comparisons reported here were done at the Laramie, WY Airport in December  
401 2019, and in January 2020. Compared to the HP site, the Laramie Airport site (indicated LA in  
402 Fig. 1) is free of obstruction, out to 120 m, and experiences larger wind speeds. By mounting the  
403 hotplate and the R.M.Young anemometer on rigid metal pipes, the hotplate's heated horizontal

404 surfaces (the up- and down-viewing plates seen in Fig. 1 of Z18) and the anemometer's spinning  
405 axis (oriented horizontally) were both positioned at 2 m AGL. The pipes were separated  
406 horizontally by 5 m. There was no precipitation on the days selected for the wind speed  
407 comparisons. The values of  $U_{\text{PRO}}$  and  $U_{\text{RMY}}$  we analyzed were recorded with a data system that  
408 time stamped the 1 Hz  $U_{\text{PRO}}$  and 1 Hz  $U_{\text{RMY}}$  with a relative timing accuracy no worse than 1 s.

409 A wind speed comparison - from 13 December 2019 - is shown in Fig. 4a.  $U_{\text{PRO}}$  was  
410 brought into the comparison by sampling it once per minute from files containing 1 Hz  
411 recordings of the one-minute running-average  $U_{\text{PRO}}$  (Sect. 2.4).  $U_{\text{RMY}}$  was brought into the  
412 comparison by starting with files containing 1 Hz recordings and converting these to one-minute  
413 averages. Fig. 4a shows no evidence of bias and Fig. 4b demonstrates that the average absolute  
414 departure between the  $U_{\text{PRO}}$  and  $U_{\text{RMY}}$  (both one-minute averages) is no larger than ~~10.5~~  $\text{m s}^{-1}$ .  
415 Table 54 has eight more precipitation-free comparisons. Included in the table are temperature  
416 and wind speed averaged over the comparison intervals (4 to 20 UTC), the slope of the linear-  
417 least-squares fit line (forced through the origin, red line), and the lower and upper quartiles of the  
418 slope. The quartiles were calculated using the method of Wolfe and Snider (2012). In contrast to  
419 Figs. 4a-b, Figs. 4c-d make the comparison using 1 Hz values of  $U_{\text{PRO}}$  and  $U_{\text{RMY}}$ . The larger  
420 scatter and larger average absolute departure seen in these panels is a consequence of the  
421 hotplate's limited time response, compared to the R.M.Young. We quantify the hotplate's  
422 response time in terms of a calculated thermal response time. During wintertime at the Laramie  
423 Airport, and with wind speed at  $5 \text{ m s}^{-1}$ , the down-viewing plate's thermal response time is  
424 approximately 60 s (results not shown). Because the temperature of the down-viewing plate is  
425 actively controlled, this does not translate to a 60 s lag between changes in wind speed and the  
426 hotplate response. The  $U_{\text{PRO}}/U_{\text{RMY}}$  departure is most evident at  $U_{\text{PRO}} > 5 \text{ m s}^{-1}$  (Fig. 4d) but this is

- 427 not a concern for  $U_{\text{PRO}}$  on 14/15 December 2016 or on 3 January 2017. Snider (2023)
- 428 demonstrated that the  $U_{\text{PRO}}$  was less than  $5 \text{ m s}^{-1}$  at the hotplate during the two WKA overflights.



444 Figure 4 – (a) Scatterplot of one-minute-averaged  $U_{\text{PRO}}$  and one-minute-averaged  $U_{\text{RMY}}$ .  
 445 Measurements were acquired at the Laramie, WY Airport 13 December 2019. The red line is a  
 446 linear-least-squares fit line (forced through the origin). (b) Average departure between one-  
 447 minute-averaged  $U_{\text{PRO}}$  and one-minute-averaged  $U_{\text{RMY}}$ . Average departures were calculated for  
 448 discrete  $U_{\text{RMY}}$  intervals, and the averages are indicated with short black horizontal lines. Gray  
 449 bars indicate  $\pm 1$  standard deviation. (c) Same as in (a) except for 1 Hz values of  $U_{\text{PRO}}$  and  $U_{\text{RMY}}$ .  
 450 (d) Same as in (b) except for 1 Hz values of  $U_{\text{PRO}}$  and  $U_{\text{RMY}}$ .

451

452

453 Table 54 -  $U_{PRO}$  versus  $U_{RMY}$  correlations

454

Date, UTC <sup>1</sup>	$\langle T \rangle^2$ , °C	$\langle U \rangle^2$ , m s <sup>-1</sup>	$\langle a \rangle^3$	a <sup>4</sup> First Quartile	a <sup>4</sup> Third Quartile
7 December 2019	-0.40	5.40	1.00	0.90	1.04
8 December 2019	2.70	4.10	0.99	0.90	1.04
10 December 2019	-5.20	3.80	0.99	0.83	1.04
13 December 2019	-1.50	6.60	1.00	0.93	1.06
18 December 2019	-6.20	3.60	0.99	0.92	1.04
19 December 2019	-6.90	2.70	0.95	0.84	0.99
6 January 2020	-6.40	8.80	1.01	0.96	1.06
8 January 2020	0.30	4.20	1.00	0.87	1.05
11 January 2020	-7.20	7.00	1.02	0.97	1.08

455

456

457 <sup>1</sup> Statistics presented are based on one-minute-averaged  $U_{PRO}$  and one-minute-averaged  $U_{RMY}$   
 458 measurements made between 04:00 to 20:00 UTC.

459

460 <sup>2</sup> Interval-averaged temperature and interval-averaged wind speed.

461

462 <sup>3</sup> Slope of the one-minute-averaged  $U_{PRO}$  versus one-minute-averaged  $U_{RMY}$  linear-least-squares  
 463 fit line, forced through the origin.

464

465 <sup>4</sup> Quartiles of the slope (see text)

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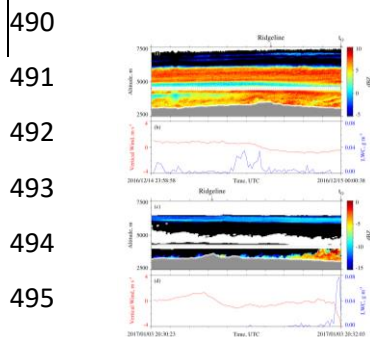
### 467 3.5 – Combined Aircraft and Surface Measurements

468 Figure 5 has WCR and WKA measurements starting 100 s prior to  $t_0$  and ending at  $t_0$ .  
469 The sequences in Figs. 5a and 5c are reflectivities from both the up- and down-looking antennas.  
470 In Fig. 5a the flight track (black dashed horizontal line) is at 4550 m and in Fig. 5c the flight  
471 track is at 4200 m. At the  $t_0$  in Fig. 5a, below the WKA, the maximum radar echo is +6 dBZ ( $Z =$   
472  $4 \text{ mm}^6 \text{ m}^{-3}$ ) and in Fig. 5c the maximum is -3 dBZ ( $Z = 0.5 \text{ mm}^6 \text{ m}^{-3}$ ). Supercooled liquid water  
473 was detected as the aircraft approached the ridgeline (Fig. 5b) and during the last 10 seconds of  
474 the time sequence in Fig. 5d. During these encounters with supercooled liquid, the maximum  
475 LWC values were  $0.03 \times 10^{-3}$  and  $0.08 \times 10^{-3} \text{ kg m}^{-3}$  on 14 December 2016 and 3 January 2017,  
476 respectively. Values of  $N$  (Sect. 2.2) at times of maximal LWC were  $3 \times 10^6$  and  $100 \times 10^6 \text{ m}^{-3}$  on  
477 14 December 2016 and 3 January 2017, respectively. Even on 3 January 2017, the  $\langle D \rangle$  (Sect.  
478 2.2) associated with maximum LWC was sufficient for hexagonal plate crystals with diameter  
479 larger than  $100 \text{ }\mu\text{m}$  to collide with the observed droplets with efficiencies  $> 0.1$  (Wang and Ji  
480 2000).

481 We temporally and spatially averaged the values of  $Z$  we compared with time-averaged  
482 values of  $S$ . There are two reasons for this: 1) As discussed in Sect. 3.1, the WCR did not sample  
483  $Z$  exactly over the hotplate, and furthermore, the width of radar beam at 1500 m range - roughly  
484 the distance between the aircraft and the ground at the overflight times - is 30 m and thus  
485 considerably smaller than the minimum horizontal distance between the aircraft and the HP. 2)  
486 Compared to the WCR, the hotplate is a relatively slow-response measurement system whose  
487 output is commonly averaged over one-minute intervals (Z18).

488

489 [FIGURE 5 WAS REVISED IN REVISION3.](#)



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513 **Figure 5—(a) 100 s of WCR reflectivity and (b) 100 s of LWC and gust probe vertical wind**  
 514 **velocity ending at  $t_0$  on 14/15 December 2016. (c) 100 s of WCR reflectivity and (d) 100 s of**  
 515 **LWC and gust probe vertical wind velocity ending at  $t_0$  on 3 January 2017. In (a) and (c), above**  
 516 **and below the flight track, is the roughly 200-m-deep WCR blind zone, reflectivity above**  
 517 **(below) the flight track is from the up-looking (down-looking) WCR antenna, black indicates**  
 518 **dBZ values smaller than minimum indicated in the color bar, white immediately above the**  
 519 **terrain indicates echo that was discarded because of ground clutter, and white above the ground**  
 520 **clutter and outside of the blind zone indicate  $\text{dBZ} < \text{minimum detectable signal}$ .**

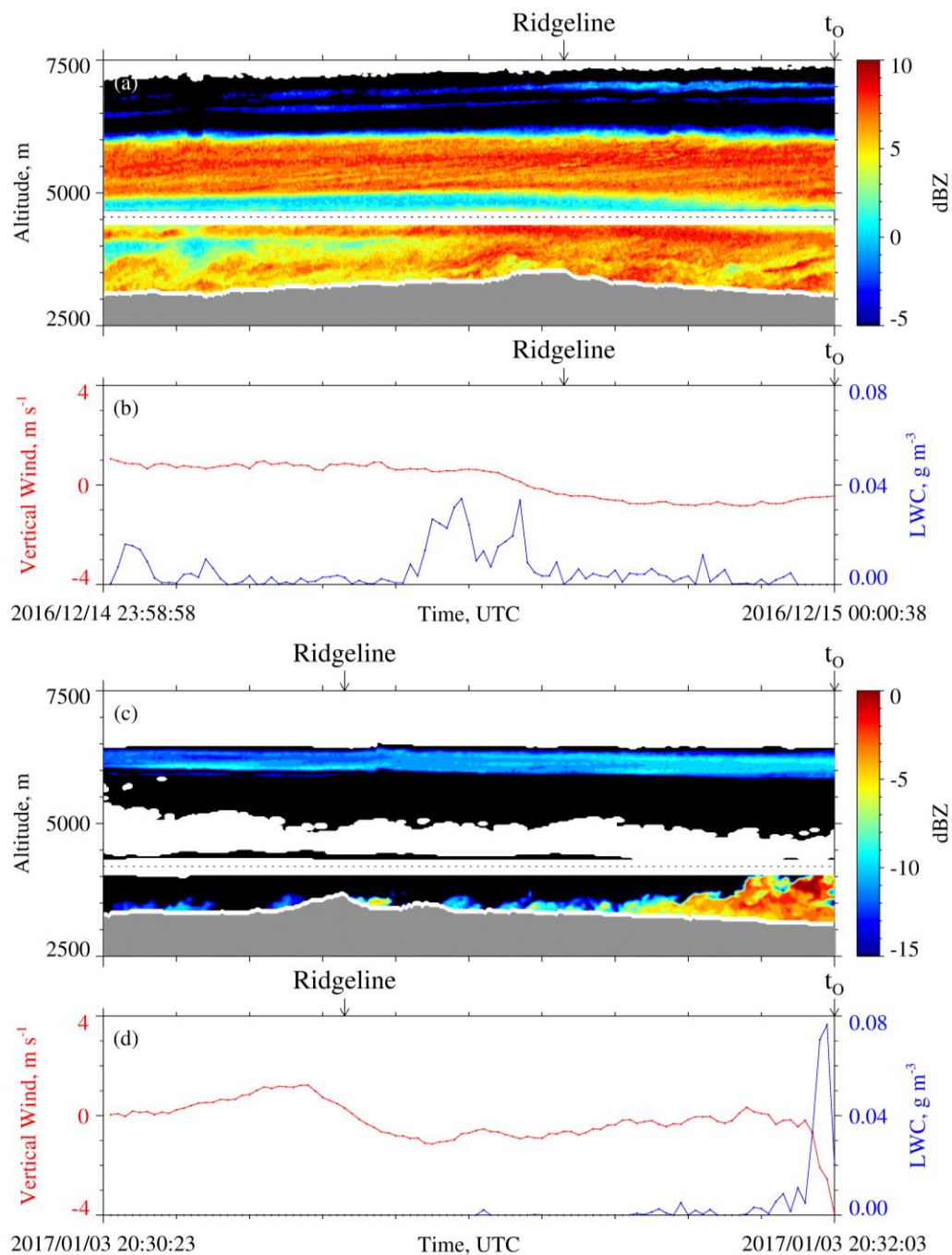


Figure 5 – (a) 100 s of WCR reflectivity and (b) 100 s of LWC and gust probe vertical wind velocity ending at  $t_0$  on 14/15 December 2016. (c) 100 s of WCR reflectivity and (d) 100 s of LWC and gust probe vertical wind velocity ending at  $t_0$  on 3 January 2017. In (a) and (c), above and below the flight track, the roughly 200-m-deep WCR blind zone is evident, reflectivity above (below) the flight track is from the up-looking (down-looking) WCR antenna,



540 black indicates dBZ values smaller than the minimum indicated in the color bar, white  
541 immediately above the terrain indicates echo that was discarded because of ground clutter, and  
542 white above the ground clutter and outside of the blind zone indicate dBZ < minimum detectable  
543 signal.

544 [In our analysis,](#) ~~t~~The HP measurements were averaged over two adjacent 60 s intervals.  
545 The first extends from  $t_0$  to  $t_0 + 60$  s (Fig. 6a) and the second from  $t_0 + 60$  s to  $t_0 + 120$  s (Fig.  
546 6c). In Fig. 6a and in Fig. 6c,  $t_{HP,B}$  symbolizes an interval's beginning time and  $t_{HP,E}$  symbolizes  
547 an interval's ending time. Formulas describing how these times were related to the beginning and  
548 ending time of a corresponding WCR averaging interval are in the Appendix. Fig. 6b is a  
549 schematic of the first WCR averaging interval and Fig. 6d is a schematic of the second. Again,  
550 the subscripts "B" and "E" are used to indicate averaging beginning and ending times. Figures 6b  
551 and 6d both have lines at the top of an averaging interval/domain. The slopes of these lines are  
552 proportional to the ratio of two speeds. These speeds are a maximum likely snow particle speed  
553 toward the ground ( $v_p$ ) and a horizontal wind advection speed ( $v_w$ ). The  $v_p$  was calculated  
554 using averaged vertical-component Doppler velocities and  $v_w$  was calculated using a vertical  
555 profile of horizontal winds, based on WKA horizontal wind measurements and AF horizontal  
556 wind measurements (Figs. A1a-b), and using the WKA track vector (Table [32](#)). An altitude ( $z'_{z'}$   
557 = 3400 m) was assumed in the calculation of  $v_w$ . This is the altitude of the ridges west and  
558 northwest of the HP site (Figs. 3a-b). Picking the altitude to be either  $z'_{z'} = 3200$  m or  $z'_{z'} =$   
559 3600 m does not alter our findings.

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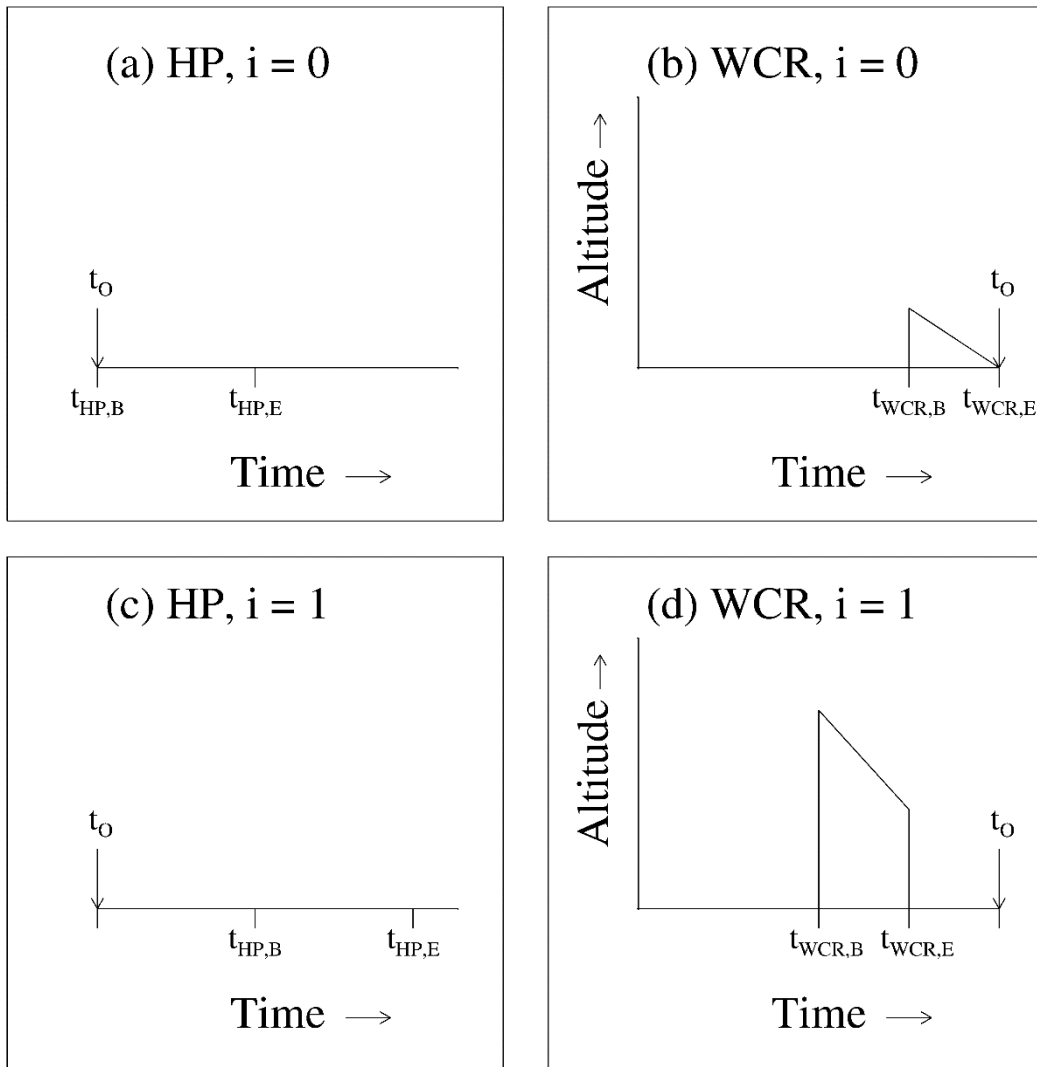


Figure 6 – (a and c) Representations of the  $i = 0$  and  $i = 1$  HP averaging intervals. (b and d)

Representations of the  $i = 0$  and  $i = 1$  WCR averaging intervals/domains. The  $t_0$  is shown in all

panels. The subscripts “B” and “E” indicate beginning and ending times of the HP averaging

(panels a and c) and the beginning and ending times of the WCR averaging (panels b and d).

586

587 All panels in Fig. 6 are labeled with an index designating either the first averaging  
 588 interval ( $i = 0$ ) or the second averaging interval ( $i = 1$ ). Figures 7 and 8 present hotplate  
 589 snowfall measurements from 14/15 December 2016 and 3 January 2017. In these, and in  
 590 subsequent figures, colored circles surround the  $i = 0$  and  $i = 1$  indexes, blue is used to color-  
 591 code 15 December 2016, and red is used to color-code 3 January 2017. Additionally, Fig. 8 has  
 592 an  $i = 2$  averaging interval. This is a special case discussed at the end of this section.

593 Figures 9a-b and Figs. 10a-b have enlarged views of the altitude-time WCR crosssections  
 594 recorded on the two flight days. Different from Fig. 5a and Fig. 5c, these measurements are only  
 595 from the WCR's down-looking antenna. Additional differences are the following: 1) The plots  
 596 are set up so that  $Z$  and  $V_D$  structures downwind of the hotplate can be seen. These structures  
 597 are discussed in the following section. 2) The WCR measurements are shown for 50 s of flight.  
 598 With the WKA ground speed approximately  $125 \text{ m s}^{-1}$  (Table 32), the distance along the abscissa  
 599 is 6250 m. 3) Colored circles that surround the  ~~$i = 0$~~ -indexes are placed below the WCR  
 600 averaging intervals/domains. The latter are drawn with solid black lines and are seen to overlay  
 601 both the  $Z$  and  $V_D$  altitude-time crosssections. Consistent with Figs. 6b and 6d, and the  
 602 Appendix, one of these black lines is vertical and another~~the other~~ is negatively sloped. Figs.  
 603 10a-b also have the  $i = 2$   ~~$i = 2$~~  intervals/domains discussed at the end of this section.

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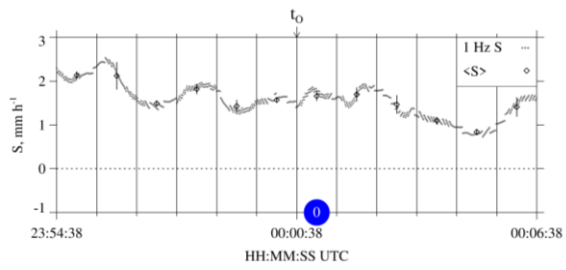
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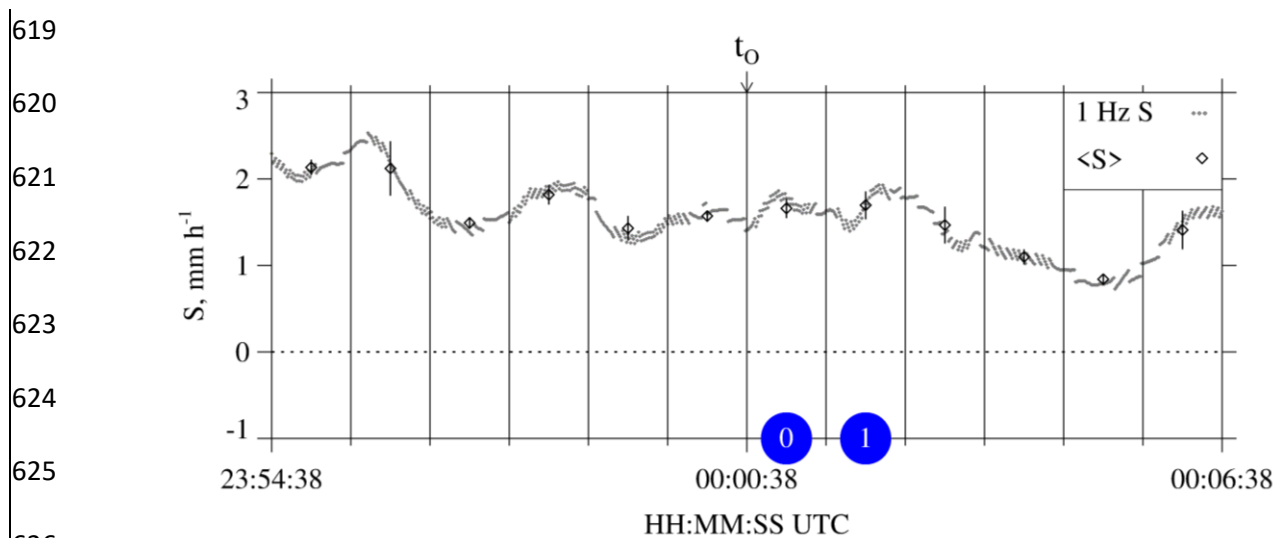
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628 Figure 7 – Twelve minutes of HP snowfall measurements from 14/15 December 2016. Gray dots  
 629 are  $S$  values calculated using hotplate output recorded at 1 Hz. Black diamonds are the one-  
 630 minute-averaged values ( $\pm 1$  standard deviation). The  $t_0$  is shown above the panel and the blue  
 631 circles designate the  $i = 0$  and  $i = 1$  HP averaging intervals.

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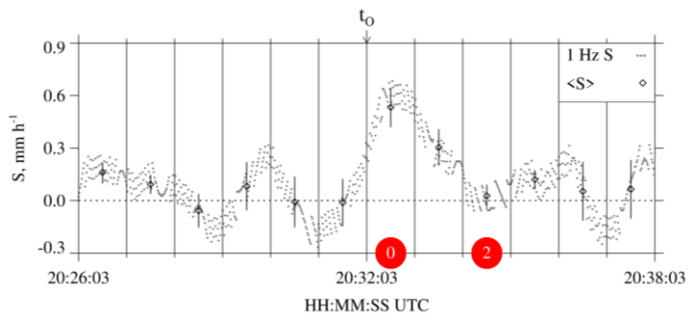
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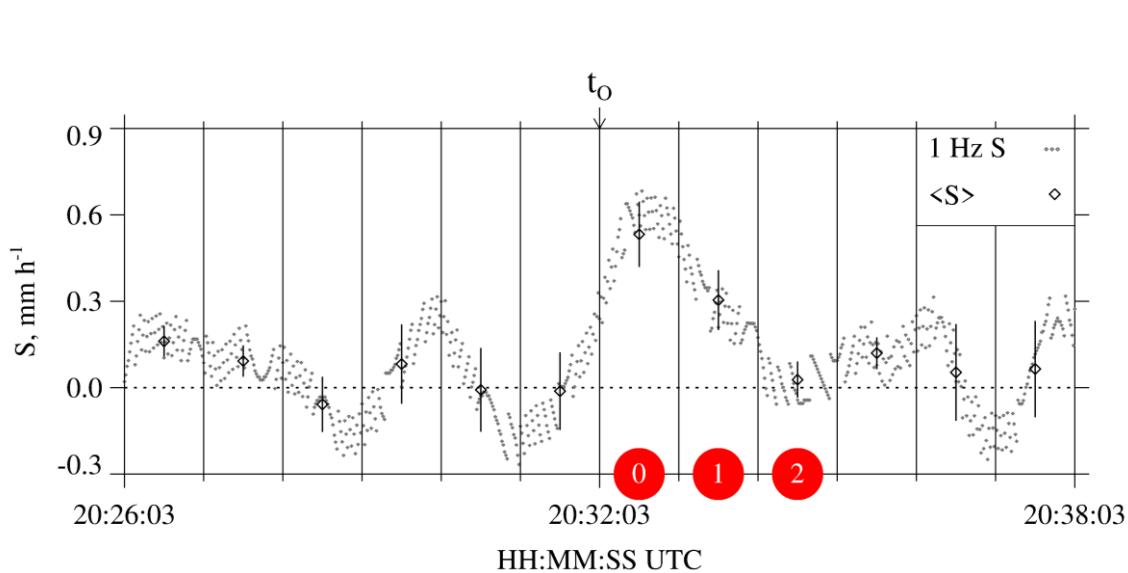
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654 Figure 8 – Twelve minutes of HP snowfall measurements from 3 January 2017. Gray dots are S  
 655 values calculated using hotplate output recorded at 1 Hz. Black diamonds are the one-minute-  
 656 averaged values ( $\pm 1$  standard deviation). The  $t_0$  is shown above the panel and, a red circle  
 657 designates the  $i = 0$ ,  $i = 1$ , and  $i = 2$  HP averaging intervals, and a red circle designates the  $i = 2$   
 658 HP averaging interval. The  $i = 2$  interval latter is a special case discussed at the end of Sect. 3.5.

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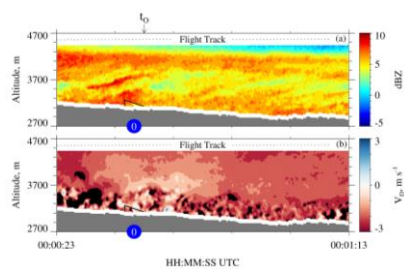
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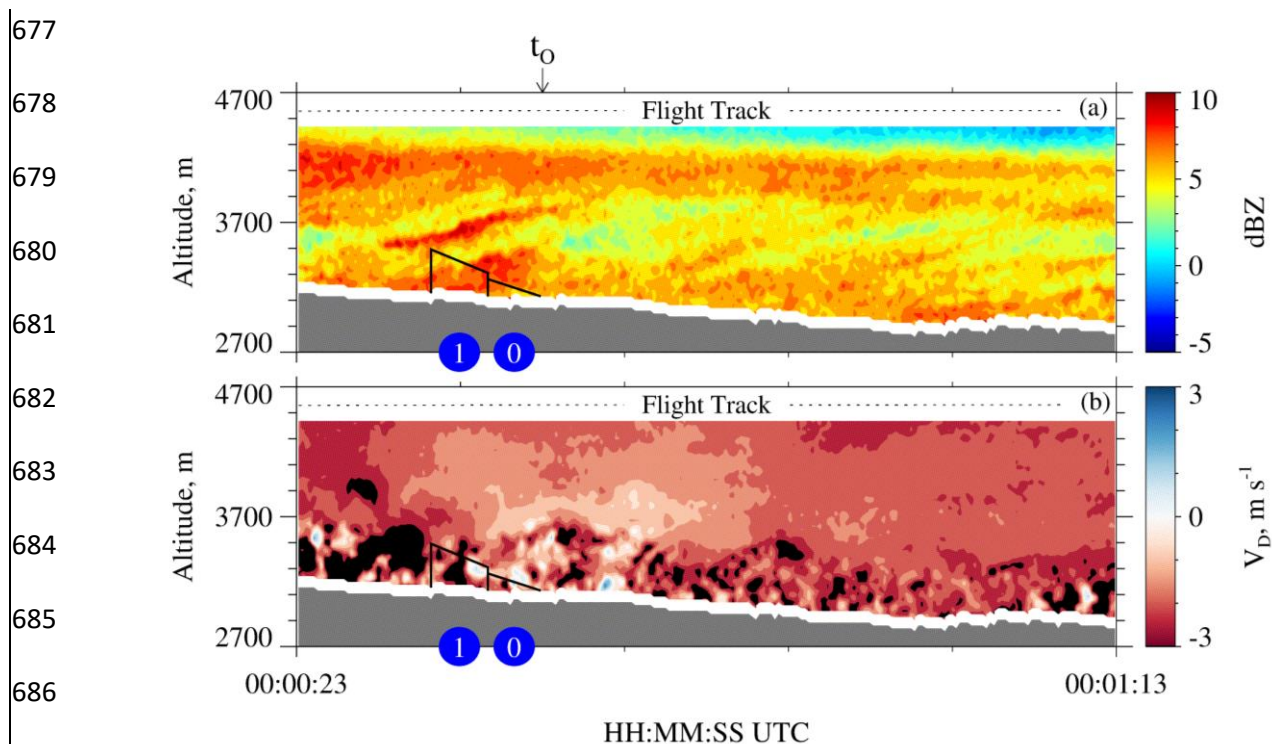
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689 Figure 9 – 50 s of measurements from the down-looking WCR antenna on 15 December 2016.

690 (a) Crosssection of reflectivity  $t_0_- 15$  s to  $t_0_+ 35$  s. (b) Crosssection of Doppler velocity  $t_0_- 15$  s to  
 691  $t_0_+ 35$  s. The  $t_0$  is shown above the top panel. In both panels, the solid black lines (vertical and  
 692 sloped) encompass the  $i = 0$  and  $i = 1$  WCR averaging intervals and blue circles  
 693 designate the  $i = 0$  WCR averaging intervals.

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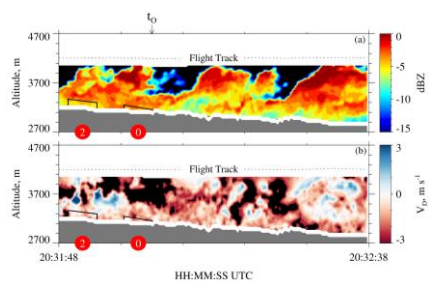
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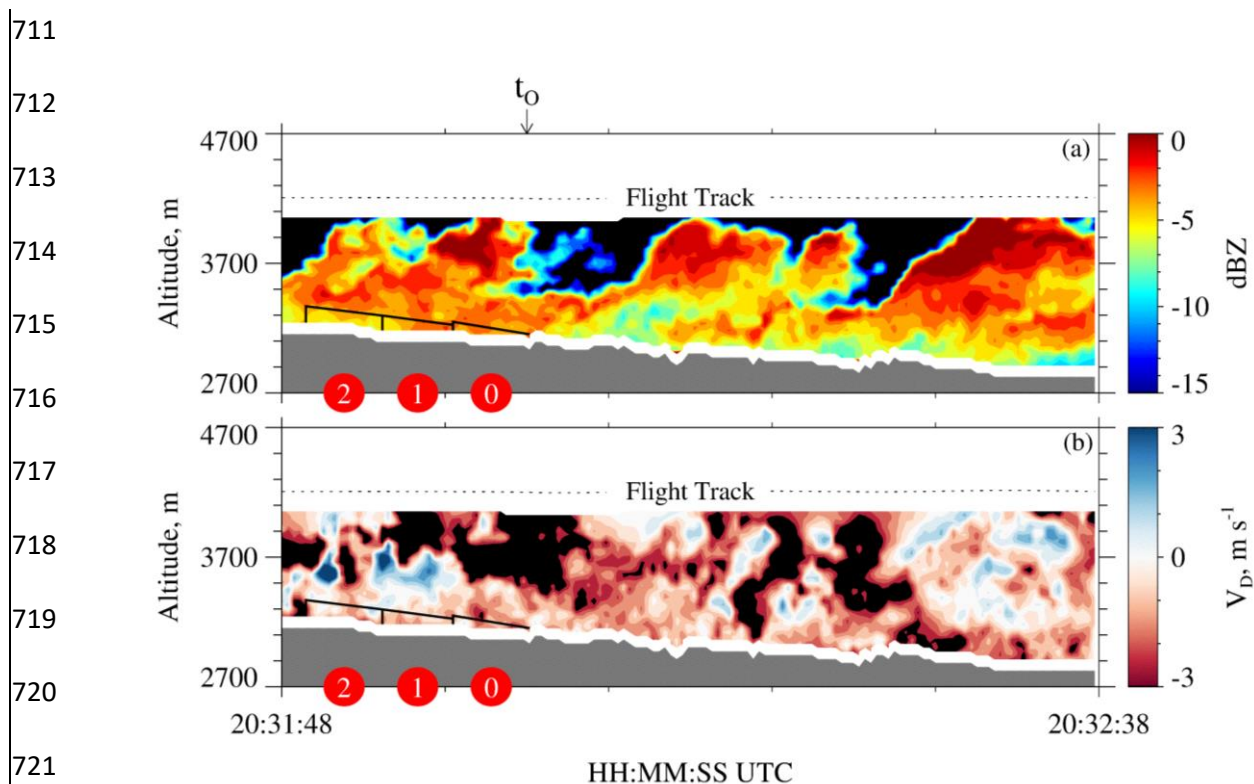
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724 Figure 10 – 50 s of measurements from the down-looking WCR antenna on 3 January 2017. (a)  
 725 Crosssection of reflectivity  $t_0 - 15$  s to  $t_0 + 35$  s. (b) Crosssection of Doppler velocity  $t_0 - 15$  s to  $t_0$   
 726 + 35 s. The  $t_0$  is shown above the top panel. In both panels, the solid black lines (vertical and  
 727 sloped) encompass the  $i = 0$ ,  $i = 1$ , and  $i = 2$  WCR averaging intervals/domains and two red  
 728 circles designate the  $i = 0$ ,  $i = 1$ , and  $i = 2$  WCR averaging intervals/domains averaging  
 729 interval, and two red circles designate the  $i = 2$  WCR averaging interval. The  $i = 2$   
 730 interval/domain is  $i = 2$  intervals/domains are a special case discussed at the end of Sect. 3.5.

731

732 The  $i = 0$  and  $i = 1$  averages of S and Z are presented in Table ~~6~~5 and the corresponding  
 733 averaging intervals are viewable in Fig. 7 and Fig. 9a (15 December 2016) and in Fig. 8 and Fig.  
 734 10a (3 January 2017). ~~The  $i = 1$  averages are also presented in Table 5.~~ According to the  
 735 averaging scheme (Fig. 6), the  $i = 1$  HP averaging interval is time-shifted positively compared to  
 736 the  $i = 0$  HP averaging interval and the  $i = 1$  WCR averaging interval is time-shifted negatively  
 737 compared of the  $i = 0$  WCR averaging interval. This arrangement of the averaging intervals is  
 738 one way to average while also accounting for wind advection of the snow particles.

739 As discussed earlier in this section, the averaging scheme initializes with 60-second  
 740 blocks of HP data between  $\underline{t_o}^{\overline{t_0}}$  and  $\overline{t_0}^{\underline{t_o}+120}$  s. When we applied the scheme to data from 3  
 741 January 2017, but outside the specified time range, an inconsistency was documented. This is  
 742 apparent in Fig. 8, where the  $\underline{t_o}^{\overline{t_0}+120}$  s to  $\underline{t_o}^{\overline{t_0}+180}$  s interval (i.e., the  $\underline{i = 2}^{\overline{i = 2}}$  interval) has  
 743 negligible average S, while in Fig. 10, the  $\underline{i = 2}^{\overline{i = 2}}$  interval has a non-negligible average Z ( $\sim$   
 744  $0.3 \text{ mm}^6 \text{ m}^{-3}$ ). A firm explanation is not available for the inconsistency, but a factor may be the  
 745 convective nature of the fields in Figs. 10a-b. Because of the inconsistency, only averages  
 746 corresponding to the  $\underline{i = 0}^{\overline{i = 0}}$  and  $\underline{i = 1}^{\overline{i = 1}}$  intervals ~~are~~were analyzed further.

747

748 Table 6 – Average wind measurements, average hotplate measurements, average WCR measurements, and attenuation-corrected  
 749 reflectivities

<u>Date</u>	$\frac{v_w^a}{\text{m s}^{-1}}$	<u>i index</u>	$\frac{S_{HP} \pm \sigma^b}{\text{mm h}^{-1}}$	$\frac{\text{WCR}}{\text{Samples}^c}$	$\frac{\langle V_D \rangle^d}{\text{m s}^{-1}}$	$\frac{\sigma_{V_D}^e}{\text{m s}^{-1}}$	$\frac{v_p^f}{\text{m s}^{-1}}$	$\frac{\langle Z \rangle \pm \sigma_Z^g}{\text{mm}^6 \text{ m}^{-3}}$	$\frac{Z'^h}{\text{mm}^6 \text{ m}^{-3}}$
<u>15 December 2016</u>	<u>7.4</u>	<u>0</u>	<u>1.7±0.1</u>	<u>42</u>	<u>-1.3</u>	<u>0.9</u>	<u>2.2</u>	<u>4.9±2.1</u>	<u>6.8</u>
<u>15 December 2016</u>	<u>7.4</u>	<u>1</u>	<u>1.7±0.2</u>	<u>149</u>	<u>-1.8</u>	<u>1.2</u>	<u>3.0</u>	<u>5.6±1.1</u>	<u>7.8</u>
<u>3 January 2017</u>	<u>8.9</u>	<u>0</u>	<u>0.5±0.1</u>	<u>22</u>	<u>-0.9</u>	<u>0.8</u>	<u>1.7</u>	<u>0.49±0.05</u>	<u>0.62</u>
<u>3 January 2017</u>	<u>8.9</u>	<u>1</u>	<u>0.3±0.1</u>	<u>35</u>	<u>-0.8</u>	<u>0.4</u>	<u>1.2</u>	<u>0.50±0.10</u>	<u>0.63</u>

750

751 <sup>a</sup> Horizontal wind advection speed (Eq. A7) calculated using values from the penultimate and last columns of Table 3.

752 <sup>b</sup> One-minute average of the undercatch-corrected liquid-equivalent snowfall rate ( $\pm 1$  standard deviation). An example averaging  
 753 interval is the  $i = 0$  interval in Fig. 7.

754 <sup>c</sup> Number of samples used to calculate the WCR statistics. The averaging intervals/domains (e.g.,  $i = 0$  in Figs. 9a-b and in Figs. 10a-  
 755 b) encompass the WCR samples which are the basis for the WCR statistics presented in this table.

756 <sup>d</sup> Average of Doppler velocity within the averaging intervals/domains.

757 <sup>e</sup> Standard deviation of Doppler velocity within the averaging intervals/domains.

758 <sup>f</sup> Maximum likely snow particle speed toward the ground (Eq. A8).

759 <sup>g</sup> Average reflectivity ( $\pm 1$  standard deviation). These values are not corrected for attenuation.

760 <sup>h</sup> Attenuation-corrected reflectivities. These were derived using reflectivities from the penultimate column of this table, attenuations  
761 from Table 4, and Eq. 1.



762

763

764 Table 5—Averaged wind, hotplate, and WCR measurements

Date	$v_w^a$ , m·s <sup>-1</sup>	i index	$\langle S \rangle \pm \sigma_S^b$ , mm·h <sup>-1</sup>	WCR Samples <sup>c</sup>	$\langle V_D \rangle^d$ , m·s <sup>-1</sup>	$\sigma_{V_D}^e$ , m·s <sup>-1</sup>	$v_p^f$ , m·s <sup>-1</sup>	$\langle Z \rangle \pm \sigma_Z^g$ , mm <sup>6</sup> ·m <sup>-3</sup>
15 December 2016	7.4	0	1.7±0.1	42	-1.3	0.9	2.2	4.9±2.1
15 December 2016	7.4	1	1.7±0.2	149	-1.8	1.2	3.0	5.6±1.1
3 January 2017	8.9	0	0.5±0.1	22	-0.9	0.8	1.7	0.49±0.05
3 January 2017	8.9	1	0.3±0.1	35	-0.8	0.4	1.2	0.50±0.10

765

766 <sup>a</sup>Horizontal wind advection speed (Eq. A7) calculated using values from the penultimate and last  
767 columns of Table 2.

768

769 <sup>b</sup>One-minute average of the undercatch-corrected liquid-equivalent snowfall rate ( $\pm 1$  standard  
770 deviation). An example averaging interval is the interval in Fig. 7.

771

772 <sup>c</sup>Number of samples used to calculate WCR statistics in the penultimate four columns. The  
773 averaging intervals/domains (e.g.,  $i=0$  in Figs. 9a-b and in Figs. 10a-b) encompass the averaged  
774 WCR samples.

775

776 <sup>d</sup>Average of Doppler velocity within the averaging intervals/domains.

777

778 <sup>e</sup>Standard deviation of Doppler velocity within the averaging intervals/domains.

779

780 <sup>f</sup>Maximum likely snow particle speed toward the ground (Eq. A8).

781

782 <sup>g</sup>Average reflectivity ( $\pm 1$  standard deviation). These values are not corrected for attenuation.

783

### 784 3.6 - Snow Particle Imagery

785 In Fig. 9a and Fig. 10a, the time for a snow particle to move the abscissa and ordinate  
 786 distances is different. The ratio of these two times is 2.6. This follows from our choice of  
 787 abscissa and ordinate ranges, from values of particle fall speed ( $1 \text{ m s}^{-1}$ ) and horizontal wind  
 788 advection speed ( $8 \text{ m s}^{-1}$ ), which we assumed, and from the WKA ground speed ( $gs \sim 125 \text{ m s}^{-1}$ ;  
 789 Table 32). The assumed values are approximately consistent with values of  $\langle V_D \rangle$  and  $v_w$ , in  
 790 Table 65, and with the  $V_D$  sign convention (Sect. 2.3). We also used  $gs = 125 \text{ m s}^{-1}$  to scale  
 791 (virtually) the time axes in Fig. 9a and Fig. 10a to a horizontal distance. Within the scaled  
 792 coordinate frames, we assumed that all snow particle trajectories have negative slope ( $\Delta z / \Delta x = -$   
 793  $1 \text{ m s}^{-1} / 8 \text{ m s}^{-1} = -0.12$ ) and that all trajectories are stationary. However, both assumptions seem  
 794 inconsistent with the reflectivity structures in Fig. 5a, where positively-sloped particle fall  
 795 streaks are evident at  $\sim 5500 \text{ m}$ , inconsistent with Fig. 9a where positively-sloped fall streaks are  
 796 at  $\sim 3500 \text{ m}$ , and inconsistent with the positively-sloped fall streaks in Fig. 10a. On both flight  
 797 days, the fall streaks evince particle sources that move horizontally and with a horizontal speed  
 798 that is larger than the  $v_w = 8 \text{ m s}^{-1}$  applied in the estimate of the trajectory slope. It may be that  
 799 the source's horizontal speed is comparable to the flight-level WKA-derived horizontal wind (27  
 800 to  $32 \text{ m s}^{-1}$ ; Table 32) but we do not have data needed to verify that assertion. Based on the  
 801 assumption that snow particles followed the fall streaks while both were advecting horizontally,  
 802 we looked *downwind* of the hotplate - at a time later than  $t_0$  in Fig. 9a and Fig. 10a - for particles  
 803 that became those that produced snowfall at the hotplate.

804 Particle images from 15 December 2016 were analyzed using the 2DP. With this  
 805 instrument the maximum all-in particle size (in the horizontal direction perpendicular to flight) is

806 6400  $\mu\text{m}$  and the particle size resolution is 200  $\mu\text{m}$  (Sect. 2.2). Within the time interval picked  
807 for this analysis (discussed below), particles sizing in the smaller of the two spectral modes, with  
808 mode size  $\sim 400 \mu\text{m}$ , were more numerous (results not shown). Because the 400  $\mu\text{m}$  particles are  
809 poorly resolved by the 2DP, and the same can be said for somewhat larger particles, those  
810 smaller than 1000  $\mu\text{m}$  were excluded from the following analysis. Figure 11a shows imagery  
811 from 12 s of measurements acquired near the end of the sequence in Fig. 9a (00:01:02 to  
812 00:01:14). This time interval was selected by tracing forward from  $t_0$ , along the slope of the fall  
813 streaks, to the flight level. Many of the particles are rounded (indicating riming) and a few have  
814 arms likely due to incomplete conversion of branched crystals to rimed snow particles. The mode  
815 size corresponding to these images is 1600  $\mu\text{m}$ . No liquid water was detected with these particles  
816 ( $\text{LWC} < 0.01 \times 10^{-3} \text{ kg m}^{-3}$ ; Fuller 2020; her Fig. 8), but liquid was detected, at  $\sim 00:00:00$ , as the  
817 aircraft approached the ridgeline (Figs. 5a-b).

818 Turning to imagery from 3 January 2017, the most appropriate location for analysis  
819 would be through the second billow structure evident in Fig. 10a ([i.e., very close to the middle of](#)  
820 [the Fig. 10a sequence](#)). This billow sourced a fall streak that terminated at the hotplate (i.e., at  
821 the time  $t_0$  indicated in the figure). However, the aircraft only clipped the top of this billow, and  
822 it was only when sampling the billow seen  $\sim 13$  s earlier that larger ice particle concentrations ( $\sim$   
823  $20,000 \text{ m}^{-3}$ ) (Fuller 2020; her Fig. 10) and larger LWC ( $\sim 0.08 \times 10^{-3} \text{ kg m}^{-3}$ ; Fig. 5d) were  
824 detected. Maximum reflectivities were the same in all three billows ( $Z \sim 1 \text{ mm}^6 \text{ m}^{-3}$ ; 0 dBZ), so it  
825 was assumed that imagery collected in the first billow (20:32:00 to 20:32:02) was representative  
826 of what was falling toward the hotplate. The 2DS was used to image these particles (Fig. 11b);  
827 with this instrument the maximum all-in particle size (in the horizontal direction perpendicular to  
828 flight) is 1280  $\mu\text{m}$  and the size resolution is 10  $\mu\text{m}$  (Sect. 2.2). Most of the objects in Fig. 11b

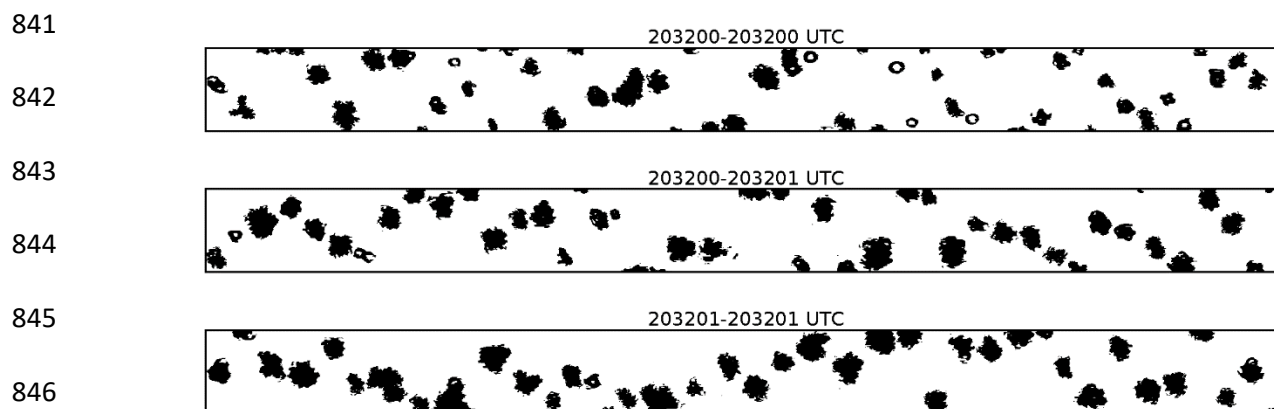
829 appear to be rimed and their mode size is  $\sim 400 \mu\text{m}$ . It is also noted that particles smaller than  
830  $100 \mu\text{m}$  were eliminated from these images, however, compared to the  $\sim 400 \mu\text{m}$  particles those  
831 smaller than  $100 \mu\text{m}$  were significantly less abundant (results not shown).

832

833 (a)



840 (b)

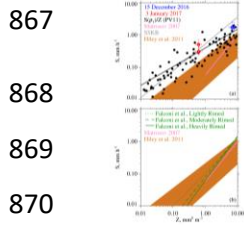


848 Figure 11 – (a) 2DP particle imagery from 15 December 2016. The height of the strips is 6400  
849  $\mu\text{m}$ . These particles are estimated to be representative of those that fell from flight level toward  
850 the hotplate. (b) 2DS particle imagery from 3 January 2017. The height of the strips is 1280  $\mu\text{m}$ .  
851 These particles are estimated to be representative of those that fell from flight level toward the  
852 hotplate.

854 **3.7 – S/Z Relationships**

855 Our S/Z pairs are presented in Table ~~65~~ where the indexes ( $i = 0$  and  $i = 1$ ) are used to  
856 indicate results derived for the averaging intervals. [In the penultimate column of Table 6,](#)  
857 [reflectivities are not corrected for attenuation, however, in the last column of Table 6 and in Fig.](#)  
858 [12, the attenuation-corrected reflectivities are presented.](#) ~~In Table 5, reflectivities are not~~  
859 ~~corrected for attenuation, however, in Fig. 12a, attenuation-corrected reflectivities are plotted.~~  
860 Reflectivities from [the penultimate column of Table 65](#), attenuations from Table ~~43~~, and Eq. 1  
861 were used to calculate the corrected reflectivities. Also shown [in Fig. 12 \(black filled circles\)](#) is a  
862 subset of the S/Z pairs from PV11's Fig. 11 ( $0.01 < Z < 10 \text{ mm}^6 \text{ mm}^{-3}$ ) and the PV11 best-fit line  
863 (black). Results from PV11 are specified as  $S(\rho_1)/Z$  because those authors applied the lower of  
864 two density-size functions ( $\rho_1$ ), and the lower of two fall speed-size functions, with airborne  
865 measurements, in calculations of snowfall rates (Sect. 1 [and Table 1](#)).

866 [THIS FIGURE WAS REVISED IN REVISION3.](#)



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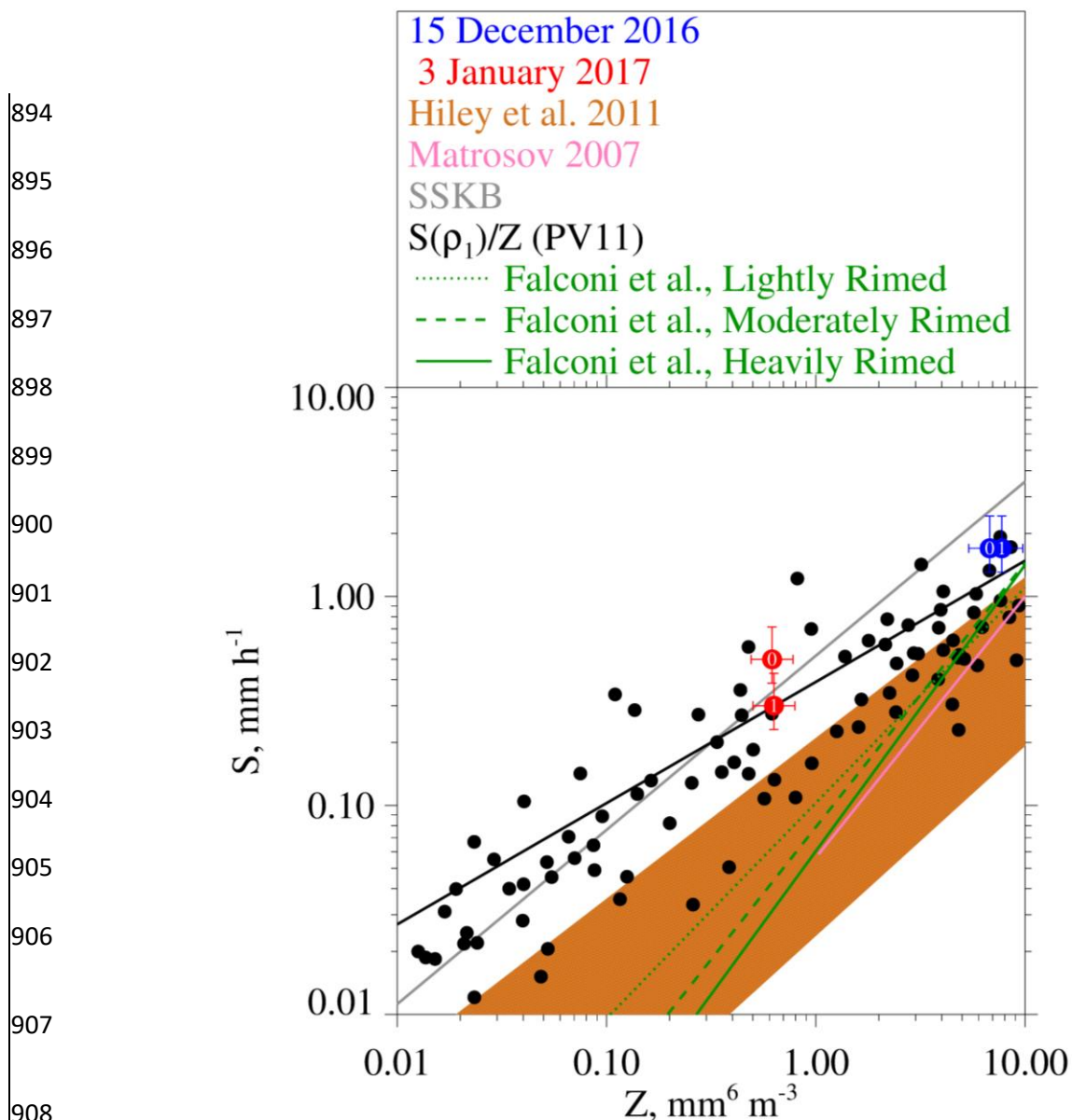
882

883

884 **Figure 12— a) Snowfall rate versus radar reflectivity. Colored circles indicate attenuation-**  
 885 **corrected reflectivities (Table 3, Table 5, and Eq. 1) for the  $i=0$  and  $i=1$  averaging intervals.**  
 886 **Error bars on these points represent the precision of the Z measurement (Sect. 2.3) and the**  
 887 **precision of the S measurement (Sect. 2.4). The  $S(\rho_1)/Z$  points are a subset from PV11’s Fig. 11**  
 888 **( $0.01 < Z < 10 \text{ mm}^6 \text{ mm}^{-3}$ ). Also plotted is the PV11 best fit line (black) (Sect. 1), the S/Z**  
 889 **relationship from Matrosov (2007) (Sect. 1), the S/Z relationship abbreviated SSKB (Sect. 1),**  
 890 **and the swath of S/Z relationships from Hiley et al. (2011) (Sect. 1). b) S/Z relationships from**  
 891 **Faloni et al. (2018) (their Table 2) (Sect. 1), the Matrosov (2007) relationship, and the swath of**  
 892 **S/Z relationships from Hiley et al. (2011) are shown.**

893





909 [Figure 12 – Snowfall rate versus radar reflectivity. Red and blue circles are plotted at](#)  
 910 [attenuation-corrected reflectivities \(Table 6\) for the  \$i = 0\$  and  \$i = 1\$  averaging intervals. Error](#)  
 911 [bars on these points represent precisions of the reflectivity \(Sect. 2.3\) and snowfall rate \(Sect.](#)  
 912 [2.4\) measurements. Also plotted are the S/Z relationship lines from Sect. 1 and Table 1. These](#)  
 913 [are the S/Z lines defining the swath of S/Z relationships from Hiley et al. \(2011\), the S/Z](#)  
 914 [relationship from Matrosov \(2007\), the S/Z relationship abbreviated SSKB, PV11’s best-fit line,](#)

915 and the S/Z relationships from Falconi et al. (2018) (their Table 2). The  $S(\rho_1)/Z$  points (black  
916 filled circles) are a subset from PV11's Fig. 11 ( $0.01 < Z < 10 \text{ mm}^6 \text{ mm}^{-3}$ ).

917           There are two potential biases in the values of [snowfall rates](#) we ~~tabulate~~ ~~measured~~  
918 (Table [6](#)) and plot (Fig. 12a). First, the two snowfall events had flight-level vertical wind  
919 velocities ([Figs. 5b and 5d](#)) that were positive (upward) upwind of the [ridgeline summit](#), and vice  
920 versa downwind of the [ridgeline summit](#). Except for the strongest downdraft on 3 January 2017,  
921 the magnitude of this variance is  $\sim 1 \text{ m s}^{-1}$  ([Figs. 5b and 5d](#)). Assuming  $1 \text{ m s}^{-1}$  was the  
922 downward wind immediately over the hotplate, the snow particles would have approached the  
923 [HP](#) gauge faster than their fall speed. Our basis for stating this is fall speeds for the mode sizes  
924 discussed in Sect. 3.6 (1600 and 400  $\mu\text{m}$ ) and our assumption that the particles were graupel.  
925 (Table [7](#) has these characteristic sizes and fall speeds.) However, the conjectured downdraft  
926 speed is likely an overestimate - because of divergence occurring as the draft approached the  
927 surface - and because the sizes in Table [7](#) likely underestimate what fell to the hotplate.  
928 Relevant to the last of these assertions, we used the altitude/T/RH measurements (Table [3](#)) to  
929 calculate the vertical distance available for growth via riming, and thus for a fall speed increase,  
930 between the flight level and the lifted condensation level. Assuming an adiabatically-stratified  
931 liquid cloud and unit collection efficiency (these assumptions overestimate growth by riming),  
932 and no change of particle cross-section (underestimates growth by riming), our calculations  
933 indicate that relative increases of size and fall speed were 40 and 20 %, respectively, on 3  
934 January 2017, and that these relative increases were a factor-of-two larger on 15 December 2016.  
935

936 Table 76 – Estimates of snow particle fall speed

Date	Mode Size, $\mu\text{m}$	Assumed Particle Type	Fall Speed, $\text{m s}^{-1}$	Reference
15 December 2016 <del>5</del>	1600	graupel	1.4	PV11; assuming $\rho_1$ in their Fig. 5
3 January 2017 <del>6</del>	400	graupel	0.7	PV11; assuming $\rho_1$ in their Fig. 5

937

938

939           Second, there is concern that values of  $S$  from 3 January 2017 are underestimated.  
940   Although values of  $S$  must be  $> 0$ , we presented 1 Hz values (gray points, Fig. 8) approaching -  
941    $0.3 \text{ mm h}^{-1}$ . Negative values resulted because we did not impose a threshold of  $0 \text{ mm h}^{-1}$  on the  
942   uncorrected snowfall rates (this thresholding is discussed in Z18) and because negative snowfall  
943   rate values (uncorrected for catch inefficiency) are amplified by the gauge-catch correction (Sect.  
944   2.4). The implication is that  $0.2 \text{ mm h}^{-1}$  could be added to the one-minute averaged values of  
945   [snowfall rate](#) $S$  in Table [65](#) and in Fig. 12a. Here, the assumption is that an averaged  $S$  of  $-0.2$   
946    $\text{mm h}^{-1}$ , in Fig. 8, ~~is indicating~~[indicates](#) no snowfall at the hotplate; however, because the  
947   hotplate was operated autonomously (Sect. 2.1) we have no way to verify the assumption.

948

949 **4 – Results**

950 Figure 12a shows ~~our~~ the four snowfall rate/reflectivity S/Z pairs (red and blue circles, ~~our~~  
 951 ~~measurements~~) after the reflectivities were corrected for attenuation. The error bars on these data  
 952 pairs represent the precision of the Z measurement (Sect. 2.3) and the precision of the S  
 953 measurement (Sect. 2.4). Presentation clarity was what guided the selection of S and Z axis  
 954 ranges in this figure but with the consequence that 32 of PV11's S/Z pairs are not shown because  
 955 they plot at  $Z > 10 \text{ mm}^6 \text{ m}^{-3}$ . The way that the PV11 data pairs scatter closest to  $Z = 10 \text{ mm}^6 \text{ m}^{-3}$ ,  
 956 combined with the fact that the PV11 data pairs ~~points~~ at  $Z > 10 \text{ mm}^6 \text{ m}^{-3}$  are not shown, could  
 957 lead to the interpretation that the slope describing the best-fit relationship, at Z approximately  $> 2$   
 958  $\text{mm}^6 \text{ m}^{-3}$ , ~~should be decreased relative to the~~ actual slope of the PV11 best-fit line. Readers who  
 959 view PV11's Fig. 11 will conclude that this interpretation is not warranted. ~~The four S/Z pairs~~  
 960 ~~(red and blue circles) plot above the PV11 best-fit line but within the variability of PV11's S/Z~~  
 961 ~~pairs.~~

962 As is discussed in Sect. 1, c ~~Computation-based~~ nal W-band S/Z relationship have inputs  
 963 from parameterized descriptions of density, shape, fall speed, PSD, and particle size ~~(Sect. 1)~~.  
 964 The computation-based S/Z relationships are in the top three rows of Table 1; the subsequent two  
 965 rows of Table 1 have S/Z relationships that resulted from a hybridization of measurements and  
 966 calculations (PV11 and Falconi et al. 2018). ~~Matrosov (2007) did calculations for the snow~~  
 967 ~~particle type known as aggregates. Hiley et al. (2011) did calculations for 20 snow particle types.~~  
 968 ~~Except for a S/Z calculation done for aggregate snowflakes, the calculations of Hiley et al.~~  
 969 ~~(2011) were for the particle type known as vapor-grown crystals. Hiley et al. (2011) did not~~  
 970 ~~model spherical snow particles. The latter were modeled by Surussavadee and Staelin (2007) and~~

971 ~~Kulie and Bennartz (2009). In Fig. 12a, the abbreviation SSKB is used to symbolize the~~  
972 ~~computational S/Z relationship for spherical snow particles.~~

973 We now compare our snowfall rates (fourth column of Table 6) to snowfall rates where  
974 they plot on an S/Z relationship line evaluated at one of our attenuation-corrected reflectivities.  
975 The departure between these is reported as a relative S difference expressed as  $|(S_{HP}-S)|/S$  where  
976  $S_{HP}$  is from Table 6 and where S is on an S/Z relationship line. All possible comparisons are  
977 presented graphically in Fig. 12. Table 1 has both the minimum relative S differences and the  
978 salient maximum relative S differences. The comparisons will be discussed in the order of  
979 presentation in Table 1.

980 In comparisons of our snowfall rates and the upper-limit S/Z relationship line from Hiley  
981 et al. (2011) the relative difference is no smaller than 0.7 and 1.0 on 15 December and 3 January,  
982 respectively. These minimum relative differences exceed the hotplate precision (Sect. 2.4) by at  
983 least a factor of two. It is concluded that our paired values of undercatch-corrected precipitation  
984 rate and attenuation-corrected radar reflectivity provide evidence that a calculation of S based on  
985 the Hiley et al. (2011) upper-limit, when applied to rimed snow particles, is associated with a  
986 low-biased estimate of S. A retrieval based on Hiley et al.'s average S/Z relationship (not  
987 shown), which bisects the orange region in Fig. 12, corresponds to an even larger low bias. This  
988 is a concern because Hiley et al. (2011) used their average S/Z relationship to retrieve global  
989 snowfall distributions and since global observations reported in Wang et al. (2013) document the  
990 frequent occurrence of supercooled liquid within snowing clouds.

991

992 Figure 12a shows the separation between our measurements S/Z pairs and the Matrosov  
 993 (2007) calculation. The separation is about a factor of two (minimum relative difference = 1.4)  
 994 for the points obtained on 15 December 2016 and corresponds to an underestimation of S (low  
 995 bias) when compared to our measurements. The points ~~from~~obtained on 3 January 2017 plot at  
 996 an attenuation-corrected reflectivity Z-smaller than the lower-limit of the calculation (Matrosov  
 997 2007). Since the particle images (Fig. 11a-b) reveal no evidence ~~offer~~ for the particle type modeled  
 998 by Matrosov (2007) (aggregate ~~snowflakes~~), it is not surprising that the Matrosov S/Z  
 999 relationship calculation is not representative of our measurements.

1000 ~~Departures between our S measurements (Fig. 12a) and S/Z calculations from Hiley et al.~~  
 1001 ~~(2011) were evaluated as the vertical distance between the top of the orange region and our S/Z~~  
 1002 ~~data pairs. Snowfall rates at the top of the orange region were calculated using attenuation-~~  
 1003 ~~corrected reflectivities (Eq. 1 and Table 5) and using the upper limit S/Z equation from Hiley et~~  
 1004 ~~al. (2011) ( $S = 0.21 \cdot (Z')^{0.77}$ ; Sect. 1 and Eq. 1). The departures were evaluated as a relative~~  
 1005 ~~difference expressed as  $(S_{HP} - S)/S$  with  $S_{HP}$  one of four snowfall rates from Table 5. The relative~~  
 1006 ~~difference is no smaller than 0.7 and 1.0 on 15 December and 3 January, respectively. These~~  
 1007 ~~minimum relative differences exceed the hotplate precision (Sect. 2.4) by at least a factor of two.~~  
 1008 ~~It is concluded that our paired values of surface-measured precipitation rate and aircraft-~~  
 1009 ~~measured radar reflectivity, after correcting for attenuation, provide evidence that a calculation~~  
 1010 ~~of S based on the Hiley et al. (2011) upper limit, when applied to rimed snow particles, is~~  
 1011 ~~associated with a low-biased estimate of S.~~

1012 ~~A plausible explanation~~ One plausible reason for the low bias discussed in the previous  
 1013 two paragraphs is the smaller density implicit in most computationally-based S/Z relationships  
 1014 and especially those which assume that snow particles are crystals. Densities are quite different



1015 for crystals versus that for rimed snow particles. For example, in Brown and Francis (1995),  
 1016 assuming a 2 mm crystal, the density is  $\sim 30 \text{ kg m}^{-3}$ , whereas in PV11 (their Eq. 1), assuming a 2  
 1017 mm graupel particle, the density is  $\sim 200 \text{ kg m}^{-3}$ . Because aggregates are collections of crystals,  
 1018 this comparison of crystal and graupel densities also seems relevant to a comparison of graupel  
 1019 and aggregate snow particle densities.

1020 ~~Fig. 12a~~ Figure 12 compares our  $S_{HP} / Z'$  data pairs to the SSKB S/Z relationship line  
 1021 ~~developed using density =  $200 \text{ kg m}^{-3}$  (Sect. 1).~~ and Table 1 presents the relative differences  
 1022 between the data pairs and the SSKB line. ~~also has the SSKB relationship. This was developed~~  
 1023 ~~using density =  $200 \text{ kg m}^{-3}$  (Sect. 1).~~ Compared to the S/Z relationship represented by top of the  
 1024 orange region in Fig. 12, and compared to the Matrosov 2007 relationship<sup>a</sup>, the SSKB line plots  
 1025 closer to our data points (minimum relative difference  $\sim 0.3$ ). We note that the only instances of  
 1026  $S_{HP} < S$  are three of four comparisons of our measurements to the SSKB relationship. A possible  
 1027 reason for this is that the density applied in SSKB (Table 1) is not entirely representative of  
 1028 conditions during our study. An analysis of the sensitivity of the SSKB to a change in density is  
 1029 needed to investigate our assertion. ~~and closer to many of those reported by PV11.~~

1030 Comparisons of our  $S_{HP} / Z'$  data pairs and PV11's best-fit line are also in Table 1. The  
 1031 table demonstrates that the agreement is reasonable - minimum relative difference no larger than  
 1032 0.3 – and Fig. 12 shows that our data pairs plot at or above the PV11 best fit line.

1033 Based on data from PV11 and our  $S_{HP} / Z'$  data pairs ~~result~~, as well as the S/Z relationship  
 1034 abbreviated SSKB ~~(Sect. 1)~~, it is expected that the S/Z relationships reported by Falconi et al.  
 1035 (2018) for rimed snow particles (Sect. 1) would plot higher in S-versus-Z space than is illustrated  
 1036 in Fig. 12~~b~~. Notably, only the upper-end of the Falconi et al. lines (i.e., at  $Z > 8 \text{ mm}^6 \text{ m}^{-3}$ ) plot

1037 above the upper-limit that Hiley et al. (2011) ~~developed~~<sup>established</sup> for unrimed snow particles.  
 1038 A plausible explanation for the lower-than-expected S/Z relationships of Falconi et al. is now  
 1039 offered. Falconi et al. used liquid water path as a proxy for the extent of snow particle riming  
 1040 (von Lerber et al. 2017). A consequence may have been that the proxy did not dependably  
 1041 exclude unrimed snow particles (crystals and aggregates) from the riming categories of Falconi  
 1042 et al. If this was ~~the case~~<sup>true</sup>, then the data groupings that were the basis for the Falconi et al. S/Z  
 1043 relationships may have been affected. When applying the heavily-rimed S/Z relationship of  
 1044 Falconi et al. with our  $S_{HP} / Z'$  data pairs we find that the minimum relative differences are 0.6  
 1045 (December 15) and 8.5 (January 3) (Table 1). Additionally, the differences are 0.5 (December  
 1046 15) and 5.9 (January 3) when applying the moderately-rimed S/Z relationship of Falconi et al.  
 1047 (results not shown). Further research is needed to resolve the reason for the mismatch between  
 1048 ~~S/Z pairs,~~ the snowfall rate/reflectivity pairs reported ~~both here and in PV11,~~ here and the S/Z  
 1049 relationships reported in Falconi et al.

1050 Our conclusion that the upper-limit S/Z relationship from Hiley et al. (2011)  
 1051 underestimates S would be modified if our WCR-derived reflectivities were negatively biased.  
 1052 Assuming the reflectivities are negatively biased by 2.5 dBZ, the minimum relative differences  
 1053 discussed previously are no smaller than 0.1 and 0.3 on 15 December and 3 January,  
 1054 respectively. A bias in reflectivity of this magnitude cannot be ruled out but neither can a  
 1055 positive bias of the same magnitude (Sect. 2.3). The latter increases the minimum relative  
 1056 differences to 1.6 and 2.2 on 15 December and 3 January, respectively. In each of these  
 1057 calculations we have summed the attenuations (Table ~~4~~<sup>3</sup>) with  $\pm 2.5$  dBZ and used Eq. 1 to  
 1058 calculate error-perturbed reflectivities.

1059 The scatter of measurements in Fig. 12a, the plausibility of a -2.5 to +2.5 dBZ bias in  
1060 WCR reflectivity measurements, and error in measurement of S (Sect. 2.4), indicate that refined  
1061 techniques will be needed in future investigations which apply the approach described here.

1062 Taking into consideration the goal of evaluating snowfall rates from space, some advance in  
1063 satellite remote sensing also seems warranted. One issue is diagnosing where riming is occurring  
1064 within clouds. Both lidars and radiometers can sense supercooled liquid water from space (e.g.,  
1065 Battaglia and Panegrossi, 2020), and if combined with Doppler radars operating at multiple  
1066 wavelengths, can diagnose precipitation attributable to rimed snow particles. Despite limitations  
1067 of the multiple-wavelength Doppler method, for example in scenarios with vertical air speed  
1068 comparable to and larger than particle fall speed (Vogl et al. 2022), the method has been  
1069 validated in ground-based field studies (Kneifel et al. 2015; Mason et al. 2018). Technical  
1070 challenges also remain for implementing the method from space (Battaglia et al.

1071 ~~2020). Additionally, improved methods are needed to diagnose situations where riming is~~  
1072 ~~occurring within clouds. Both lidars and radiometers can sense supercooled liquid water from~~  
1073 ~~space (e.g., Battaglia and Panegrossi, 2020), and if combined with Doppler radar, can diagnose~~  
1074 ~~precipitation attributable to rimed snow particles. These approaches are being tested in ground-~~  
1075 ~~based field studies (Kneifel et al. 2015; Moisseev et al. 2017; Mason et al. 2018) but are most~~  
1076 ~~reliable in scenarios with the magnitude of vertical air speed smaller than particle fall speed.~~

## 1077 **5 — Conclusions**

1078 We have reported ~~The reported measurements consist of~~ surface measurements of S and  
1079 near-surface measurements of Z. The latter came from overflights of a ground site, where a  
1080 precipitation gauge was operated, and were acquired using an airborne W-band radar. The values  
1081 of Z were corrected for attenuation.

1082 The reported  $S/S_{HP} / Z'/Z$  pairs plot at or above the S-versus-Z best-fit line of PV11 (Fig.  
 1083 [12](#)) and the ~~minimum relative S difference~~ (Table 1) is no larger than 0.3. ~~However, the points do~~  
 1084 ~~not depart beyond the variability evident in a replotting of S/Z pairs from PV11.~~ The PV11 data  
 1085 came from airborne measurements of W-band reflectivity, acquired within  $\pm 100$  m of flight  
 1086 level, and from coincident measurements of snow particle imagery. PV11 used a density-size  
 1087 function and a fall speed-size function, and measurements (PSD and particle images) to calculate  
 1088 [S for snow particles that were classified as both rimed crystals and graupel.](#) ~~This classification~~  
 1089 [is also consistent with the particle imagery we have presented \(Fig. 11\).](#)

1090 ~~There is a~~ We have documented a substantial difference in comparisons ~~n offset~~ between  
 1091 ~~our the snowfall rates~~ [S points, reported here,](#) and reflectivity-dependent S values calculated ~~at~~  
 1092 [using](#) an upper-limit S/Z relationship for unrimed snow particles (Hiley et al. 2011). [Here the](#)  
 1093 [minimum relative S differences are 0.7 and 1.0 for our two overflights and in a comparison to](#)  
 1094 [our measurements correspond to an underestimation of snowfall rate \(Fig. 12\).](#) ~~The relative~~  
 1095 ~~differences offset are~~ [is approximately a factor of two](#) larger than the precision of [our snowfall](#)  
 1096 ~~rate~~ ~~the S~~ measurement. [We also report a substantial difference, and S underestimation compared](#)  
 1097 [to our measurements \(Fig. 12\), for the comparison made to an S/Z relationship which assumes](#)  
 1098 [the snow particles are aggregates \(Matrosov 2007\). The snowfall rate underestimates obtained](#)  
 1099 [using both Hiley et al.'s and Matrosov's S/Z relationships \(Fig. 12\) are perhaps expected given](#)  
 1100 [that the density factored into those S/Z calculations is small compared to that for rimed snow](#)  
 1101 [particles. It is also expected that the larger density and spherical shape applied in the SSKB S/Z](#)  
 1102 [relationship contributed to the better agreement \(minimum relative difference  \$\sim 0.3\$ \) with our](#)  
 1103 [S<sub>HP</sub> / Z' pairs.](#) Our conclusion is that some snowfall retrievals (e.g., Hiley et al. 2011) will  
 1104 [underestimate S for weather targets containing rimed snow particles. We also state that our](#)

1105 [conclusion is at odds with measurements and analysis in Falconi et al. Those researchers](#)  
1106 [reported S/Z relationships for rimed snow particles which in instances with  \$Z < 8 \text{ mm}^6 \text{ m}^{-3}\$  plot](#)  
1107 [below the upper-limit of Hiley et al. \(Fig. 12\). The consequence is that the minimum relative S](#)  
1108 [difference in our comparison to Falconi et al. \(assuming Falconi et al.'s heavily-rimed](#)  
1109 [classification\) is comparable to and larger than in our comparison to the Hiley et al.'s upper-limit](#)  
1110 [S/Z relationship.](#)

1111 ~~This suggests that a measured Z and the Hiley et al. (2011) upper limit will produce an~~  
1112 ~~underestimate of precipitation in scenarios dominated by rimed snow particles.~~

1113 New research is needed to refine the S/Z relationship for rimed snow particles. This could  
1114 be computational – e.g., investigation ~~ofing~~ the utility of parameterizing S in terms of both Z and  
1115 density – or could be observational. Unlike the investigation of PV11, where only an airborne  
1116 platform was employed, we have demonstrated that useful information can be obtained using  
1117 coordinated ground-based and airborne systems. Another approach would be with only ground-  
1118 based instrumentation. This would avoid some of the complications encountered in this study,  
1119 including W-band attenuation and a reliance on particle imagery acquired aloft. A study with  
1120 both ground-based and airborne systems would [also](#) be useful for understanding [an](#) S/Z  
1121 mismatch, apparent at  $Z < 8 \text{ mm}^6 \text{ m}^{-3}$ , ~~and which is larger than the offset summarized in the~~  
1122 ~~previous paragraph.~~ Elements of the mismatch are ~~the S/Z measurements reported by PV11,~~ the  
1123 measurements reported here, [PV11's best-fit line](#), and the measurement-based S/Z relationships  
1124 reported by Falconi et al. (2018). These three research teams reported measurements relevant to  
1125 the development of [an](#) S/Z relationship for rimed snow particles.

1126 **6 – Appendix**

1127 This appendix explains how HP (hotplate) and WCR (Wyoming Cloud Radar) averages  
 1128 were evaluated. The scheme starts with an HP averaging interval (duration 60 s) and derives a  
 1129 WCR averaging interval and a WCR averaging domain. The latter encompasses a subset of the  
 1130 altitude-time crossection sampled by the WCR. The top boundary of the domain was derived  
 1131 using vertical-component Doppler velocities within the interval/domain. Because of this  
 1132 dependence, the line defining the top boundary ~~had to be~~ was derived iteratively.

1133 With the overflight time symbolized  $t_0$ , the beginning and ending times of ~~the first of two~~  
 1134 60-second HP averaging intervals are

$$1135 \quad \underline{t_{HP,B} = t_0} \quad \del{t_{HP,B} = t_0} \quad (A1)$$

$$1136 \quad t_{HP,E} = t_0 + 60 \quad (A2)$$

1137 Since two adjacent HP averaging intervals are evaluated in this analysis, we express the  
 1138 averaging times with the following recursive equations

$$1139 \quad t_{HP,B}(i) = t_0 + i \cdot 60 \quad (A3)$$

1140 and

$$1141 \quad t_{HP,E}(i) = t_0 + (i+1) \cdot 60. \quad (A4)$$

1142 In Eqs. A3-A4 the index is  ~~$i \in \{0, 1\}$~~   $i \in \{0, 1\}$ . A special case with  ~~$i = 2$~~  is also analyzed (~~in~~ Sect.  
 1143 3.5).

1144 Analogous to the recursion in Eq. A4, the ending time of a WCR averaging interval is

$$1145 \quad t_{WCR,E}(i) = t_0 - i \cdot 60 \cdot v_w / g_s. \quad (A5)$$

1146 Here  $v_w$  is a wind advection speed (discussed below) and the second term on the rhs is a wind  
 1147 advection distance divided by the WKA (Wyoming King Air) ground speed ( $gs$ ). Analogous  
 1148 to the Eq. A5, the beginning time of a WCR averaging interval is

$$1149 \quad t_{WCR,B}(i) = t_{WCR,E} - (i+1) \cdot 60 \cdot v_w / gs \quad (A6)$$

1150 The wind advection speed ( $v_w$ ) in Eqs. A5-A6 was calculated using an altitude-  
 1151 dependent west-to-east wind velocity ( $u$ ) and an altitude-dependent south-to-north wind  
 1152 velocity ( $v$ ). These altitude-dependent component velocities were calculated using the  
 1153 horizontal wind vectors in the penultimate and last columns of Table 32. Plots of the component  
 1154 velocities versus altitude and the linear functions used to relate component velocities to altitude  
 1155 are presented in Figs. A1a-b.

1156 An altitude ( $z' = 3400$  m) was assumed for evaluating the horizontal wind advection  
 1157 vector. This is the altitude of the ridges west and northwest of the HP site (Figs. 3a-b).

1158 The WKA track vector (Table 32) defines the vertical plane of the WCR measurements.  
 1159 We assumed that wind advection of snow particles occurred parallel to this vector. With the  
 1160 assumption stated in the previous paragraph, the horizontal wind advection speed ( $v_w$ ) was  
 1161 calculated as the projection of the horizontal wind vector onto the track vector.

$$1162 \quad v_w = \frac{u(z') \cdot gs_x + v(z') \cdot gs_y}{(gs_x^2 + gs_y^2)^{1/2}} \quad (A7)$$

1163 In Eq. A7 the west-to-east and south-to-north components of the track vector are symbolized  $gs_x$   
 1164 and  $gs_y$ . Vector representations of the track vector are in Table 32. On 14/15 December 2016 and  
 1165 3 January 2017, the values of  $v_w$  are 7.4 and 8.9 m s<sup>-1</sup>, respectively.

1166 In addition to the properties  $gs$  and  $v_w$  used to evaluate Eqs. A5-A6, a WCR  
 1167 averaging interval/domain was evaluated using a snow particle downward speed (Eq. A8).

$$1168 \quad v_p = | \langle V_D \rangle | + \sigma_{V_D} \quad (A8)$$

1169 Here,  $\langle V_D \rangle$  is the average of Doppler velocities within an averaging interval/domain,  
 1170  $| \langle V_D \rangle |$  is the absolute value of the average, and  $\sigma_{V_D}$  is the standard deviation of the average.

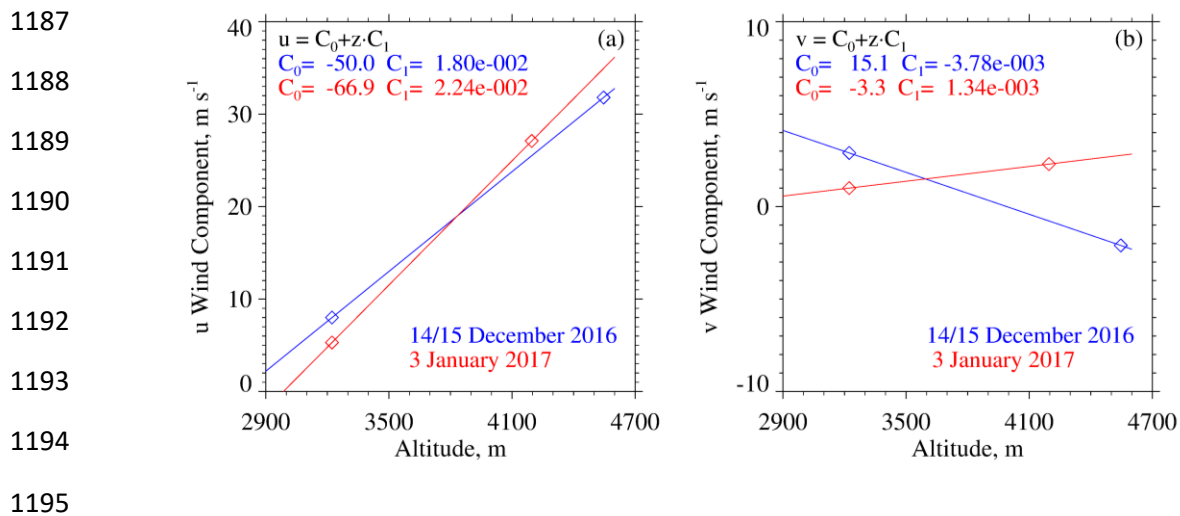
1171 On both the lhs and rhs of Eq. A8, all terms are greater than zero.

1172 We interpret  $v_p$  as the maximum likely snow particle speed toward the ground. There are  
 1173 three reasons for this: 1) For the WCR averaging intervals/domains we analyzed, values of  
 1174  $\langle V_D \rangle$  were consistently less than zero (Table 65). This indicates that snow particles (on  
 1175 average) were moving toward the ground. 2) Again, for the WCR averaging intervals/domains  
 1176 we analyzed,  $\sigma_{V_D}$  was comparable to  $| \langle V_D \rangle |$ . This indicates that turbulent eddies transported  
 1177 snow particles upward and downward at a speed comparable their downward speed in still air. 3)  
 1178 The  $V_D$  are reflectivity weighted (Haimov and Rodi 2013) and are thus indicative of the motion  
 1179 of the largest particles within an averaging interval/domain.

1180 We now focus on the top boundary of a WCR averaging interval/domain. Figures 6b and  
 1181 6d have representations of the boundary. The slope defining this boundary was calculated as  
 1182  $-v_p \cdot gs / v_w$ . That is, particles below this boundary moved downward sufficiently fast and  
 1183 horizontally sufficiently slow to advect reasonably close to the hotplate. Starting with diagnosed  
 1184 values of  $gs$  and  $v_w$ , the values of  $v_p$  and slope, were derived iteratively. The precision of the  
 1185 derived  $v_p$  is  $\pm 0.1 \text{ m s}^{-1}$ .

1186





1196 Figure A1 – (a) West-to-east ( $u$ ) wind velocity derived using measurements from the WKA  
 1197 and the AmeriFlux (AF) tower. Also shown is the linear function used to relate  $u$  to altitude.  
 1198 (b) South-to-north ( $v$ ) wind velocity derived using measurements from the WKA and AF. Also  
 1199 shown is the linear function used to relate  $v$  to altitude. WKA and AF velocities are presented  
 1200 as vectors in the penultimate and last columns of Table 32.  
 1201

1202 Data Availability. The WKA and WCR measurements can be obtained from the SNOWIE data  
1203 archive of NCAR/EOL, which is sponsored by the National Science Foundation. Hotplate gauge  
1204 measurements are at <https://doi.org/10.15786/20103146>. The US-GLE AmeriFlux measurements  
1205 are at <https://ameriflux.lbl.gov/>. The Brooklyn Lake SNOTEL gauge measurements are at  
1206 <https://www.wcc.nrcs.usda.gov/snow/>. Merged Hotplate, SNOTEL, and AmeriFlux data  
1207 sequences from 14/15 December 2016 and 3 January 2017 are in Snider (2023).

1208

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1210 measurements were performed by SF, SM, SH, MB, and JS. SF wrote her MS dissertation, and  
1211 this was adapted for this paper by JS. KS processed the snow particle imagery. AM maintained  
1212 the measurement sites. All authors contributed to the editing of this paper.  
1213

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1221

1222 **References**

- 1223 AmeriFlux, <https://ameriflux.lbl.gov/>, 2021
- 1224 Battaglia, A. and Panegrossi, G., What Can We Learn from the CloudSat Radiometric Mode Observations  
1225 of Snowfall over the Ice-Free Ocean?, 12, 3285, <https://doi.org/10.3390/rs12203285>, 2020
- 1226 [Battaglia, A., Tanelli, S., Tridon, F., Kneifel, S., Leinonen, J., and Kollias, P., Triple-Frequency Radar](#)  
1227 [Retrievals, In: Levizzani, V., Kidd, C., Kirschbaum, D.B., Kummerow, C.D., Nakamura, K., Turk,](#)  
1228 [F.J. \(eds\) \*Satellite Precipitation Measurement, Advances in Global Change Research, vol 67.\*](#)  
1229 [Springer, Cham. <https://doi.org/10.1007/978-3-030-24568-9> 13, 2020](#)
- 1230 Boudala, F.S., R. Rasmussen, G.A. Isaac, and B. Scott, Performance of Hot Plate for Measuring Solid  
1231 Precipitation in Complex Terrain during the 2010 Vancouver Winter Olympics, J. Atmos. Oceanic  
1232 Technol., 31, 437–446, <https://doi.org/10.1175/JTECH-D-12-00247.1>, 2014
- 1233 Braham , R. R., Snow Particle Size Spectra in Lake Effect Snows. J. Appl. Meteor. Climatol., 29, 200–207,  
1234 [https://doi.org/10.1175/1520-0450\(1990\)029<0200:SPSSIL>2.0.CO;2](https://doi.org/10.1175/1520-0450(1990)029<0200:SPSSIL>2.0.CO;2), 1990
- 1235 Brock, F. V., and Richardson, S. J., Meteorological Measurement Systems, Oxford University Press, New  
1236 York, 304 pp., 2001
- 1237 Brown, P. R. A., and P. N. Francis, Improved Measurements of the Ice Water Content in Cirrus Using a  
1238 Total-Water Probe. J. Atmos. Oceanic Technol., 12, 410–414, [https://doi.org/10.1175/1520-0426\(1995\)012<0410:IMOTIW>2.0.CO;2](https://doi.org/10.1175/1520-0426(1995)012<0410:IMOTIW>2.0.CO;2), 1995
- 1239
- 1240 Cocks, S.B., S.M. Martinaitis, B. Kaney, J. Zhang, and K. Howard, MRMS QPE Performance during the  
1241 2013/14 Cool Season, J. Hydrometeor., 17, 791–810, <https://doi.org/10.1175/JHM-D-15-0095.1>,  
1242 2016
- 1243 Faber, S., French, J. R., and Jackson, R., Laboratory and in-flight evaluation of measurement uncertainties  
1244 from a commercial Cloud Droplet Probe (CDP), Atmos. Meas. Tech., 11, 3645–3659,  
1245 <https://doi.org/10.5194/amt-11-3645-2018>, 2018
- 1246 Falconi, M. T., von Lerber, A., Ori, D., Marzano, F. S., and Moisseev, D.: Snowfall retrieval at X, Ka and  
1247 W bands: consistency of backscattering and microphysical properties using BAECC ground-based  
1248 measurements, Atmos. Meas. Tech., 11, 3059–3079, <https://doi.org/10.5194/amt-11-3059-2018>,  
1249 2018

- 1250 Field, P.R., Hogan, R.J., Brown, P.R.A., Illingworth, A.J., Choullarton, T.W. and Cotton, R.J.,  
1251 Parametrization of ice-particle size distributions for mid-latitude stratiform cloud. *Q.J.R. Meteorol.*  
1252 *Soc.*, 131: 1997-2017. <https://doi.org/10.1256/qj.04.134>, 2005
- 1253 Fuller, S.E., Improvement of the Snowfall / Reflectivity Relationship for W-band Radars, MS Thesis,  
1254 Department of Atmospheric Science, University of Wyoming, 2020
- 1255 Geerts, B., Q. Miao, Y. Yang, R. Rasmussen, and D. Breed, An Airborne Profiling Radar Study of the  
1256 Impact of Glaciogenic Cloud Seeding on Snowfall from Winter Orographic Clouds, *J. Atmos. Sci.*,  
1257 67, 3286–3302, <https://doi.org/10.1175/2010JAS3496.1>, 2010
- 1258 Haimov, S., and Rodi, A., Fixed-Antenna Pointing-Angle Calibration of Airborne Doppler Cloud Radar,  
1259 *Journal of Atmospheric and Oceanic Technology*, 30, 2320-2335, [https://doi.org/10.1175/JTECH-](https://doi.org/10.1175/JTECH-D-12-00262.1)  
1260 [D-12-00262.1](https://doi.org/10.1175/JTECH-D-12-00262.1), 2013
- 1261 Hiley, M. J., M. S. Kulie, and R. Bennartz, Uncertainty Analysis for CloudSat Snowfall Retrievals, *J. Appl.*  
1262 *Meteor. Climatol.*, 50, 399–418, 2011
- 1263 Kneifel, S., von Lerber, A., Tiira, J., Moisseev, D., Kollias, P., and Leinonen, J., Observed relations between  
1264 snowfall microphysics and triple-frequency radar measurements. *J. Geophys. Res. Atmos.*, 120,  
1265 6034– 6055, doi: 10.1002/2015JD023156, 2015
- 1266 Kochendorfer, J., Nitu, R., Wolff, M., Mekis, E., Rasmussen, R., Baker, B., and Jachcik, A, Testing and  
1267 development of transfer functions for weighing precipitation gauges in WMO-SPICE, *Hydrology*  
1268 *and Earth System Sciences*, 2, 1437-1452, <https://doi.org/10.5194/hess-22-1437-2018>, 2018
- 1269 Korolev, A. V., E. F. Emery, J. W. Strapp, S. G. Cober, G. A. Isaac, M. Wasey, and D. Marcotte, Small ice  
1270 particles in tropospheric clouds: Fact or artifact? Airborne Icing Instrumentation Evaluation  
1271 Experiment, *Bull. Amer. Meteor. Soc.*, 92, 967–973, <https://doi.org/10.1175/2010BAMS3141.1>,  
1272 2011
- 1273 Kulie, M. S., and R. Bennartz, Utilizing Spaceborne Radars to Retrieve Dry Snowfall, *J. Appl. Meteor.*  
1274 *Climatol.*, 48, 2564–2580, <https://doi.org/10.1175/2009JAMC2193.1>, 2009
- 1275 Kulie, M. S., Milani, L., Wood, N. B., Tushaus, S. A., Bennartz, R., and L'Ecuyer, T. S., A Shallow  
1276 Cumuliform Snowfall Census Using Spaceborne Radar, *Journal of Hydrometeorology*, 4, 1261-  
1277 1279, <https://doi.org/10.1175/JHM-D-15-0123.1>, 2016
- 1278 Lawson, R. P., O'Connor, D., Zmarzly, P., Weaver, K., Baker, B., Mo, Q., and Jonsson, H., The 2D-S  
1279 (Stereo) Probe: Design and Preliminary Tests of a New Airborne, High-Speed, High-Resolution

- 1280 Particle Imaging Probe, *J. Atmos. Ocean. Tech.*, 23, 1462–1477,  
1281 <https://doi.org/10.1175/JTECH1927.1>, 2006
- 1282 Liebe, H.J., Manabe, T., and Hufford, G.A., Millimeter–wave attenuation and delay rates due fog/cloud  
1283 conditions, *IEEE Trans. Antenn. Propag.*, 37, 1617–1623, 1989
- 1284 Liu, C.-L., and A. J. Illingworth, Toward more accurate retrievals of ice water content from radar  
1285 measurements of clouds, *J. Appl. Meteor.*, 39, 1130–1146, 2000
- 1286 Locatelli, J.D. and Hobbs, P.V., Fall speed and masses of solid precipitation particles, *J. Geophys. Res.*, 79,  
1287 2185–2197, <https://doi.org/10.1029/JC079i015p02185>, 1974
- 1288 Macklin, W.C., The density and structure of ice formed by accretion, *Q.J.R.Meteorol.Soc.*, 88: 30-50.  
1289 [doi:10.1002/qj.49708837504](https://doi.org/10.1002/qj.49708837504), <https://doi.org/10.1002/qj.49708837504>, 1962
- 1290 Marlow, S.A, J.M. Frank, M. Burkhart, B. Borkhuu, S.E. Fuller, and J.R. Snider, Snowfall Measurements  
1291 at Wind-exposed and Sheltered Sites in the Rocky Mountains of Southeastern Wyoming, in  
1292 revision for the *Journal of Applied Meteorology and Climatology*, [http://www-](http://www-das.uwyo.edu/~jsnider/manuscript_revision2.docx)  
1293 [das.uwyo.edu/~jsnider/manuscript\\_revision2.docx](http://www-das.uwyo.edu/~jsnider/manuscript_revision2.docx), 2023
- 1294 Martinaitis, S.M., S.B. Cocks, Y. Qi, B.T. Kaney, J. Zhang, and K. Howard, Understanding winter  
1295 precipitation impacts on automated gauge observations within a real-rime system, *J. Hydrometeor.*,  
1296 16, 2345-2363, <https://doi.org/10.1175/JHM-D-15-0020.1>, 2015
- 1297 Mason, S. L., Chiu, C. J., Hogan, R. J., Moisseev, D., and Kneifel, S., Retrievals of riming and snow density  
1298 from vertically pointing Doppler radars, *Journal of Geophysical Research: Atmospheres*, 123,  
1299 13,807– 13,834, <https://doi.org/10.1029/2018JD028603>, 2018
- 1300 Matrosov, S.Y., Modeling Backscatter Properties of Snowfall at Millimeter Wavelengths, *J. Atmos. Sci.*,  
1301 64, 1727-1736, <https://doi.org/10.1175/JAS3904.1>, 2007
- 1302 ~~Moisseev, D., von Lerber, A., and Tiira, J., Quantifying the effect of riming on snowfall using ground-~~  
1303 ~~based observations, *J. Geophys. Res. Atmos.*, 122, 4019–4037, [doi:10.1002/2016JD026272](https://doi.org/10.1002/2016JD026272), 2017~~
- 1304 Nemarich, J., Wellman, R.J., and Lacombe, J., Backscatter and attenuation by falling snow and rain at 96,  
1305 140, and 225 GHz, *IEEE Trans. Geosci. Remote*, 26, 319–329, 1988
- 1306 Panofsky, H.A. and Dutton, J.A., *Atmospheric Turbulence*, Wiley-Interscience, New York, 397 pp., 1984

- 1307 Pokharel, B. and G. Vali, Evaluation of Collocated Measurements of Radar Reflectivity and Particle Sizes  
1308 in Ice Clouds, *J. Appl. Meteor. Climatol.*, 50, 2104–2119, [https://doi.org/10.1175/JAMC-D-](https://doi.org/10.1175/JAMC-D-1005010.1)  
1309 1005010.1, 2011
- 1310 Rasmussen, R.M., J. Hallett, R. Purcell, S.D. Landolt, and J. Cole, The Hotplate precipitation gauge, *J.*  
1311 *Atmos. Oceanic Technol.*, 28, 148-164, <https://doi.org/10.1175/2010JTECHA1375.1>, 2011
- 1312 R.M. Young Company, Model 05103 Wind Monitor, 2001
- 1313 Skofronick-Jackson, G., and Coauthors, The Global Precipitation Measurement (GPM) Mission for  
1314 science and society, *Bull. Amer. Meteor. Soc.*, 98, 1679–1695, [https://doi.org/10.1175/BAMS-D-](https://doi.org/10.1175/BAMS-D-15-00306.1)  
1315 15-00306.1, 2017
- 1316 Smith, P.L., Equivalent radar reflectivity factors for snow and ice particles, *J. Climatol. Appl. Meteor.*, 23,  
1317 1258–1260, [https://doi.org/10.1175/1520-0450\(1984\)023<1258:ERRFFS>2.0.CO;2](https://doi.org/10.1175/1520-0450(1984)023<1258:ERRFFS>2.0.CO;2), 1984
- 1318 Snider, J.R., Supplemental dataset for Marlow et al. (2023), <https://doi.org/10.15786/20247870>, 2023
- 1319 Surussavadee, C., and D. H. Staelin, Millimeter-Wave Precipitation Retrievals and Observed-versus-  
1320 Simulated Radiance Distributions: Sensitivity to Assumptions. *J. Atmos. Sci.*, 64, 3808–3826,  
1321 <https://doi.org/10.1175/2006JAS2045.1>, 2007
- 1322 Tessendorf, S. A., and Coauthors, A transformational approach to winter orographic weather modification  
1323 research: The SNOWIE Project, *Bulletin of the American Meteorological Society*, 100, 71–92,  
1324 <https://doi.org/10.1175/BAMS-D-17-0152.1>, 2019
- 1325 Ulaby, F.T., Moore, R.K., and Fung, K., *Microwave Remote Sensing: Active and Passive*, Vol. 1,  
1326 *Microwave Remote Sensing Fundamentals and Radiometry*, ARTECH HOUSE Inc., Norwood,  
1327 MA, p. 456., 1981
- 1328 Vali, G. and Haimov, S., Observed extinction by clouds at 95 GHz, *IEEE Trans. Geosci. Remote*, 39, 190–  
1329 193, 2001
- 1330 [Vogl, T., Maahn, M., Kneifel, S., Schimmel, W., Moisseev, D., and Kalesse-Los, H.: Using artificial neural  
1331 networks to predict riming from Doppler cloud radar observations, \*Atmos. Meas. Tech.\*, 15, 365–  
1332 381, <https://doi.org/10.5194/amt-15-365-2022>, 2022](https://doi.org/10.5194/amt-15-365-2022)
- 1333 von Lerber, A., D. Moisseev, L. F. Bliven, W. Petersen, A. Harri, and V. Chandrasekar: Microphysical  
1334 Properties of Snow and Their Link to Ze–S Relations during BAECC 2014. *J. Appl. Meteor.*  
1335 *Climatol.*, 56, 1561–1582, <https://doi.org/10.1175/JAMC-D-16-0379.1>, 2017



- 1336 [Wang, Y., G.Liu, E.Seo, and Y.Fu, Liquid water in snowing clouds: Implications for satellite remote](#)  
1337 [sensing of snowfall, Atmos. Res., 60-72, 10.1016/j.atmosres.2012.06.008, 2013](#)
- 1338 Wang, P.K., and W. Ji, Collision Efficiencies of Ice Crystals at Low–Intermediate Reynolds Numbers  
1339 Colliding with Supercooled Cloud Droplets: A Numerical Study, *Journal of the Atmospheric*  
1340 *Sciences*, 57, 1001-1009, [https://doi.org/10.1175/1520-0469\(2000\)057<1001:CEOICA>2.0.CO;2](https://doi.org/10.1175/1520-0469(2000)057<1001:CEOICA>2.0.CO;2),  
1341 2000
- 1342 Wilson, J., and E. Brandes, Radar measurement of rainfall—A summary, *Bull. Amer. Meteor. Soc.*, 60,  
1343 1048–1058, [https://doi.org/10.1175/1520-0477\(1979\)060<1048:RMORS>2.0.CO;2](https://doi.org/10.1175/1520-0477(1979)060<1048:RMORS>2.0.CO;2), 1979
- 1344 Wolfe, J.P., and J.R. Snider, A relationship between reflectivity and snow rate for a high-altitude S-band  
1345 radar, *J. Appl. Meteor. Climatol.*, 51, 1111–1128, <https://doi.org/10.1175/JAMC-D-11-0112.1>,  
1346 2012
- 1347 Zaremba, T.J., and Coauthors, Vertical motions in orographic cloud systems over the Payette River Basin.  
1348 Part 1: Recovery of vertical motions and their uncertainty from airborne Doppler radial Velocity  
1349 Measurements, in press at the *Journal of Applied Meteorology and Climatology*,  
1350 <https://doi.org/10.1175/JAMC-D-21-0228.1>, 2022
- 1351 Zelasko, N., Wettlaufer, A., Borkhuu, B., Burkhart, M., Campbell, L. S., Steenburgh, W. J., and Snider,  
1352 J.R., Hotplate precipitation gauge calibrations and field measurements, *Atmos. Meas. Tech.*, 11,  
1353 441-458, <https://doi.org/10.5194/amt-11-441-2018>, 2018
- 1354 Zikmunda, J. and Vali, G., Fall patterns and fall velocities of rimed ice crystals, *J. Atmos. Sci.*, 29, 1334–  
1355 1347, [https://doi.org/10.1175/1520-0469\(1972\)029<1334:FPAFVO>2.0.CO;2](https://doi.org/10.1175/1520-0469(1972)029<1334:FPAFVO>2.0.CO;2), 1972
- 1356