

A retrieval of $x\text{CO}_2$ from ground-based mid-infrared NDACC solar absorption spectra and comparison to TCCON

Rafaella Chiarella¹, Matthias Buschmann¹, Joshua Laughner², Isamu Morino³, Justus Notholt¹, Christof Petri¹, Geoffrey Toon², Voltaire A Velazco⁴, and Thorsten Warneke¹

¹Institute of Environmental Physics, University of Bremen, Bremen, Germany

²Jet Propulsion Laboratory, California Institute of Technology, Pasadena, CA, USA

³Earth system Division, National Institute for Environmental Studies (NIES), Onogawa 16-2, Tsukuba, Ibaraki 305-8506, Japan

⁴School of Earth Atmospheric and Life Sciences, University of Wollongong, NSW 2522, Australia. *Now at: Deutscher Wetterdienst (DWD), Meteorological Observatory Hohenpeissenberg, 82383, Germany

Correspondence: Rafaella Chiarella (rachi@iup.physik.uni-bremen.de)

Abstract.

Two global networks of ground-based Fourier transform spectrometers are measuring abundances of atmospheric trace gases that absorb in the near and mid infrared, the Network for the Detection of Atmospheric Composition Change (NDACC) and the Total Carbon Column Observing Network (TCCON). The first lacks a CO_2 product, therefore this study focuses on developing a $x\text{CO}_2$ retrieval method for NDACC from a spectral window in the 4800 cm^{-1} region. This retrieval will allow to extend ground-based measurements back in time, which we will demonstrate with historical data available from Ny-Ålesund, Svalbard. At this site, routinely both TCCON and NDACC, measurements are performed which is an advantage for collocated comparisons. The results are compared with collocated TCCON measurements of column-averaged dry-air mole fractions of CO_2 (denoted by $x\text{CO}_2$) in Ny-Ålesund, Svalbard and only TCCON in Burgos, Philippines. We found that it is possible to retrieve $x\text{CO}_2$ from NDACC spectra with a precision of 0.2%. The comparison between the new retrieval to TCCON showed that the sensitivity of the new retrieval is high in the troposphere and lower in the upper stratosphere, similar to TCCON, as seen in the averaging kernels and that the seasonality is well captured as seen in the retrieved time series. Additionally we have included a retrieval strategy suggestion to improve the quality of the $x\text{CO}_2$ product.

1 Introduction

Carbon Dioxide (CO_2) is the most important anthropogenic greenhouse gas. Fossil fuel combustion and deforestation are the main net sources of CO_2 , the ocean and terrestrial ecosystems currently act as net sinks, absorbing approximately half of the anthropogenic emissions (IPCC, 2022). Remote sensing measurements provide a column integral, that is less affected by vertical transport and local sources. The CO_2 column derived from ground based Fourier transform infrared (FTIR) spectrometry from near infrared radiation (NIR) solar absorption spectra can achieve a precision better than 0.25% (Wunch et al., 2011a).

20 The Total Carbon Column Observing Network (TCCON), a worldwide network, has currently 26 operational measurement sites since 2004. The network was founded for satellite validation and remotely measures abundances of CO_2 , CO , CH_4 , and other molecules absorbing in the near-infrared covering the spectral range from 4000 cm^{-1} to 11000 cm^{-1} .

The Network for the Detection of Atmospheric Composition Change Infrared Working Group (NDACC-IRWG) was founded in 1991 and has a total of 25 sites. The network provides total column abundances and profiles of several atmospheric constituents, with a focus on the O_3 cycle (De Maziere et al., 2018) retrieved from the mid infrared covering the spectral region 25 2000 to 5000 cm^{-1} uses optical filter to limit the spectral range of the recorded spectrum. The NDACC official filters are listed in the Appendix of Blumenstock et al. (2021).

NDACC trace gas products, in contrast to TCCON, don't include CO_2 . An extension of the retrieval capabilities of NDACC spectra to include a CO_2 product would expand the temporal and spatial coverage of the total column products. In this study 30 one set of historical data, for Ny-Ålesund is presented, where the CO_2 spectra date back to 1997. Two major challenges have to be faced on the way to an NDACC $x\text{CO}_2$ product. TCCON retrieval method uses the ratio of CO_2 from the 6300 cm^{-1} band and CO_2 from the 7885 cm^{-1} band (Yang et al., 2002), in contrast there are no CO_2 absorption lines present in the NDACC MIR spectra; therefore there is no proxy for the dry-air column to which to take a ratio. N_2 lines are present in the 4800 cm^{-1} region, however, the lines are too weak. Additionally the presence of multiple interfering gases hinders the use of 35 broad spectral windows (Buschmann et al., 2016).

Previous efforts towards a $x\text{CO}_2$ product using MIR spectra include Barthlott et al. (2015) and Buschmann et al. (2016). The column-averaged dry-air mole fractions of CO_2 ($x\text{CO}_2$) retrieval proposed by Barthlott et al. (2015) using four microwindows in the 2620 cm^{-1} region was appropriate for long-term monitoring of instrument stability and consistency of trends of tropospheric species. However, due to the low sensitivity of the MIR averaging kernels to the surface, the proposal by Barthlott 40 et al. (2015) was not applicable for shorter timescales therefore it did not provide new information on the carbon cycle, as the annual trends are already well understood. Similarly, Buschmann et al. (2016) presented an approach for the retrieval of $x\text{CO}_2$ from several NDACC MIR micro windows in the 2620 to 3350 cm^{-1} region. Nonetheless, this approach showed to have a strong sensitivity to the chosen a priori and low sensitivity in the troposphere due to the small averaging kernels, in comparison to TCCON.

45 In this study a retrieval of the column average dry-air mole fraction of CO_2 from MIR solar spectra in the 4800 cm^{-1} region is described. We will discuss the different retrievals, their sensitivities and dependence on the a priori information and airmass factor. We will present the averaging kernels, and their influence on the retrieval and our approach to an error budget, covering standard errors, the diurnal variation and sensitivity to several error sources and finally their application to Ny-Ålesund historical data.

50 In the next section information on the selected sites is given and the window and the retrieval used are described. Then in the third to fifth sections the influence of the averaging kernels, the a priori and airmass factor on the retrieval is investigated and compared to TCCON, respectively. The sixth section includes the error budget and error source tests. In the seventh section the time series for both Burgos and Ny-Ålesund historical data is presented. Finally, in section seven an acquisition strategy is proposed, followed by a conclusion about the retrieval method.

2.1 Location and Measurements

Data from two sites were used, Ny-Ålesund in the Arctic and Burgos in the tropics. Ny-Ålesund provides the collocated measurements of NDACC and TCCON. On the other hand Burgos gives us the opportunity to assess the retrieval in an atmosphere with higher temperature and water content.

60 The measurements in Ny-Ålesund (Spitzbergen, 78.92°N, 11.92°E) were performed using the Bruker IFS 120-5 HR instrument with Indium Gallium Arsenide (InGaAs) and liquid nitrogen cooled Indium Antimonide (InSb) detectors. NDACC spectra are recorded with the InSb detector since 1992 which covers the mid-infrared spectral region with an optical path difference (OPD) of 180 cm, giving a spectral resolution of approximately 0.005 cm^{-1} . The acquisition is performed with different band-pass filters. The filter of interest for this study transmits from 4044 cm^{-1} to 4822 cm^{-1} , will be referred to as
 65 filter 4433 as its center wave number, and started being used in 1996. On the other hand, TCCON uses the InGaAs detector for its measurements since 2004 covering the spectral region 4000 cm^{-1} to 11000 cm^{-1} (Wunch et al., 2011a).

Burgos (Philippines, 18.53°N 120.65°W) has a warm and humid climate. There, only TCCON InGaAs measurements are performed with a FTS model Bruker 125 HR. The operations started in 2017 (Morino et al., 2018; Velazco et al., 2017). The tropics face different challenges with a higher water vapour content along the light path and a higher tropopause.

70 The spectra available were separated in two groups, InSb (from NDACC) and InGaAs (from TCCON), both were used to retrieve $x\text{CO}_2$ from the new window and compared to the $x\text{CO}_2$ retrieved from the two TCCON CO_2 windows from InGaAs spectra.

Additionally, collocated TCCON and aircraft profiles from campaigns over TCCON stations and AirCore were used where available to do a comparison with in situ data. This allows to determine the systematic biases in the spectroscopy of the column
 75 measurement as is similarly done for TCCON windows in the recent GGG2020 soon to be released.

2.2 CO_2 window in the MIR

The mid-infrared region not only has CO_2 absorption lines but also other gases with strong absorption lines. The high resolution measurements of NDACC allow for the use of narrower windows or single lines. The selected spectral window is centred at 4790 cm^{-1} and has a 20 cm^{-1} width, hence we will refer to it as **w4790**. It contains water lines but minimal interference from
 80 other gases.

To choose the windows, we made use of information on the NDACC filters and the intensity of the transitions of CO_2 in the region. The first step to select prospect windows was to study the NDACC spectra available from Ny-Ålesund and select which of the available regions will be used. The region of 4800 cm^{-1} acquired using the filter 4433 was selected because it contains a strong band of CO_2 corresponding to the transition $21113 \rightarrow 01101$ (quantum numbers: $\nu_1\nu_2l_2\nu_3n$) for the main isotope
 85 and weaker bands for the other isotopes (Toth et al., 2008). This is referred to as a "hot" band because it contains a transition between two excited vibrational states. The population of the initial state is dictated by the Boltzmann distribution, this makes the band temperature dependent, as the intensity is proportional to the population of the excited initial state (Buckingham,

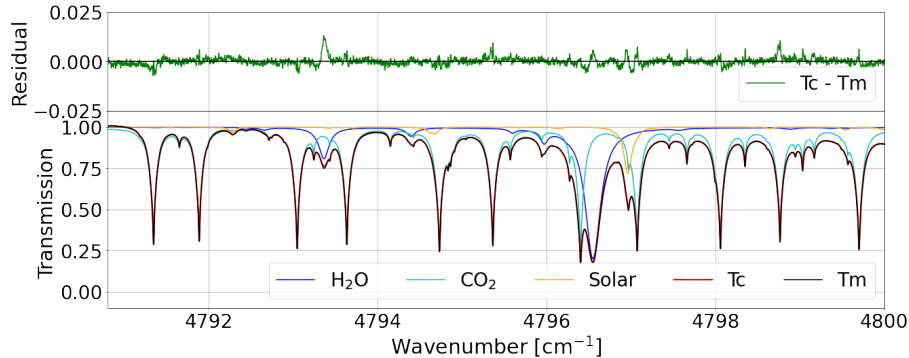


Figure 1. An example of the computed transmittance (T_c) and the measured transmittance (T_m) for the w4790 window, CO_2 absorption lines and other gases, and the residual ($T_m - T_c$) for a typical InSb spectrum acquired in Ny-Ålesund.

1976). With a ground-state energy $E'' = 858 \text{ cm}^{-1}$ the estimated theoretical error for a 2 K error in temperature is between 1.2 to 1.8% of the retrieved $x\text{CO}_2$. However, from tests performed, the temperature sensitivity is approx. 1.5%/K (see subsection 90 5.2). The CO_2 transitions and the intensity of each line was taken from the line parameters from the GFIT atm.161 line list, which is based on the HITRAN 2016 (high-resolution transmission molecular absorption) database (Toon et al., 2016). The line list and an evaluation of the temperature and the impact of using isotopes for the retrieval are addressed in the Appendix E.

An example of a spectral fit is shown in figure 1 where we can observe how the measured spectra fits the calculated spectrum. On the left, wave numbers lower than 4794 cm^{-1} , there is an overlap between measured transmittance (TM) and CO_2 . However, after that, at higher wavenumbers, measured spectrum slopes down and we can see a considerable gap between it and the CO_2 lines towards the end of the window. This is caused by the filter used to record this spectra. The w4790 window is located near the end of the filter 4433, where the transmission has started to decline (see Appendix C).

To provide the best fit to the measured spectrum and minimize the residuals, other gas profiles and other parameters are 100 scaled and adjusted. The gas mole fraction is retrieved from these scaled profiles (Wunch et al., 2015). The parameters fitted are: continuum level, continuum tilt, continuum curvature, frequency shift and solar lines. The gases fitted are: CO_2 , H_2O , HDO, CH_4 and N_2O . See in Appendix A the full window fitting parameters used in the retrieval.

For comparison the TCCON $x\text{CO}_2$ data from Ny-Ålesund (Buschmann et al., 2023) and Burgos (Morino et al., 2023) were used. These windows are centred at 6220.00 cm^{-1} and 6339.50 cm^{-1} with spectral widths of 80 cm^{-1} and 85 cm^{-1} 105 respectively (Wunch et al., 2011a). Additionally, TCCON is introducing a new window in the 4800 cm^{-1} region called 1CO_2 , for more details refer to the Appendix G.

In this study we work with two types of spectra, that we will denote with the detector used to record, **InGaAs** and **InSb**. Following this, we have three windows used for retrievals, the w4790 and the two TCCON windows around the **6300** cm^{-1} . Details of the three $x\text{CO}_2$ retrievals are shown in the Table 1.

Table 1. The names of the 3 different xCO₂ retrievals, with the spectra details, the resolution of each spectra used and the data availability for each site.

Name	Details	Resolution	Data available since	
			Ny-Ålesund	Burgos
w4790 InSb	from NDACC spectra using w4790	0.005	1997	None
w4790 InGaAs	from TCCON spectra using w4790	0.02	2004	2017
6300	from TCCON spectra using TCCON windows	0.02	2004	2017

110 2.3 Retrieval Method

The retrieved xCO₂ in this study is obtained by the profile scaling algorithm GFIT (version 5.28 in GGG2020) nonlinear least-squares fitting algorithm, which is also used for the TCCON xCO₂ retrievals. A full description is available in Laughner et al. (2020)

115 The CO₂ column averaged dry-air mole fraction (DMF) retrieved by TCCON is calculated using CO₂ obtained from the band at 7885 cm⁻¹. The well mixed CO₂ is used to estimate the total dry-air column. The column averaged dry air mole fraction is derived by dividing the vertical columns (VC) of CO₂ by the VC of O₂ (Wunch et al., 2011a). For the purpose of this retrieval the O₂ mole fraction is assumed constant.

$$xCO_2 = \frac{VC_{CO_2}}{VC_{O_2}} \times 0.2095 \quad (1)$$

120 w4790 xCO₂ was also retrieved using the GFIT software, for both InSb and InGaAs spectra. However, InSb spectra used here don't contain any O₂ window. An additional difference between the w4790 window and the 6300 TCCON windows is that we do not currently apply an airmass dependent correction (ADCF) or in situ correction factor (AICF) to the w4790 xCO₂, while the TCCON xCO₂ includes both. The mole fraction for the MIR spectra was calculated using the dry-air column abundance inferred from the surface pressure (Wunch et al., 2011a) with the following equation:

$$xCO_2 = \frac{VC_{CO_2}}{\frac{P_s N_A}{m_{air}^{dry} \{g\}} - \frac{VC_{H_2O} m_{H_2O}}{m_{air}^{dry}}} \quad (2)$$

125 VC_{CO₂} is the CO₂ vertical column from the GGG2020 output from w4790, VC_{H₂O} is the vertical column from the GGG2020 output for water vapour from the window at 4576.85 cm⁻¹ of width 1.90 cm⁻¹, P_s is the surface pressure in hPa, N_a = 6.0221415 10²³ molecules/mole, the Avogadro number; m_{air}^{dry} = 28.9644 g/mole, mass of dry air; m_{H₂O} = 18.01534 g/mole, the mass of water and the column-averaged gravitational acceleration {g} = 9.81 ms⁻².

130 These are two main important differences between the 6300 and the w4790 retrievals, the calculation of the mole fraction using CO₂ or pressure and the inclusion of an airmass and in situ correction or lack of (both corrections are explained in sections 4.2 and 4.4 respectively).

The retrieved mole fraction is quality controlled following a similar flagging as TCCON (Wunch et al., 2011a). Data points with a high solar zenith angles (SZA) (>83° as used by TCCON in Burgos) and/or high relative retrieval errors (10% of the average) were discarded; spectra with negative error output were also removed. Finally, data points with high relative retrieval error (>20% of the average) of H₂O were filtered out.

For the time series, an error-weighted daily mean (\bar{x}^{daily}) and the standard deviation of the daily mean (σ_{w4790}) was calculated. Because InSb spectra recorded each day on the filter covering w4790 is not abundant (usually less than 20 spectra per day), the weighted daily mean of the 6300 was used to calculate the standard deviation.

$$\bar{x}^{daily} = \frac{\sum_N^i \frac{x_i}{\epsilon_i^2}}{\sum_N^i \frac{1}{\epsilon_i^2}} \quad (3)$$

$$\sigma_{w4790} = \sqrt{\frac{\sum_N^i \left(\frac{x_i - \bar{x}^{daily}}{\epsilon_i} \right)^2}{\sum_N^i \frac{1}{\epsilon_i^2}}} \quad (4)$$

Where x_i is a given xCO₂ value and ϵ_i its corresponding relative retrieval error.

The error budget was approximated by using the standard deviations of the daily means (eq. 4) and the standard error to better reflect the uncertainty in the daily mean which is affected by the number of measurements. In addition, the diurnal variation was calculated to determine the precision following Yang et al. (2002):

$$DV = \left(\frac{x}{\bar{x}^{daily}} - 1 \right) \times 100 \quad (5)$$

In the next sections several sensitivity tests and error budgets are presented to determine the quality of the retrieval.

3 Averaging Kernels

150 In this section the effect of the different averaging kernels on the retrieved xCO₂ is evaluated, by comparing two different retrievals (Rodgers and Connor, 2003). For a perfect column measurement, the column averaging kernel should be 1.0 at all altitudes, but in practice, there is a greater sensitivity to some altitudes than others. The column averaging kernels depend on the retrieval method and the choice of parameters to be fitted and the solar zenith angle (Wunch et al., 2011a). The main difference in the averaging kernels originates in the shape and depth of the absorption lines. In this case the w4790 InSb CO₂ averaging kernels show a high sensitivity in the troposphere and it decreases towards the upper atmosphere. High sensitivity remains towards the stratosphere because the lines used are weak and don't saturate.

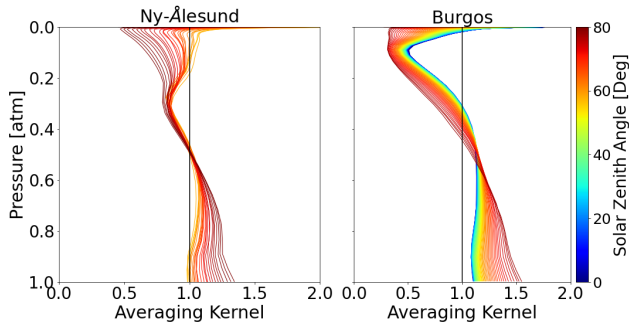


Figure 2. w4790 averaging kernels averaged to 1° for all InGaAs Ny-Ålesund on the left and Burgos on the right.

In figure 2 we see the averaging kernels for w4790 InGaAs in Ny-Ålesund, those corresponding to w4790 InSb spectra look very similar (see supplemental Figure I1 in appendix).

160 We observe that the averaging kernels for Burgos look different to Ny-Ålesund, however, follow a similar shape but the minimum lies at different altitudes. When seeing the averaging kernels plotted against altitude (see in supplemental plots I3 and I4 in Appendix) the overall shape is similar but the minimum occurs around the 10 km for Ny-Ålesund and around 15 km in Burgos, and the maximum is between 40 and 50 km for both. This is probably due to the difference in the height of the tropopause in both locations, Burgos having a higher tropopause than Ny-Ålesund.

165 4 Sensitivity studies

4.1 A priori influence

As described by Rodgers (2000), the retrieved quantity \hat{x} relates to the true atmospheric quantity x , the a priori x_a and the averaging kernel A by the following equation:

$$\hat{x} - x_a = A(x - x_a) + \epsilon_x \quad (6)$$

170 where ϵ_x is the random and systematic error term. The a priori profile will influence the retrieved $x\text{CO}_2$ depending on how much the measured information can constrain the retrieval (Rodgers, 2000). The prior profiles of GGG2020 are produced using the Goddard Earth Observing System Forward Product for Instrument Teams (GEOS-5 FP-IT or GEOS FP-IT) (Lucchesi, R., 2015) reanalysis product that has a temporal resolution of three hours. The full description is found in Laughner et al. (2022). The use of a priori profiles that are close to the true atmosphere can give the impression of a successful retrieval, even if the information content of the measured quantity is not sufficient. To discard this possibility, the influence of the a priori needs to be evaluated with a test retrieval performed with a modified a priori, as shown in this section. The modified a priori is initially fixed to 400 ppm at all altitudes and includes a linear increase of 0.1 ppm for each modelled profile (see figure I5 in the Appendix). The $x\text{CO}_2$ retrieved using the modified a priori is then compared to the $x\text{CO}_2$ retrieved using the standard a priori.

180 Apart from the different a priori, the same retrieval algorithm, procedure and post processing parameters have been used as in the original retrievals with the standard a priori.

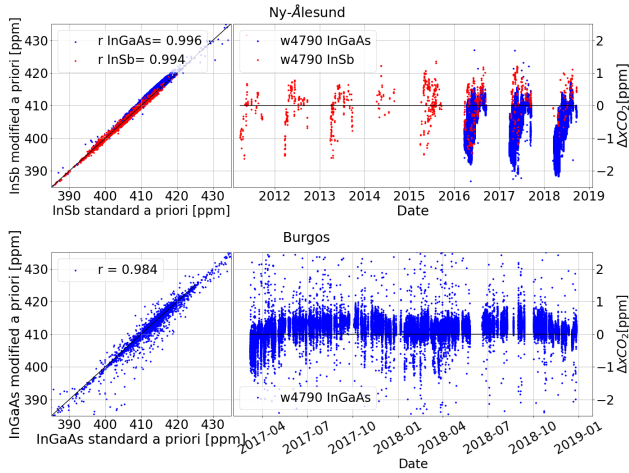


Figure 3. On the top Ny-Ålesund, InGaAs (2016-2018) in blue and InSb (2012-2018) in red. On the bottom Burgos (2017-2018). On the left the correlation plots and on the right the difference between xCO_2 retrieved with the standard a priori minus the xCO_2 retrieved with the modified a priori, ΔxCO_2 .

For both locations, the correlation coefficients r between the retrievals with the fixed and the standard a priori are better than 0.95 which means a strong correlation. From figure 3 we observe the scattering for Burgos is higher than for Ny-Ålesund, likely due to the higher humidity and temperature given that the window is temperature sensitive. For Ny-Ålesund we see in the latest years a tendency to shift towards lower ΔxCO_2 . The modified a priori used for these tests include a linear increase of xCO_2 . This increase might not correctly represent the atmospheric evolution and results in an over estimation. For both locations, the ΔxCO_2 is mostly smaller than 2 ppm.

4.2 Solar zenith angle dependence

The w4790 xCO_2 has an airmass-dependent artifact and an airmass independent artifact similarly to the TCCON xCO_2 . The airmass-dependent artifacts are primarily caused by systematic errors introduced by spectroscopic inadequacies in the linelist and instrumental problems (Wunch et al., 2011a).

From Wunch et al. (2011a), the TCCON xCO_2 product has a SZA or airmass-dependent artifact causing the retrieval to be larger, by approximately 1% at 20° SZA than at 80° SZA. To correct this, TCCON applies an empirical correction (ADCF). In GGG2014, the correction was derived separately for each xGAS product. In GGG2020, it is derived for each retrieval window. In this study we did not apply the airmass correction (ADCF) to the w4790 retrievals shown, to determine if the retrieval of xCO_2 has to be corrected for airmass artifacts. We show in Figure 4, $xCO_2 - \bar{x}CO_2$ against SZA, where $\bar{x}CO_2$ is the daily mean. Under the assumption that, on a given day, any variation of xCO_2 that is symmetrical around noon is an artifact and anti-symmetrical variations are real, the dependence to the SZA is observed (Wunch et al., 2011a).

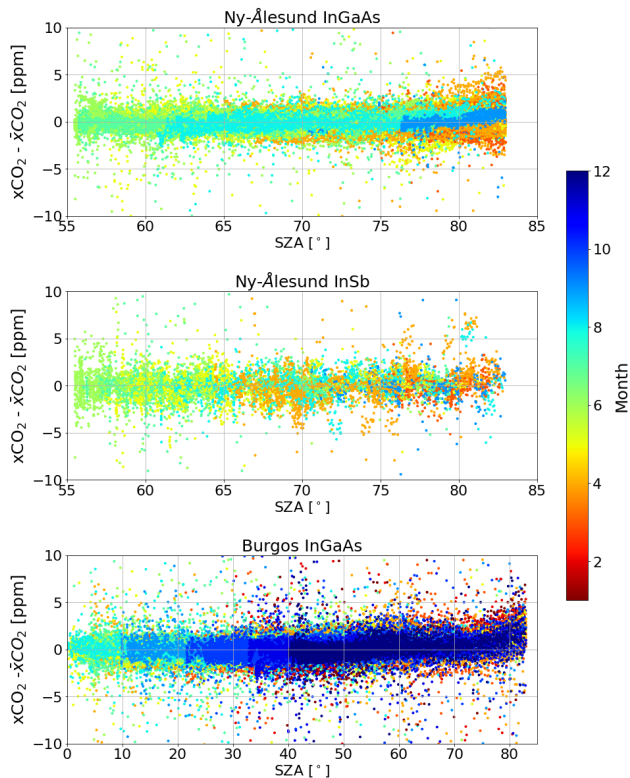


Figure 4. Top: Ny-Ålesund w4790 InGaAs (2016-2018) xCO₂ minus the daily mean. Middle: Ny-Ålesund w4790 InSb (1997-2018) xCO₂ minus the daily mean. Bottom: Burgos w4790 InGaAs (2017-2018)xCO₂ minus the daily mean.

200 For w4790 InGaAs, we can see that there is an increase of the scattering of xCO₂ in SZA larger than 75° for Ny-Ålesund. Some values can be approximately 1% larger at 83° than at SZA lower than 75°, others remain within the range ± 2 ppm. w4790 InSb seems to remain mostly unchanged for the SZA range (50° to 83°), but there is the possibility that this is due to the low number of data points.

For Burgos increase of all xCO₂ values for SZA larger than 50°, with values around 83° being 1% larger than for SZA values below 50°. This asymmetry around zero indicates an airmass dependence for large SZA. On the other hand we found that for the 6300 window, prior to the airmass correction, the tendency is consistent with the findings of Wunch et al. (2011a) where at lower SZA the values are higher than at high SZA (see figure I6 and I7 in the appendix). This indicates that both retrievals have an airmass dependence, especially for high SZA, but the observed artifacts are different.

4.3 Site to site consistency

210 This sections serves to investigate if the scaling between 6300 and w4790 xCO₂, is consistent between location and to emulate a correction via a scaling factor, a ratio between 6300 and w4790 for each data point was calculated.

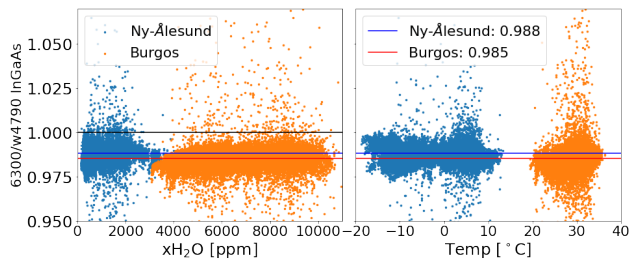


Figure 5. The ratios ($6300 \times \text{CO}_2 / \text{w4790 InGaAs} \times \text{CO}_2$) of Ny-Ålesund (2016-2018) in blue and Burgos (2017-2018) in orange plotted against $x\text{H}_2\text{O}$ on the left and against temperature on the right. The means of the ratio presented as lines, blue for Ny-Ålesund and red for Burgos.

The means of the ratios (shown in figure 5) were calculated with their corresponding standard deviation, these values are presented in table 2. The difference between the ratios' means are within the error, indicating a good consistency between both sites. These values also serve to determine the global scaling factor (GSF) to be applied to both w4790 retrievals shown in section 7. To determine a global SF, all data points from Ny-Ålesund and Burgos were used to calculate the mean. Table 2 shows the values for the ratios and the SF.

Table 2. The ratio means and standard deviations of w4790 InGaAs/6300.

Name	Mean	σ
Ny-Ålesund	0.9880	0.0050
Burgos	0.9852	0.0060
Global Scaling Factor	0.9863	0.0058

220 4.4 Comparison with Aircraft profiles

The airmass-independent correction factor (AICF) (also called in-situ correction) is determined with collocated in situ profiles. The procedure for this comparison is similar to the calibration of TCCON described in Wunch et al. (2010). We also check for correlation between the TCCON - in situ difference and both Xluft and SZA (See supplemental figure I8). Xluft is used to diagnose instrument or retrieval errors, and is calculated as a ratio of two columns of dry air (one derived from surface pressure and the prior H2O profile, and the second derived from the retrieved O2 column). We use this correlation to check how sensitive the w4790 window is to instrument errors. Similarly, we use the correlation with SZA to check whether the airmass correction for this window is likely to be significant..

The correlation between w4790 $x\text{CO}_2$ and in situ $x\text{CO}_2$ shown in figure 6 right plot shows a good performance of w4790 in the sites evaluated. The correlation coefficient R^2 is 0.9995.

230 The w4790 has a slightly larger scatter and stronger relationship between Xluft and the bias vs. in situ $x\text{CO}_2$ than the TCCON 6300 windows. This means that if xluft deviates much from the nominal 0.999 value, there will be an increased bias in $x\text{CO}_2$

(see figure 6 center plot). There is a weak correlation between the bias and the SZA (see Fig 6 right plot). The variation with SZA is smaller than the scattering, therefore the lack of airmass correction is a minor component. The higher scatter is to be expected as the w4790 has higher sensitivity towards the surface and this might be driven by the surface variability of CO₂, that aircrafts and balloons can't capture, in addition to the temperature sensitivity of the window. These features make the w4790 single data point uncertainties larger than those of 6300.

The mean ratio between w4790 xCO₂ and in situ xCO₂ is 1.01 for the 6300 windows and 1.005 for w4790 window suggesting that the line strengths in the 6300 windows are biased lower than in the w4790. For the 6300 window, this bias is removed by the in situ correction. Likewise, we will similarly apply an in situ correction for the w4790 derived from this analysis. Additionally, while the correlation between the bias and SZA in Fig 6 right plot is small, we will derive an airmass-dependent correction factor for the w4790 xCO₂ in the future to remove this small dependence.

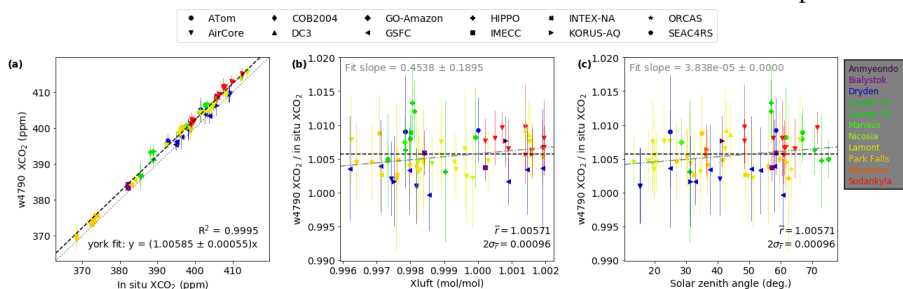


Figure 6. Left: Correlation between w4790 xCO₂ and in situ xCO₂. Centre: Ratio of w4790 xCO₂ window / in situ xCO₂ against xluft between 0.996 and 1.002. Right: Ratio of w4790 xCO₂ window / in situ xCO₂ against solar zenith angle.

5 Error Analysis

In this section we will look into the systematic and random errors of this retrieval. This analysis was performed on filtered data as described in section 2.3. A total of 3304 data points for InGaAs were flagged and removed, leaving 46307 usable points. For InSb 121 data points were flagged and removed, leaving 1115 usable data points. In total, less than 10% of the original data points were filtered out.

As described by equation 4, an error weighted standard deviation of the daily mean, σ_{day} was calculated for the years presented in the previous sections. To evaluate the distribution of σ_{day} , we will list below which value 95% of σ_{day} (2 standard deviations) are for each location and retrieval. For 6300, 95% of σ_{day} are below 1.5 ppm for Ny-Ålesund and below 2 ppm for Burgos. For w4790 InGaAs, over 95% of the error σ_{day} are below 2 ppm for both locations. For w4790 InSb, around 95% are below 2.75 ppm. The σ_{day} is larger for w4790 InSb, but one thing to consider is the difference in number of data points between InSb and InGaAs that affects the standard deviation. For this reason the standard error was also calculated (shown in table 3) to have a representation of mean error.

Table 3. Estimated errors for the retrievals, the mean of the absolute value of the diurnal variation, DV; the mean standard deviation, σ ; and the standard error, σ/\sqrt{N} , of the daily means of Burgos (2017 and 2018) and Ny-Ålesund (2016-2018)

Location	Retrieval	DV[%]	σ_{day} [ppm]	σ_{day}/\sqrt{N} [ppm]
Ny-Ålesund	w4790 InGaAs	0.182	1.041	0.167
	w4790 InSb	0.103	1.472	0.893
	6300	0.085	0.601	0.105
Burgos	w4790 InGaAs	0.214	1.195	0.128
	6300	0.140	0.628	0.109

255 5.1 Diurnal variations

The precision of the column-averaged dry air mole fraction is estimated from its diurnal variation (Yang et al., 2002), see equation 5 for definition. Part of the diurnal variation (DV) is caused by the real variations in the atmospheric $x\text{CO}_2$, dependent on the local natural diurnal cycles, while the other part are the errors, therefore this method gives an upper limit for the precision. However this strategy was still chosen as, due to the small amount of data points of InSb spectra, it is the shorter time period to
 260 make a meaningful average.

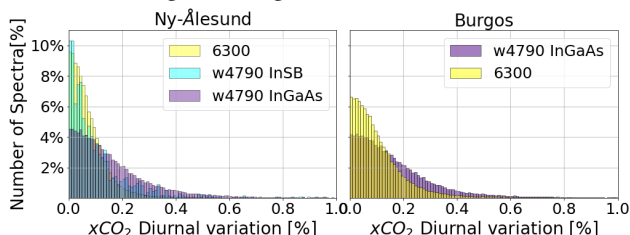


Figure 7. Histograms of the diurnal variations, Ny-Ålesund on the left and Burgos on the right.

The diurnal variations follow a similar pattern for all InGaAs retrievals, following a normal distribution. However, w4790 InSb looks different than the rest. For w4790 InGaAs, 95% of the diurnal variations are below 0.384% in Ny-Ålesund and 0.425% in Burgos, while for w4790 InSb 95% are below 0.246%. The fewer amount of data points measured per day for InSb might
 265 explain why the DV extends to 1%. There is a total of less than 500 data points for the three years for InSb, while there are over 4600 InGaAs data points for the same three years. For 6300, 95% of the diurnal variations are below 0.103% in Ny-Ålesund and 0.247% in Burgos. As we saw in section 5, the retrievals for w4790 have more scattering than 6300, this can be seen in the diurnal variation as well.

Table 4. The w4790 error budget, in the first column the error source, the second is the magnitude of the perturbation. The last two columns are the average magnitudes of the fractional difference (FD) per perturbation of the retrieved xCO_2 for Ny-Ålesund and Burgos. * Corresponds to the perturbations used for the calculation of the total sum of the squared errors from these sources as similarly performed in Wunch et al. (2011a)

Error source	Magnitude of perturbation	Ny-Ålesund μFD [%]	Burgos μFD [%]
CO ₂ profile*	constant 400ppm	0.0971	0.1067
H ₂ O profile*	-5%	0.0005	0.0081
H ₂ O profile	+5%	-0.0005	-0.0077
Temperature profile*	-1°C	-1.5762	-1.3501
Temperature profile	+1°C	1.5438	1.3678
Surface pressure*	-0.1%	-0.1102	-0.1148
Surface pressure	+0.1%	0.1101	0.1144
Time*	-10s	-0.0120	-0.0183
Time	+10s	0.0119	0.0185
Total = $\sum_{n=5} \mu FD^*$ ²	-	2.5061	1.8477

5.2 Perturbations of potential error sources

- 270 This subsection presents a sensitivity study of the w4790 xCO_2 retrieval, where several retrieval input parameters were perturbed by a realistic amount following a similar method to Wunch et al. (2011a). For the InGaAs tests, Burgos spectra were used and for the InSb tests, Ny-Ålesund spectra were used. The quantities are listed in table 4 followed by the average of each of the perturbations for each site. All tests, except for the CO₂ a priori profile, were performed with positive and negative perturbations (i.e. +5s and -5s), this is to evaluate if they behave in a symmetric way.
- 275 The perturbations were performed by slightly modifying variables in different retrieval steps. Two perturbations were done by multiplying, adding or subtracting from the whole profile in the a priori input files. The H₂O profile was multiplied by 1.05 or 0.95 and the temperature profile $\pm 1^\circ C$ was added. The CO₂ perturbation was done by replacing the a priori profile with 400 ppm for all layers. For pressure, the measured surface pressure (*pout*) was multiplied by 1.0001 or 0.9999. Lastly, time of measurement was perturbed by adding $\pm 10s$. Then the output of each perturbed retrieval was evaluated against the
- 280 unperturbed case by calculating the fractional difference (FD) with the following formula:

$$FD = 100 \times (xCO_2^{unp} - xCO_2^p) / xCO_2^{unp} \quad (7)$$

Where xCO_2^{unp} is the unperturbed total column and xCO_2^p is the perturbed total column.

The w4790 retrieval is more sensitive to pressure perturbations than TCCON, which is expected, as it makes use of pressure in the calculation of the dry-air mole fraction. For TCCON the pressure error (-0.1% profile perturbation) is -0.036 at SZA 20°

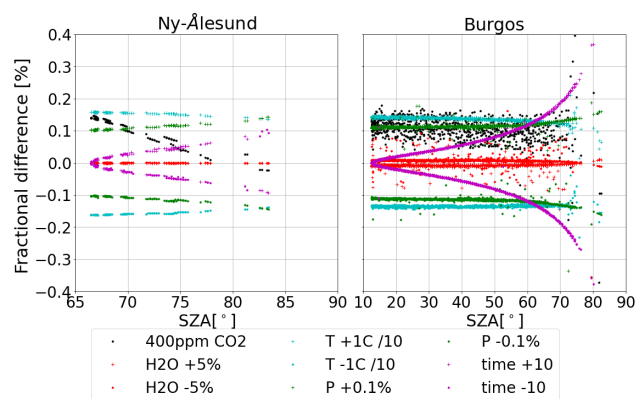
285 and -0.033 at SZA 70° (Wunch et al., 2011a). From Wunch et al. (2011a) we know that the largest errors for xCO₂ computed using surface pressure are zero-level offsets, surface pressure errors and Sun Tracker pointing errors and that those are larger compared to using CO₂/O₂. This is consistent with the findings of the perturbation tests performed for this study.

Along with pressure, as mentioned in previous sections, the temperature sensitivity of w4790 is also an important source of error. Ny-Ålesund and Burgos temperatures perturbations behave symmetrically and are the largest source of error. The
 290 negative perturbation's mean is -1.5%/K and the positive perturbation's mean is 1.5%/K.

The time perturbations have both, positive and negative effects depending on the time of the day. For the +10 s case, the effect is a negative bias in the morning and a positive error in the afternoon. The opposite happens in the -10 s case. Both intersect at the zero line at the minimum SZA of the day. This behaviour was expected due to the nature of the SZA and time corrections observed in spectroscopy gas retrievals. The results of the perturbations of pressure and H₂O that have both positive and
 295 negative magnitudes behave symmetrically. For pressure, a perturbation of +0.1% generates a negative difference on the xCO₂ retrieval of approximately -0.1% and vice-versa, for both Burgos and Ny-Ålesund. For H₂O, the smallest of all perturbations, a positive perturbation also causes a negative difference in the xCO₂ retrieval. However, the magnitude of the difference, is larger in Burgos than in Ny-Ålesund. This is to be expected, given that the atmospheric water content in Burgos is larger.

For the perturbations of xCO₂ a priori profile, we have a different effect in both locations. For Burgos, a constant a priori, causes an offset of less than 0.1%. But for Ny-Ålesund, the effect is SZA dependent, having the largest difference (-0.122%)
 300 at the largest SZA during the morning. Then it decreases, crossing zero at 65° and at mid day, when the SZA is the smallest (~ 60°), the difference is positive (~0.05%). Finally, at the end of the day, the difference is negative once again.

The total average error caused by all the four sources is calculated by adding the square of the mean of the negative perturbations (denoted by * in the table 4), resulting in 2.5% for Ny-Ålesund and -1.8% for Burgos.



305

Figure 8. Fractional difference of perturbations (CO₂ a priori profile, H₂O a priori profile, surface pressure, time and temperature/10 a priori profile) in % of the retrieved CO₂ for Ny-Ålesund (InSb) on the left and Burgos (InGaAs) on the right. Remark: the values for the temperature perturbations are divided by 10 to fit in the plot range.

6 xCO₂ time series

In this section the time series is presented, for historical data in Ny-Ålesund from 1997 to 2018. There are some spectra recorded since 1992, however, the specific filter used was installed later.

The data was processed, filtered, scaled and the daily mean calculated, for all three retrievals. Comparing the w4790 xCO₂ to the 6300 xCO₂ for the overlapping time will show how well the seasonality is represented as well as the scattering in comparison to the 6300 window.

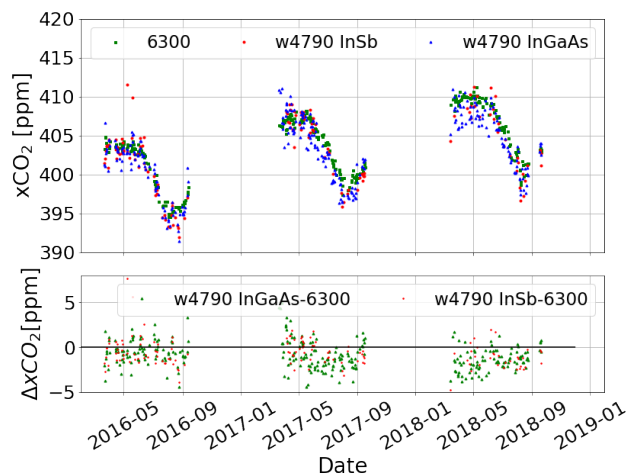


Figure 9. Ny-Ålesund weighted daily mean of w4790 InGaAs (in blue triangles) and w4790 InSb (in red dots) xCO₂ compared with the daily means of 6300 (in green squares) xCO₂ for the overlapping years. In the bottom the difference between w4790 InGaAs and 6300 (in green triangles) and Insb and 6300 (in red dots).

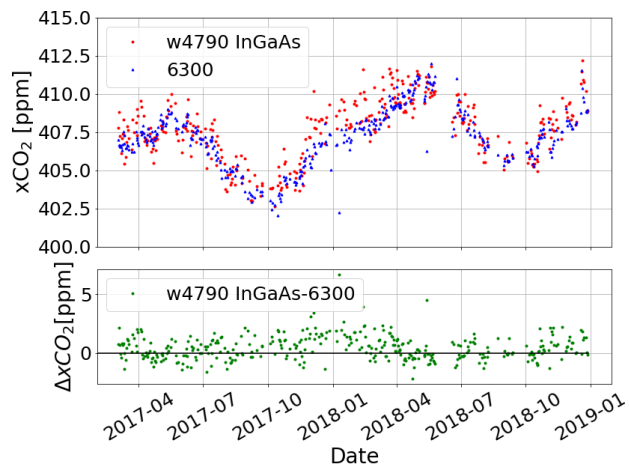


Figure 10. Burgos weighted daily mean of w4790 InGaAs xCO₂ (in red dots) compared with the daily means of 6300 xCO₂ (in blue triangles) and difference (in green) between them on the bottom

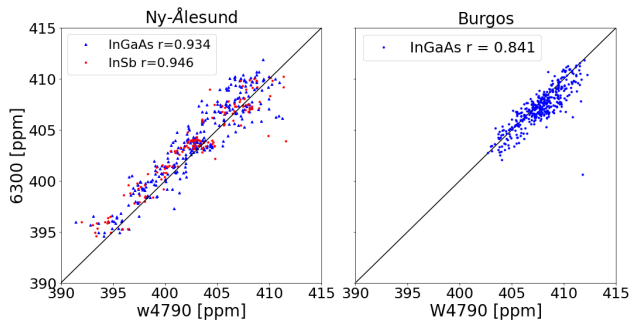


Figure 11. On the left, the correlation between w4790 and 6300 $\times\text{CO}_2$ for the overlapping years in Ny-Ålesund. In blue triangles w4790 InGaAs and 6300 $\times\text{CO}_2$ daily means and in red dots w4790 InSb and 6300 $\times\text{CO}_2$ daily means. On the right, the correlation between the weighted daily mean of w4790 InGaAs $\times\text{CO}_2$ and the daily means of 6300 $\times\text{CO}_2$ for Burgos.

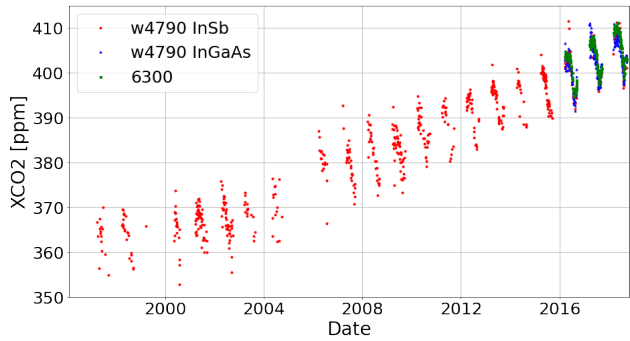


Figure 12. Ny-Ålesund weighted daily mean of w4790 InSb $\times\text{CO}_2$ (in red dots) for time series of all spectra available and weighted daily mean of w4790 InGaAs (in blue triangles) and the daily means of 6300 (in green squares) for the three overlapping years.

We can see that the $\times\text{CO}_2$ retrieved from w4790 can reproduce the seasonal cycle with the same amplitude of 10 ppm successfully. However, the w4790 $\times\text{CO}_2$ data points show more scattering than the 6300 $\times\text{CO}_2$, this is due to the influence of the averaging kernels as is addressed in the Appendix.

320 In Ny-Ålesund the recorded data covers March to October. During this period the solar zenith angle range changes. At the peak of summer the smallest SZA is around 55° and during March and October the smallest SZA is around 73° . This means a difference in the minimum SZA of 18° . Given that the maximum SZA in the datasets is 83° , the range of SZA during Spring and Autumn is quite limited. We observe in figure 9 that the difference between w4790 InGaAs and 6300 changes during the year, being higher for Spring and Autumn than for the peak of summer. Taking into account section 4.2 and the lack of air mass
 325 correction for both data sets, the changes in range of the solar zenith angle can be responsible for this observed characteristic. The mean of the difference between w4790 InGaAs and 6300 is -0.895 ppm with a standard deviation of 1.513 ppm. The mean of the difference between w4790 InSb and 6300 is -0.620 ppm with a standard deviation of 1.516 ppm.

In Burgos, where the seasonal cycle includes a dry (October to May) and a rainy season. The behaviour of its seasonality ,
330 unlike Ny-Ålesund's, can not be fitted to a cosine curve. In Burgos, like in Ny-Ålesund, there is a change in SZA depending on
the month, but larger. Around December the smallest SZA is around 40° while for June it reaches 0° , resulting in a difference
in the minimum SZA of 40° , twice that of Ny-Ålesund. This means the dry season contains data with a smaller range of SZA
than the wet season. We can observe that the scattering is larger during the first three months of 2018, corresponding to the dry
335 season. Lastly, the scattering of both w4790 and 6300 is larger for the last two months of 2018 (see figure 10). This is similar
to what is observed in Ny-Ålesund, where periods with smaller SZA range have a higher w4790 InGaAs - 6300 difference.
This can also be due to a different sensitivity towards the surface and to thin clouds. The mean of the difference between
w4790 InGaAs and 6300 is 0.456 ppm with a standard deviation of 1.014 ppm.

There are several InGaAs measurements per day performed for TCCON, while there are only a couple of InSb NDACC
340 measurements per filter per day. This influences the scattering of the InSb data points to the fitted curve. There are several years
that there is very little data points or none. In 2005 and 1999 there were technical difficulties with the instrument, therefore
those years have one or no data points. The low number of measurements per year make the InSb product very sensitive to thin
clouds. All spectra with cloud contamination have been filtered out.

The correlation coefficients r between the daily means of w4790 and 6300 (figure 11) are 0.934 for Ny-Ålesund InSb, 0.946
345 for Ny-Ålesund InGaAs and 0.841 for Burgos.

7 Retrieval strategy suggestion

Here we present recommendations on the set up for the acquisition of spectra to perform a $x\text{CO}_2$ from the 4800 cm^{-1} region.
There are eight standard filters used by NDACC to acquire spectra in different regions (Blumenstock et al., 2021), but there
are several other filters available for use. In Ny-Ålesund the non-standard NDACC filter 4433 has been used since 1997 and in
350 Bremen another non-standard filter, 4825, that covers 4570 to 5080 cm^{-1} is used. Both filters have a good transmission in the
region of the w4790 window (see Appendix figure C3 and C4). For the 4433 filter the w4790 window is located near the end of
the filter range but still above the 50% cut-off. Both filters have been tested for the retrieval and we can confidently recommend
either.

Similarly to the protocols of NDACC, a KBr or CaF_2 beam splitter that covers the spectral range can be used for acquisition
355 (<https://ndacc.larc.nasa.gov/data/protocols/appendix-ii-infrared-ftir>).

Different resolutions were tested with sample sets of InSb spectra measured in Bremen, March 2021, and used with the MIR
 $x\text{CO}_2$ retrieval. Lowering the resolution from 0.005 cm^{-1} to 0.02 cm^{-1} was found to have a negligible effect on the individual
data points, while a larger number of measurements gives a higher temporal resolution and improves the precision of the
retrieval as an average of more measurements bet down the noise. Lower resolutions didn't show further benefit on the precision
360 and very low resolution affects the retrieval as the spectral line shape is not resolved sufficiently. Furthermore, lower resolution
allows for faster measurements therefore more measurements which allow better performance in cloudy conditions. Given that

the retrieval works just as well at a TCCON resolution of 0.02 cm^{-1} (OPD 45 cm), we recommend this resolution as to increase the data points collected.

To keep temperature errors low the understanding and representation of the atmospheric temperature profile should improve (as seen section 5.2) and use data when a smoothed xluft mean is between 0.996 and 1.002 (as seen in section 4.4). The input file where the spectral parameters to be fitted in GFIT are listed, known as the window file w4790.gnd, is shown in Appendix A.

8 Conclusions

This study showed that it is possible to successfully retrieve the dry-air mole fraction $x\text{CO}_2$ from InSb NDACC spectra and from InGaAs TCCON spectra in the spectral window w4790. The averaging kernels show high sensitivity towards the surface. The retrieval proved to not have a big dependence on the a priori to correctly represent the daily and seasonal cycles (with correlation coefficients of at least 0.980 for all 3 retrievals). This is an improvement from Buschmann et al. (2016) where the averaging kernels limited the sensitivity making the retrieval highly dependent on the a priori. The retrieval also proved useful to retrieve daily and subdaily values, which is a different goal and purpose of Barthlott et al. (2015) study. However, the w4790 InGaAs and the 6300 $x\text{CO}_2$ both have an airmass dependence. For w4790 InGaAs, the values at larger SZA increase, while for 6300 it decreases. Additionally, w4790 retrievals are temperature dependent and will require very accurate temperature measurements. Temperature is the largest error source with $\pm 1.5\%/K$ followed by pressure with $\pm 0.11\%$ for $\pm 0.1\%$ error in the pressure measurement.

We showed that the $x\text{CO}_2$ product from w4790 InGaAs is site consistent and has a global scaling factor (GSF) to the 6300 $x\text{CO}_2$ product of 0.9863 ± 0.0058 . That GSF was used for both time series and the corresponding correlations. The time series shown for the daily means show a good agreement between 6300 and w4790 (InGaAs and InSb) with a larger scattering for w4790 caused by the influence of the averaging kernels (see Appendix) and possible temperature inconsistencies.

The errors for w4790 retrievals are larger than 6300 for σ_{day} and $\frac{\sigma_{day}}{\sqrt{N}}$ but of similar magnitude for the diurnal variation (DV). In agreement with the findings by Wunch et al. (2011a), the retrieval is most sensitive to pressure perturbations, which will require to have well calibrated pressure sensors. Implementing the new suggested setup for current and new NDACC measurement sites will provide valuable additional information on the carbon cycle.

Appendix A: The window fitting parameters

These are the contents of the window file w4790.gnd used as input in the GFIT software specifying which windows will be used, their centre and width, the gases to retrieve from each window and other parameters. The O₂ line is commented out but can be used if the spectra include it.

2 2

Center	Width	MIT	A	I	F	Parameters to fit	Gases to fit
4555.00	0.12	0	1	1	0		: luft
395 6146.90	1.60	0	1	1	0		: luft
4565.20	2.50	15	1	1	0	cl ct fs so	: h2o co2 ch4
4570.35	3.10	15	1	1	0	cl ct fs so	: h2o co2 ch4
4571.75	2.50	15	1	1	0	cl ct fs so	: h2o co2 ch4
4576.85	1.90	15	1	1	0	cl ct fs so	: h2o ch4
400 4790.60	20.00	20	1	1	0	cl ct cc fs so	: co2 h2o hdo ch4 n2o
: 7885.00	240.00	15	1	1	0	cl ct fs so	: o2 0o2 h2o hf co2

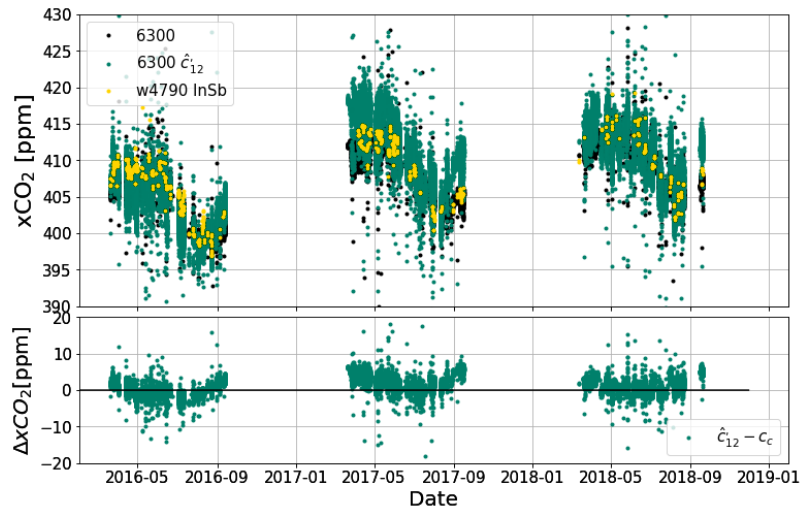
Where MIT is the maximum number of iterations, A is apodization, I is interpolation, F is frequency reference frame (0=instrument, 1=sun). The parameters to fit: cl is continuum level, ct is continuum tilt, fs is frequency shift, so is solar lines and ak is used to generate the averaging kernels which is an optional addition. The gases to fit with the first species being the main species to fit and the following list any interfering species to account in the window.

Appendix B: The effect of the averaging kernels

To evaluate how the averaging kernels (AK) affect the retrieval a smoothing of the 6300 retrieval with the w4790 InSb averaging kernels was done. Using the 1° SZA averaged AK, it was possible to interpolate to the exact solar zenith angle (SZA) of each of the spectra in 6300 and using Eq.(25) from Rodgers and Connor (2003) as done by Wunch et al. (2011b):

$$\hat{c}'_{12} = c_c + \sum_j h_j a_{1j} (\gamma x_c - x_c) \quad (\text{B1})$$

where \hat{c}'_{12} is the smoothed total column, InSb = 1 and 6300 = 2, h_j is the pressure weighting, a is the averaging kernels from the InSb spectra, γ is the 6300 scaling factor applied to the a priori profile, x_c , to get the final 6300 profile that then is integrated to produce the total column \hat{c}_2 (Wunch et al., 2011b).



415

Figure B1. The comparison of $x\text{CO}_2$ from 6300 in black, under the 6300 smoothed with the InSb averaging kernels in green and in yellow, the InSb w4790. Bottom panel is the difference between the 6300 smoothed \hat{c}'_{12} and the 6300 $x\text{CO}_2$ \hat{c}_2 .

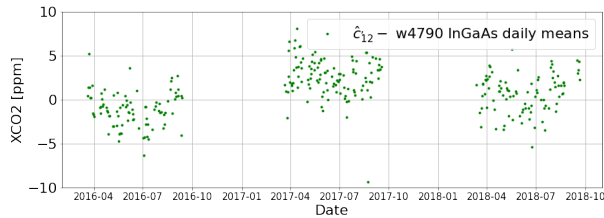


Figure B2. The smoothed TCCON \hat{c}'_{12} daily mean minus w4790 InSb daily mean.

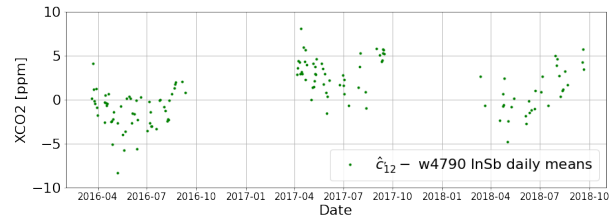


Figure B3. The smoothed TCCON \hat{c}'_{12} daily mean minus w4790 InGaAs daily mean.

This comparison was chosen over using aircraft profiles due to availability. Aircraft profiles are scarce and do not cover a broad range of weather conditions nor the variation with SZA. Hence a comparison with aircraft would have been very limited.

Appendix C: The filters and their spectra

420 Here we show the measurement of solar spectra with each of the filters. The first is the NDACC 4433 used in Ny-Ålesund, the second is the 4750 filter used in Bremen. The signal to noise ratio (SNR) for a single InGaAs spectra in Ny-Ålesund is around 140 (calculated as an average of 21.03.2017 measurements) and in Bremen is also around 140 (calculated as an average of 16.01.2020 measurements). The SNR for NDACC is 536.5 (derived from the residuum of the spectra in Figure 1).

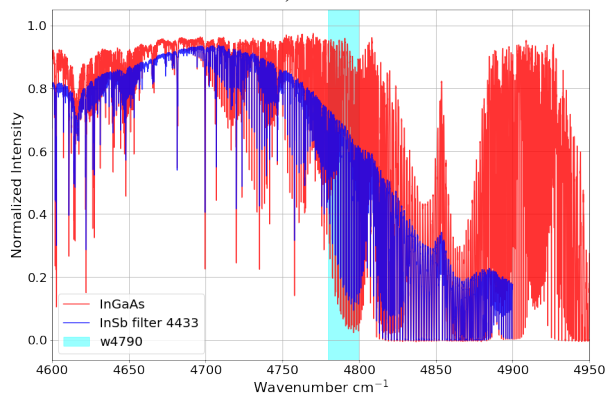


Figure C1. Sample solar spectra for InGaAs (in red) and InSb using the filter 4433 (in blue). Both spectra collected in Ny-Ålesund.

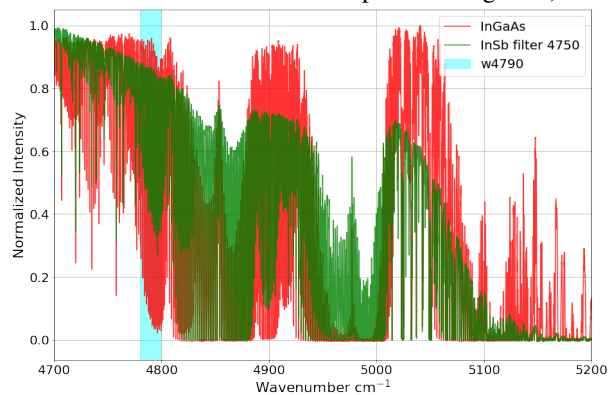


Figure C2. Sample solar spectra for InGaAs (in red) and InSb using the filter 4750 (in green). Spectra collected in Ny-Ålesund and Bremen.

425 The transmission curves for both filters.

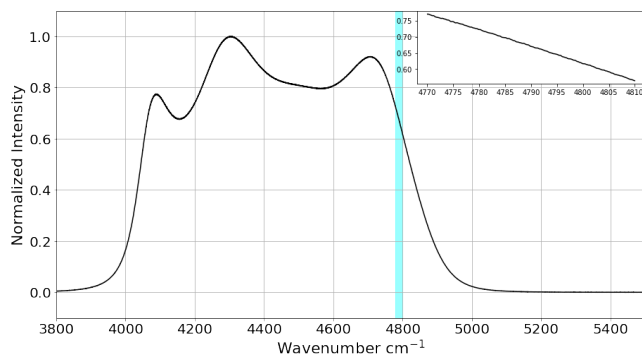


Figure C3. The transmission curve for the filter 4433 and a zoom in for the w4790 window.

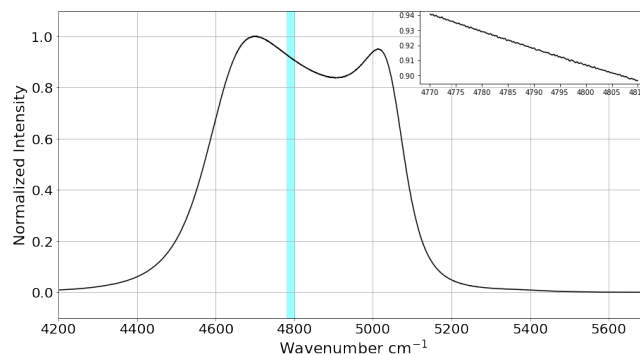


Figure C4. The transmission curve for the filter 4750 and a zoom in for the w4790 window.

Appendix D: Reduced resolution tests

In this section we show the results of the resolution tests performed in three clear days in Bremen using the 4750 cm^{-1} filter, 2nd of March 2021 for the first test shown in Fig D1 and 26th and 28th of April 2021 for the test shown in Figure D2. On

430 the first day, four different resolutions where measured, the controls: TCCON (reference) with optical path difference (OPD) = 68.3 cm (in black), the original NDACC OPD of 180 cm (in red), then the tests, 90.01 cm, 64.3 cm, and 45.01 cm (in blue). On the second and third day, lower resolutions where measured, 18.01 cm, 12.01 cm, 9.01 cm, 6.01 cm, 4.51 cm, 3.01 cm 2.26 cm and 1.81 cm (in green) with the corresponding controls, NDACC and TCCON.

The strategy on the first day consisted of 15 minutes of measurements of each resolution and alternate two measurements of TCCON (in red) every 30 minutes as control. In total, four rounds of measurements were performed. The figure below is showing the mean (black dot) and the measurements (smaller color dots) and the variation of each set of measurements.

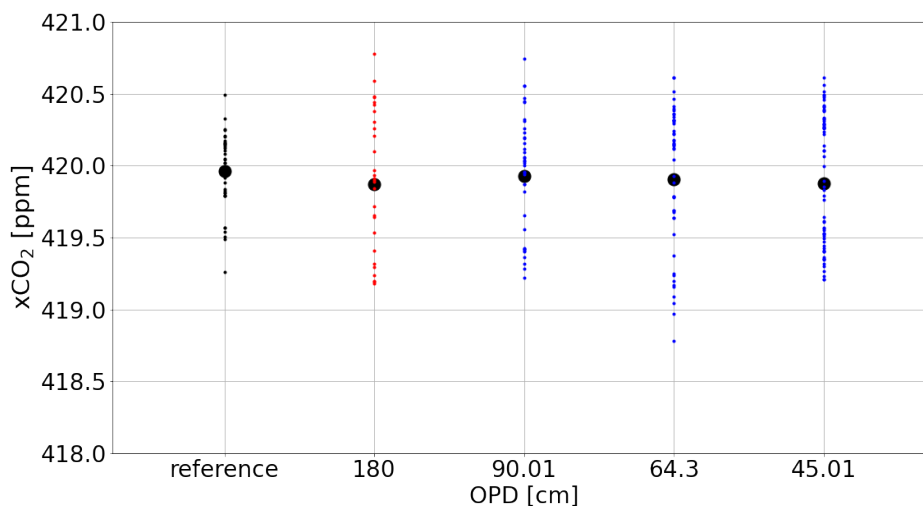
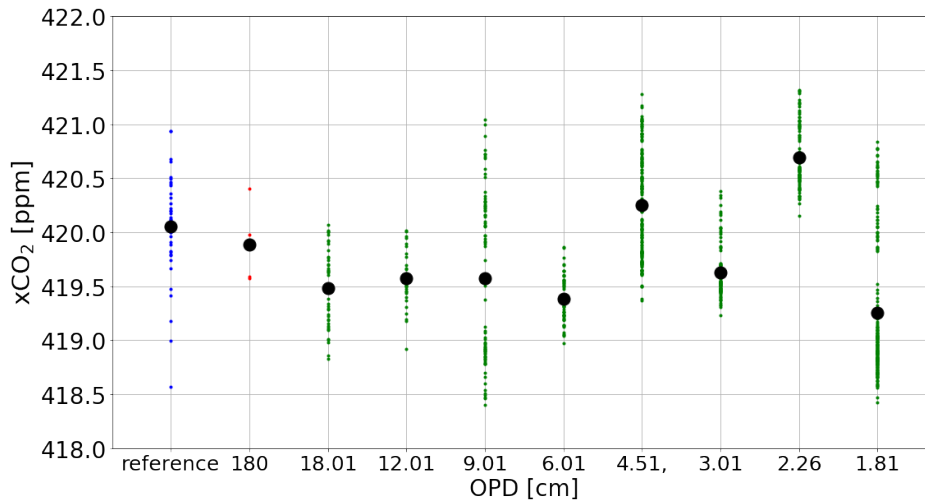


Figure D1. The variation on xCO₂ of the resolution test by OPD for the higher resolutions tested. In black is the reference spectra, xCO₂ retrieved from 6300 with the standard TCCON resolution of 45 cm. In red is the standard NDACC resolution of 180 cm, then in blue the test resolutions, for InSb spectra, of 90cm, 63 cm and 45 cm

The lower resolution tests, performed in two days, with more random alternations, but covering at least 15 minutes of measurements. The control TCCON measurements are performed at the beginning, in the middle and end of the other measurements.



440

Figure D2. The variation on $x\text{CO}_2$ of the resolution test by OPD for the lower resolutions tested. In blue is the reference spectra, $x\text{CO}_2$ retrieved from 6300 with the standard TCCON resolution of 45 cm. In red is the standard NDACC resolution of 180. Then in green the resolution tests for InSb spectra.

In Fig D1 in the 64 cm OPD there are a few outliers. This is seen below the 419 ppm line for resolution 64.3 that has the lowest values from the rest of the tests.

The goal is to find the optimal resolution to improve the precision of the retrieval without compromising other aspects. An OPD lower than 45 cm doesn't significantly decrease the standard deviation of the mean from increased the number of measurements, therefore we see no advantage in using lower resolutions. At the same time 45 cm results in a well resolved spectral fit, while a lower resolution starts to misrepresent the actual spectral lines.

445

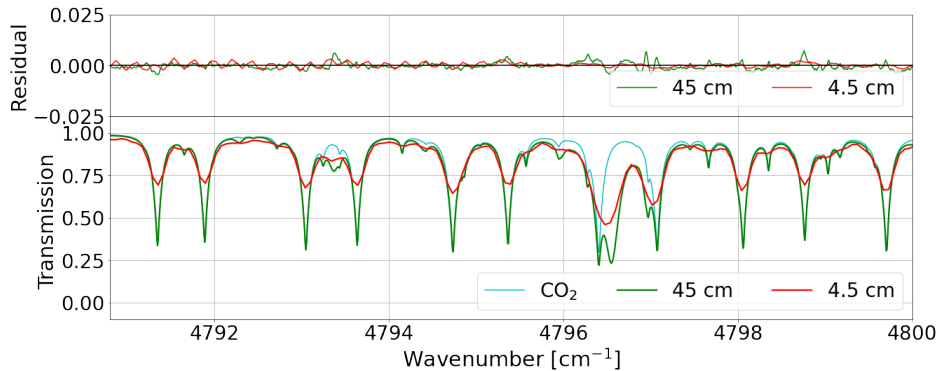
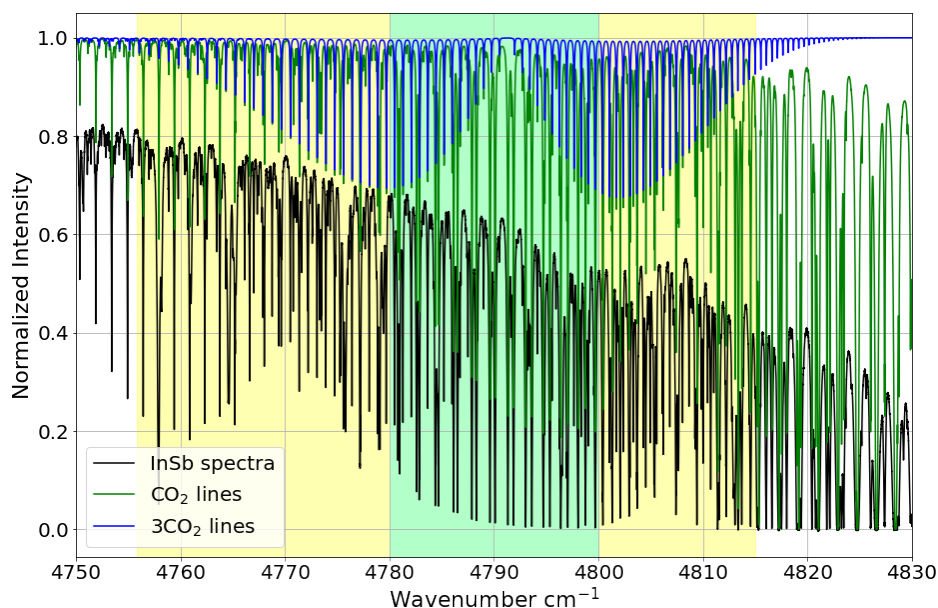


Figure D3. Spectral fit and residuum of spectra of different resolution. In green the calculated spectra (TM) with OPD 45 cm and in red the calculated spectra (TM) with OPD 4.5 cm, in cyan, the CO_2 absorption lines

Appendix E: Temperature dependence and alternative retrieval

As mentioned in section 2.2 the band chosen is a "hot" band, which makes the retrieval temperature dependent. With a lower mean energy level $E'' = 858 \text{ cm}^{-1}$ the estimated theoretical error for a 2 K error in temperature is between 1.2 to 1.8% of the retrieved $x\text{CO}_2$.

One alternative window considered for this retrieval was to use the third isotope $^{16}\text{O}^{12}\text{C}^{18}\text{O}$ (named 3CO_2 by HITRAN) in the same region as shown in figure E1, in yellow. Using the 3CO_2 band would yield a less temperature dependent product, because it has a lower mean energy level, $E'' = 217 \text{ cm}^{-1}$.



455

Figure E1. Spectra and spectral lines, in black a sample InSb spectra, in green the FTIR-atlas CO_2 lines and in blue 3CO_2 . Two windows shown, in green the original w4790, and in yellow the alternative window to use 3CO_2 .

However, tests showed that due to the averaging kernels low sensitivity towards the surface, the retrieval doesn't capture the seasonal cycle properly and is heavily dependent on the a priori. This alternative brings benefits as it captures the stratosphere, however, there is an offset to be calculated that is possibly due to GFIT's assumed isotopic fractionation, which can be easily corrected for.

460 **Appendix F: Pressure dependence and the pressure sensor**

The pressure sensor used in Ny-Ålesund is the Digiquartz 6000-16B barometer with an accuracy of ± 0.08 hPa. This sensor is not re-calibrated regularly. Single comparisons to other sensors have been performed and the difference was within the error of both instruments. The pressure sensor used in Burgos is the Setra270-12V range 800-1100 hPa with an accuracy (at constant temp) of $\pm 0.05\%$ FS. This sensor was compared twice since 2017. Once in September 2017, against Japan's CS106, the
465 difference was within the sum of the precisions, no calibration was needed. In November 2023 the differences against PTB330 from Japan were again within the sum of the precisions, but 0.041 hPa were added to Setra 270 as offset.

We suggest to calibrate the sensor biannually or more frequently to avoid drifts. Drifts in the pressure measurements could introduce a retrieval, this would affect the $x\text{CO}_2$ retrieved from w4790 while it would not affect the $x\text{CO}_2$ retrieved from TCCON the pressure cancels out due to the use of O_2 .

Table G1. The mid-IR line list used in this study. Each line is characterized by the center wavenumber. Additionally, the corresponding molecular transition for the quantum numbers $\nu_1\nu_2l_2\nu_3n$ is given. Where three of these, ν_1, ν_2, ν_3 , express the number of quanta activated for each fundamental; l_2 is the l value for the degenerate ν_2 fundamental and its overtones; the fifth integer is the n th component of the Fermi interacting ν_1 and $2\nu_2$ vibrational states including their overtone and combination states) (Toth et al., 2008) Data taken from the TCCON GGG2020 linelist, adapted from HITRAN (Rothman et al., 2009).

Center [cm ⁻¹]	Line intensity	Quantum Transition [cm ⁻¹ (moleculecm ⁻²)]
4780.99	5.583×10^{-24}	2 1 1 13 → 0 1 1 01
4782.86	6.534×10^{-24}	2 1 1 13 → 0 1 1 01
4784.70	7.498×10^{-24}	2 1 1 13 → 0 1 1 01
4786.15	8.615×10^{-24}	2 1 1 13 → 0 1 1 01
4786.53	8.431×10^{-24}	2 1 1 13 → 0 1 1 01
4787.90	9.616×10^{-24}	2 1 1 13 → 0 1 1 01
4789.63	1.050×10^{-23}	2 1 1 13 → 0 1 1 01
4790.12	9.994×10^{-24}	2 1 1 13 → 0 1 1 01
4791.35	1.120×10^{-23}	2 1 1 13 → 0 1 1 01
4791.89	1.051×10^{-23}	2 1 1 13 → 0 1 1 01
4793.05	1.166×10^{-23}	2 1 1 13 → 0 1 1 01
4793.64	1.079×10^{-23}	2 1 1 13 → 0 1 1 01
4794.42	6.197×10^{-25}	3 0 0 14 → 1 0 0 02
4794.73	1.180×10^{-23}	2 1 1 13 → 0 1 1 01
4795.36	1.078×10^{-23}	2 1 1 13 → 0 1 1 01
4796.40	1.158×10^{-23}	2 1 1 13 → 0 1 1 01
4797.05	1.193×10^{-24}	2 0 0 13 → 0 0 0 01
4797.07	1.044×10^{-23}	2 1 1 13 → 0 1 1 01
4797.45	1.015×10^{-24}	3 0 0 14 → 1 0 0 02
4798.06	1.097×10^{-23}	2 1 1 13 → 0 1 1 01
4798.77	9.756×10^{-24}	2 1 1 13 → 0 1 1 01
4798.95	1.158×10^{-24}	3 0 0 14 → 1 0 0 02
4799.17	1.817×10^{-24}	2 0 0 13 → 0 0 0 01
4799.70	9.933×10^{-24}	2 1 1 13 → 0 1 1 01
4800.43	1.258×10^{-24}	3 0 0 14 → 1 0 0 02
4800.44	8.634×10^{-24}	2 1 1 13 → 0 1 1 01

Appendix H: TCCON's ICO_2 window

TCCON is working on a new window in the same region centred at 4852.87 cm^{-1} and of 86.26 cm^{-1} width that uses the same band to retrieve CO_2 . The ICO_2 window, was not developed with the same purposes w4790 was developed, therefore, it is not ideal for retrieving historical NDACC spectra from Ny-Ålesund as done in this paper because the window is located pass the 475 50% cut off the 4433 filter used there. However, the window would work with TCCON and NDACC spectra with other filters such as 4750 shown in Appendix C.

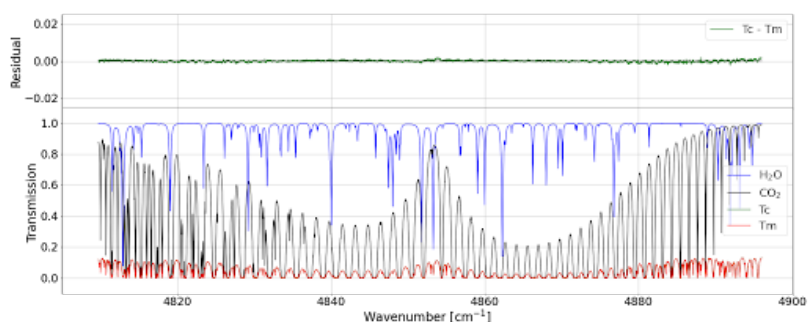


Figure H1. A example of the calculated spectra (Tc) and the measured spectra (Tm) for the LCO_2 window, CO_2 absorption lines, other gases and the residual (Tm – Tc) for a typical spectra recorded in Ny-Ålesund.

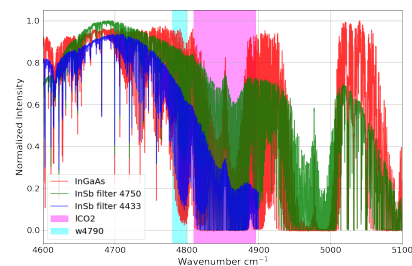


Figure H2. Sample solar spectra for In-GaAs (in red) and InSb using the filter 443 (in blue) and filter 4750 (in green), collected in Ny-Ålesund. LCO_2 window in magenta.

The ICO_2 and the W4970 windows have a large difference in the averaging kernels. ICO_2 AKs have little variation with SZA. For low SZA w4790 is closest to 1 and the largest difference between both windows.

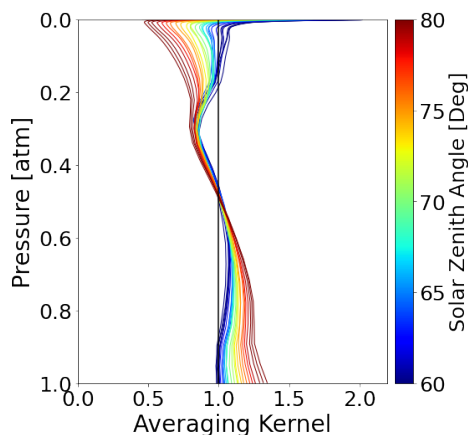


Figure H3. w4790 averaging kernels averaged to 1° for InGaAs Ny-Ålesund.

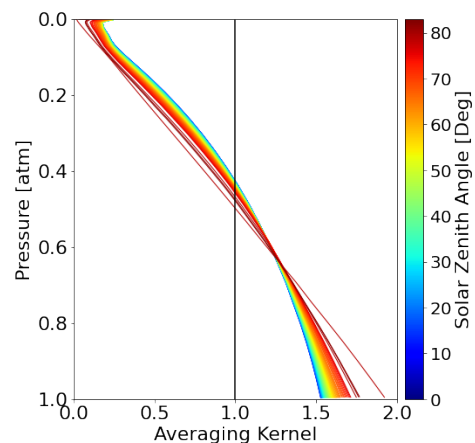


Figure H4. LCO_2 averaging kernels not averaged for InGaAs Ny-Ålesund.

Appendix I: Supplemental plots

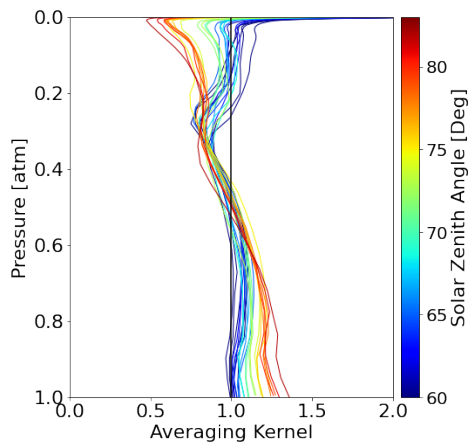


Figure 11. w4790 averaging kernels averaged to 1° for InSb Ny-Ålesund spectra.

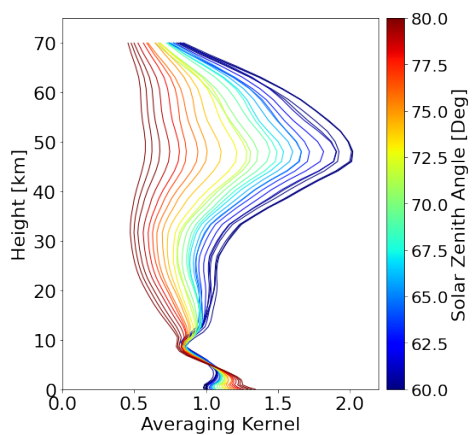


Figure 13. w4790 averaging kernels averaged to 1° SZA for InGaAs Ny-Ålesund spectra plotted against Altitude in Km.

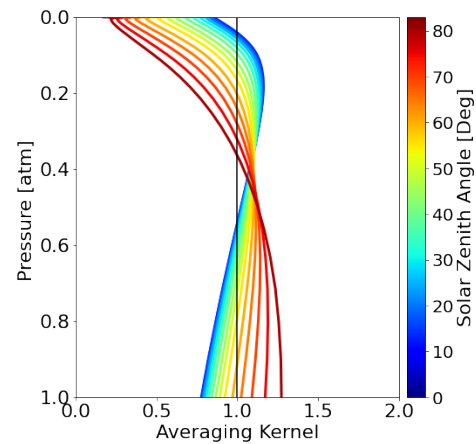


Figure 12. The averaging kernels for the Burgos TCCON product (from ggg2014).

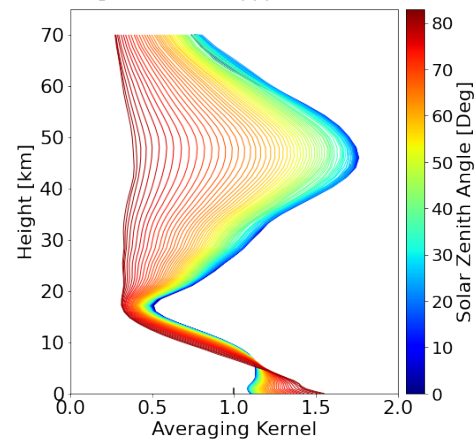


Figure 14. w4790 averaging kernels averaged to 1° SZA for InGaAs Burgos spectra plotted against Altitude in Km.

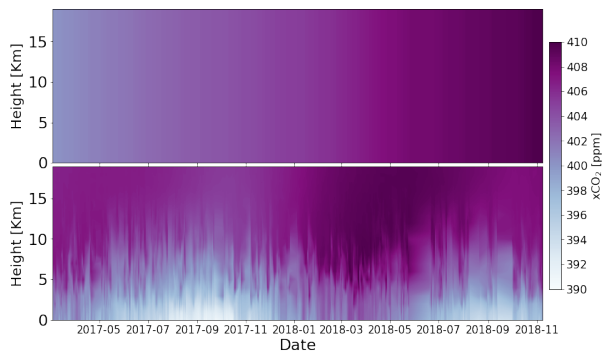


Figure I5. The standard (bottom) and deseasonalized or modified (Top) a priori profiles for Burgos

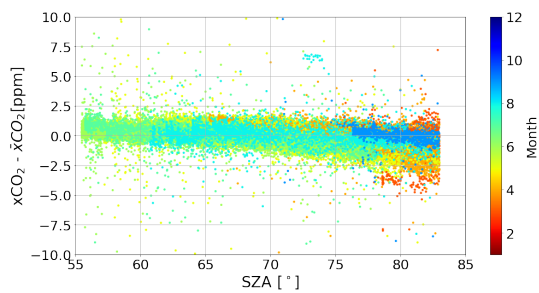


Figure I6. Ny-Ålesund 6300 CO₂, prior to the airmass correction, minus the daily mean of the corresponding month/
485

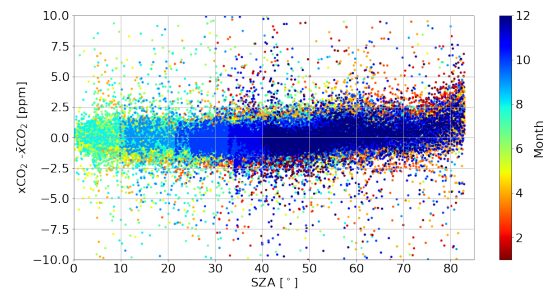


Figure I7. Burgos 6300 xCO₂, prior to the airmass correction, minus the daily mean of the corresponding month.

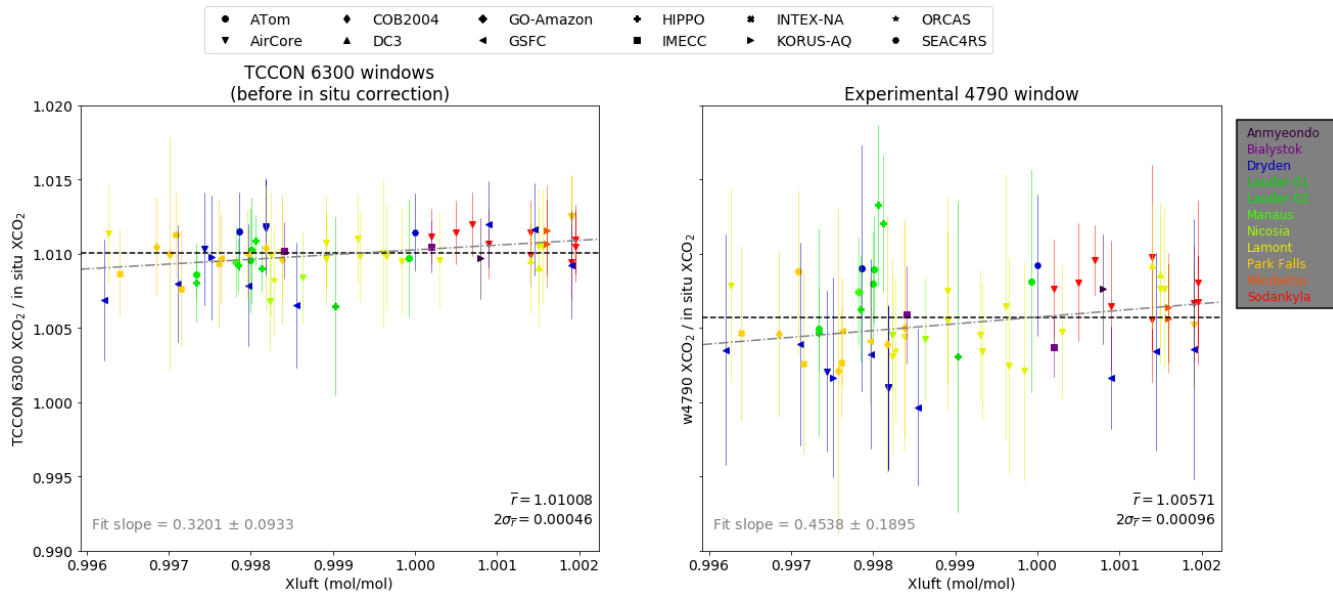


Figure 18. Left: Ratio of TCCON xCO_2 / in situ xCO_2 against xluft between 0.996 and 1.002. Left: Ratio of w4790 xCO_2 window / in situ xCO_2 against xluft between 0.996 and 1.002

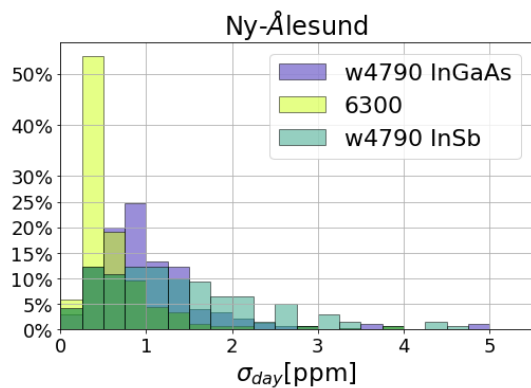


Figure 19. Histogram of the standard deviation of the daily means of CO_2 in Ny-Ålesund.

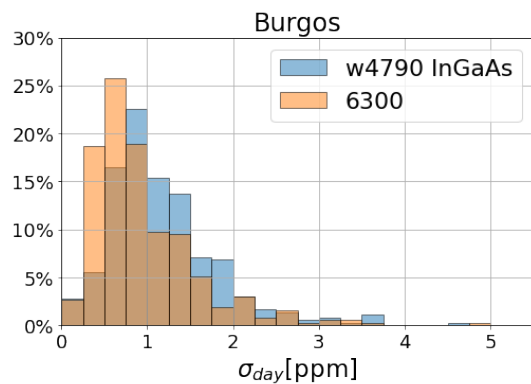


Figure 10. Histogram of the standard deviation of the daily means of CO_2 in Burgos.

Author contributions. RC determined the window, retrieved the data for Ny-Ålesund and Burgos, performed the a priori, perturbation and resolution tests, the site to site consistency and the error budget evaluation and wrote the manuscript. JL provided the in situ comparison
490 of section 4.4. MB assisted RC closely through the process in the retrieval and post processing. TW and JN guided RC the content of the research. CP assisted RC in the retrieval using GFIT. All authors contributed to the final version of the manuscript.

Competing interests. One author is a member of the editorial board of journal Atmospheric Measurement Techniques. The peer-review process was guided by an independent editor, and the authors have also no other competing interests to declare.

Acknowledgements. A portion of this research was carried out at the Jet Propulsion Laboratory, California Institute of Technology, under a
495 contract with the National Aeronautics and Space Administration (80NM0018D0004).

The TCCON station in Burgos is supported in part by the GOSAT series project. Local support for Burgos is provided by the Energy Development Corporation (EDC, Philippines).

We gratefully acknowledge the funding by the Deutsche Forschungsgemeinschaft (DFG, German Research Foundation) – Projektnummer
500 268020496 - TRR 172, within the Transregional Collaborative Research Center "Arctic Amplification: Climate Relevant Atmospheric and Surface Processes, and Feedback Mechanisms (AC)³"

References

- Barthlott, S., Schneider, M., Hase, F., Wiegele, A., Christner, E., Gonzalez, Y., Blumenstock, T., Dohe, S., Garcia, O. E., Sepúlveda, E., Strong, K., Mendonca, J., Weaver, D., Palm, M., Deutscher, N. M., Warneke, T., Notholt, J., Lejeune, B., Mahieu, E., Jones, N., Griffith, D. W. T., Velazco, V. A., Smale, D., Robinson, J., Kivi, R., Heikkinen, P., and Raffalski, U.: Using XCO₂ retrievals for assessing the long-term consistency of NDACC/FTIR data sets, *Atmospheric Measurement Techniques*, 8, 1555–1573, <https://doi.org/10.5194/amt-8-1555-2015>, 2015.
- Blumenstock, T., Hase, F., Keens, A., Czurlok, D., Colebatch, O., Garcia, O., Griffith, D. W. T., Grutter, M., Hannigan, J. W., Heikkinen, P., Jeseck, P., Jones, N., Kivi, R., Lutsch, E., Makarova, M., Imhasin, H. K., Mellqvist, J., Morino, I., Nagahama, T., Notholt, J., Ortega, I., Palm, M., Raffalski, U., Rettinger, M., Robinson, J., Schneider, M., Servais, C., Smale, D., Stremme, W., Strong, K., Sussmann, R., Té, Y., and Velazco, V. A.: Characterization and potential for reducing optical resonances in Fourier transform infrared spectrometers of the Network for the Detection of Atmospheric Composition Change (NDACC), *Atmospheric Measurement Techniques*, 14, 1239–1252, <https://doi.org/10.5194/amt-14-1239-2021>, publisher: Copernicus GmbH, 2021.
- Buckingham, A. D.: Vibrational spectroscopy, *Nature*, 263, 803–803, <https://doi.org/10.1038/263803b0>, 1976.
- Buschmann, M., Deutscher, N. M., Sherlock, V., Palm, M., Warneke, T., and Notholt, J.: Retrieval of xCO₂ from ground-based mid-infrared (NDACC) solar absorption spectra and comparison to TCCON, *Atmospheric Measurement Techniques*, 9, 577–585, <https://doi.org/https://doi.org/10.5194/amt-9-577-2016>, 2016.
- Buschmann, M., Petri, C., Palm, M., Warneke, T., and Notholt, J.: TCCON data from Ny-Ålesund, Svalbard (NO), Release GGG2020.R0, <https://doi.org/10.14291/TCCON.GGG2020.NYALESUND01.R0>, 2023.
- De Maziere, M., Thompson, A. M., Kurylo, M. J., Wild, J. D., Bernhard, G., Blumenstock, T., Braathen, G. O., Hannigan, J. W., Lambert, J.-C., Leblanc, T., McGee, T. J., Nedoluha, G., Petropavlovskikh, I., Seckmeyer, G., Simon, P. C., Steinbrecht, W., and Strahan, S. E.: The Network for the Detection of Atmospheric Composition Change (NDACC): history, status and perspectives, *Atmospheric Chemistry and Physics*, 18, 4935–4964, <https://doi.org/10.5194/acp-18-4935-2018>, publisher: Copernicus GmbH, 2018.
- IPCC: Climate Change 2022: Impacts, Adaptation and Vulnerability, Summary for Policymakers, Cambridge University Press, Cambridge, UK and New York, USA, 2022.
- Laughner, J., Toon, G. C., Wunch, D., Roche, S., Mendonca, J., Kiel, M., Roehl, C. M., Wennberg, P., Oh, Y. S., Feist, D. G., Morino, I., Velazco, V. A., Griffith, D. W. T., Deutscher, N. M., Iraci, L. T., Podolske, J. R., Strong, K., Sussmann, R., Herkommer, B., Gross, J., Garca, O. E., Pollard, D., Robinson, J., Petri, C., Warneke, T., Te, Y. V., Jeseck, P., Dubey, M. K., Maziere, M. D., Sha, M. K., Rettinger, M., Shiomi, K., and Kivi, R.: The GGG2020 TCCON Data Product, AGU, <https://agu.confex.com/agu/fm20/meetingapp.cgi/Paper/675531>, 2020.
- Laughner, J. L., Roche, S., Kiel, M., Toon, G. C., Wunch, D., Baier, B. C., Biraud, S., Chen, H., Kivi, R., Laemmle, T., McKain, K., Quéhé, P.-Y., Rousogonous, C., Stephens, B. B., Walker, K., and Wennberg, P. O.: A new algorithm to generate a priori trace gas profiles for the GGG2020 retrieval algorithm, *Atmospheric Measurement Techniques Discussions*, pp. 1–41, <https://doi.org/10.5194/amt-2022-267>, publisher: Copernicus GmbH, 2022.
- Lucchesi, R.: File Specification for GEOS-5 FP-IT (forward processing for instrument teams), <https://gmao.gsfc.nasa.gov/pubs/docs/Lucchesi865.pdf>, 2015.

- Morino, I., Velazco, V. A., Hori, A., Uchino, O., and Griffith, D. W.: TCCON data from Burgos, Ilocos Norte (PH), Release GGG2014.R0, <https://doi.org/10.14291/TCCON.GGG2014.BURGOS01.R0>, medium: application/x-netcdf Version Number: GGG2014.R0 type: dataset, 2018.
- 540 Morino, I., Velazco, V. A., Hori, A., Uchino, O., and Griffith, D. W.: TCCON data from Burgos, Ilocos Norte (PH), Release GGG2020.R0, <https://doi.org/10.14291/TCCON.GGG2020.BURGOS01.R0>, 2023.
- Rodgers, C. D.: *Inverse Methods for Atmospheric Sounding: Theory and Practice*, vol. 2, World Scientific, Singapore, 2000.
- Rodgers, C. D. and Connor, B. J.: Intercomparison of remote sounding instruments: INTERCOMPARISON OF REMOTE SOUNDERS, *Journal of Geophysical Research: Atmospheres*, 108, n/a–n/a, <https://doi.org/10.1029/2002JD002299>, 2003.
- 545 Rothman, L., Gordon, I., Barbe, A., Benner, D., Bernath, P., Birk, M., Boudon, V., Brown, L., Campargue, A., Champion, J.-P., Chance, K., Coudert, L., Dana, V., Devi, V., Fally, S., Flaud, J.-M., Gamache, R., Goldman, A., Jacquemart, D., Kleiner, I., Lacombe, N., Lafferty, W., Mandin, J.-Y., Massie, S., Mikhailenko, S., Miller, C., Moazzen-Ahmadi, N., Naumenko, O., Nikitin, A., Orphal, J., Perevalov, V., Perrin, A., Predoi-Cross, A., Rinsland, C., Rotger, M., Simeckova, M., Smith, M., Sung, K., Tashkun, S., Tennyson, J., Toth, R., Vandaele, A., and Vander Auwera, J.: The HITRAN 2008 molecular spectroscopic database, *Journal of Quantitative Spectroscopy and Radiative Transfer*, 110, 533–572, <https://doi.org/10.1016/j.jqsrt.2009.02.013>, 2009.
- 550 Toon, G. C., Blavier, J.-F., Sung, K., Rothman, L. S., and E. Gordon, I.: HITRAN spectroscopy evaluation using solar occultation FTIR spectra, *Journal of Quantitative Spectroscopy and Radiative Transfer*, 182, 324–336, <https://doi.org/10.1016/j.jqsrt.2016.05.021>, 2016.
- Toth, R. A., Brown, L. R., Miller, C. E., Malathy Devi, V., and Benner, D. C.: Spectroscopic database of CO₂ line parameters: 4300–7000cm⁻¹, *Journal of Quantitative Spectroscopy and Radiative Transfer*, 109, 906–921, <https://doi.org/10.1016/j.jqsrt.2007.12.004>, 2008.
- 555 Velazco, V., Morino, I., Uchino, O., Hori, A., Kiel, M., Bukosa, B., Deutscher, N., Sakai, T., Nagai, T., Bagtasa, G., Izumi, T., Yoshida, Y., and Griffith, D.: TCCON Philippines: First Measurement Results, Satellite Data and Model Comparisons in Southeast Asia, *Remote Sensing*, 9, 1228, <https://doi.org/10.3390/rs9121228>, 2017.
- Wunch, D., Toon, G. C., Wennberg, P. O., Wofsy, S. C., Stephens, B. B., Fischer, M. L., Uchino, O., Abshire, J. B., Bernath, P., Biraud, S. C., Blavier, J.-F. L., Boone, C., Bowman, K. P., Browell, E. V., Campos, T., Connor, B. J., Daube, B. C., Deutscher, N. M., Diao, M., Elkins, 560 J. W., Gerbig, C., Gottlieb, E., Griffith, D. W. T., Hurst, D. F., Jiménez, R., Keppel-Aleks, G., Kort, E. A., Macatangay, R., Machida, T., Matsueda, H., Moore, F., Morino, I., Park, S., Robinson, J., Roehl, C. M., Sawa, Y., Sherlock, V., Sweeney, C., Tanaka, T., and Zondlo, M. A.: Calibration of the Total Carbon Column Observing Network using aircraft profile data, *Atmospheric Measurement Techniques*, 3, 1351–1362, <https://doi.org/10.5194/amt-3-1351-2010>, 2010.
- Wunch, D., Toon, G. C., Blavier, J.-F. L., Washenfelder, R. A., Notholt, J., Connor, B. J., Griffith, D. W. T., Sherlock, V., and Wennberg, 565 P. O.: The Total Carbon Column Observing Network, *Philosophical Transactions of the Royal Society A: Mathematical, Physical and Engineering Sciences*, 369, 2087–2112, <https://doi.org/10.1098/rsta.2010.0240>, 2011a.
- Wunch, D., Wennberg, P. O., Toon, G. C., Connor, B. J., Fisher, B., Osterman, G. B., Frankenberg, C., Mandrake, L., O’Dell, C., Ahonen, P., Biraud, S. C., Castano, R., Cressie, N., Crisp, D., Deutscher, N. M., Eldering, A., Fisher, M. L., Griffith, D. W. T., Gunson, M., Heikkinen, P., Keppel-Aleks, G., Kyro, E., Lindenmaier, R., Macatangay, R., Mendonca, J., Messerschmidt, J., Miller, C. E., Morino, I., Notholt, J., 570 Oyafuso, F. A., Rettinger, M., Robinson, J., Roehl, C. M., Salawitch, R. J., Sherlock, V., Strong, K., Sussmann, R., Tanaka, T., Thompson, D. R., Uchino, O., Warneke, T., and Wofsy, S. C.: A method for evaluating bias in global measurements of CO₂ total columns from space, *Atmospheric Chemistry and Physics*, 11, 12 317–12 337, <https://doi.org/10.5194/acp-11-12317-2011>, 2011b.

Wunch, D., Toon, G. C., Sherlock, V., Deutscher, N. M., Liu, C., Feist, D. G., and Wennberg, P. O.: Documentation for the 2014 TCCON Data Release, <https://doi.org/10.14291/TCCON.GGG2014.DOCUMENTATION.R0/1221662>, medium: .pdf Publisher: CaltechDATA Version 575 Number: GGG2014.R0, 2015.

Yang, Z., Toon, G. C., Margolis, J. S., and Wennberg, P. O.: Atmospheric CO₂ retrieved from ground-based near IR solar spectra, *Geophysical Research Letters*, 29, 53–1–53–4, <https://doi.org/10.1029/2001GL014537>, 2002.