

Greenhouse Gas Retrievals for the CO2M mission using the FOCAL method: First Performance Estimates

Stefan Noël¹, Michael Buchwitz¹, Michael Hilker¹, Maximilian Reuter¹, Michael Weimer¹, Heinrich Bovensmann¹, John P. Burrows¹, Hartmut Bösch¹, and Ruediger Lang²

¹Institute of Environmental Physics, University of Bremen, FB 1, P.O. Box 330440, 28334 Bremen, Germany

²EUMETSAT, Eumetsat Allee 1, 64295 Darmstadt, Germany

Correspondence: S. Noël (stefan.noel@iup.physik.uni-bremen.de)

Abstract. The Anthropogenic Carbon Dioxide Monitoring (CO2M) mission is a constellation of satellites currently planned to be launched in 2026. CO2M is planned to be a core component of a Monitoring and Verification Support (MVS) service capacity under development as part of the Copernicus Atmosphere Monitoring Service (CAMS). The CO2M radiance measurements will be used to retrieve column-averaged dry-air mole fractions of atmospheric carbon dioxide (X_{CO_2}), methane (5 X_{CH_4}) and total columns of nitrogen dioxide (NO_2). Using appropriate inverse modelling, the atmospheric greenhouse gas (GHG) observations will be used to derive United Nations Framework Convention on Climate Change (UNFCCC) COP 21 Paris Agreement relevant information on GHG sources and sinks. This challenging application requires highly accurate X_{CO_2} and X_{CH_4} retrievals. Three different retrieval algorithms to derive X_{CO_2} and X_{CH_4} are currently under development for the operational processing system at EUMETSAT. One of these algorithms uses the heritage of the FOCAL (Fast atmOspheric traCe gAs retrievaL) method, which has already successfully been applied to measurements from other satellites. Here, we show recent results generated using the CO2M version of FOCAL, called FOCAL-CO2M. 10

To assess the quality of the FOCAL-CO2M retrievals, a large set of representative simulated radiance spectra has been generated using the radiative transfer model SCIATRAN. These simulations consider the planned viewing geometry of the CO_2 instrument and corresponding geophysical scene data (including different types of aerosols and varying surface properties) 15 which were taken from model data for the year 2015. We consider instrument noise and systematic errors caused by the retrieval method but have not considered additional error sources due to e.g. instrumental issues, spectroscopy, or meteorology. On the other hand, we have also not taken advantage in this study of CO2M's MAP (Multi Angle Polarimeter) instrument, which will provide additional information on aerosols and cirrus clouds. By application of the FOCAL retrieval to these simulated data confidence is gained that the FOCAL method is able to fulfil the challenging requirements on systematic errors for the CO2M 20 mission (spatio-temporal bias ≤ 0.5 ppm for X_{CO_2} and ≤ 5 ppb for X_{CH_4}).

1 Introduction

Carbon dioxide (CO_2) and methane (CH_4) are the two most important anthropogenic atmospheric greenhouse gases. Their atmospheric concentrations are rising as a result of anthropogenic activity. There is a scientific consensus that this is driving

global warming and related climate change (see the recent report of the Intergovernmental Panel on Climate Change (IPCC),
25 2023). In November 2015, the Paris Agreement of the United Nations Framework Convention on Climate Change (UNFCCC)
was adopted to limit global warming to well below 2°C (UNFCCC, 2015). Actually, this treaty introduced a preferred limit of
1.5°C. As part of the Paris agreement, progress of emission reduction efforts is tracked on a regular basis. In this context, the
European Commission (EC), the European Space Agency (ESA), the European Centre for Medium-Range Weather Forecasts
(ECMWF), the European Organisation for the Exploitation of Meteorological Satellites (EUMETSAT), and international ex-
30 perts are developing an operational capacity for monitoring anthropogenic CO₂ emissions as a new CO₂ service under the EC's
Copernicus program (e.g. Janssens-Maenhout et al., 2020; Balsamo et al., 2021). A core component of this Monitoring and Ver-
ification Support (CO2MVS) capacity are satellite observations, in particular data from the European Anthropogenic Carbon
Dioxide Monitoring (CO2M) satellite mission (ESA, 2020; Lespinas et al., 2020; Sierk et al., 2021), which – with additional
instrumentation – builds on the heritage of the CarbonSat concept (Bovensmann et al., 2010; Velazco et al., 2011; Buchwitz
35 et al., 2013; Broquet et al., 2018) and the first retrievals of the column average dry-air mole fractions of CO₂ (XCO₂) and CH₄
(XCH₄) retrieved using passive remote sensing observations in the Near Infrared (NIR) and shortwave infrared (SWIR) made
by the Scanning Imaging Absorption Spectrometer for Atmospheric Chartography (SCIAMACHY) on Envisat (Burrows et al.,
1995; Bovensmann et al., 1999; Buchwitz et al., 2005).

CO2M is planned to be a core component of a Monitoring and Verification Support (MVS) service capacity under devel-
40 opment as part of the Copernicus Atmosphere Monitoring Service (CAMS) (Janssens-Maenhout et al., 2020; Balsamo et al.,
2021; Hegglin et al., 2022). The CO2M mission will consist of a constellation of 2–3 satellites which will monitor globally
XCO₂ and XCH₄. The satellites will be placed in a sun-synchronous polar orbit at 735 km altitude with an equator crossing
at about 11:30 local time in a descending node. The first CO2M satellite is planned to be launched in 2026. Each satellite has
a payload comprising three instruments:

- 45 – An imaging spectrometer (CO2I), which measures the upwelling radiance in wavelength ranges having atmospheric ab-
sorption, which on mathematical inversion yield the total and tropospheric columns of nitrogen dioxide (NO₂), column-
averaged dry-air mole fractions of atmospheric carbon dioxide (XCO₂) and methane (XCH₄), SIF (solar induced flu-
orescence) and additional quantities such as the column-averaged dry-air mole fractions of water vapour (XH₂O). The
spatial resolution of CO2I ground scenes is about 2 × 2 km².
- 50 – A multi-angle polarimeter (MAP), from which aerosol data products are retrieved. The spatial resolution of MAP is
about 4 × 4 km².
- A cloud imager (CLIM), which measures the upwelling radiance in a selection of broad band spectral channels. The
spatial resolution for CLIM is better than that of CO2I being about 0.4 × 0.4 km².

A driving motivation for the selection of CO2M was the quantification of anthropogenic emissions of CO₂. However other
55 important objectives of the mission include the provision of knowledge about anthropogenic CH₄ emissions and on large-scale
natural CO₂ and CH₄ surface fluxes.

Three different retrieval algorithms to derive XCO₂ and XCH₄ are currently under development for the operational processing system at EUMETSAT. One of the foreseen operational CO2M algorithms is based on the FOCAL (Fast atmOspheric traCe gAs retrieval) method (Reuter et al., 2017a, b), which is the topic of this study. The other two algorithms are RemoTAP (Remote sensing of Trace gas and Aerosol Product Lu et al., 2022) and the Flexible and Unified Spectral InversiON ALgorithm Platform (Fusional-P-UOL-FP) based on the retrieval algorithm as described in Cogan et al. (2012). RemoTAP is an iterative approach to retrieve aerosol properties as well as CO₂ and CH₄ total columns from spectral data. The Fusional-P-UOL-FP retrieval is based on an algorithm which was originally developed for the NASA Orbiting Carbon Observation (OCO) mission. It is also an iterative approach to derive XCO₂ and XCH₄ based on optimal estimation, which takes into account aerosols and cirrus clouds. Both RemoTAP and Fusional-P-UOL-FP consider polarisation and can use as input CO2I and MAP measurements for a joined retrieval. The requirements on data product quality for these algorithms are high (ESA, 2020), systematic errors (spatio-temporal bias) should not exceed 0.5 ppm for XCO₂ (about 0.12%) and 5 ppb for XCH₄ (about 0.28%). The corresponding maximum random errors for XCO₂ and XCH₄ are 0.7 ppm and 10 ppb, respectively, for a specific scenario (solar zenith angle 50°, surface albedo in NIR, SWIR-1 and SWIR-2: 0.2, 0.1, 0.05).

In this paper we show recent results generated using the current CO2M version of FOCAL, which was applied to a set of simulated measurement data in order to assess the quality of the retrieved XCO₂ and XCH₄ data products. Special emphasis is placed on the verification of the systematic error requirements, which are actually more challenging for the retrieval. This is because the random errors are mainly related to the noise of the spectra which is determined by instrument design. Although the results are obtained from the analysis of top of the atmosphere radiances simulated using a state of the art radiative model, this study provides some first estimates of the data product quality from the FOCAL-CO2M retrieval algorithm.

The structure of the paper is described and summarised as follows. After this introduction, we describe the input data used in this study and how they were generated in Sect. 2. In Sect. 3 we explain the FOCAL retrieval and the methods used for performance assessment. The results of the study are presented in Sect. 4. Finally, our conclusions are summarised in Sect. 5.

2 Input Data

The main input data used in this study are simulated radiance spectra in the near-infrared (NIR) and short-wave infrared (SWIR) bands to be measured by CO2I (see Table 1). These have been generated using the SCIATRAN radiative transfer model (RozaNov et al., 2017) using CO2M geolocation and viewing geometry information for the year 2015 provided by EUMETSAT as input. The SCIATRAN calculations are more complex than the FOCAL forward model. For example, they consider surface BRDF (bidirectional reflectance distribution function) effects, different aerosol types and distributions as well as clouds.

In the context of the current study we have generated two types of test data sets, which will be used for the performance assessments: (i) a full-year global data set with a reduced spatial sampling and (ii) a spatially high-resolved scene over Europe (the so-called ‘Berlin scene’). Both are described in the following sub-sections.

In order to be as consistent as possible with real measurements, random noise has been added to the simulated spectra. This noise N has been calculated for each radiance R using band-specific parameters A and B via:

$$90 \quad N = \sqrt{R A + B^2} / A \quad (1)$$

The assumed values for A and B are given in Table 2. These values were derived from a study on CO2M requirements and performance (Buchwitz et al., 2020) and have been shown to be consistent with the measurements of the selected CO2M detectors.

2.1 Full-year global subset

95 To assess the impact of large scale temporal and spatial variations on the FOCAL-CO2M results a global data set covering at least a full year is required. However, SCIATRAN simulations are computationally expensive. Therefore it is not currently feasible to compute a complete CO2I full year data set for one of the CO2M satellites within a reasonable time. For the full-year data we therefore selected a subset of CO2I measurement geometries containing every 15th out of 110 across-track ground pixels and every 20th out of roughly 9200 along-track scanlines per orbit for solar zenith angles lower than 80°. This
100 results in a subset with 300 times less data than the whole CO2M data set, but with similar spatial and temporal coverage. The meteorological information (pressure, temperature, water vapour) used in the SCIATRAN simulations is taken from the fifth generation of the ECMWF re-analysis (ERA5) data (Hersbach et al., 2020) (temporal resolution 1 h, spatial resolution 0.25°). CO₂ and CH₄ profiles use the results from the CAMS model data for 2015 (spatial resolution about 2° × 3°), namely v20r1 for CO₂ (Chevallier et al., 2005; Chevallier et al., 2010; Chevallier, 2013) and v20r1 for CH₄ (Segers, 2022). The reflectivity of the surface is modelled using BRDF parameters from the Moderate Resolution Imaging Spectroradiometer (MODIS) MCD43C1 Version 6.1 BRDF and albedo model parameters dataset (Schaaf and Wang, 2021). These BRDF parameters have been interpolated spectrally to the centres of the three CO2I bands. Within one band, the BRDF is assumed to be constant for the SCIATRAN calculations. We also tested a linear wavelength dependency of the BRDF within the bands, but this only
105 post-processing – did not significantly change the derived XCO₂ and XCH₄ results. Solar induced chlorophyll fluorescence irradiance is simulated by scaling an irradiance spectrum obtained from the publication of Rascher et al. (2009). The scaling factor is obtained by assuming a linear relationship between SIF irradiance at 740 nm and MODIS NDVI (Didan, 2021) derived by the Rutherford Appleton Lab (RAL, 2022). Clouds in the dataset are considered by SCIATRAN using ERA5 specific cloud liquid water content and specific cloud ice water content as input. However, for the current study we only consider completely
115 cloud-free soundings. Aerosol is simulated in SCIATRAN using as input different aerosol types, phase functions, single scattering albedo and vertical distribution of the mass mixing ratio, considering dependencies of particle size on humidity. These aerosol parameters are taken from the CAMS global reanalysis EAC4 (Inness et al., 2019). Land/water information is taken from GTOPO30 (Earth Resources Observation and Science Center, U.S. Geological Survey, U.S. Department of the Interior, 1997), surface altitude / pressure is taken from ERA5. The SCIATRAN calculations have been performed in scalar mode
120 without consideration of inelastic scattering processes. This is expected to have only a minor impact on the retrieval results,

which has been tested using simulated data from the RAL (2022) study as input. SCIATRAN (and also FOCAL) are run in plan-parallel mode, although both SCIATRAN and FOCAL could consider sphericity; however, in case of CO2M (normally nadir looking with a swath of about 240 km, relevant solar zenith angles less than 75°) spherical geometry has no major impact and is therefore neglected. We also assumed a uniform scene within each ground pixel. So far, only nadir data over land are modelled, which results in a total of about 6 million spectra per year for each band.

Although the SCIATRAN calculations are quite complex compared to the more simple FOCAL forward model, they do not consider all possible physical processes like 2D/3D effects of clouds and aerosols. However, even if the radiative transfer model would be able to consider this the required input data are usually not available. This is a general limitation of all forward models.

Fig. 1 shows as an example for the sampling of the XCO₂ subset data over part of Europe for one CO2M orbit (only data over land). The shown region corresponds to the range of the high-resolution scene addressed in the following sub-section.

2.2 High-resolution scene

In addition to the full-year global subset data we used SCIATRAN to model also the NIR and SWIR radiances for a full 3 minute granule of CO2I data containing about 67000 measurements of which about 37000 are over land and cloud-free. This granule from 3 July 2015 (referred to as the ‘Berlin scene’, see Fig. 2) is one of the typical test scenes, used within the CO2M project, because of the availability of high-resolution model data for this scene. The calculations for the high-resolution scene use the same SCIATRAN setup except for geolocation, geopotential, pressure, temperature, specific humidity, CO₂ and CH₄, which were provided by EUMETSAT using high-spatial resolution (9 km) data from the CAMS nature run model (Agustí-Panareda et al., 2022). As can be seen from Fig. 2, with this resolution XCO₂ plumes from power plants in Eastern Germany are clearly visible, although the increase of XCO₂ in these plumes is only a few ppm above background. Fig. 3 shows the corresponding XCH₄ data.

3 Algorithms

3.1 FOCAL-CO2M retrieval

The FOCAL retrieval method is based on optimal estimation. FOCAL models the propagation of light through the atmosphere. Scattering is approximated by a infinitely thin single scattering layer, which is characterised by the vertical position of the layer (pressure relative to surface pressure), the optical thickness of the layer and the Ångström exponent describing the wavelength dependence of the scattering (see e.g. Reuter et al., 2017b, for details). Scattering at this layer is assumed to be isotropic. All scattering quantities are effective, they describe the whole scattering (including e.g. Rayleigh scattering) and thus should not be interpreted as e.g. aerosol properties. The FOCAL forward model divides the atmosphere into 20 layers, which are defined such that that they contain the same number of dry-air molecules. Inside a layer, all atmospheric parameters are assumed to be constant. In the retrieval, FOCAL determines the concentrations (sub-columns) for five output layers, each also containing

the same number of molecules. The layers are fitted individually such that the shape of the profiles may change. However, the amount of change is limited by the use of an a-priori covariance matrix. In the present case, we use for XCO₂ and XCH₄ matrices derived from the Simple cLImatological Model (SLIM, see Noël et al., 2022), which give a reasonable variability. The final XCO₂ and XCH₄ is then derived from the average of the corresponding sub-columns in each layer.

Applications to OCO-2, GOSAT and GOSAT-2 have shown that FOCAL is fast and produces accurate results. For example, the spatio-temporal bias of the FOCAL XCO₂ product derived from TCCON comparisons is (after bias correction) in the order of 0.6 ppm for OCO-2 (Reuter and Hilker, 2022), and 0.6 (1.1) ppm for GOSAT (GOSAT-2) (Noël et al., 2022). FOCAL is therefore well suited for the analysis of large data sets.

FOCAL-CO2M is an adaptation of the FOCAL method for use in the CO2M mission. FOCAL permits “full physics” (FP) and “proxy” (PR) retrievals. FP retrievals are based on directly retrieving the quantity of interest, i.e., XCO₂ or XCH₄, whereas PR retrievals are based on computing the ratio of the retrievals of the two gases and using modelled XCO₂ or XCH₄ for correction (see, e.g. Schepers et al., 2012, for details). The main output products of the FOCAL-CO2M retrieval are total column FP XCO₂ and XCH₄, but there will also be corresponding additional PR data and SIF and water vapour (XH₂O) products. However, in the current study we only consider the FP XCO₂ and XCH₄ products.

The retrieval consists of three steps: pre-processing, inversion and post-processing.

The inputs to the pre-processing include (1) the spectral data from CO2I (measured radiances and their uncertainties as well as related measurement times and measurement geometry, geolocation etc.) and (2) related meteorological information and a-priori profiles for the considered gases. For the current study, we use simulated data, see Sect. 2.

The objective of pre-processing is to filter the input data to minimise the waste of computational time for unsuitable atmosphere and ground scenes or soundings. For the purpose of this study, we filter out all cloudy data and data over water surfaces, because these are not required for the verification of the systematic error requirements. However, the retrieval is also planned to be applied to data over ocean, especially in glint mode. We also remove all data with solar zenith angles larger than 75° and data for which the signal-to-noise is lower than 100 at the wavelengths, 755 nm, 1624 nm and 2036 nm, i.e. one spectral region in each band where absorption is low.

The inversion uses an optimal estimation retrieval approach (Rodgers, 2000). It has four fitting windows in the near-infrared (NIR) and short-wave infrared (SWIR) spectral regions, see Table 3. The corresponding state vector elements and their a-priori values are listed in Table 4. The assumed a-priori uncertainties for the gas profiles consider covariances and are the same as those used in GOSAT and GOSAT-2 FOCAL retrievals, which were derived based on the SLIM (Simple cLImatological Model for atmospheric CO₂ or CH₄) climatology (see Noël et al., 2022, for details). As for OCO-2, GOSAT and GOSAT-2, we consider an additional forward model error in the retrieval, which takes into account possible limitations of the forward model and is determined from the simulated CO2M measurements, see e.g. Reuter et al. (2017a, b) for details. The instrument line shape (ILS) functions are currently assumed to be Gaussian with a full-width at half maximum (FWHM) as given by the spectral resolution in Table 1.

During post-processing, the output data from the inversion are filtered for e.g. outliers. Furthermore, a bias correction is performed to remove systematic offsets arising e.g. from limitations of the forward model. The underlying data base for the

post-processing is generated using a subset of (uncorrected) retrieval results as input. Here, we use the results of the retrieval after inversion for the April 2015 subset data. We only use one month of data instead of the whole year for the following reasons:

- 190 1. We want to be as close to “real” conditions as possible. During the commissioning phase we need to re-determine the post-processing data base, and there will be most likely only a limited amount of data available at that time.
2. With the current setup it is possible to show that the post-processing is working also for data / time periods which were not used during generation of the data base.

The retrieval results for April 2015 are then filtered for convergence and fit quality. Using these data, the current post-
195 processing data base has been derived as follows.

The filtering of the data is similar to the filtering performed for OCO-2 and GOSAT(-2) data and comprises two filtering steps (see e.g. Noël et al., 2022, for details). First, data are filtered for retrieval quality (see Reuter et al., 2017b). Second, additional filter parameters and their limits are determined using a variance minimisation method. The idea of this second step is that outliers largely contribute to the scatter and the method finds thresholds for parameters which most efficiently remove
200 these outliers from the final data set.

Within this second step, an iterative procedure is used to determine a set of maximal 10 parameters which have the largest effect on the variance reduction of the bias, i.e. the difference between the retrieved value and an assumed ‘true’ value, for a prescribed percentage of data to be filtered out. The percentage of data to be filtered out is a trade-off between the remaining scatter of the data and the number of remaining data after filtering. For the simulated data used in the present study we
205 prescribed that 15% shall be removed.

The bias correction is based on a machine learning regression, which determines the function and the 10 (or less) best parameters to reduce the bias based on a set of training and test data (each 50% of the input data). This is similar to the method described in Noël et al. (2022), but here we use a regression based on a gradient boosting method (currently XGBoost, Chen and Guestrin (2016)) instead of a random forest regression. For the current test data set, XGboost performs better than random
210 forest regression.

The final determination of the post-processing data bases is done in an iterative way:

1. Apply the first step basic filtering for retrieval quality.
2. Determine and apply the bias correction to the resulting basically filtered data set.
3. Determine the (final) filter settings using the variance filter method with the data from the previous step as input.
- 215 4. Apply these filters to the basically filtered data from step 1.
5. Determine the (final) bias correction based on the output data from the previous step.

Performing a preliminary bias correction before the determination of the filter settings has the advantage, that data which can be sufficiently well corrected via the bias correction are not necessarily filtered out.

220 For simulated data, the ‘true’ XCO₂ and XCH₄ values are perfectly known, because they have been used for the generation of the simulated spectra. Therefore, the current filtering and bias correction does not consider any additional errors resulting systematic differences between the estimated meteorological conditions and the actual atmosphere. The impact of this additional error source on the retrieval results can only be quantified by comparisons of real measurements with independent data. The retrieval results presented later therefore do not include the impact of limited knowledge of the true values.

225 Tables 5 and 6 show the derived filter parameters and their limits for XCO₂ and XCH₄, respectively. As can be seen from these tables, there are only filters on polynomial parameters and their errors applied, although also e.g. the derived scattering parameters were possible candidates. This means the filtering of the simulated data is based on surface albedo properties.

Fig. 4 shows the derived bias correction parameters as a function of their importance. For both XCO₂ and XCH₄ the most relevant parameter for the bias correction is the derived Ångström coefficient. This means that largest (uncorrected) biases are related to scattering, i.e. most likely aerosol since we are using only cloud-free data here. This also indicates that there is a 230 strong correlation between the derived scattering parameters and aerosol abundance.

As an example for the spatial distribution and magnitude of the bias correction, Figs. 5 and 6 show the derived values for XCO₂ and XCH₄. The mean correction is small (0.1 ppm XCO₂ and 2.1 ppb for XCH₄), but there are significant local differences. Larger corrections occur over Northern Africa, the Arabian peninsula and India, i.e. regions with typically larger surface albedo and aerosol load.

235 Note that the quality of the post-processing may in principle be improved by extending the input data set used to determine the post-processing data base (especially regarding the training of the bias correction). However, at the beginning of the CO2M mission, the amount of available measurement data will be limited. In order to show that our post-processing would even work with a minimum amount of data we use only one month of simulated data here.

3.2 Adaptations for real data

240 The FOCAL-CO2M retrieval software has been designed such that it can be applied to both simulated data (as in the present study) and to real measurement data. However, the application to actual measurements requires some adaptations.

This includes the incorporation of results from the on-ground calibration (e.g. updated ILS data) as well as updates of filtering and bias correction parameters, which can only be determined during the commissioning phase based on the analysis of in-flight measurements.

245 In the pre-processing, e.g. cloud and signal-to-noise filters need to be adjusted. For the retrieval, the forward model error needs to be re-determined. Furthermore, the post-processing data base needs to be re-calculated using adapted filter settings and bias correction parameters. It also has to be checked if additional information, e.g. aerosol parameters derived by the MAP instrument, may be used in both pre- and post-processing.

3.3 Performance Assessments

250 The primary objective of this study is to obtain a first estimate of the performance of the FOCAL-CO₂M retrieval with respect to known sources of systematic errors. As already mentioned above, the corresponding requirements on the resulting XCO₂ and XCH₄ are high (systematic error ≤ 0.5 ppm and 5 ppb, respectively), see ESA (2020).

However, these requirements are formulated in a general way. Therefore, there is a need for some interpretation to verify these requirements. We consider that the requirements should be verified by using cloud-free data over land only. Furthermore, 255 the interpretation of systematic errors depends on the application, i.e. the purpose for which the data shall be used. CO₂M has two main application areas:

1. Quantification of anthropogenic emissions.
2. Quantification of natural large scale fluxes.

For the quantification of anthropogenic emissions it is important that local enhancements (e.g. emission plumes) can be 260 separated from the background. The background values themselves are less important. A verification therefore requires spatially highly resolved scene data with e.g. emission plumes.

For the quantification of natural large scale fluxes local variations are less relevant. Here, it is important that large scale structures and their variations in both time and space are correct. This requires global data covering at least a full year to consider possible long-term / large-scale errors.

265 According to the ESA (2020), CO₂ plume imaging (i.e. anthropogenic emissions) is the driving application for the precision requirements. Nevertheless, knowledge about larger scale or areal fluxes are also important for e.g. global modelling. Therefore, we consider both applications here. The verification of the requirements thus has to take these different scales into account. In the following sub-section we describe the verification methods for both application areas.

For the verification of the systematic error requirements for natural large scale fluxes we use the retrieval results from the 270 full-year global subset measurements as these provide a good spatial and temporal coverage. We then determine a running average of the difference between the retrieved value and the true value within a $1^\circ \times 1^\circ$ latitude/longitude box. This results in a low-pass filtered bias data set. For this data set we compute the standard deviation, considering the cosine of the latitude as weights to account for different sizes of the averaging area. To fulfil the systematic error requirement, the resulting weighted standard deviation of the low-pass filtered bias should then be ≤ 0.5 ppm.

275 For the verification of the systematic error requirements for anthropogenic emissions we take as input the high-resolution Berlin scene. We then apply – similar as for the large scale fluxes – a $1^\circ \times 1^\circ$ low-pass filter to the difference between the retrieved value and the true value, which results in a spatially smoothed bias. This smoothed bias is then subtracted from the original data, which gives us a high-passed filtered bias data set (for this scene). The standard deviation of these high-pass filtered bias data should then be ≤ 0.5 ppm to fulfil the requirement on systematic errors.

280 Fig. 7 shows as an example for the different filtering procedures the unfiltered XCO₂ bias (retrieved - true values) for the high-resolution Berlin scene and the resulting low- and high-pass filtered bias.

4 Results

4.1 Application to anthropogenic emissions

As explained above, the verification of the performance requirements for anthropogenic emissions is achieved by using the
285 high-resolution ‘Berlin scene’.

Fig. 8 shows the FOCAL-CO2M XCO₂ retrieval results for this scene. The retrieved XCO₂ (after post-processing) is shown in the left plot, the true XCO₂ in the centre and their difference in the right plot. Some statistical information is also given in the figure below these plots. Note that these are rounded values.

All structures of the scene shown in the true XCO₂ can also be identified in the retrieved data. The mean difference between
290 the retrieved and the true XCO₂ is -0.2 ppm. The standard deviation of the difference is 0.6 ppm. After application of the low- and high-pass filters this reduces to 0.2 ppm and 0.5 ppm. The values for the high-pass filtered data do not only contain the systematic error component but also the noise on the data. The (rounded) mean noise error of the data in this scene is also about 0.5 ppm. This means that the high-pass standard deviation is dominated by noise; thus the real systematic error is probably well below 0.5 ppm. If we subtract the noise related variance from the high-pass variance and then take the square root, we get
295 the value given in brackets after the high-pass variance in the plot, namely 0.1 ppm. This can be considered as a lower estimate for the high-pass standard deviation as it does not consider potential systematic error contributions to the a-posteriori noise error.

The average a-posterior error of the retrieved XCO₂ (including the noise and the smoothing error) is about 0.6 ppm, i.e. very close to the noise error. Compared to the assumed a-priori uncertainty for CO₂ of 5ppm (see Table 4) this corresponds to an
300 uncertainty reduction of about a factor of 8.

A small gradient is visible in the difference between the retrieved and the true XCO₂ from north-east to south-west. This could be related to aerosol effects. In this scene, most aerosol is located in the south-west. Differences in the handling of surface properties by SCIATRAN and FOCAL could also play a role. However, since we are interested in the quantification for anthropogenic emissions, these larger scale effects are less relevant.

As mentioned in Table 4, the XCO₂ a-priori values used in the retrieval are taken from the meteorological data, which were
305 also used in the generation of the input spectra. They are therefore identical with the true values. This is because we aim to be as consistent as possible with the procedures to be applied to real data at a later time, and for real measurements we will also use the (predicted) meteorological input data as truth for the post-processing corrections. However, in reality of course the truth will deviate from the model data. To show that the sensitivity of the retrieval to the choice of the a-priori is low, we have
310 performed the retrieval for the ‘Berlin scene’ also for a fixed CO₂ a-priori for all measurements by assuming a constant value of 400 ppm for all altitudes. As can be seen from Fig. 9, this has hardly any impact on the retrieval results. All XCO₂ features can be reproduced even with the fixed a-priori. There is only a small mean offset of about 0.2 ppm compared to the values where the true XCO₂ was used as a-priori.

Fig. 10 shows a zoom-in of Fig. 8 on the region of the power plants in Eastern Germany. Despite the noise on the data,
315 the plumes from the different power plants can be clearly identified in the retrieval results. No plume structures are visible in

the difference map. The high-pass standard deviation for this sub-scene is 0.5 ppm similar to the noise error. The high-pass standard deviation is thus also dominated by noise. Subtraction of the noise contribution results in a standard deviation of 0.1 ppm. The requirement on systematic errors is therefore fulfilled for XCO₂ for this scene. Note that in reality 2D/3D effects (vertical/horizontal distribution of the plume), which are not fully considered in our simulations, may affect the results. This can only be checked with real data.

The results for XCH₄ using the true values as a-priori are shown in Fig. 11. For this case, also the main structures of the true XCH₄ field are re-produced in the retrieval. As for XCO₂, the difference between retrieved and true XCH₄ is dominated by noise. The mean offset for this scene is -1.4 ppb with a standard deviation of the (unfiltered) difference of 5.2 ppb, including a noise error of 4.8 ppb. The average a-posterior error for XCH₄ is 5.8 ppb, compared the a-priori uncertainty for CH₄ of 45ppb from Table 4. The uncertainty is therefore reduced as for CO₂ by about a factor of 8.

The high-pass filtered mean standard deviation is 5.0 ppb with a lower (noise-corrected) estimate of 1.3 ppb. The requirement of maximum 5 ppb is therefore fulfilled. The difference map for XCH₄ shows a similar gradient as for XCO₂ from north-east to south west, most likely for the same reasons.

4.2 Application to large scale fluxes

The verification of the requirement for large scale natural fluxes is based on the full-year global subset data. As an example, Fig. 12 shows the FOCAL-CO2M XCO₂ retrieval results for April 2015. The corresponding XCH₄ data are shown in Fig. 13.

As can be seen from these figures, the retrieved data reproduce all large-scale patterns present in the true/a-priori data. The scatter in the differences between retrieved and true values is dominated by noise. Since the April 2015 data are used in the derivation of the post-processing data bases, Figs. 12 and 13 show the best case. However, the quantitative assessments described in the following show that other months have a similar performance.

For these quantitative assessments of the systematic error for large scale fluxes we apply a low-pass filter to the differences and determine the weighted standard deviation for the low-pass filtered data as described in section 3.3. This is done for each month as well as for the whole year 2015. The results are shown in Fig. 14 and Fig. 15.

For the verification of the systematic error requirements the red line in the middle plots is relevant. It shows the weighted standard deviation for the low-pass filtered data for each month and the value for the complete year (i.e. not the average over the monthly data) in the legend of each panel.

The yearly average low-pass standard deviation for XCO₂ is 0.5 ppm and therefore just fulfils the systematic error requirement for large scale fluxes. For XCH₄, the yearly average low-pass standard deviation is 3.7 ppb and therefore smaller than the required 5 ppb.

The lowest XCO₂ and XCH₄ standard deviations are achieved in April 2015. The biases at this month are also zero. This is not surprising, because this is the month which was used for the training of the bias correction. Slightly higher standard deviations occur in other months, but the standard deviations of the low-pass filtered data are always below 0.6 ppm for XCO₂ and 4. ppb for XCH₄. Largest standard deviations occur for both gases in December and January, where also the number of

valid data is lowest. In general, it is expected that the results improve if more months (e.g. a full year subset data set) are used
350 for the generation of the post-processing data base.

However, the simulated data used here do not fully represent reality because of the limitations and underlying assumptions in the radiative transfer and the retrieval. Even under these conditions the estimated systematic errors for large scale fluxes are especially for XCO_2 very close to the requirements. This indicates that fulfilling these requirements for real data might be possible but will be a challenge.

355 4.3 Aerosol dependence

Up to the present, the FOCAL-CO2M retrieval does not use any external information about aerosols (e.g. from the MAP instrument). The systematic error requirements are only applicable up to an aerosol optical depth of 0.5 (ESA, 2020). Therefore, we also checked the aerosol dependence of the FOCAL-CO2M retrieval results. Figs. 16 and 17 show the (binned) differences between the retrieved and the true XCO_2 and XCH_4 for the full-year 2015 subset data as a function of the aerosol optical depth
360 (AOD) at 550 nm, which was assumed for the generation of the simulated spectra with SCIATRAN.

As mentioned above, the SCIATRAN calculations for the simulated data consider different aerosol types and distributions, but the FOCAL retrieval does not explicitly consider aerosol, it assumes only one effective scattering layer. Nevertheless, as can be seen from Fig. 16, mean systematic offsets due to aerosol for the complete year are less than about 0.2 ppm for XCO_2 with a mean of zero for all AODs up to 0.5. The standard deviation of the XCO_2 difference is on average 0.7 ppm and typically
365 smaller for lower AOD. The functional dependence on AOD is similar for XCH_4 (see Fig. 17). Systematic XCH_4 offsets are usually smaller than 1 ppb.

These results could possibly be improved when using extended training data for the post-processing and/or additional information from the MAP instrument.

5 Conclusions

370 FOCAL is one of three retrieval algorithms under development for the operational retrieval of XCO_2 , XCH_4 and other parameters from the constellation of CO2M satellites to be launched from 2026 onward. These data products contain information on anthropogenic and natural sources and sinks of the two greenhouse gases CO_2 and CH_4 which will be extracted using appropriate inverse modelling to support emission monitoring in the context of the Paris Agreement on climate change. This application requires high accuracy as even small biases can lead to significant emission errors (ESA, 2020).

375 The FOCAL retrieval has been successfully adapted to simulated CO2M data. First performance tests using data simulated with SCIATRAN as input have been performed. Based on these simulated cloud-free nadir data over land, we show that the requirement of a maximum systematic error of 0.5 ppm for XCO_2 and 5 ppb for XCH_4 is fulfilled by the FOCAL retrieval for (1) anthropogenic emissions (high-pass filtered data), using a high-resolution scene containing XCO_2 emission plumes from power plants and (2) natural large scale fluxes (low-pass filtered data), based on a full year global sub-sampled data set. Good
380 retrieval results are obtained up to AOD 0.5, even without using external aerosol information as input.

All results shown here are based on simulated data. Furthermore, the calculations currently assume a perfect CO₂I instrument and do not consider any systematic errors in spectroscopy or meteorology. The SCIATRAN simulations do not (and cannot) take into account all physical processes. On the retrieval side, information on aerosols and cirrus clouds derived from the MAP instrument is also not considered yet. However, the inclusion of MAP Level 2 data (e.g. for post-processing) is already foreseen
385 in the current software. Therefore, the results of this study cannot be seen as a final verification of the CO₂M requirements. Finally, the performance of the FOCAL-CO₂M retrieval (and all other retrieval methods) needs to be determined based on real measurements. Fulfilling the requirements for XCO₂ natural large scale fluxes is probably the most challenging task in this context. However, the current results give confidence that the FOCAL-CO₂M retrieval algorithm will be able to generate products meeting the product quality requirements of the CO₂M mission.

390 *Data availability.* The data used in this study are available on request from the authors.

Author contributions. R. Lang provided the CO₂M geolocation information. M. Reuter developed the FOCAL method and provided the geophysical input data for the SCIATRAN simulations. M. Hilker developed the original python implementation of FOCAL (OCO-2 version) and computed the simulated spectra with SCIATRAN. S. Noël adapted the FOCAL method to CO₂M and performed the retrievals and the performance checks. All authors provided support in writing the paper.

395 *Competing interests.* The authors declare that there are no competing interests.

Acknowledgements. ERA5 meteorological data were provided by the European Center for Medium Range Weather Forecasts (ECMWF).

Large parts of the calculations reported here were performed on HPC facilities of the IUP, University of Bremen, funded under DFG/FUGG grant INST 144/379-1 and INST 144/493-1.

The work has been carried out with funding by the European Union Copernicus program through EUMETSAT contract EUM/CO/19/4600002372/RL,
400 and the State and the University of Bremen.

Part of this work is funded by the BMBF project 'Integrated Greenhouse Gas Monitoring System for Germany - Observations (ITMS B)' under grant number 01 LK2103A.

References

- Agustí-Panareda, A., McNorton, J., Balsamo, G., Baier, B. C., Bousserrez, N., Boussetta, S., Brunner, D., Chevallier, F., Choulga, M.,
405 Diamantakis, M., Engelen, R., Flemming, J., Granier, C., Guevara, M., Denier van der Gon, H., Elguindi, N., Haussaire, J.-M., Jung,
M., Janssens-Maenhout, G., Kivi, R., Massart, S., Papale, D., Parrington, M., Razinger, M., Sweeney, C., Vermeulen, A., and Walther,
S.: Global nature run data with realistic high-resolution carbon weather for the year of the Paris Agreement, *Scientific Data*, 9, 160,
<https://doi.org/10.1038/s41597-022-01228-2>, 2022.
- Balsamo, G., Engelen, R., Thiemert, D., Agustí-Panareda, A., Bousserrez, N., Broquet, G., Brunner, D., Buchwitz, M., Chevallier, F.,
410 Choulga, M., Denier Van Der Gon, H., Florentie, L., Haussaire, J.-M., Janssens-Maenhout, G., Jones, M. W., Kaminski, T., Krol, M.,
Le Quééré, C., Marshall, J., McNorton, J., Prunet, P., Reuter, M., Peters, W., and Scholze, M.: The CO₂ Human Emissions (CHE)
Project: First Steps Towards a European Operational Capacity to Monitor Anthropogenic CO₂ Emissions, *Front. Remote Sens.*, 2,
<https://doi.org/10.3389/frsen.2021.707247>, 2021.
- Bovensmann, H., Burrows, J. P., Buchwitz, M., Frerick, J., Noël, S., Rozanov, V. V., Chance, K. V., and Goede, A. H. P.: SCIAMACHY —
415 Mission Objectives and Measurement Modes, *J. Atmos. Sci.*, 56, 127–150, 1999.
- Bovensmann, H., Buchwitz, M., Burrows, J. P., Reuter, M., Krings, T., Gerilowski, K., Schneising, O., Heymann, J., Tretner, A., and Erzinger,
J.: A remote sensing technique for global monitoring of power plant CO₂ emissions from space and related applications, *Atmos. Meas.
Tech.*, 3, 781–811, <https://doi.org/10.5194/amt-3-781-2010>, 2010.
- Broquet, G., Bréon, F.-M., Renault, E., Buchwitz, M., Reuter, M., Bovensmann, H., Chevallier, F., Wu, L., and Ciais, P.: The potential of
420 satellite spectro-imagery for monitoring CO₂ emissions from large cities, *Atmos. Meas. Tech.*, 11, 681–708, <https://doi.org/10.5194/amt-11-681-2018>, 2018.
- Buchwitz, M., de Beek, R., Noël, S., Burrows, J. P., Bovensmann, H., Bremer, H., Bergamaschi, P., Körner, S., and Heimann, M.: Carbon
monoxide, methane and carbon dioxide columns retrieved from SCIAMACHY by WFM-DOAS: year 2003 initial data set, *Atmos. Chem.
Phys.*, 5, 3313–3329, 2005.
- 425 Buchwitz, M., Reuter, M., Bovensmann, H., Pillai, D., Heymann, J., Schneising, O., Rozanov, V., Krings, T., Burrows, J. P., Boesch, H.,
Gerbig, C., Meijer, Y., and Löscher, A.: Carbon Monitoring Satellite (CarbonSat): assessment of atmospheric CO₂ and CH₄ retrieval
errors by error parameterization, *Atmos. Meas. Tech.*, 6, 3477–3500, <https://doi.org/10.5194/amt-6-3477-2013>, 2013.
- Buchwitz, M., Noël, S., Reuter, M., Bovensmann, H., R., A., L., J., v. H., H., Veeffkind, P., de Haan, J., and Boesch, H.: CO₂M-
REB Study Final Report (with ANNEXes), ESA Study on Consolidating Requirements and Error Budget for CO₂ Monitoring
430 Mission (CO₂M-REB), Tech. rep., University of Bremen, [http://www.iup.uni-bremen.de/carbon_ghg/CO₂M-REB_TNs/CO₂M-REB_](http://www.iup.uni-bremen.de/carbon_ghg/CO2M-REB_TNs/CO2M-REB_FinalReport_withANNEXes_v1.2.pdf)
[FinalReport_withANNEXes_v1.2.pdf](http://www.iup.uni-bremen.de/carbon_ghg/CO2M-REB_TNs/CO2M-REB_FinalReport_withANNEXes_v1.2.pdf), last access: 18-July-2023, 2020.
- Burrows, J., Hölzle, E., Goede, A., Visser, H., and Fricke, W.: SCIAMACHY – scanning imaging absorption spectrometer for atmospheric
chartography, *Acta Astr.*, 35, 445–451, [https://doi.org/https://doi.org/10.1016/0094-5765\(94\)00278-T](https://doi.org/https://doi.org/10.1016/0094-5765(94)00278-T), earth Observation, 1995.
- Chen, T. and Guestrin, C.: XGBoost: A Scalable Tree Boosting System, CoRR, abs/1603.02754, <http://arxiv.org/abs/1603.02754>, 2016.
- 435 Chevallier, F.: On the parallelization of atmospheric inversions of CO₂ surface fluxes within a variational framework, *Geosci. Model Dev.*, 6,
783–790, <https://doi.org/10.5194/gmd-6-783-2013>, 2013.
- Chevallier, F., Fisher, M., Peylin, P., Serrar, S., Bousquet, P., BréOn, F. M., ChéDin, A., and Ciais, P.: Inferring CO₂
sources and sinks from satellite observations: Method and application to TOVS data, *J. Geophys. Res. Atmos.*, 110, D24309,
<https://doi.org/10.1029/2005JD006390>, 2005.

- 440 Chevallier, F., Ciais, P., Conway, T. J., Aalto, T., Anderson, B. E., Bousquet, P., Brunke, E. G., Ciattaglia, L., Esaki, Y., Fröhlich, M., Gomez, A., Gomez-Pelaez, A. J., Haszpra, L., Krummel, P. B., Langenfelds, R. L., Leuenberger, M., Machida, T., Maignan, F., Matsueda, H., Morguá, J. A., Mukai, H., Nakazawa, T., Peylin, P., Ramonet, M., Rivier, L., Sawa, Y., Schmidt, M., Steele, L. P., Vay, S. A., Vermeulen, A. T., Wofsy, S., and Worthy, D.: CO₂ surface fluxes at grid point scale estimated from a global 21 year reanalysis of atmospheric measurements, *J. Geophys. Res. Atmos.*, 115, <https://doi.org/https://doi.org/10.1029/2010JD013887>, 2010.
- 445 Cogan, A. J., Boesch, H., Parker, R. J., Feng, L., Palmer, P. I., Blavier, J.-F. L., Deutscher, N. M., Macatangay, R., Notholt, J., Roehl, C., Warneke, T., and Wunch, D.: Atmospheric carbon dioxide retrieved from the Greenhouse gases Observing SATellite (GOSAT): Comparison with ground-based TCCON observations and GEOS-Chem model calculations, *Journal of Geophysical Research: Atmospheres*, 117, <https://doi.org/10.1029/2012JD018087>, 2012.
- Didan, K.: The Aqua Moderate Resolution Imaging Spectroradiometer (MODIS) Vegetation Indices Monthly (MYD13C2) Version 6.1
450 product: MODIS/Aqua Vegetation Indices Monthly L3 Global 0.05Deg CMG V061, distributed by NASA EOSDIS Land Processes Distributed Active Archive Center, <https://doi.org/10.5067/MODIS/MYD13C2.061>, 2021.
- Earth Resources Observation and Science Center, U.S. Geological Survey, U.S. Department of the Interior: USGS 30 ARC-second Global Elevation Data, GTOPO30, <https://doi.org/10.5065/A1Z4-EE71>, 1997.
- ESA: Copernicus CO₂ Monitoring Mission Requirements Document, Tech. rep., ESA Earth and Mission Science Division, https://esamultimedia.esa.int/docs/EarthObservation/CO2M_MRD_v3.0_20201001_Issued.pdf, last access: 23-August-2023, 2020.
- 455 //esamultimedia.esa.int/docs/EarthObservation/CO2M_MRD_v3.0_20201001_Issued.pdf, last access: 23-August-2023, 2020.
- Gordon, I., Rothman, L., Hill, C., Kochanov, R., Tan, Y., Bernath, P., Birk, M., Boudon, V., Campargue, A., Chance, K., Drouin, B., Flaud, J.-M., Gamache, R., Hodges, J., Jacquemart, D., Perevalov, V., Perrin, A., Shine, K., Smith, M.-A., Tennyson, J., Toon, G., Tran, H., Tyuterev, V., Barbe, A., Császár, A., Devi, V., Furtenbacher, T., Harrison, J., Hartmann, J.-M., Jolly, A., Johnson, T., Karman, T., Kleiner, I., Kyuberis, A., Loos, J., Lyulin, O., Massie, S., Mikhailenko, S., Moazzen-Ahmadi, N., Müller, H., Naumenko, O.,
460 Nikitin, A., Polyansky, O., Rey, M., Rotger, M., Sharpe, S., Sung, K., Starikova, E., Tashkun, S., Auwera, J. V., Wagner, G., Wilzewski, J., Wcisło, P., Yu, S., and Zak, E.: The HITRAN2016 molecular spectroscopic database, *J. Quant. Spectr. Rad. Transf.*, 203, 3 – 69, <https://doi.org/https://doi.org/10.1016/j.jqsrt.2017.06.038>, *HITRAN2016 Special Issue*, 2017.
- Hegglin, M. I., Bastos, A., Bovensmann, H., Buchwitz, M., Fawcett, D., Ghent, D., Kulk, G., Sathyendranath, S., Shepherd, T. G., Quegan, S., Röthlisberger, R., Briggs, S., Buontempo, C., Cazenave, A., Chuvieco, E., Ciais, P., Crisp, D., Engelen, R., Fadnavis, S., Herold, M.,
465 Horwath, M., Jonsson, O., Kpaka, G., Merchant, C. J., Mielke, C., Nagler, T., Paul, F., Popp, T., Quaife, T., Rayner, N. A., Robert, C., Schröder, M., Sitch, S., Venturini, S., van der Schalie, R., van der Vliet, M., Wigneron, J.-P., and Woolway, R. I.: Space-based Earth observation in support of the UNFCCC Paris Agreement, *Front. Remote Sens.*, 10, <https://doi.org/10.3389/fenvs.2022.941490>, 2022.
- Hersbach, H., Bell, B., Berrisford, P., Hirahara, S., Horányi, A., Muñoz Sabater, J., Nicolas, J., Peubey, C., Radu, R., Schepers, D., Simmons, A., Soci, C., Abdalla, S., Abellan, X., Balsamo, G., Bechtold, P., Biavati, G., Bidlot, J., Bonavita, M., De Chiara, G., Dahlgren, P., Dee, D., Diamantakis, M., Dragani, R., Flemming, J., Forbes, R., Fuentes, M., Geer, A., Haimberger, L., Healy, S., Hogan, R. J., Hólm, E.,
470 Janisková, M., Keeley, S., Laloyaux, P., Lopez, P., Lupu, C., Radnoti, G., de Rosnay, P., Rozum, I., Vamborg, F., Villaume, S., and Thépaut, J.-N.: The ERA5 global reanalysis, *Quart. Jour. R. Met. Soc.*, pp. 1–51, <https://doi.org/10.1002/qj.3803>, 2020.
- Inness, A., Ades, M., Agustí-Panareda, A., Barré, J., Benedictow, A., Blechschmidt, A.-M., Dominguez, J. J., Engelen, R., Eskes, H., Flemming, J., Huijnen, V., Jones, L., Kipling, Z., Massart, S., Parrington, M., Peuch, V.-H., Razinger, M., Remy, S., Schulz, M., and Suttie, M.: The CAMS reanalysis of atmospheric composition, *Atmos. Chem. Phys.*, 19, 3515–3556, <https://doi.org/10.5194/acp-19-3515-2019>,
475 2019.

- Intergovernmental Panel on Climate Change (IPCC): Climate Change 2021 – The Physical Science Basis: Working Group I Contribution to the Sixth Assessment Report of the Intergovernmental Panel on Climate Change, Cambridge University Press, <https://doi.org/10.1017/9781009157896>, 2023.
- 480 Janssens-Maenhout, G., Pinty, B., Dowell, M., Zunker, H., Andersson, E., Balsamo, G., Bézy, J.-L., Brunhes, T., Bösch, H., Bojkov, B., Brunner, D., Buchwitz, M., Crisp, D., Ciais, P., Counet, P., Dee, D., van der Gon, H. D., Dolman, H., Drinkwater, M. R., Dubovik, O., Engelen, R., Fehr, T., Fernandez, V., Heimann, M., Holmlund, K., Houweling, S., Husband, R., Juvyns, O., Kentarchos, A., Landgraf, J., Lang, R., Löscher, A., Marshall, J., Meijer, Y., Nakajima, M., Palmer, P. I., Peylin, P., Rayner, P., Scholze, M., Sierk, B., Tamminen, J., and Veefkind, P.: Toward an Operational Anthropogenic CO₂ Emissions Monitoring and Verification Support Capacity, *Bull. Am. Met.*
- 485 *Soc.*, 101, E1439 – E1451, <https://doi.org/https://doi.org/10.1175/BAMS-D-19-0017.1>, 2020.
- Lespinas, F., Wang, Y., Broquet, G., Bréon, F.-M., Buchwitz, M., Reuter, M., Meijer, Y., Loesch, A., Janssens-Maenhout, G., Zheng, B., and Ciais, P.: The potential of a constellation of low earth orbit satellite imagers to monitor worldwide fossil fuel CO₂ emissions from large cities and point sources, *Carbon Balance Manage.*, 15, 18, <https://doi.org/10.1186/s13021-020-00153-4>, 2020.
- Lu, S., Landgraf, J., Fu, G., van Diedenhoven, B., Wu, L., Rusli, S. P., and Hasekamp, O. P.: Simultaneous Retrieval of Trace
- 490 Gases, Aerosols, and Cirrus Using RemoTAP - The Global Orbit Ensemble Study for the CO₂M Mission, *Front. Remote Sens.*, 3, <https://doi.org/10.3389/frsen.2022.914378>, 2022.
- Noël, S., Reuter, M., Buchwitz, M., Borchardt, J., Hilker, M., Schneising, O., Bovensmann, H., Burrows, J. P., Di Noia, A., Parker, R. J., Suto, H., Yoshida, Y., Buschmann, M., Deutscher, N. M., Feist, D. G., Griffith, D. W. T., Hase, F., Kivi, R., Liu, C., Morino, I., Notholt, J., Oh, Y.-S., Ohyama, H., Petri, C., Pollard, D. F., Rettinger, M., Roehl, C., Rousogonous, C., Sha, M. K., Shiomi, K., Strong, K., Sussmann,
- 495 R., Té, Y., Velasco, V. A., Vrekoussis, M., and Warneke, T.: Retrieval of greenhouse gases from GOSAT and GOSAT-2 using the FOCAL algorithm, *Atmos. Meas. Tech.*, 15, 3401–3437, <https://doi.org/10.5194/amt-15-3401-2022>, 2022.
- RAL: Provision of Top-Of-Atmosphere simulations for the evaluation of data processing for the CO₂ monitoring mission: Task 1,2 and 3 Report, Tech. rep., RAL Space Remote Sensing Group, https://www-cdn.eumetsat.int/files/2023-01/RAL_EUM_CO2Msims_TN123_v1p1.pdf, 2022.
- 500 Rascher, U., Agati, G., Alonso, L., Cecchi, G., Champagne, S., Colombo, R., Damm, A., Daumard, F., de Miguel, E., Fernandez, G., Franch, B., Franke, J., Gerbig, C., Gioli, B., Gómez, J. A., Goulas, Y., Guanter, L., Gutiérrez-de-la Cámara, O., Hamdi, K., Hostert, P., Jiménez, M., Kosvancova, M., Lognoli, D., Meroni, M., Miglietta, F., Moersch, A., Moreno, J., Moya, I., Neininger, B., Okujeni, A., Ounis, A., Palombi, L., Raimondi, V., Schickling, A., Sobrino, J. A., Stellmes, M., Toci, G., Toscano, P., Udelhoven, T., van der Linden, S., and Zaldei, A.: CEFLES2: the remote sensing component to quantify photosynthetic efficiency from the leaf to the region by measuring
- 505 sun-induced fluorescence in the oxygen absorption bands, *Biogeosciences*, 6, 1181–1198, <https://doi.org/10.5194/bg-6-1181-2009>, 2009.
- Reuter, M. and Hilker, M.: End-to-End ECV Uncertainty Budget Version 3 (E3UBv3) for the FOCAL XCO₂ OCO-2 Data Product CO₂_OC₂_FOCA (v10), Tech. Rep. version 3, 6 Feb 2022, ESA Climate Change Initiative “Plus” (CCI+), https://www.iup.uni-bremen.de/carbon_ghg/docs/GHG-CCIplus/CRDP7/E3UBv3_GHG-CCI_CO2_OC2_FOCA_v10.pdf, last access: 06 September 2023, 2022.
- Reuter, M., Buchwitz, M., Schneising, O., Noël, S., Bovensmann, H., and Burrows, J. P.: A Fast Atmospheric Trace Gas Retrieval for
- 510 Hyperspectral Instruments Approximating Multiple Scattering – Part 2: Application to XCO₂ Retrievals from OCO-2, *Rem. Sens.*, 9, 1102, <https://doi.org/10.3390/rs9111102>, 2017a.
- Reuter, M., Buchwitz, M., Schneising, O., Noël, S., Rozanov, V., Bovensmann, H., and Burrows, J. P.: A Fast Atmospheric Trace Gas Retrieval for Hyperspectral Instruments Approximating Multiple Scattering – Part 1: Radiative Transfer and a Potential OCO-2 XCO₂ Retrieval Setup, *Rem. Sens.*, 9, 1159, <https://doi.org/10.3390/rs9111159>, 2017b.

- 515 Rodgers, C. D.: Inverse Methods for Atmospheric Sounding: Theory and Practice, World Scientific Publishing, Singapore, 2000.
- Rozanov, V., Dinter, T., Rozanov, A., Wolanin, A., Bracher, A., and Burrows, J.: Radiative transfer modeling through terrestrial atmosphere and ocean accounting for inelastic processes: Software package SCIATRAN, *J. Quant. Spectr. Rad. Transf.*, 194, 65–85, <https://doi.org/https://doi.org/10.1016/j.jqsrt.2017.03.009>, 2017.
- Schaaf, C. and Wang, Z.: The Moderate Resolution Imaging Spectroradiometer (MODIS) MCD43C1 Version 6.1 Bidirectional Reflectance Distribution Function and Albedo (BRDF/Albedo) Model Parameters dataset: MODIS/Terra+Aqua BRDF/AlbedoModel Parameters Daily L3 Global 0.05Deg CMG V061, distributed by NASA EOSDIS Land Processes Distributed Active Archive Center, <https://doi.org/10.5067/MODIS/MCD43C1.061>, last access: 20-July-2023, 2021.
- 520 Schepers, D., Guerlet, S., Butz, A., Landgraf, J., Frankenberg, C., Hasekamp, O., Blavier, J.-F., Deutscher, N. M., Griffith, D. W. T., Hase, F., Kyro, E., Morino, I., Sherlock, V., Sussmann, R., and Aben, I.: Methane retrievals from Greenhouse Gases Observing Satellite (GOSAT) shortwave infrared measurements: Performance comparison of proxy and physics retrieval algorithms, *J. Geophys. Res. Atmos.*, 117, <https://doi.org/https://doi.org/10.1029/2012JD017549>, 2012.
- 525 Segers, A.: Description of the CH₄ Inversion Production Chain, Tech. rep., TNO, https://atmosphere.copernicus.eu/sites/default/files/2022-10/CAMS255_2021SC1_D55.5.2.1-2021CH4_202206_production_chain_CH4_v1.pdf, last access: 25-August-2023, 2022.
- Sierk, B., Fernandez, V., Bézy, J.-L., Meijer, Y., Durand, Y., Courrèges-Lacoste, G. B., Pachot, C., Löscher, A., Nett, H., Minoglou, K., Boucher, L., Windpassinger, R., Pasquet, A., Serre, D., and te Hennepe, F.: The Copernicus CO₂M mission for monitoring anthropogenic carbon dioxide emissions from space, in: International Conference on Space Optics — ICSO 2020, edited by Cugny, B., Sodnik, Z., and Karafolas, N., vol. 11852, p. 118523M, International Society for Optics and Photonics, SPIE, <https://doi.org/10.1117/12.2599613>, 2021.
- 530 UNFCCC: UNFCCC Paris Agreement, https://unfccc.int/sites/default/files/english_paris_agreement.pdf, last access: 28-August-2023, 2015.
- Velazco, V. A., Buchwitz, M., Bovensmann, H., Reuter, M., Schneising, O., Heymann, J., Krings, T., Gerilowski, K., and Burrows, J. P.: Towards space based verification of CO₂ emissions from strong localized sources: fossil fuel power plant emissions as seen by a CarbonSat constellation, *Atmos. Meas. Tech.*, 4, 2809–2822, <https://doi.org/10.5194/amt-4-2809-2011>, 2011.
- 535

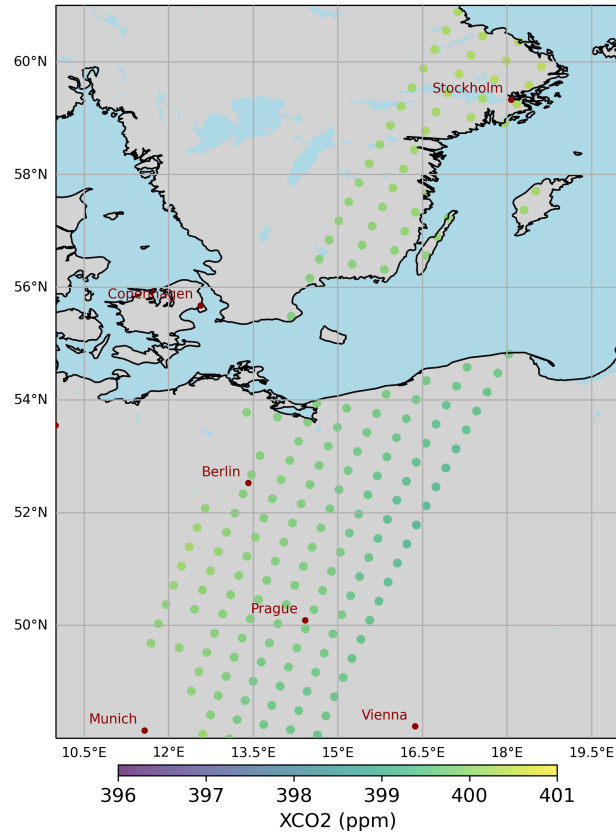


Figure 1. Example for the subset data: Modelled XCO₂ over part of Europe for one orbit on 2015-07-03. Only cloud-free data over land are shown because only these will be used later in the retrieval. No post-processing filters are applied. Note that only the centre points of the ground pixels are plotted and that the size of the markers is much larger than the original ground pixel size.

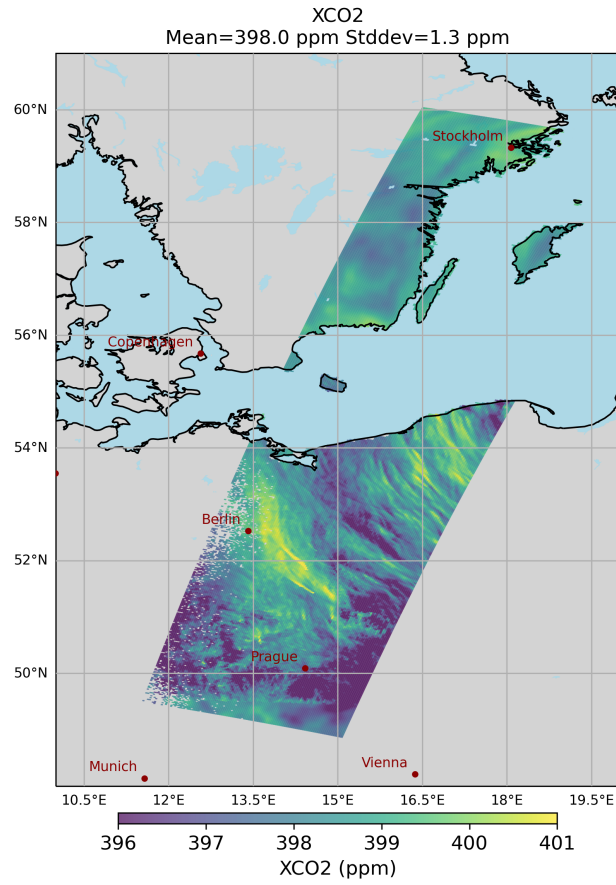


Figure 2. High-resolution scene: XCO₂. Only cloud-free data over land; no post-processing filters are applied.

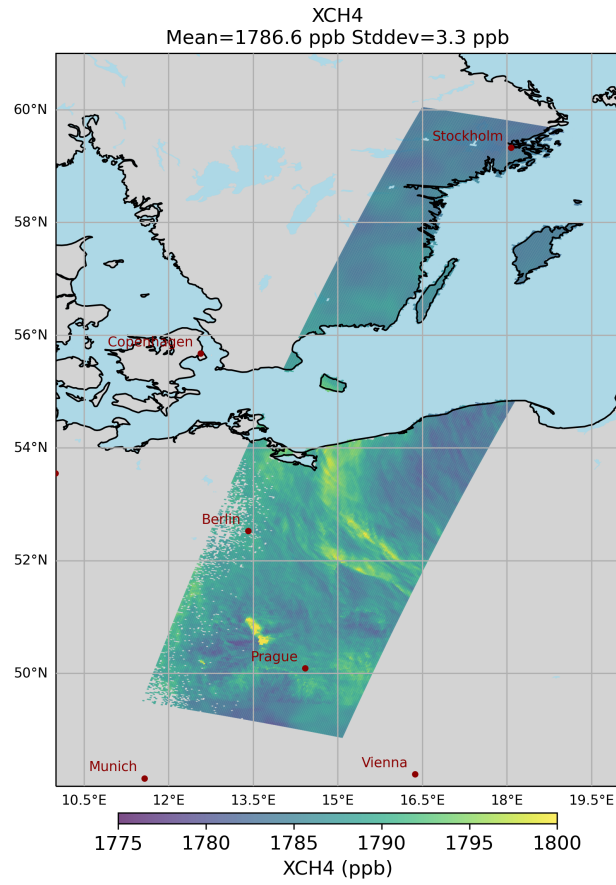


Figure 3. As Fig. 2, but for XCH₄.

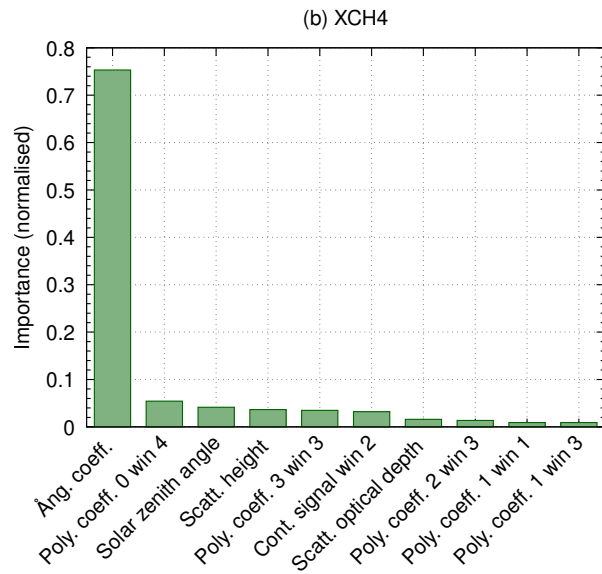
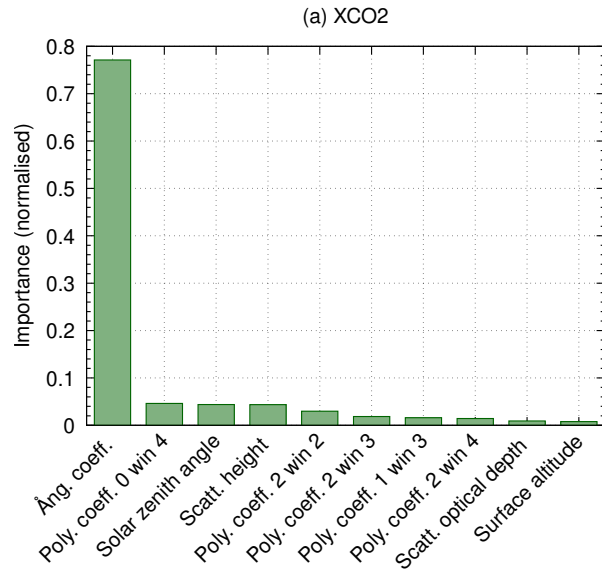


Figure 4. Bias correction parameters and their relative importance (normalised such that the sum of all importances is 1.). a) XCO₂. b) XCH₄.

Bias correction FOCAL-CO2M Subset 2015-04 (cloudfree)

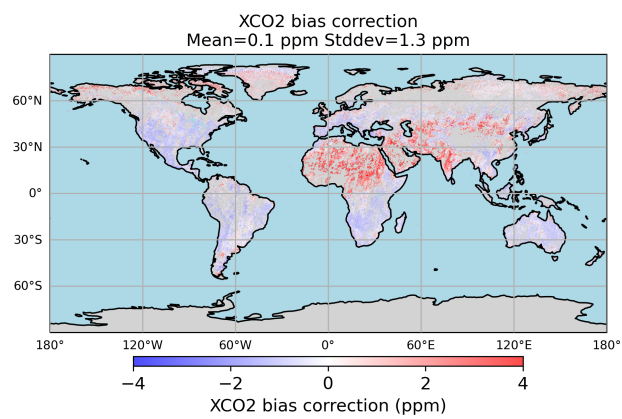


Figure 5. Map of the derived XCO₂ bias for the subset data of April 2015.

Bias correction FOCAL-CO2M Subset 2015-04 (cloudfree)

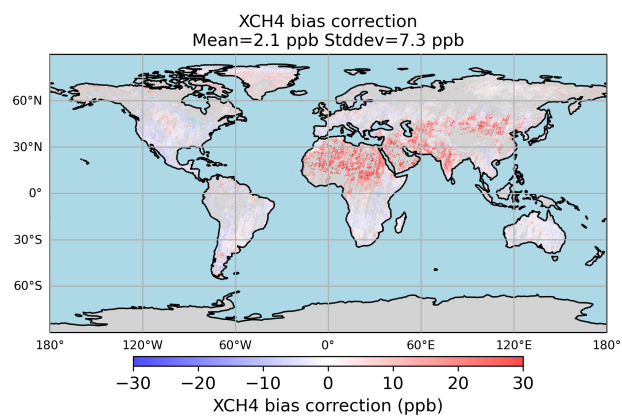


Figure 6. As Fig. 5, but for XCH₄.

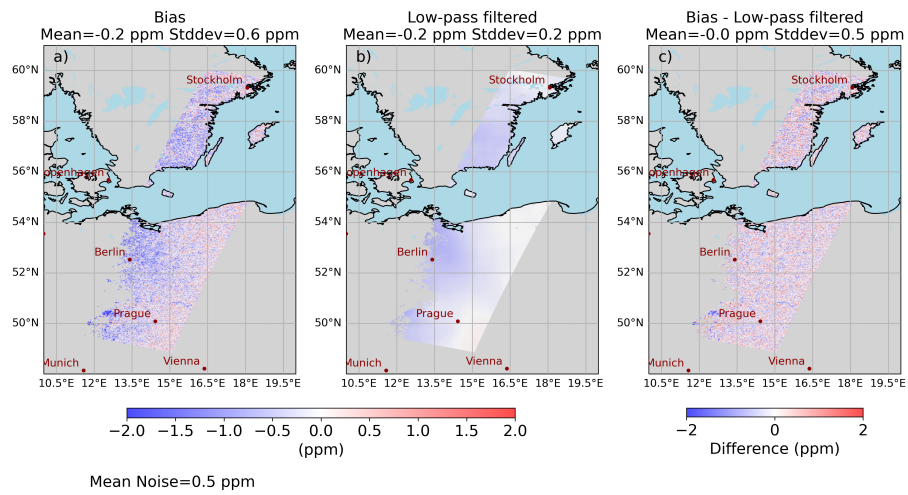


Figure 7. Example for low-/high-pass filtering (Berlin scene). a) Bias (FOCAL-CO₂M retrieved - true XCO₂). b) $1^\circ \times 1^\circ$ low-pass filtered bias. c) High-pass filtered bias = Bias - Low-pass filtered bias.

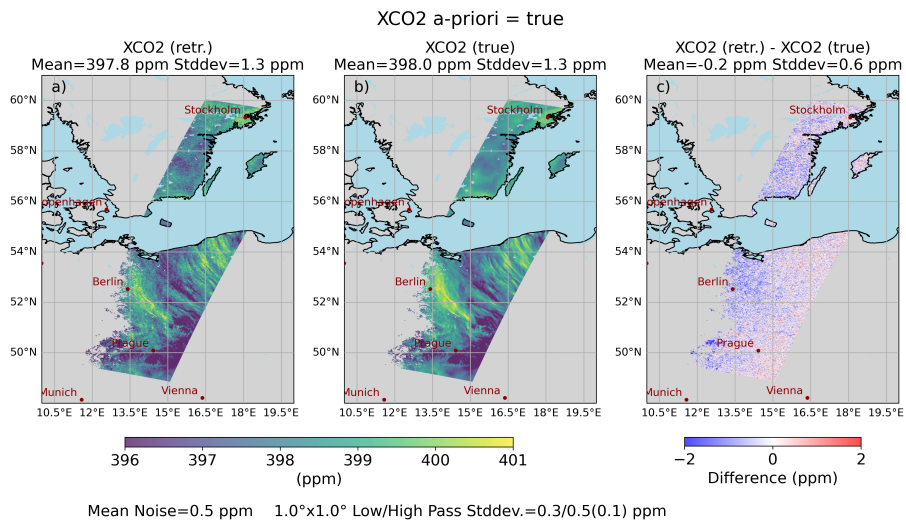


Figure 8. FOCAL-CO₂M XCO₂ retrieval results for the ‘Berlin scene’ (only cloud-free data over land). a) Retrieved XCO₂. b) True XCO₂. c) Difference Retrieved - True XCO₂. The same post-processing filtering has been applied to all data shown in the plots. The number in brackets after the high-pass standard deviation gives an estimate for the high-pass standard deviation without noise.

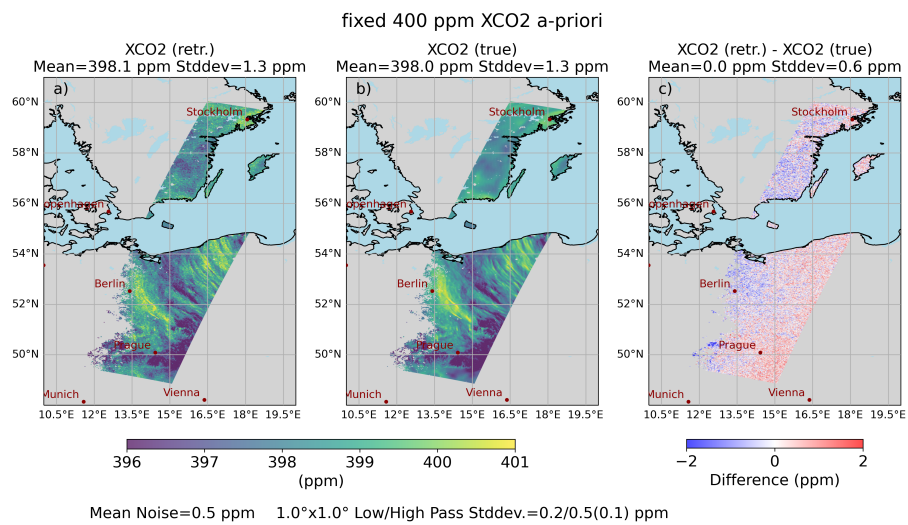


Figure 9. As Fig. 8, but for a fixed 400 ppm a-priori

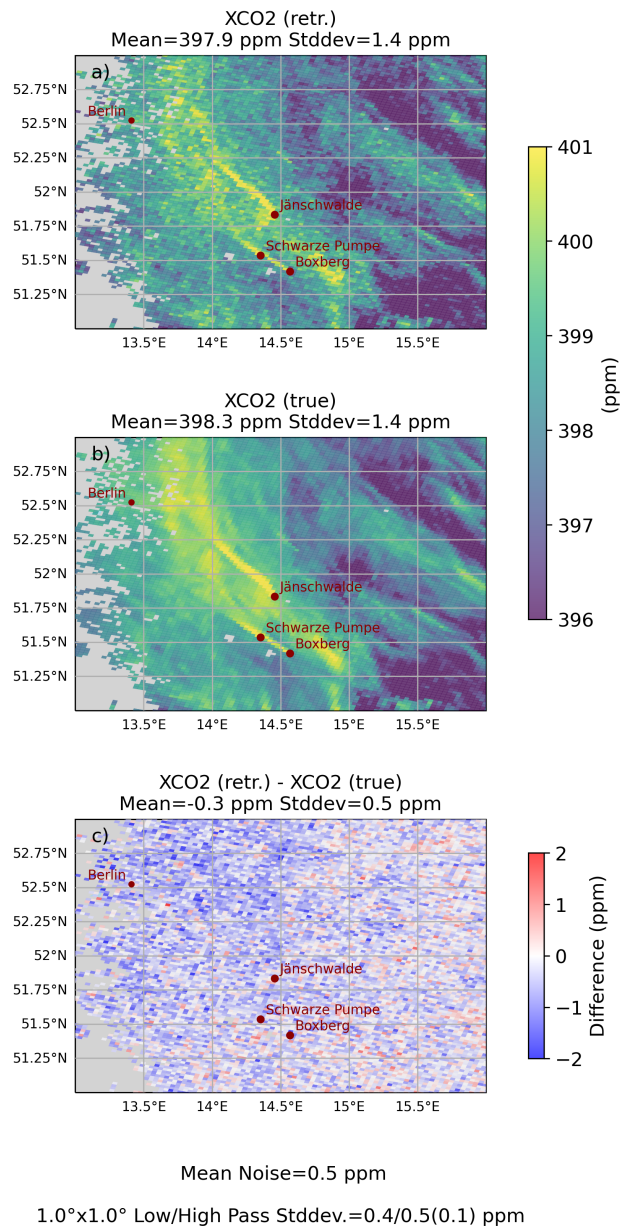


Figure 10. Zoom of Fig. 8.

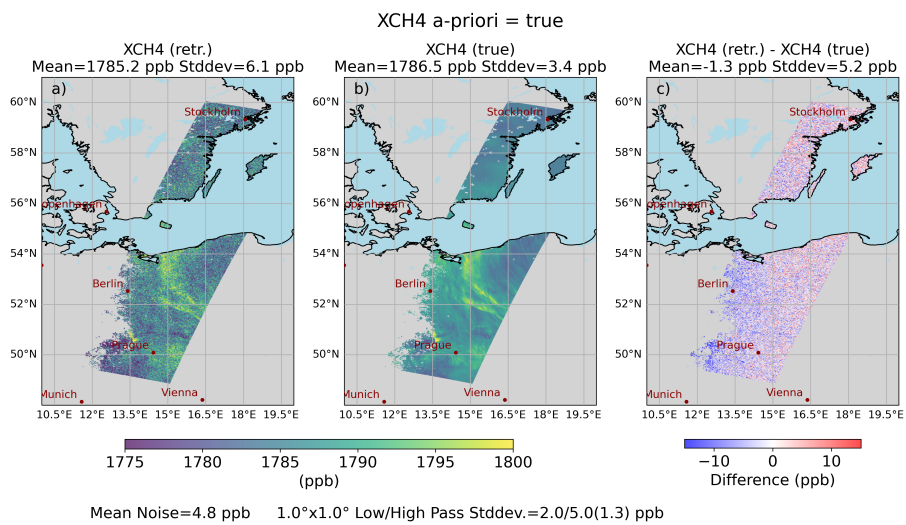


Figure 11. As Fig. 8, but for FOCAL-CO2M XCH₄.

FOCAL-CO2M Subset 2015-04 (cloudfree)

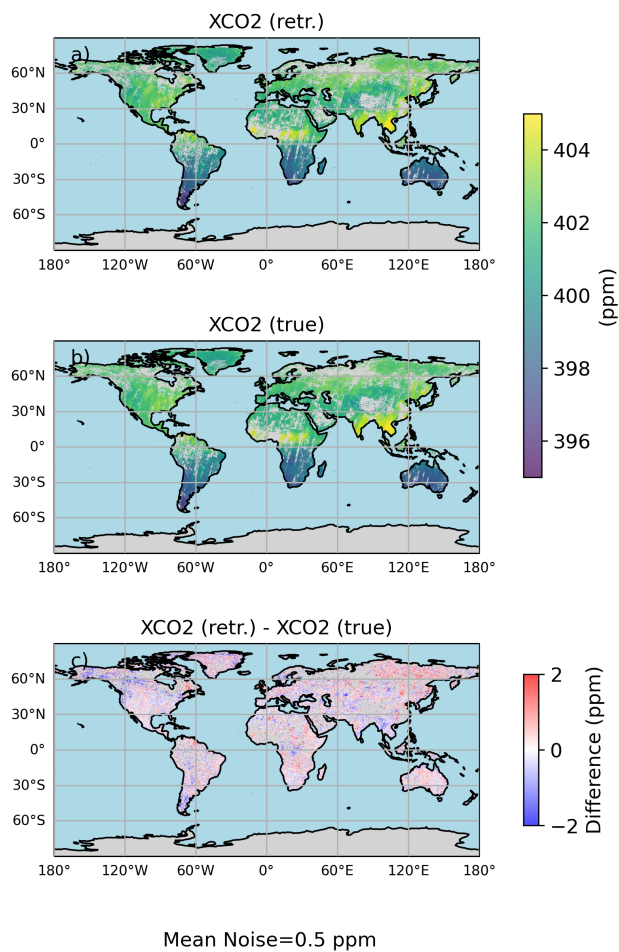


Figure 12. FOCAL-CO2M XCO₂ retrieval results for April 2015 (cloud-free subset data over land). a) Retrieved XCO₂. b) True XCO₂. c) Difference Retrieved - True XCO₂.

FOCAL-CO2M Subset 2015-04 (cloudfree)

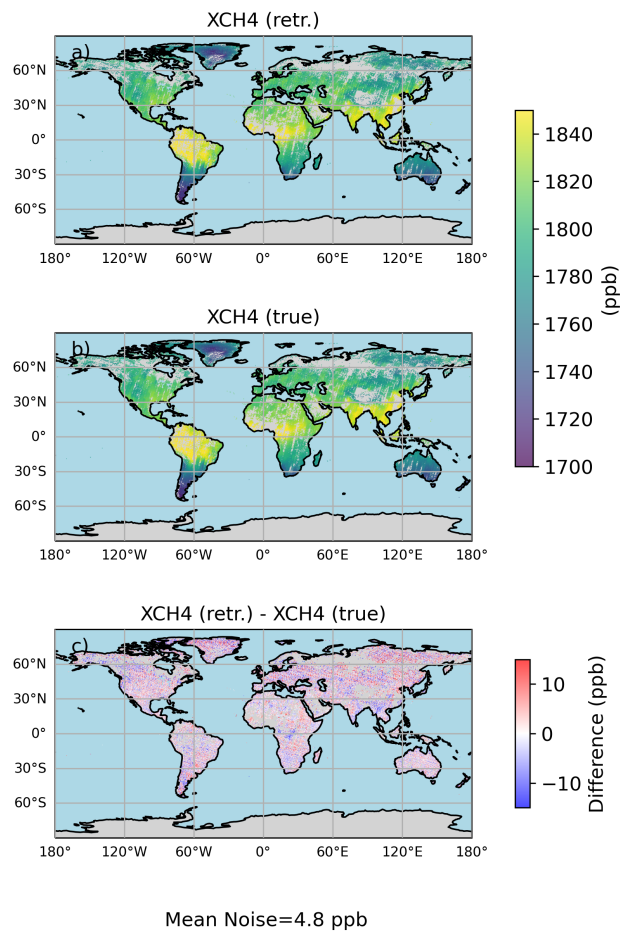


Figure 13. As Fig. 12, but for XCH₄.

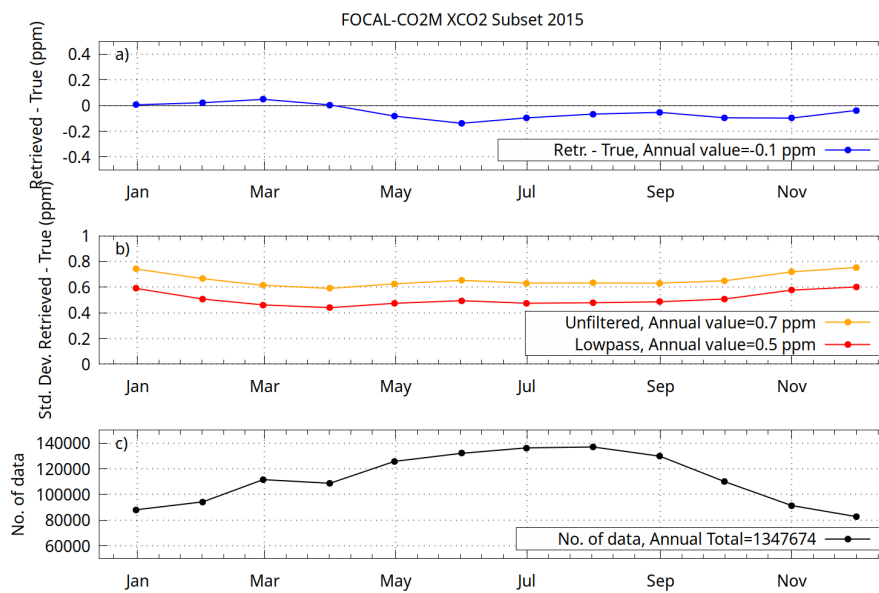


Figure 14. Monthly means and standard deviations of 2015 global subset data. a) Mean difference retrieved – true XCO₂. b) Standard deviation retrieved – true XCO₂ (orange: unfiltered, red: low-pass filtered). c) Number of data after post-processing. Annual values are given in the labels.

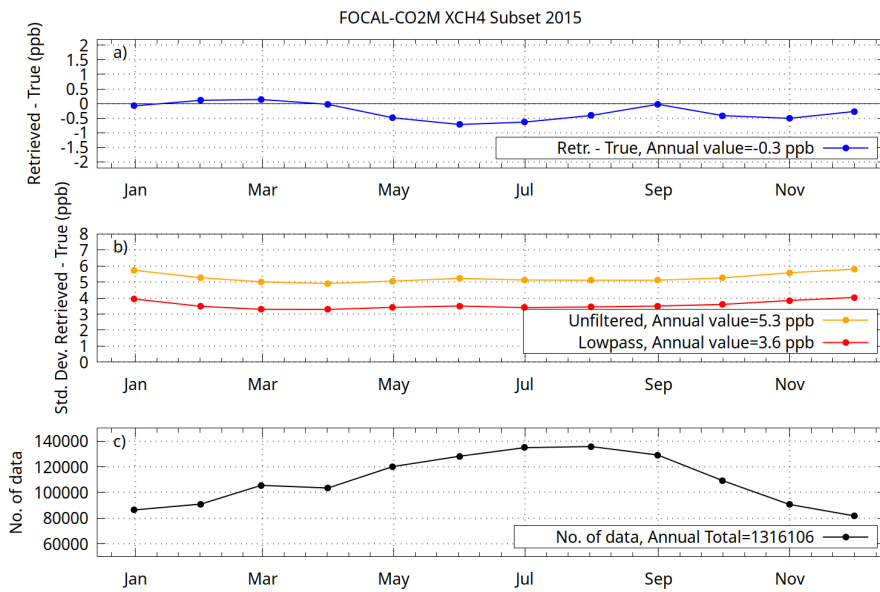


Figure 15. As Fig. 14, but for XCH₄.

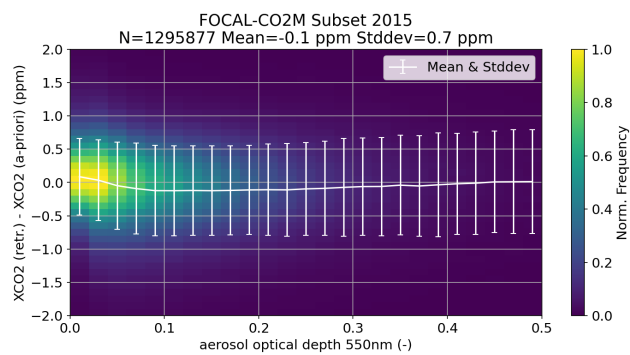


Figure 16. Difference between retrieved and true XCO₂ as function of AOD at 550 nm.

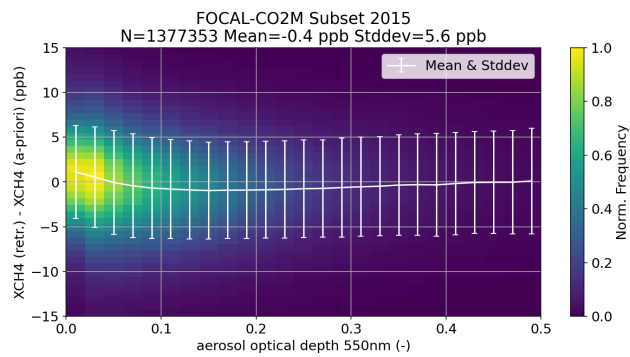


Figure 17. As Fig. 16, but for XCH₄.

Table 1. CO2M instruments and their characteristics.

CO2I (Imaging Spectrometer)		
Band	Spectral range	Spectral resolution
VIS	405 – 490 nm	0.6 nm
NIR	747 – 773 nm	0.12 nm
SWIR-1	1590 – 1675 nm	0.3 nm
SWIR-2	1990 – 2095 nm	0.35 nm

MAP (Multi-Angle Polarimeter)		
Band	Central wavelength	Band width
VNIR-1	410 nm	20 nm
VNIR-2	443 nm	20 nm
VNIR-3	490 nm	20 nm
VNIR-4	555 nm	20 nm
VNIR-5	670 nm	20 nm
VNIR-6	753 nm	9 nm
VNIR-7	865 nm	40 nm

CLIM (Cloud Imager)		
Band	Band centre	Band width
CLIM-1	670 nm	20 nm
CLIM-2	753 nm	9 nm
CLIM-3	1370 nm	15 nm

Table 2. Parameters of instrument noise model. Unit of A is 10^{-7} photons $^{-1}$ s nm cm 2 sr.

Parameter	NIR	SWIR-1	SWIR-2
A	0.2	1.32	1.54
B	140	450	450

Table 3. Definition of FOCAL-CO2M spectral fit windows. Cross sections are from HITRAN2016 (Gordon et al., 2017, downloaded on 23 March 2021).

No.	Name	Wavelength range (nm)	Considered gases
1	SIF	747.0 – 759.0	O ₂ , H ₂ O
2	O ₂	759.2 – 773.0	O ₂ , H ₂ O
3	Weak CO ₂	1590.0 – 1670.0	CO ₂ , H ₂ O, CH ₄
4	Strong CO ₂	1990.0 – 2090.0	CO ₂ , H ₂ O, CH ₄

Table 4. State vector elements and related retrieval settings. A priori values are also used as first guess. “Fit windows” lists the spectral windows (see Table 3) from which the element is determined. “each” means that a corresponding element is fitted in each fit window. A priori values labelled as “PP” are taken from the provided meteorological data; “est.” denotes that they have been estimated from the background signal.

Element	Fit windows	A priori	A priori uncertainty	Comment
Gases / SIF				
co2_lay	3,4	PP	5.0	CO ₂ profile (5 layers), in ppm
ch4_lay	3,4	PP	0.045	CH ₄ profile (5 layers), in ppm
h2o_lay	3,4	PP	4500.	H ₂ O profile (5 layers), in ppm
sif_fac	1	0.	5.	SIF spectrum scaling factor
Scattering parameters				
pre_sca	1–4	0.2	1.	Layer height (rel. pressure, 0=surface, 1=infinity)
tau_sca_0	1–4	0.01	1.	Optical depth
ang_sca	1–4	4.0	1.	Ångström coefficient
Polynomial coefficients (surface albedo)				
poly0	each	est.	0.1	estimated surface albedo
poly1	each	0.0	0.01	
poly2	each	0.0	0.01	
poly3	each	0.0	0.01	
Spectral corrections				
wav_shi	each	0.0	0.1	Wavelength shift
wav_squ	each	0.0	0.001	Wavelength squeeze
ils_squ	each	1.0	0.1	Slit function squeeze

Table 5. Filter variables and limits for FOCAL-CO2M XCO₂ (land). “–” means that no limit is applied.

Variable	Valid range	
	min.	max.
Poly. coeff. 0 win 3	$8.52 \cdot 10^{-2}$	–
Poly. coeff. 0 win 4	$4.05 \cdot 10^{-2}$	–
Poly. coeff. 0 win 1	0.11	–
Poly. coeff. 1 win 4	$-8.49 \cdot 10^{-5}$	–
Poly. coeff. 0 win 2	0.12	–
Poly. coeff. 1 win 4 unc.	$1.40 \cdot 10^{-5}$	$5.97 \cdot 10^{-5}$

Table 6. Filter variables and limits for FOCAL-CO2M XCH₄ (land). “-” means that no limit is applied.

Variable	Valid range	
	min.	max.
Poly. coeff. 0 win 3	$9.68 \cdot 10^{-2}$	-
Poly. coeff. 0 win 4	$4.07 \cdot 10^{-2}$	-
Poly. coeff. 1 win 4	$-1.05 \cdot 10^{-4}$	-