# Consideration of the cloud motion for aircraft-based stereographically derived cloud geometry and cloud top heights

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**Abstract.** Cloud geometry and in particular cloud top heights can be derived from 2-D camera measurements by applying a stereographic method to data from an overflight over a scene of clouds (see e.g. Kölling et al., 2019). Although airplane overpasses are relatively fast, cloud motion with the wind is important and can result in errors in the cloud localization. Here, the impact of the wind is investigated using the method from Kölling et al. (2019) for measurements of the airborne hyperspectral imaging system specMACS (spectrometer of the Munich Aerosol Cloud Scanner). Further, a method for the cloud motion correction using model winds from ECMWF is presented. It is shown that the update is important as the original algorithm without the cloud motion correction can over- or underestimate the cloud top heights by several hundred meters dependent on the wind speed and the relative wind direction. This is validated using data from the EUREC$^4$A campaign as well as realistic 3-D radiative transfer simulations. From the comparison of the derived cloud top heights to the expected ones from the model input an average accuracy of the cloud top heights of less than $(20 \pm 140)\,\mathrm{m}$ (mean deviation and one standard deviation) is estimated for the updated method.

## 1 Introduction

The macro- and microphysical properties of clouds have a large impact on the Earth's radiation and energy budgets as they determine the cloud's interaction with solar and terrestrial radiation. Since clouds have a high spatial and temporal variability representing them accurately in both numerical weather prediction as well as global climate models is difficult, such that parametrizations of the cloud properties are important. Those often rely on observational studies which have been widely extended in recent decades. In particular, one aim has been to obtain a better understanding of the role of clouds in climate change. An important contribution to the characterization of cloud properties is provided by active and passive remote sensing instruments which can be ground-, aircraft- or satellite-based and sensitive to different wavelengths both in the solar and terrestrial spectral range. One of them is the airborne spectrometer of the Munich Aerosol Cloud Scanner (specMACS, Ewald et al. (2016); Pörtge et al. (2023); Weber et al. (2023)) operated onboard of the German High Altitude and LOng range research aircraft HALO (Krautstrunk and Giez, 2012). specMACS consists of two hyperspectral line cameras measuring radiances in the wavelength range between $400\,\mathrm{nm}$ and $2500\,\mathrm{nm}$ (Ewald et al., 2016) as well as two polarization resolving RGB cameras (Phoenix 5.0 MP Polarization Model) (Pörtge et al., 2023; Weber et al., 2023). That way, the solar radiation reflected from

clouds is measured with a high spectral and spatial resolution and a wide field of view ($32.7°$ and $35.5°$ for the line cameras (Ewald et al., 2016) and $91° \times 117°$ for the two polarization cameras combined (Weber et al., 2023)). The specMACS measurements are used for microphysical retrievals of cloud properties, both using a bispectral approach as described by Nakajima and King (1990) as well as from a polarimetric retrieval described in Pörtge et al. (2023), which uses multi-angle polarized radiance observations of the cloudbow to derived cloud droplet size distributions (CDSD). In general, passive observations usually do not provide cloud top height or structure with height resolution. However, for the interpretation and geolocalization of the microphysical retrievals, the exact location of the observed clouds in 3-D space is important. For that, the stereographic derived cloud geometry is used.

One approach for the localization of clouds in 3-D space is the stereographic reconstruction from multi-angle intensity measurements while flying over a scene of clouds. For example, this has been used for spaceborne instruments such as the Multi-angle Imaging SpectroRadiometer (MISR) (Moroney et al., 2002; Seiz and Davies, 2006) and the Advanced Spaceborne Thermal Emission and Reflection Radiometer (ASTER) (Seiz et al., 2006). For specMACS, the clouds are located in 3-D space using the 2-D intensity measurements of the polarization cameras. The algorithm is described in detail by Kölling et al. (2019) and is based on the identification of points on the cloud surface using contrast gradients. Afterwards, the points are re-identified in subsequent images and located in 3-D space using the multi-angle observation. Then, the derived cloud top heights are for example used for the geolocalization of the cloud targets observed by the polarimetric retrieval for the determination of the CDSD. The retrieval is based on the aggregation of the polarized radiance measured for a cloud target in subsequent images to obtain the full signal of the cloudbow, which is sensitive to both, the effective radius and variance of the CDSD. Thereby, accurate cloud top heights are important as small errors in the cloud top height assigned to cloud targets will lead to wrong localizations of the targets in subsequent images. Consequently, this leads to a wrong aggregation of the cloudbow signal and thus, errors in the derived CDSD (Pörtge et al., 2023).

So far, the stereographic retrieved cloud top heights were compared by Kölling et al. (2019) to the cloud top heights derived from the WALES lidar (WAter vapor Lidar Experiment in Space, Wirth et al., 2009) for simultaneous measurements during the NAWDEX campaign in October 2016. They found a median bias of $126\,\mathrm{m}$ with the stereo heights found to be lower. It was indicated that the most prominent outliers in regions of high lidar cloud top height and low stereo height were observed for thin cirrus layers above cumulus clouds. In those scenes, the lidar is sensitive to the upper ice cloud layer while the stereo algorithm detects image areas with high contrasts which are preferably observed for lower cloud layers. Volkmer et al. (2023b) applied the stereographic reconstruction algorithm to synthetic measurements obtained from realistic 3-D radiative transfer simulations and found an average underestimation of the stereographic cloud top heights by $(70 \pm 130)\,\mathrm{m}$ without correcting for any cloud motion. Kölling et al. (2019) argued that in contrast to spaceborne methods employed e.g. to MISR (Moroney et al., 2002; Seiz and Davies, 2006) and ASTER (Seiz et al., 2006), no correction of the clouds wind movement needs to be applied. This is due to the much smaller time difference between two successive images (framerate of $1\,\mathrm{Hz}$ used for the stereo algorithm) and the much lower operating altitude leading to a much more rapid change in the observation angle compared to the satellite observations. However, the observation of the clouds from multiple viewing perspectives has been exploited to derive an estimate of the underlying 3-D wind field.

In subsequent evaluations of measurement data, the impact of the cloud motion on the stereographic derived cloud top heights has been further investigated by comparing the derived cloud top heights for flight legs which were flown forward and backward within a time difference of about 70 minutes. Deviations of several hundred meters despite the temporally highly resolved observation of the clouds from multiple viewing angles have been observed. This is due to the faster movement of the clouds through the field of view of the instrument when the aircraft is flying against the wind and leads to an overestimation of the cloud top heights. Correspondingly, flying with the wind direction leads to an underestimation of the cloud top heights. Hence, an approach for the cloud motion correction using the 3-D wind field of the ERA5 reanalysis data (Hersbach et al., 2020) has been developed and will be presented in Sect. 2 in this study. In Sect. 3, the cloud motion correction will be validated using measurement data. Finally, the approach will be validated using realistic 3-D radiative transfer simulations of the measurements performed with MYSTIC (Monte Carlo code for the physically correct tracing of photons in cloudy atmospheres, Mayer, 2009; Volkmer et al., 2023b) in Sect. 4.

## 2 Wind correction based on ERA5 reanalysis data

To correct for the movement of clouds within the observation time, the ERA5 reanalysis data on 37 pressure levels between $1000\,\mathrm{hPa}$ and $1\,\mathrm{hPa}$ on a regular latitude-longitude grid of $0.25° \times 0.25°$ are used. The data have a temporal resolution of $1\,\mathrm{h}$ (Hersbach et al., 2020). Only the horizontal wind movement is considered since the convective movement of the clouds observed by specMACS is not resolved in the ERA5 data.

The aircraft-based stereographic reconstruction of the 3-D cloud geometry is based on the observation of ~~the~~ clouds from different perspectives by flying over them. Points on the cloud surface are identified using contrasts and then re-identified in subsequent images using the optical flow algorithm described by Lucas and Kanade (1981). Then, the points are located in 3-D space using a triangular geometry as schematically shown in Fig. 1. In order to correct for cloud motion, the wind vector $\boldsymbol{v}$ at the cloud location is needed, which however is not known yet. Hence, the stereographic reconstruction is performed iteratively by first calculating the location of the point without considering the movement of the observed cloud as described in Kölling et al. (2019). Next, the horizontal wind vector is estimated at the location and time of the point found at the clouds surface by linear interpolation of the gridded reanalysis data.

Afterwards, the calculation of the point is repeated with the estimated cloud motion. To do so, the aircraft's locations are virtually shifted with half the wind vector each which assures that the point identified on the cloud surface is located in between the two actual locations as it is still observed under the same viewing angles. This is schematically depicted in Fig. 1. The two real aircraft positions at $P_1 = (t, \boldsymbol{x})$ and $P_2 = (t + \Delta t, \boldsymbol{x} + \Delta \boldsymbol{x})$ from which the cloud is observed are moved with the horizontal wind vector obtained from the interpolation of the ERA5 data at the initially estimated cloud top height. The initial viewing points $P_1$ and $P_2$ are shifted to the points $P_1' = (t, \boldsymbol{x} + \frac{\Delta t}{2}\boldsymbol{v})$ and $P_2' = (t + \Delta t, \boldsymbol{x} + \Delta \boldsymbol{x} - \frac{\Delta t}{2}\boldsymbol{v})$. Using this modification guarantees that the reference point $P_{\mathrm{ref}}$ for the observer location remains the same. With that modified geometry, the location of the point on the cloud surface $(P_{\mathrm{CS}})$ is calculated again. Since the wind vector can only be estimated at the cloud surface height location initially found by the method, the correction is iterated five times. Hereby, a stepwise corrected height for the

Diagram showing tracking geometry with aircraft positions $P_1$, $P_2$, $P_1'$, $P_2'$, reference point $P_{\text{ref}}$, cloud surface point $P_{\text{CS}}$, and vectors $\vec{d}$, $\vec{d'}$, $\vec{m}$, $\vec{m}/2$, $\vec{v}$, $\vec{v}/2$, $-\vec{v}/2$. Legend: solid arrow "real geometry", dashed arrow "computed geometry".
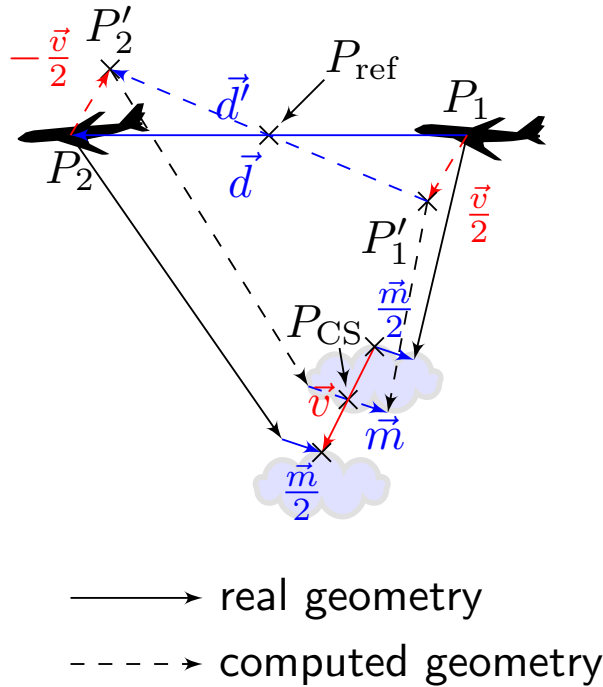
**Figure 1.** Tracking geometry for the location of points on the cloud surface as in Kölling et al. (2019) but with the modification for the cloud motion correction. The real geometry is shown in solid vectors, while the actually computed geometry is visualized by the dashed vectors. Hereby, $\boldsymbol{v}$ denotes the wind vector at $P_{\text{CS}}$. The vector $\boldsymbol{d}$ refers to the distance vector between the two aircraft positions (typically around 200 m) and $\boldsymbol{d'}$ is the corresponding quantity for the modified geometry. The point $P_{\text{ref}}$ is the reference viewing point from which the point on the cloud $P_{\text{CS}}$ is observed. Finally, $\boldsymbol{m}$ is the so-called mis-pointing vector, which takes into account that two straight lines in 3-D space do not necessarily meet. However, its length is only on the order of a few meters.

estimation of an improved wind vector is used each time. It has been tested that more iteration steps do not improve the result significantly anymore.

## 3 Validation using measurements from the EUREC⁴A campaign

The validation of the cloud motion correction on the cloud top heights derived by the stereographic reconstruction algorithm described above was conducted by considering two consecutive straight flight legs flown by HALO to the NTAS (Northwest Tropical Atlantic Station) buoy and back on 28 January 2020 during the EUREC⁴A campaign. As described by Stevens et al. (2021), that day was associated with shallow cumulus clouds which could also be observed on the two mentioned straight legs. On the one hand, those shallow cumulus clouds provide good contrasts such that they are well recognized by the stereographic reconstruction algorithm. On the other hand, there were no additional cloud layers above the low shallow cumuli and hence the signal measured by specMACS and the backscatter signal measured by the WALES lidar operated simultaneously on HALO

originate from the same cloud targets. Thus, the derived cloud top heights are well comparable. The straight legs were chosen for the validation because the NTAS buoy was located in the northeast of the standard "EUREC$^4$A-circle" flown by HALO

105 (Stevens et al., 2021). Given the prevailing north-easterly trade winds in this region at that time of the year, the first leg towards the buoy (HALO-0128_sl1) is flown against the wind while immediately afterwards the return leg (HALO-0128_sl2) is flown with the wind. The time difference between the start of the first leg and the end of the second leg (the maximum time difference for a given position in the following analysis) was about 70 minutes. WALES measurements which are not affected by the cloud movement showed no significant changes in cloud top height during this time with median values of about 745 m on the

110 first leg and 738 m on the second one.
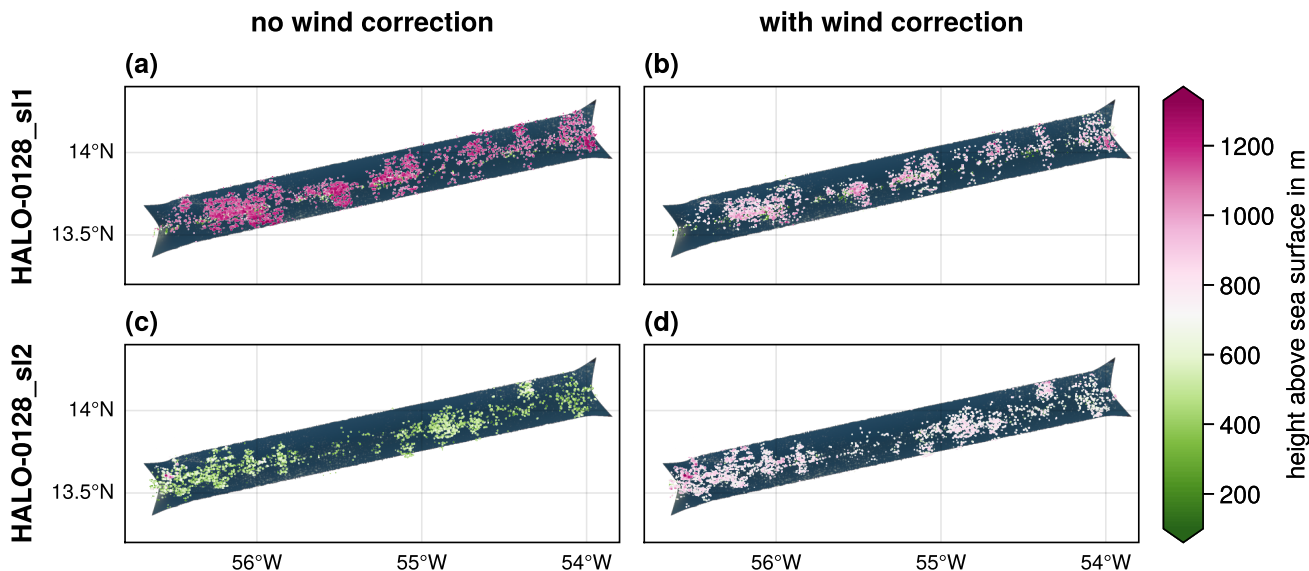
**Figure 2.** Example for the cloud motion correction of the stereographic retrieved cloud top heights of the flight segments HALO-0128_sl1 and HALO-0128_sl2 during the EUREC$^4$A campaign. The legs were flown to the NTAS buoy on 28 January 2020 and directed toward the northeast such that the leg towards the buoy (sl1) was flown approximately against the wind while the wind was moving the clouds in flight direction on the way back. On the left, the stereographic retrieved cloud top heights without cloud motion correction are shown for both legs. On the right, the cloud motion correction based on the ERA5 reanalysis data is included. The background shows images from the two polarization resolving cameras of specMACS projected onto a surface at 1 km altitude.

Figure 2 shows the retrieved cloud top heights from the two consecutively flown straight legs projected to specMACS images of the respective flight legs. The corresponding histograms are given in Fig. 3 including the histograms and the median of the cloud top heights derived from measurements of the WALES lidar using all measurements which are referred to as most likely cloudy (Wirth, 2021). It can be seen that the stereographically derived cloud top heights on the way to the NTAS buoy and back

115 differ by more than 600 m in the median without any cloud motion correction. This is due to the overestimation of the cloud top heights on the way to the buoy while flying against the wind and the underestimation on the downwind directed way back.

The total horizontal wind speed was about $7\,\mathrm{ms^{-1}}$ as measured by a dropsonde launched from HALO at the end of the first leg. Including the cloud motion correction based on the ERA5 reanalysis data results in a shift of the stereographically derived cloud top heights to lower (HALO-0128_sl1) and higher (HALO-0128_sl2) values respectively such that the median values only differ by less than $60\,\mathrm{m}$. Thus, they are now in the same order of magnitude considering that not exactly the same clouds are observed on both legs and that they might develop over time. Finally, a comparison to the histograms and the median values of the lidar heights shows a much better agreement for the wind corrected heights. The difference between the stereographic derived cloud top heights and the median of the WALES measurements reduces from about $\pm300\,\mathrm{m}$ without the cloud motion correction to about $40\,\mathrm{m}$ on the way to the buoy and less than $5\,\mathrm{m}$ on the way back when the cloud motion correction is included.

## 4  Accuracy estimation using realistic simulated measurements from 3-D radiative transfer simulations

To further constrain the accuracy of the presented method, realistic 3-D radiative transfer simulations with the radiative transfer model MYSTIC (Mayer, 2009; Emde et al., 2010) as part of the libRadtran radiative transfer package (Mayer and Kylling, 2005; Emde et al., 2016) were performed and the stereographic reconstruction algorithm was applied to the simulated measurements of a one minute overflight over a field of large eddy simulated (LES) shallow cumulus clouds as presented by Volkmer et al. (2023b). The radiative transfer simulations were conducted for the LES cloud field with a horizontal extent of $25.6 \times 12.8\,\mathrm{km^2}$ at a horizontal resolution of $20\,\mathrm{m}$ and a vertical resolution of about $25\,\mathrm{m}$. A flight altitude of $10\,\mathrm{km}$ was assumed. Figure 4 shows the underlying model wind field as obtained from the LES simulations, indicating wind directions between approximately $140\,^\circ$ at low altitudes and $340\,^\circ$ at higher altitudes. The average wind speed is between $0.6\,\mathrm{ms^{-1}}$ at about $2500\,\mathrm{m}$ and $3.2\,\mathrm{ms^{-1}}$ between $100\,\mathrm{m}$ and $900\,\mathrm{m}$ and hence overall smaller than for the real measurements considered before. The aircraft was simulated to fly towards the North with a horizontal aircraft alignment (all three Euler angles are zero). This corresponds to a mainly downwind flight direction for clouds lower than about $2400\,\mathrm{m}$ where the wind direction exceeds $270\,^\circ$.

For the comparison of the model heights to the stereographically derived cloud top heights, we used the same method as presented by Volkmer et al. (2023b). The expected cloud top heights were obtained from the first scattering events of Monte Carlo based reference simulations, where the photons are started at the detector. For each simulated pixel, 1000 photons were computed and the scattering events of all photons not scattered at the ground were averaged to determine the height from where the optical signal originates. In Fig. 5 the expected model heights (panel a) and the corresponding stereographically derived cloud top heights including the cloud motion correction (panel c) are shown for the simulated measurements together with their respective histograms (panels b and d). On the left, the points found are projected to the measurement simulated after a flight time of $30\,\mathrm{s}$. The flight direction is to the right of the simulated measurement. Mean cloud top heights of about $1628\,\mathrm{m}$ for the expected model heights and $1644\,\mathrm{m}$ for the stereographically derived cloud top heights are found. On the bottom of Fig. 5, the point-wise difference between the stereographic and the model heights is shown (panel e). From all point-wise differences, a mean difference of about $15\,\mathrm{m}$ between the stereo and model heights and a standard deviation of about $133\,\mathrm{m}$ is derived as
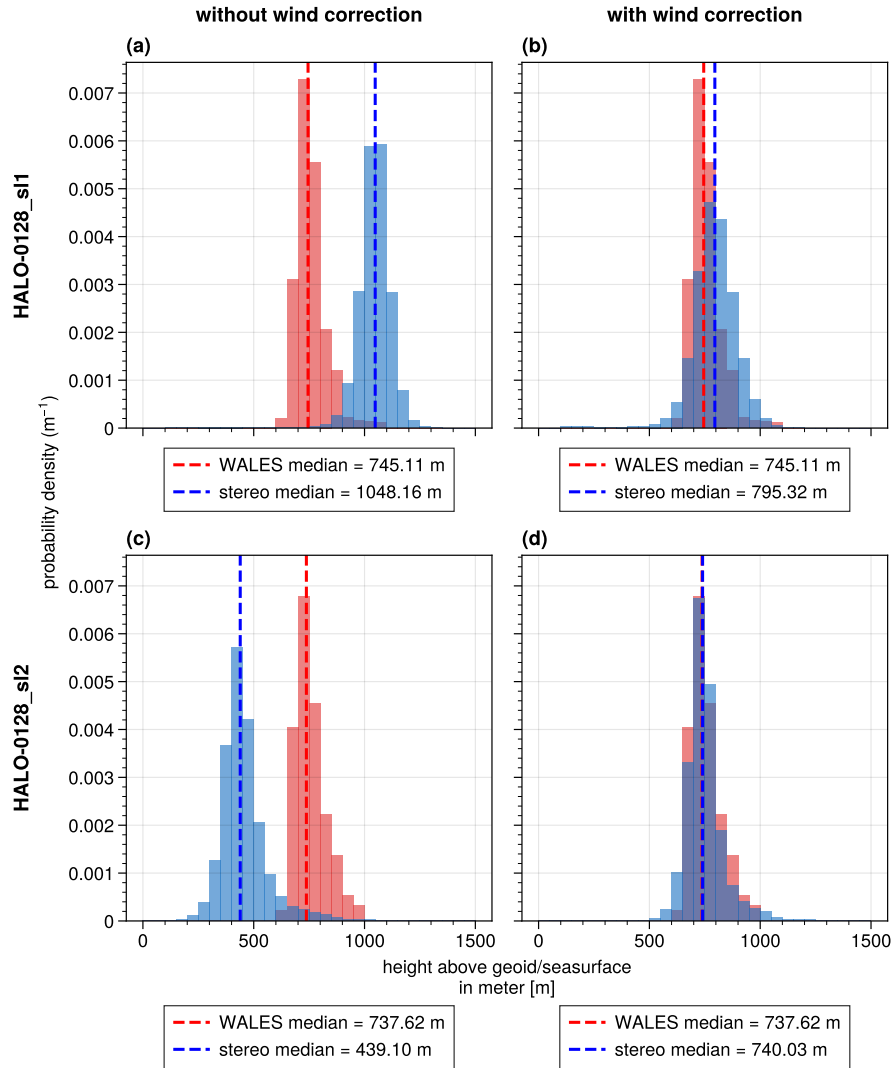
**Figure 3.** Histograms of the stereographically retrieved cloud top heights (blue) and the corresponding histograms of the WALES lidar cloud top height measurements (red) of the flight segments HALO-0128_sl1 and HALO-0128_sl2 as described in Figure 2. On the left, the histograms of the stereographically retrieved cloud top heights without cloud motion correction are shown for both legs. On the right, the cloud motion correction based on the ERA5 reanalysis data is included. Next to the median of the stereographically derived cloud top heights (~~black~~ blue dashed vertical line), the median of the cloud top heights derived by the WALES lidar is shown (red line).

shown in the corresponding histogram in Fig. 5f. Without any cloud motion correction the stereographic derived cloud top heights for the considered LES cloud field deviated on average by $(-70 \pm 130)\,\mathrm{m}$ from the expected cloud top heights of the model input (Volkmer et al., 2023b). Thus, the absolute mean bias is reduced by approximately $55\,\mathrm{m}$ by considering the cloud movement for the considered cloud field and aircraft direction (about $2\,\mathrm{ms}^{-1}$ in flight direction). It can again be observed that
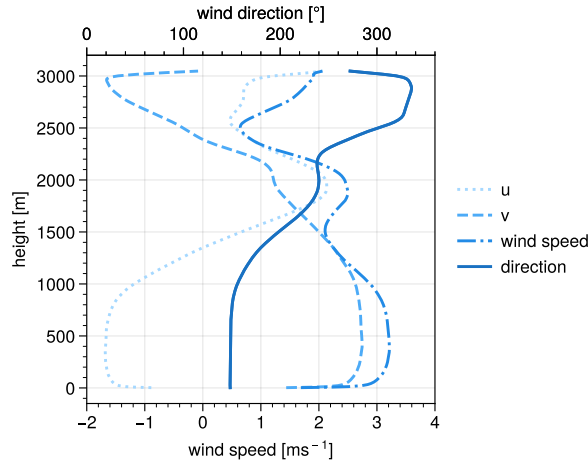
**Figure 4.** Average vertical profiles of the horizontal wind vector of the LES cloud field after a simulation time of $30\,\mathrm{s}$. The horizontal wind speed as well as the $u$- and $v$-component are shown with respect to the lower axis, while the wind direction is shown with regard to the upper axis.

the point-wise differences between the stereographically derived cloud top heights and the model heights can be up to $\pm 500\,\mathrm{m}$ with the positive values occurring rather where the cloud is generally lower (cloud edges and in shadow regions), while the negative ones are observed at the highest cloud tops.

While the mean bias is reduced to approximately $15\,\mathrm{m}$, the standard deviation which shows the spread of the single measurements is about $130\,\mathrm{m}$ with and without wind correction. One possible ~~explanation for this~~ error source, the evolution of the observed clouds, has been studied by Volkmer et al. (2023b) using a similar setup as described above but with non-developing and non-moving clouds. Hereby, an absolute mean bias of $(46 \pm 140)\,\mathrm{m}$ was found. While the larger mean bias might be explained by a remaining uncertainty in the wind estimation and a cancellation of the error sources, the standard deviation and hence, the error of the single measurement, remains approximately constant. One possible explanation for the uncertainty found here is given by Kölling et al. (2019, Appendix A): At a cloud-aircraft distance of $10\,\mathrm{km}$, a relative change of $0.01\,^{\circ}$ ($1/3\,\mathrm{px}$) in the viewing angle results in a wrongly calculated distance between the aircraft and the cloud of $100\,\mathrm{m}$. Hence, it is emphasized that an accuracy on the order of $100\,\mathrm{m}$ can only be achieved if one averages over multiple measurements and if one can reduce any systematic error in the geometric camera calibration to less than $1/3\,\mathrm{px}$. Compared to the accuracy of the stereographic cloud top heights derived from MISR measurements which is found to be $280\,\mathrm{m}$ for an advanced sub-pixel least squares matching technique (Seiz et al., 2006), the standard deviation found here is about half as big. For ASTER, Seiz et al. (2006) found a systematic error of $12.5\,\mathrm{m}$ with an additional uncertainty of about $100\,\mathrm{m}$ for every $1\,\mathrm{ms}^{-1}$ uncertainty in the wind component along track of the satellite.
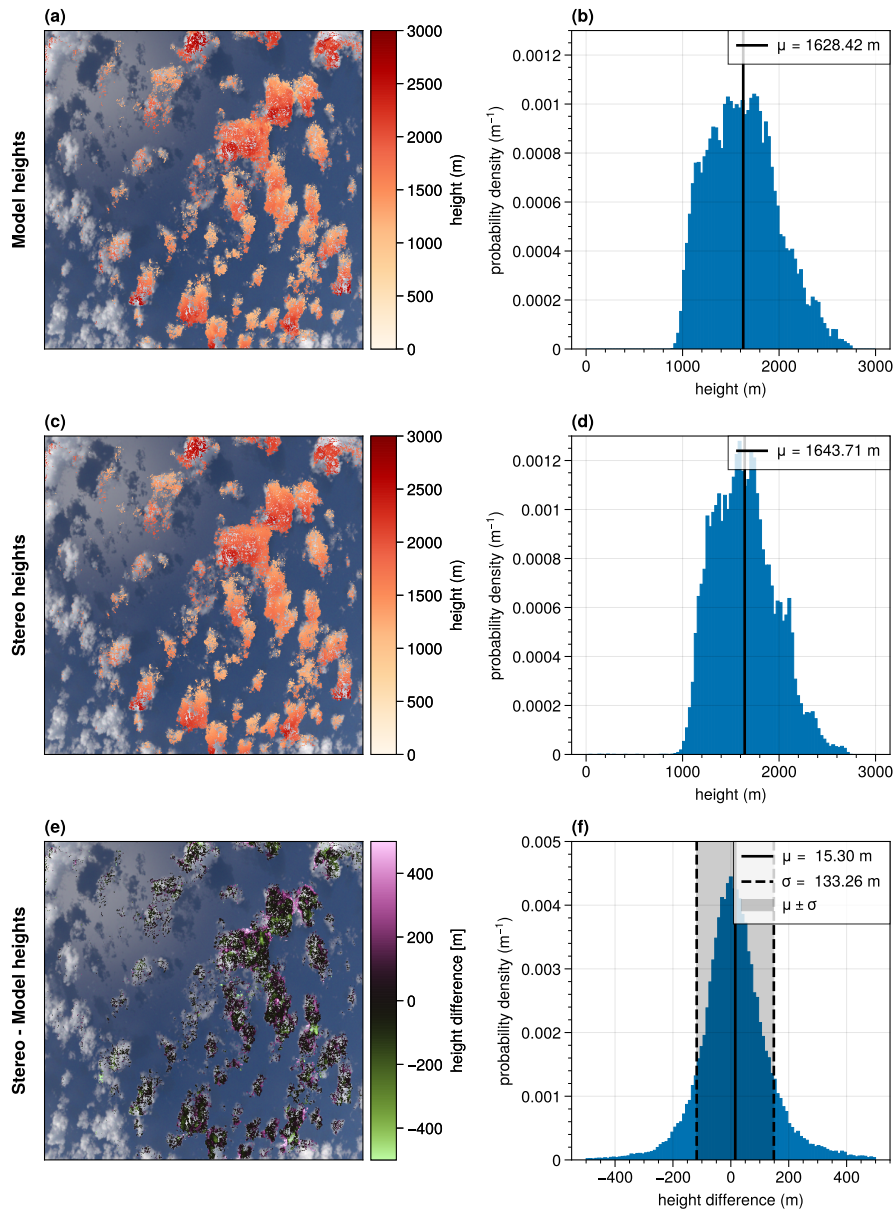
**Figure 5.** Comparison of the cloud top heights expected from the model and derived from the stereographic reconstruction algorithm. The cloud top heights as expected from the model input (Model heights) are shown in panel a (only for those points where the stereo method provided information). The stereographic derived cloud top heights can be seen in panel c. Below, the point-wise differences are shown (panel e). The derived points were projected onto the simulated RGB image and the corresponding histograms are shown in panels b, d and f. The solid vertical lines indicate the mean values. The vertical dashed lines in panel f refer to the boundaries of the $\mu \pm \sigma$ interval.

# 5 Conclusions

In this paper, we presented an improvement of the stereographic reconstruction method for the determination of 3-D cloud geometry from measurements of specMACS as developed by Kölling et al. (2019). The improvement of the method includes the estimation of the clouds wind movement using ERA5 reanalysis data. It could be shown that the consideration of the cloud movement with the wind is important for the estimated cloud top heights. Without any cloud motion correction the cloud top heights from two flight legs deviated by more than $600\,\mathrm{m}$ depending on the wind direction while the median of the cloud top heights derived from measurements of the WALES lidar remained approximately constant. With the consideration of the cloud motion a much better agreement between the stereographically derived cloud top heights and the ones from the WALES measurements could be achieved with median differences of about $50\,\mathrm{m}$ for the first leg and less than $3\,\mathrm{m}$ on the way back.

The improvement of the derived cloud top heights when the wind movement is considered could also be validated using realistic 3-D radiative transfer simulations following the method from Volkmer et al. (2023b). While the mean difference between the stereographically derived cloud top heights and the expected ones from the model input was $(-70 \pm 130)\,\mathrm{m}$ without the consideration of the wind movement (Volkmer et al., 2023b), the consideration of the clouds wind movement reduced the average difference to about $(15 \pm 133)\,\mathrm{m}$. Thus, while the mean bias reduces, the spread, which can be taken as a measure for the single points, is approximately constant. Hence, the accuracy of the cloud top heights from the 3-D stereographic reconstruction method for real measurements can be estimated to be better than $(20 \pm 140)\,\mathrm{m}$.

While this study is based on observed and simulated shallow cumulus clouds, the performance of the stereographic retrieval including the wind correction should in future also be tested for other cloud types. In particular, the retrieval should also work in more inhomogeneous cloud fields, with cloud tops spanning larger altitude ranges. This will be investigated in the future, using observations from past and upcoming field campaigns addressing different cloud types as well as corresponding simulated observations.

*Data availability.* The 3-D cloud geometry data from the stereographic reconstruction are available on the EUREC[4]A database on the Aeris dataserver (Volkmer et al., 2023a). The WALES (Wirth, 2021) and dropsonde data (George, 2021) are available on the database as well.

*Author contributions.* LV and TK implemented the wind correction in the stereographic reconstruction algorithm. LV applied the method to the measurements of the EUREC[4]A campaign and processed and published the data. TK, TZ and BM actively participated in the EUREC[4]A campaign and contributed all to the manuscript. TZ and BM further helped developing the implementation of the wind correction by discussing the intermediate results.

*Competing interests.* At least one of the (co-)authors is a member of the editorial board of Atmospheric Measurement Techniques.

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