

1 **Field assessments on impact of CO<sub>2</sub> concentration fluctuations along with complex**  
2 **terrain flows on the estimation of the net ecosystem exchange of temperate forests**

3 Dexiong Teng<sup>1,2</sup>, Jiaojun Zhu<sup>1,2,3,\*</sup>, Tian Gao<sup>1,2,3</sup>, Fengyuan Yu<sup>1,2</sup>, Yuan Zhu<sup>1,2</sup>, Xinhua  
4 Zhou<sup>3,4</sup>, Bai Yang<sup>4</sup>

5 1 CAS Key Laboratory of Forest Ecology and Silviculture, Institute of Applied Ecology, Chinese  
6 Academy of Sciences, Shenyang 110000, China

7 2 Qingyuan Forest CERN, National Observation and Research Station, Liaoning Province,  
8 Shenyang 110016, China

9 3 CAS-CSI Joint Laboratory of Research and Development for Monitoring Forest Fluxes of Trace  
10 Gases and Isotope Elements, Institute of Applied Ecology, Chinese Academy of Sciences,  
11 Shenyang 110016, China

12 4 Campbell Scientific Incorporation, Logan, Utah 84321, USA

13 **\* Corresponding Author: Jiaojun Zhu**

14 Tel : +86 24 83970342

15 Email: [jiaojunzhu@iae.ac.cn](mailto:jiaojunzhu@iae.ac.cn)

16 **Abstract**

17 The CO<sub>2</sub> storage ( $F_s$ ) is the cumulation or depletion in CO<sub>2</sub> amount over a period  
18 in an ecosystem. Along with the eddy-covariance flux and wind-stream advection of  
19 CO<sub>2</sub>, it is a major term in the net ecosystem CO<sub>2</sub> exchange (NEE) equation and even  
20 dominates in the equation under a stable atmospheric stratification while this equation  
21 is used for forest ecosystems over complex terrains. However, estimating the  $F_s$  remains  
22 challenging due to the frequent gusts and random fluctuations in boundary-layer flows  
23 that arouse tremendous difficulties in catching the true trend of CO<sub>2</sub> changes for its  
24 storage estimation from eddy-covariance along with the atmospheric profile techniques.  
25 Using the measurements from Qingyuan Ker Towers equipped with NEE instrument  
26 systems separately covering mixed-broadleaf, oak, and larch forests towers in a  
27 mountain watershed, this study investigates the gust periods and CO<sub>2</sub> fluctuation  
28 magnitudes while examining their impact on  $F_s$  estimation in relation to the terrain  
29 complexity index (TCI). The gusts induce CO<sub>2</sub> fluctuations at numerous periods of 1 to  
30 10 min over two hours. Diurnal, seasonal, and spatial differences ( $P < 0.01$ ) in the  
31 maximum amplitude of CO<sub>2</sub> fluctuations ( $A_m$ ) ranges from 1.6 to 136.7 ppm and these  
32 difference in a period ( $P_m$ ) at the same significant level ranges 140 to 170 second. The  
33  $A_m$  and  $P_m$  are significantly correlated to the magnitude and random error of  $F_s$  with  
34 diurnal and seasonal differences. These correlations decrease as CO<sub>2</sub> averaging time  
35 windows becomes longer. To minimize the uncertainties of  $F_s$ , a constant [CO<sub>2</sub>]  
36 averaging time window for the  $F_s$  estimates is not ideal. Dynamic averaging time  
37 windows and a decision-level fusion model can reduce the potential underestimation of

38  $F_s$  by 29%–33% for temperate forests in complex terrains. The relative contribution of  
 39  $F_s$  to the 30-min NEE observations ranged from 17% to 82% depending on turbulent  
 40 mixing and TCI. The study’s approach is notable as it incorporates TCI and utilizes  
 41 three flux towers for replication, making the findings relevant to similar regions with a  
 42 single tower.

43 **Keywords:** Eddy covariance, complex terrain, carbon flux, storage term, carbon  
 44 dioxide concentration, random uncertainty

## 45 **1 Introduction**

46 The accurate estimation of the net ecosystem exchange (NEE) of carbon dioxide  
 47 ( $\text{CO}_2$ ) in forest ecosystems is crucial for a comprehensive understanding of the global  
 48 carbon cycle. The eddy covariance (EC) technique has been widely used in forest  
 49 ecosystems due to its capacity to directly measure the NEE while measurement  
 50 conditions satisfy the underlying theory. The EC technique is based on a simplified  
 51 mass conservation equation (after the Reynolds averaging), given by:

$$\begin{aligned}
 \text{NEE} = & \underbrace{\frac{1}{V_m} \int_0^h \left( \frac{\partial \bar{c}}{\partial t} \right) dz}_{\text{I}} + \underbrace{\frac{1}{V_m} (\overline{w'c'})}_h}_{\text{II}} \\
 & + \underbrace{\frac{1}{V_m} \int_0^h \left( \bar{w}(z) \frac{\partial \bar{c}}{\partial z} \right) dz}_{\text{III a}} + \underbrace{\bar{c}(z) \frac{\partial \bar{w}}{\partial z}}_{\text{III b}} dz, \quad (1) \\
 & + \underbrace{\frac{1}{V_m} \int_0^h \left( \bar{u}(z) \frac{\partial \bar{c}}{\partial x} + \bar{v}(z) \frac{\partial \bar{c}}{\partial y} \right) dz}_{\text{IV}}
 \end{aligned}$$

53 where  $V_m$  is the volume of dry air in the control volume;  $c$  is the  $\text{CO}_2$  mixing ratio;  $t$  is  
 54 the time;  $h$  is the measure height;  $u$ ,  $v$ , and  $w$  denote the velocity components in the  $x$ ,

55  $y$ , and  $z$  directions, respectively; and an overbar denotes Reynolds averaging. This  
56 equation conceptualizes the NEE within a control volume from the ground to the  
57 measurement height ( $h$ ), while ignoring the horizontal turbulence term divergence  
58 (Feigenwinter et al., 2004). In this equation, term I is the CO<sub>2</sub> storage ( $F_s$ ) representing  
59 the change in the average CO<sub>2</sub> concentration (hereafter [CO<sub>2</sub>]). Terms II, IIIa, IIIb, and  
60 IV represent the vertical turbulent flux ( $F_c$ ), the vertical advection, the interface vertical  
61 mass advection, such as the evaporation process (Webb et al., 1980), and the horizontal  
62 advection, respectively.

63 Most flux measurements typically lack the solutions for terms III and IV, and can  
64 only estimate the NEE by summing  $F_c$  and  $F_s$ , and even a significant number of sites  
65 ignored the  $F_s$ . The  $F_s$  in the vertical gas column within a canopy can be substantial,  
66 requiring attention in NEE estimates (Aubinet et al., 2000). The  $F_s$  contributes ~60% to  
67 nocturnal turbulent flux underestimation in forest ecosystems with “ideal” topography  
68 (Mchugh et al., 2017). Especially, during atmospherically stable periods such as the  
69 early morning, sunset, and nighttime transitions, the  $F_s$  has a significant impact on the  
70 NEE. For 30-min ecosystem carbon flux measurements, ignoring  $F_s$  would  
71 underestimate the NEE (Zhang et al., 2010). The  $F_s$  value typically ranges from  $-2$  to  
72  $-5 \mu\text{mol m}^{-2} \text{s}^{-1}$  in the early morning, and the  $F_s$  is about  $1-3 \mu\text{mol m}^{-2} \text{s}^{-1}$  after sunset  
73 for temperate forests. The effect of the  $F_s$  on the NEE of forest ecosystems decreases  
74 with the increase of timescale (Li et al., 2020). However, neglecting the  $F_s$  value can  
75 lead to a misunderstanding of the CO<sub>2</sub> exchange processes, such as ecosystem  
76 respiration and photosynthesis, and their relationship with key control factors such as

77 solar radiation, temperature, and moisture (Mchugh et al., 2017). Therefore, it is  
78 imperative not to overlook  $F_s$  to ensure more precise NEE estimates of forest  
79 ecosystems, particularly in complex terrains.

80 Despite the challenges inherent in monitoring forest conditions, understanding the  
81 carbon flux of forest ecosystems in complex terrains or with heterogeneous underlying  
82 surfaces remains an area of great interest. Topography complexity plays a complex role  
83 in the transportation of momentum, energy, and mass in the atmospheric boundary layer,  
84 with direct impacts on the airflow patterns, spatiotemporal characteristics, and gas  
85 concentration fluctuations (Sha et al., 2021; Finnigan et al., 2020). Differences in  
86 airflow along the slope, lateral  $\text{CO}_2$  discharge downhill, and spatiotemporal variations  
87 in soil respiration result in the  $\text{CO}_2$  outflow from slopes and valleys lagging behind the  
88 flat top of the mountain (De Araújo et al., 2010). At night, under stable atmospheric  
89 stratification, cold air moves from valley forest canopy to the ground the and then flows  
90 to low-lying areas, causing a “carbon pooling” effect. The gradient of  $[\text{CO}_2]$  below the  
91 EC sensors fluctuates significantly, and the cold air discharge above the canopy reduces  
92  $\text{CO}_2$  storage, leading to an underestimation of forest ecosystem respiration (Yao et al.,  
93 2011; De Araújo et al., 2008; De Araújo et al., 2010).

94 According to the theoretical definition,  $F_s$  estimates are derived by averaging the  
95  $[\text{CO}_2]$  of the control volume at the beginning and the end of the EC averaging period  
96 (30 min or 1 h) and dividing by the EC averaging period (Finnigan, 2006). The  
97 estimation of  $F_s$  at numerous sites frequently employs a vertical profile system. This  
98 approach operates under the assumption that the  $F_s$  represents the integration of the time

99 derivative of the vertically determined column-averaged  $[\text{CO}_2]$ . It is noteworthy that  
100 the column-averaged  $[\text{CO}_2]$  may not accurately represent the average  $[\text{CO}_2]$  of the  
101 control volume in cases of inadequate air mixing, leading to insufficient sampling.  
102 Previous study showed that relying solely on tower-top measurements can lead to  
103 underestimation of  $F_s$  by up to 34% compared to the eight-level profile approach (Gu  
104 et al., 2012). The NEE magnitude with the  $F_s$  based on the 2-min  $[\text{CO}_2]$  averaging time  
105 window (instantaneous concentration approach) was found to be 5% higher than that of  
106 the 30-min-window-based  $F_s$  (averaging concentration approach), particularly during  
107 nighttime in the growing season (Wang et al., 2016). A proper measuring system with  
108 improving the horizontal representativeness can reduce the bias of  $F_s$  to 2–10%  
109 (Nicolini et al., 2018). Most research has examined how vertical and horizontal gas  
110 concentration sampling point distribution affects the uncertainty in  $F_s$  estimation  
111 (Bjorkegren et al., 2015; Wang et al., 2016; Yang et al., 2007; Yang et al., 1999), with a  
112 small number of studies examining the effect of  $[\text{CO}_2]$  sampling frequency on the  $F_s$   
113 (Finnigan, 2006; Heinesch et al., 2007). Certain studies have experimentally validated  
114 new concepts, such as correlating the gas sampling point concentration with the  
115 horizontal distribution (Nicolini et al., 2018). Some studies have approached the true  
116 value theoretically, such as through defining the control volume represented by flux  
117 measurements (Metzger, 2018; Xu et al., 2019). However, the number of complete  
118 column samples required to describe the column-averaged  $[\text{CO}_2]$  of each 30-min or 1-  
119 h  $F_s$  estimate is still undetermined.

120 Previous studies have emphasized the significance of the  $F_s$  to the NEE and the

121 influence of [CO<sub>2</sub>] dynamics on F<sub>s</sub> estimates in complex terrains. To overcome any  
122 disparities between sensors and obtain precise changes in the [CO<sub>2</sub>] gradient above and  
123 below the forest canopy, individual gas analyzers are extensively utilized to measure  
124 [CO<sub>2</sub>] levels vertically (Siebicke et al., 2011). However, a single gas analyzer introduces  
125 time delays when monitoring multi-point [CO<sub>2</sub>] curves. Accurately determining the F<sub>s</sub>  
126 estimates can be challenging due to the spatial and temporal resolution of [CO<sub>2</sub>]  
127 measurements (Wang et al., 2016). The random error of the F<sub>s</sub> estimates using one  
128 complete column sample is considerably high due to short-term [CO<sub>2</sub>] fluctuations  
129 (Nicolini et al., 2018). The calculation of the F<sub>s</sub> using time-averaged [CO<sub>2</sub>] profiling  
130 leads to significant information loss at high frequency, resulting in a substantial  
131 underestimation bias. Furthermore, time-averaged [CO<sub>2</sub>] profiling is employed to  
132 represent the [CO<sub>2</sub>] average within control volume due to resource constraints. This  
133 leads to the gap that the systematic bias and random error in F<sub>s</sub> estimate are  
134 irreconcilable. This issue necessitates further efforts to characterize [CO<sub>2</sub>] fluctuations  
135 across different sites and demonstrate the mechanisms influencing F<sub>s</sub> magnitudes,  
136 uncertainties, and their contributions to NEE observations in complex terrains. Thus,  
137 this study aims to bridge this gap by introducing a statistical method to estimate F<sub>s</sub>  
138 values and their uncertainties.

139 This paper employed an innovative EC experimental setup with three flux towers  
140 (Qingyuan-Ker Towers) to monitor three typical types of temperate forest stands  
141 located in complex terrains in northeastern China. This study introduces a decision-  
142 level fusion model based on weighing the underestimation bias and random error of the

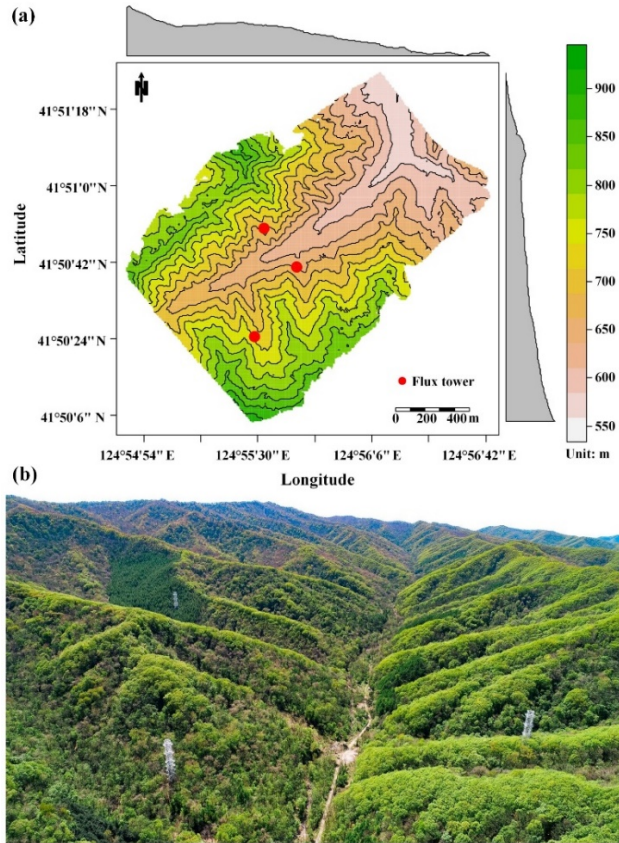
143  $F_s$  to obtain more accurate results. The objectives of this study were to: 1) compare  
144 diurnal, seasonal, and spatial differences in  $[CO_2]$  fluctuations,  $F_s$ , and its uncertainty;  
145 2) examine the variation in  $F_s$  uncertainty with different  $[CO_2]$  averaging time windows;  
146 and 3) investigate the response of  $F_s$  and its uncertainty to  $[CO_2]$  fluctuations, wind  
147 above the canopy, and terrain complexity, and quantify the impact of the  $F_s$  on the NEE  
148 estimates under these conditions.

## 149 **2 Materials and methods**

### 150 2.1 Study site and instrumental set-up

151 This study was conducted in temperate forests in a watershed based on the Ker  
152 towers (Zhu et al., 2021; Gao et al., 2020), situated in northeast China ( $41^{\circ}50'N$ ,  
153  $124^{\circ}56'E$ ). The region experiences a temperate continental monsoon climate, with an  
154 average annual temperature of  $4.3^{\circ}C$  and annual rainfall of 758 mm from 2010 to 2021  
155 (Li et al., 2023). The Ker towers consist of three 50-m-high EC towers (Fig. 1) that  
156 observe a mixed broadleaved forest (MBF), a Mongolian oak forest (MOF), and a Larch  
157 plantation forest (LPF).





158

159 Fig. 1 Overview of the study area. The first map (a) depicts the topography of the study site, with  
 160 black curves indicating elevation contours, and marginal distributions represented as a gray graph,  
 161 averaged over rows and columns. The second image (b) features an aerial photograph of the  
 162 Qingyuan-Ker towers captured in the growing season (Gao et al., 2020).

163 The basic information regarding Ker towers in this study is presented in Table 1.  
 164 The CPEC310 integrated system from Campbell Scientific comprising an EC155  
 165 closed-path infrared gas analyzer (IRGA) and a CSAT3A sonic anemometer, was  
 166 employed to monitor the three-dimensional wind speed and CO<sub>2</sub>/H<sub>2</sub>O concentrations  
 167 (10 Hz). The atmospheric profiling system (AP200, Campbell Scientific Ltd., Logan,  
 168 UT, USA) was utilized to measure the CO<sub>2</sub>/H<sub>2</sub>O concentrations with eight height levels.  
 169 Each level was measured for 15 s (with 10 s for the flushing of the manifold and 5 s for  
 170 logging the average), leading to a measurement cycle of 2 min. **Due to calibration, filter**  
 171 **changes, and rugged weather, 10% CPEC data and 3% AP200 data were missed in our**

172 study period.

173 Table 1 Basic information of Ker towers

Forest	Mixed broad-leaved	Mongolian oak	Larch plantation
Experiment period	Jan 01, 2020– Dec 31, 2021	Jan 01, 2020– Dec 31, 2021	Jan 01, 2020– Dec 31, 2021
Elevation (m)	634	669	721
Slope (°)	14.8 ± 2.1	19.1 ± 2.9	16.2 ± 5.3
Canopy height (m)	21.5 ± 1.8	13.9 ± 0.6	19.5 ± 0.6
Leaf area indices	3.0 ± 0.5	3.1 ± 0.8	3.9 ± 0.6
Eddy covariance system	CPEC310	CPEC310	CPEC310
Eddy covariance sensor height (m)	46	46	36
Atmospheric profiling system	AP200	AP200	AP200
Profile heights (m)	0.5, 2, 6, 11, 16, 21, 26, 36	0.5, 2, 6, 11, 16, 21, 26, 36	0.5, 2, 6, 11, 16, 21, 26, 36

174 2.2 Calculation of storage flux

175 Averaging the [CO<sub>2</sub>] in a time window was utilized to calculate the F<sub>s</sub> values, in  
176 addition to data on the air pressure, CO<sub>2</sub>/H<sub>2</sub>O molar fractions, and air temperature at  
177 different heights above the ground surface (Finnigan, 2006; Montagnani et al., 2018;  
178 Xu et al., 2019). The molar mixing ratio and mass mixing ratio are conserved quantities  
179 with the variation of air temperature, air pressure, and water vapor concentration,  
180 whereas the molar fraction is not. This study determined the F<sub>s</sub> using the molar mixing  
181 ratio obtained from CO<sub>2</sub>/H<sub>2</sub>O molar fraction observations, applying the ideal gas law  
182 and Dalton's partial pressure law (Montagnani et al., 2009). The water vapor molar  
183 mixing ratio ( $\chi_v$ ) in mmol mol<sup>-1</sup> is given by

$$\chi_v = \frac{c_v}{1 - c_v \times 10^{-3}}, \quad (2)$$

184 where  $c_v$  is the water vapor molar fraction in  $\text{mmol mol}^{-1}$ , and the  $\text{CO}_2$  molar mixing

185 ratio ( $\chi_c$ ) in  $\mu\text{mol mol}^{-1}$  is given by

$$\chi_c = \frac{c_c}{1 - c_v \times 10^{-3}}, \quad (3)$$

186 where  $c_c$  is the  $\text{CO}_2$  molar fraction in  $\mu\text{mol mol}^{-1}$ .

187 The dry air density ( $\bar{\rho}_d$ ) in  $\text{mol m}^{-3}$  is calculated as follows:

$$\bar{\rho}_d = \frac{\bar{P}}{(\bar{T} + 273.15) \times (R^* + \chi_v \times 10^{-3} \cdot R^* \cdot M_d/M_v)}, \quad (4)$$

188 where  $R^*$  is the air gas constant ( $8.31441 \text{ Pa m}^3 \text{ K}^{-1} \text{ mol}^{-1}$ ),  $\bar{P}$  is the air pressure in

189 Pa, and  $\bar{T}$  is the average air temperature in Celsius.  $M_d$  and  $M_v$  are the dry air and

190 water vapor molar mass ( $18.015 \text{ g mol}^{-1}$ ), respectively.  $M_d$  is calculated from the  $\text{CO}_2$

191 molar mixing ratio (Khélifa et al., 2007):

$$M_d = 28.9635 + M_c \cdot (\chi_c \times 10^{-6} - 0.0004), \quad (5)$$

192 where  $M_c$  is the carbon molar mass ( $12.011 \text{ g mol}^{-1}$ ).

193 The  $F_s$  estimated from eight-level profiles are calculated as follows:

$$F_s = \bar{\rho}_d \int_0^h \frac{d\bar{\chi}_c}{dt} dz \doteq \bar{\rho}_d \sum_{i=1}^8 \frac{\Delta\bar{\chi}_{c_i} \Delta h_i}{\Delta t}, \quad (6)$$

194 where  $\bar{\chi}_c$  is the average  $\text{CO}_2$  molar mixing ratio and  $\Delta h_i$  is the height represented by

195 each level.

196 When measuring the  $F_s$  by sampling  $\text{CO}_2$  at several levels using a single analyzer,

197 the synchronous observations of  $\text{CO}_2$  profile are impractical. Consequently, discrete

198 temporal sampling and time averaging become necessary. To ensure the temporal

199 alignment of  $F_s$  with  $F_c$ , the average  $[\text{CO}_2]$  measurements within the control volume at

200 the beginning and end ( $t$ ) of an averaging period (30 min) are calculated by averaging

201 over a time window ( $\tau$  min) as follows:

$$\bar{\chi}_{c_i} = \frac{2}{\tau} \sum_{t-\frac{\tau}{2} < t \leq t+\frac{\tau}{2}} \chi_{c_i}(t), \quad (7)$$

202 where  $\tau = 4, 8, \dots, 28$  min. Theoretically, the time window should be kept as short as  
203 possible in comparison to the turbulence flux averaging period to comply with the  
204 principle of Reynolds decomposition. We use large windows here for CO<sub>2</sub> averaging in  
205 an attempt to demonstrate the effects of different window sizes on the accuracy of  
206 storage flux estimates.

### 207 2.3 Data analysis

208 To evaluate the impact of [CO<sub>2</sub>] fluctuations on F<sub>s</sub> measurements and its  
209 corresponding uncertainty, empirical modal decomposition (EMD) and Fourier  
210 spectrum analysis (FSA) were used to extract the period and amplitude of fluctuations  
211 in the high-frequency [CO<sub>2</sub>] time series (10 Hz). EMD was used to decompose the [CO<sub>2</sub>]  
212 time series into intrinsic mode functions based on local signal properties (Huang and  
213 Wu, 2008), which yield instantaneous frequencies as functions of time, allowing for the  
214 identification of embedded structures of eddies. EMD is applicable to non-linear and  
215 non-stationary processes (Huang et al., 1998). The period and amplitude of [CO<sub>2</sub>]  
216 fluctuations above the forest canopies reflected the eddy size. Subsequently, the  
217 maximum period and amplitude of [CO<sub>2</sub>] fluctuations in a short term (2h) was  
218 indicative of large eddies under the influence of gust.

219 Due to the diurnal and seasonal variability of flux measurements, this study  
220 defined the transition period and growing season. The solar elevation angle was used

221 to define the transition period as 1-h before sunrise (sunset) to 2-h after sunrise (sunset).  
222 The growing degree days (GDDs) were calculated using the base temperature ( $T_{base}$ ) to  
223 determine the beginning and end of the growing season, and the formula was as follows  
224 (Mcmaster and Wilhelm, 1997):

$$GDD = \frac{1}{2}(T_{max} + T_{min}) - T_{base}, \quad (8)$$

225 where  $T_{base}$  is 6°C. Considering the persistent demand of temperature to support  
226 vegetation growth, the fourth day of the first GDD greater than zero (less than zero)  
227 over a span of five consecutive days was defined as the starting (ending) time of the  
228 growing season.

229 The main data processing and analysis steps are outlined below:

230 1. EMD and Fourier spectrum analysis of  $[CO_2]$  high-frequency time series were  
231 used to extract the maximum amplitude ( $A_m$ ) and corresponding period ( $P_m$ ) of  $[CO_2]$   
232 fluctuations every 2 h. The data were divided into two subsets based on  $P_m$ , with a cut-  
233 off of 150 s.

234 2.  $CO_2$  storage fluxes were calculated for different  $[CO_2]$  averaging time windows  
235 ( $\tau$ ), ranging from 4 to 28 min in increments of 4 min.

236 3. The standardized major axis (SMA) regression model (Warton et al., 2012) was  
237 used to compare the slope differences (bias) between  $F_{s_\tau}$  and  $F_{s_{28}}$  for different  $P_m$  and  
238 the forest stands. The SMA model offers routines for comparing parameters  $a$  and  $b$   
239 among groups for symmetric problems.

240 4. The normalized root mean square error (NRMSE) and slope were used to  
241 evaluate the relative error and bias between  $F_{s_\tau}$  and  $F_{s_{28}}$ . The NRMSE is calculated as

242 follows:

$$NRMSE = 100 \times \sqrt{\frac{\sum_{i=1}^N (F_{s_\tau}^{(i)} - F_{s_{28}}^{(i)})^2}{\sum_{i=1}^N (F_{s_{28}}^{(i)} - \overline{F_{s_{28}}})^2}} \quad (9)$$

243 where  $i$  indicates the  $i^{\text{th}}$  observation.

244 5. The normalized weighting coefficient ( $w$ ) of  $F_{s_\tau}$  was estimated based on the  
245 NRMSE and slope (Wang et al., 2020). The details are shown in Appendix A1. Then,  
246 using the decision-level fusion model,  $F_{s\_comb}$  was calculated as follows:

$$F_{s\_comb} = w_1^* \cdot F_{s_4} + w_2^* \cdot F_{s_8} + \dots + w_7^* \cdot F_{s_{28}} \quad (10)$$

247 The decision-level fusion model automatically assigned weights to the  $F_s$  based on  
248 different  $[\text{CO}_2]$  averaging time windows. Its purpose in this study was to balance the  
249 relative error and bias of  $F_s$  estimates caused by  $[\text{CO}_2]$  sampling. The analysis was  
250 performed using the EMD and smatr R packages (Warton et al., 2012; Huang et al.,  
251 1998).

## 252 2.4 Uncertainty analysis

253 To improve the accuracy of estimating the uncertainty of  $F_s$  using individual tower,  
254 this work has made modifications to the 24-h difference method by extending the  
255 sampling time windows and applying meteorological condition constraints (Hollinger  
256 and Richardson, 2005). This method trades time for space to estimate the uncertainty  
257 of  $F_s$ . To determine the uncertainty of  $F_s$ , expressed as  $\sigma(\varepsilon_s)$ , in this case, we compared  
258 the observations at moment  $i$  within a day to the average of several observations during  
259 a similar period and with similar meteorological conditions. The specific computations  
260 were as follows:

$$\bar{F}_s^{(i)} = \frac{1}{N} \sum_{t \in \Omega, \lambda_t \in \Lambda} I(\lambda_t) \cdot F_s^{(t)}, \quad (11)$$

$$\Lambda = \{\lambda_t | \sqrt{\frac{(u_*^{(\lambda_t)} - u_*^{(i)})^2}{\sigma_{u_*}} + \frac{(\text{Ta}(\lambda_t) - \text{Ta}^{(i)})^2}{\sigma_{\text{Ta}}} + \frac{(\text{H}(\lambda_t) - \text{H}^{(i)})^2}{\sigma_{\text{H}}}} < \delta\}, \quad (12)$$

$$\varepsilon_s^{(i)} = F_s^{(i)} - \bar{F}_s^{(i)}, \quad (13)$$

$$\bar{\varepsilon}_s^{(i)} = \frac{1}{N} \sum_{t \in \Omega, \lambda_t \in \Lambda} I(\lambda_t) \cdot \varepsilon_s^{(t)}, \quad (14)$$

$$\sigma(\varepsilon_s)^{(i)} = \sqrt{\frac{1}{N} \sum_{t \in \Omega, \lambda_t \in \Lambda} I(\lambda_t) \cdot (\varepsilon_s^{(t)} - \bar{\varepsilon}_s^{(i)})^2}, \quad (15)$$

261 where  $\Omega$  was the moment interval ( $i-0.5$  h,  $i+0.5$  h) within a certain time window (15  
 262 d);  $I$  was indicator function; the set  $\Lambda$  represented consisted of elements that meet  
 263 similar meteorological conditions, including the  $u_*$ , air temperature (Ta), and sensible  
 264 heat flux (H);  $\sigma_{u_*}$ ,  $\sigma_{\text{Ta}}$ , and  $\sigma_{\text{H}}$  are the standard deviation of the  $u_*$ , Ta, and H,  
 265 respectively;  $\delta$  was the threshold of Euclidean distance; and  $\varepsilon_s$  was the random error  
 266 of  $F_s$ .

267 After estimating the uncertainty of  $F_s$ , this study extended the work conducted by  
 268 Richardson et al. (2008) to analyze its relationship with the magnitude of flux  
 269 measurements ( $|F_s|$ ),  $[\text{CO}_2]$  fluctuations ( $A_m$  and  $P_m$ ),  $u_*$ , and terrain complexity index  
 270 (TCI). A comprehensible description of the TCI can be found in Appendix A2. This  
 271 relationship can be approximated by using the following equation:

$$\sigma(\varepsilon_s) = \beta_0 + \sum_{i=1} \beta_i \cdot x_i, \quad (16)$$

272 where the nonzero intercept term  $\beta_0$  indicates the size of the random uncertainty as  
 273  $x_i$  approaches 0, which varies with the observation site, with larger value of  $\beta_0$

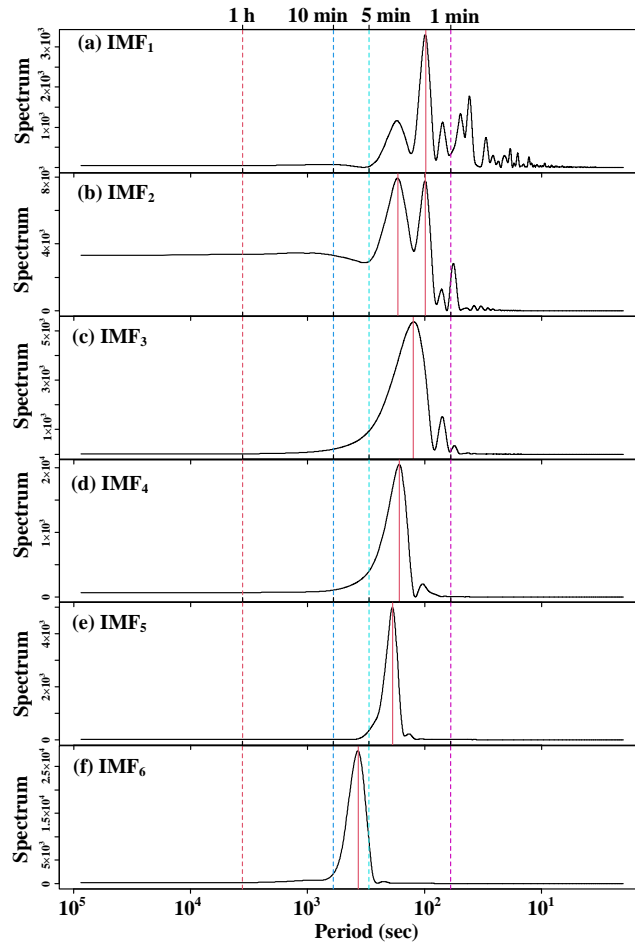
274 indicating greater uncertainty. The slope term  $\beta_i$  indicates the sensitivity of the size of  
275 the random uncertainty of  $x_i$ , with smaller  $\beta_i$  values indicating a probability  
276 distribution of uncertainty closer to white noise.

## 277 **3 Results**

### 278 3.1 Characterization of [CO<sub>2</sub>] fluctuation and F<sub>s</sub> variations

279 The [CO<sub>2</sub>] high-frequency time series above the forest canopies were decomposed  
280 using EMD, followed by spectral analysis to extract the fluctuation period and  
281 amplitude of [CO<sub>2</sub>] at different time scales. As depicted in Fig. 2, it became evident that  
282 the [CO<sub>2</sub>] above the canopies displayed short-term fluctuations with periods ranging  
283 from 1 to 10 min, and the amplitude of these fluctuations showed an increasing trend  
284 with longer periods. This observation strongly suggested the presence of large eddies  
285 influenced by gusts above the canopies, and these eddies were responsible for the  
286 increasing amplitude of [CO<sub>2</sub>] fluctuations as their size increased.





287

288 Fig. 2 Power spectral density of the intrinsic mode function (IMF) of above-canopy CO<sub>2</sub>  
 289 concentrations in the Mongolian oak forest on July 2, 2020 (24 h).

290 To examine the spatio-temporal variations in large eddies, this study compared the  
 291  $A_m$  and  $P_m$  values above canopies across different forest stands. The analysis utilized  
 292 data from daytime, nighttime, and transition periods in both the growing and dormant  
 293 seasons. The averages of  $A_m$  and  $P_m$  averages for the above-canopy [CO<sub>2</sub>] in the three  
 294 forest stands ranged from 1.588 to 136.667 ppm and from 2.313 to 2.784 min,  
 295 respectively (Table 2). Fig. 3 demonstrated significant seasonal and diurnal differences  
 296 ( $P < 0.01$ ) in  $P_m$ , with higher values during daytime in the growing season, and lower  
 297 values during the daytime in the dormant season. Moreover,  $P_m$  was significantly  
 298 different ( $P < 0.01$ ) among different forest stands during the same time period, with

299 MBF stand having the highest values, followed by the MOF, and the lowest values in  
 300 the LPF. During the growing season, the  $A_m$  values were significantly higher than those  
 301 during the dormant season, with both daytime and nighttime values also exhibiting  
 302 significant differences ( $P < 0.01$ ) among different forest stands. This observation  
 303 provided evidence of significant spatio-temporal variability in large eddies influenced  
 304 by gusts.

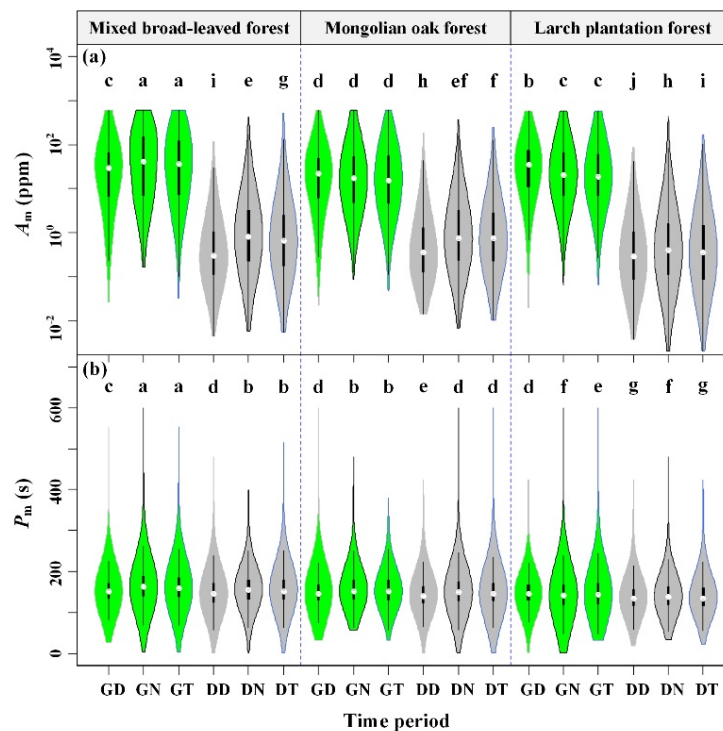
305 Table 2 Mean of the  $A_m$  in ppm and  $P_m$  in second (s) for three forest stands at different  
 306 periods

Variable	Tower site	Growing season			Dormant season		
		DT <sup>1</sup>	NT <sup>2</sup>	TP <sup>3</sup>	DT	NT	TP
$A_m$ <sup>4</sup> (ppm)	MBF <sup>6</sup>	57.932	<b>139.667</b>	136.717	2.219	5.212	4.944
	MOF <sup>7</sup>	36.160	57.945	55.777	2.699	5.175	4.637
	LPF <sup>8</sup>	52.688	58.816	60.147	<b>1.588</b>	2.985	2.456
$P_m$ <sup>5</sup> (s)	MBF	154.563	<b>167.024</b>	164.824	158.449	151.428	158.121
	MOF	151.986	160.633	159.146	153.091	147.491	153.274
	LPF	149.003	143.950	145.696	143.458	<b>138.794</b>	142.009

307 <sup>1</sup> DT represents daytime; <sup>2</sup> NT represents nighttime; <sup>3</sup> TP represents transition period. <sup>4</sup>  $A_m$   
 308 represents the maximum amplitude of short-term CO<sub>2</sub> concentration fluctuations; <sup>5</sup>  $P_m$  represents  
 309 the corresponding period of maximum amplitude. <sup>6</sup> MBF represents mixed broad-leaved forest; <sup>7</sup>  
 310 MOF represents Mongolian oak forest; <sup>8</sup> LPF represents Larch plantation forest.

311 To estimate the uncertainty of  $F_s$  using an individual tower, a comprehensive  
 312 analysis of its diurnal and seasonal dynamics, as well as the functional relationship  
 313 between  $F_s$  and  $u^*$ , was necessary. **Significant diurnal variations and seasonal**  
 314 **differences in  $F_s$  were observed across the three forest stands, as shown in Fig. 4.** During  
 315 the growing season, the median diurnal variation of  $F_s$  for the three forest stands ranged  
 316 from  $-2.960$  to  $2.647 \mu\text{mol m}^{-2} \text{s}^{-1}$ , whereas during the dormant season, it ranged from

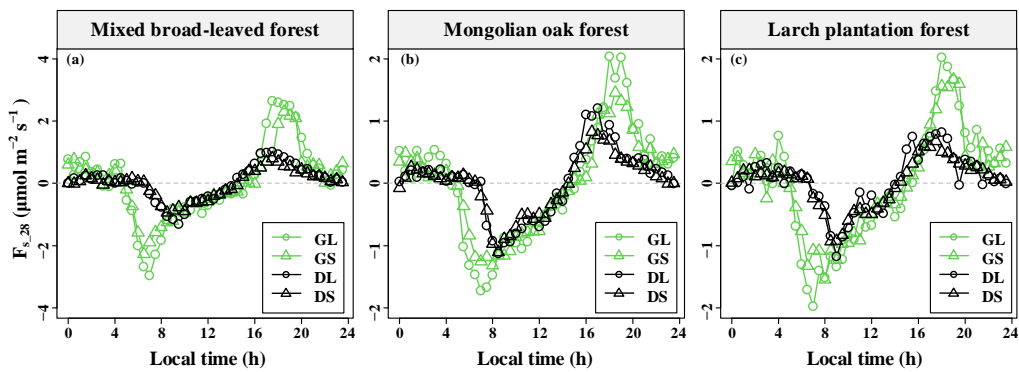
317  $-1.306$  to  $1.012 \mu\text{mol m}^{-2} \text{s}^{-1}$ . Comparing the extent of  $F_s$  diurnal variation among the  
 318 three forest stands, MBF exhibited the largest extent during the growing season, while  
 319 the extent of the three forest stands were similar during the dormant season. Notably, it  
 320 was observed that the amplitudes for longer  $P_m$  values were greater than those for  
 321 shorter  $P_m$  values. This observation indicated that the larger the eddies, the greater the  
 322 magnitude of  $F_s$ .



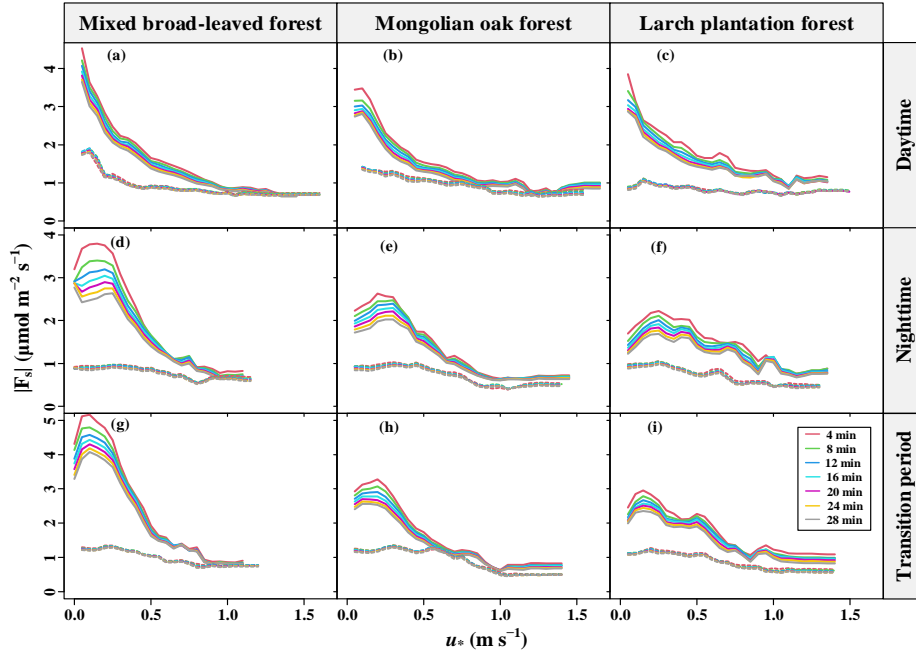
323  
 324 Fig. 3 Maximum amplitude ( $A_m$ ) (a) and corresponding period ( $P_m$ ) (b) of short-term CO<sub>2</sub>  
 325 concentration fluctuations in different forest stands for seasonal and diurnal variations, where GD,  
 326 GN, GT, DD, DN, and DT denote the growing season daytime, growing season nighttime,  
 327 growing season transition period, dormant season daytime, dormant season nighttime, and  
 328 dormant season transition period, respectively. Columns with different lowercase letters are  
 329 significantly different ( $P < 0.05$ ) according to Fisher's least significant difference test.

330 Furthermore, a  $u^*$  threshold value was identified for the variation of  $F_s$  with  $u^*$   
 331 during daytime in both the dormant and growing seasons (Fig. 5). When  $u^*$  fell below  
 332 the  $u^*$  threshold, the magnitude of  $F_s$  ( $|F_s|$ ) decreased with increasing  $u^*$ . Conversely,

333 when  $u^*$  exceeded the  $u^*$  threshold, the  $|F_s|$  tended to remain relatively constant. Notably,  
 334 a maximum point for the  $|F_s|$  was observed when the  $u^*$  was less than 0.5 m/s during the  
 335 growing season, whereas not during the dormant season. This phenomenon was  
 336 particularly evident during the nighttime and transition periods of the growing season,  
 337 where  $|F_s|$  exhibited an initial increase followed by a subsequent decrease with  $u^*$ . These  
 338 observations strongly indicated that the effect of the turbulent mixing strength on the  
 339  $|F_s|$  over complex terrains was nonlinear and exhibited diurnal and seasonal differences.



340  
 341 Fig. 4 Median diurnal variation of CO<sub>2</sub> storage flux ( $F_s$ ) based on 28-min CO<sub>2</sub> concentration  
 342 averaging time windows in the three forest stands during different seasons. GS indicates the  
 343 growing season and a short period of maximum amplitude ( $P_m$ ), GL indicates the growing season  
 344 and a long  $P_m$ , DS indicates the dormant season and a short  $P_m$ , and DL indicates the dormant  
 345 season and a long  $P_m$ .



346

347 Fig. 5 Magnitudes of CO<sub>2</sub> storage flux ( $|F_s|$ ) determined with different CO<sub>2</sub> concentration average  
 348 time windows as a function of the friction velocity ( $u^*$ ) and moving block averages from all 30-  
 349 min data for the years 2020-2021. Dashed and solid lines indicate the dormant and growing  
 350 seasons, respectively.

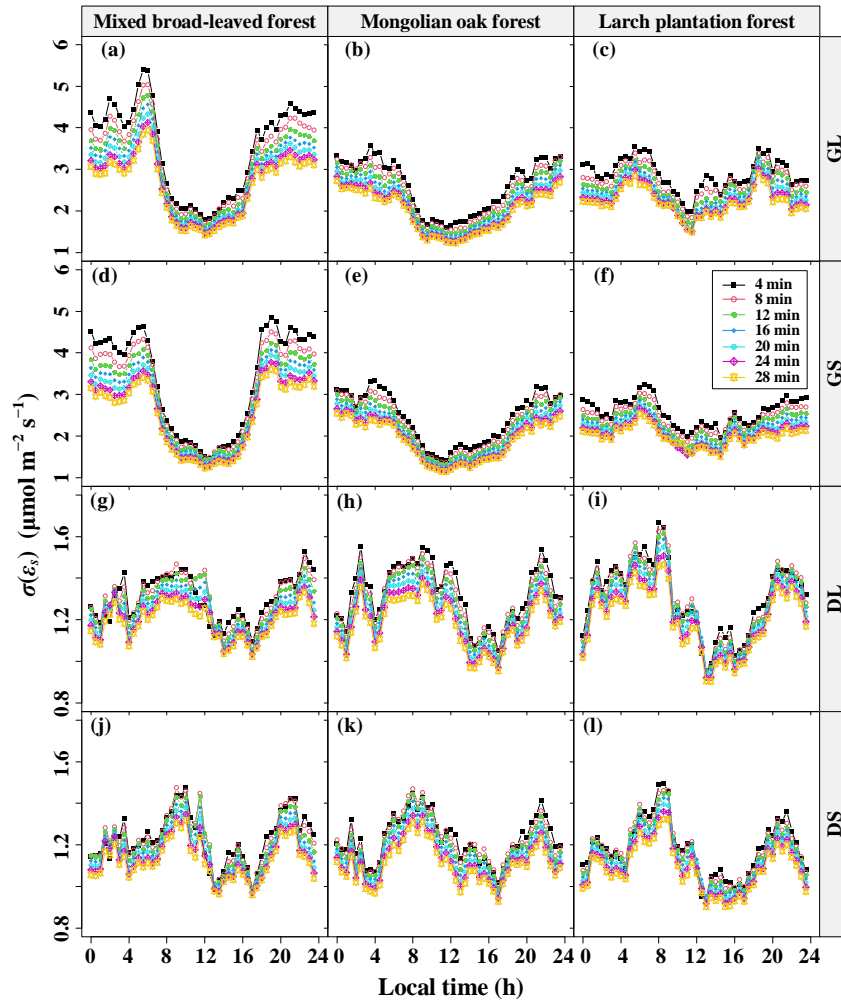
### 351 3.2 Effect of [CO<sub>2</sub>] fluctuations on the $F_s$ and its uncertainty

352 To investigate the influence of the [CO<sub>2</sub>] fluctuation periods on the error of  $F_s$   
 353 measurement, this study computed the diurnal average of the standard deviation  $\sigma(\varepsilon_s)$   
 354 of the 30-min  $F_s$  uncertainty ( $\varepsilon_s$ ) separately for different  $P_m$  values and the seasons. The  
 355 overall distribution of  $\varepsilon_s$  showed a non-normal distribution with a high peak (kurtosis >  
 356 2 and  $P < 0.05$ , results presented in Supplementary Table 1–4). The daily variation  
 357 curves of  $\sigma(\varepsilon_s)$  at various [CO<sub>2</sub>] averaging time windows are presented in Fig. 6. It  
 358 was observed that the diurnal variation range of  $\sigma(\varepsilon_s)$  was higher during the growing  
 359 season compared to the dormant season, regardless of the  $P_m$  lengths, indicating a  
 360 seasonal difference independent of the  $P_m$ . Additionally, during the growing season,  
 361 both MBF and MOF demonstrated evident diurnal variation in  $\sigma(\varepsilon_s)$ , with the peak

362 occurring at night and the trough during the daytime. The diurnal variation range of  
363  $\sigma(\varepsilon_s)$  varied across the three forest stands, with MBF exhibiting the largest amplitude.

364 Furthermore, a significantly positive correlation was observed between  $\sigma(\varepsilon_s)$  the  
365  $|F_s|$  ( $P < 0.01$ ), with site, seasonal, and diurnal differences (Fig. 7). **The relationship**  
366 **between  $\sigma(\varepsilon_s)$  the  $|F_s|$  was characterized by intercepts and slopes ranging from 1.99**  
367 **to 2.82  $\mu\text{mol m}^{-2} \text{s}^{-1}$  and from 0.24 to 0.28, respectively (results presented in the**  
368 **Supplementary Tables 5–6).** Both decreased as the  $[\text{CO}_2]$  averaging time window  
369 increased, with the growing season exhibiting larger values compared to the dormant  
370 season (results shown in the Supplementary Tables 5–6). These findings suggested that  
371 increasing the  $[\text{CO}_2]$  averaging time window, results in a reduction of the random error  
372 in  $F_s$  and the correlation coefficient between  $\sigma(\varepsilon_s)$  and  $|F_s|$ . This indicated a decrease  
373 in variability of  $\sigma(\varepsilon_s)$  and a behavior similar to white noise.

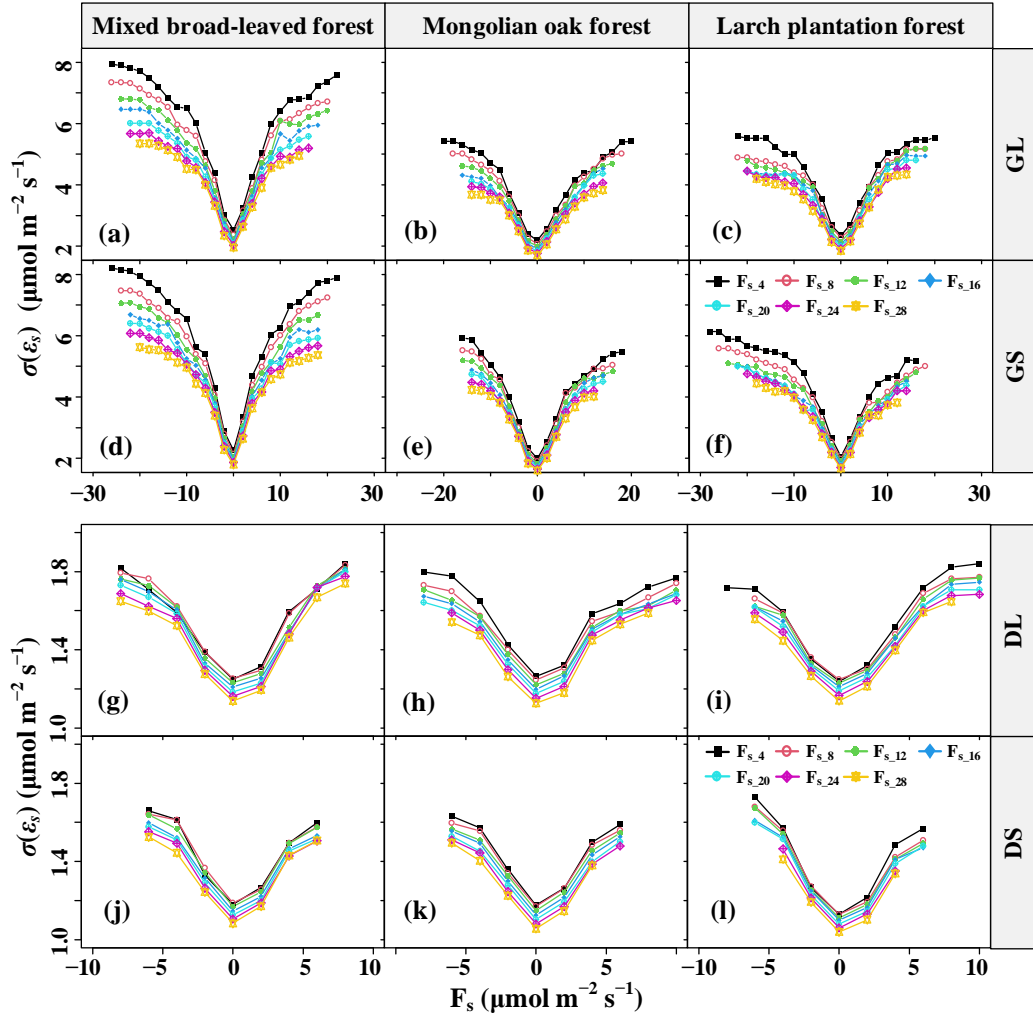
374 To assess the impact of  $[\text{CO}_2]$  fluctuations on the error and bias of  $F_s$  measurement,  
375 this study compared the NRMSE and slopes of  $F_s$  based on different  $[\text{CO}_2]$  averaging  
376 time windows, with reference to the baseline  $F_{s\_28}$ , across various  $P_m$  values, time  
377 periods, and sites. As shown in Fig. 8, the NRMSE decreased and approached  
378 convergence as the  $[\text{CO}_2]$  averaging time windows increased. During both daytime and  
379 nighttime in the growing season, the NRMSE corresponding to longer  $P_m$  was greater  
380 than that corresponding to shorter  $P_m$ , while the opposite trend was observed during the  
381 dormant season. Additionally, the longer the  $[\text{CO}_2]$  averaging time window, the greater  
382 the relative underestimation of  $F_s$ .



383

384 Fig. 6 Diurnal variations in the random uncertainty ( $\sigma(\varepsilon_s)$ ) of  $\text{CO}_2$  storage flux ( $F_s$ ) errors ( $\varepsilon_s$ ) at  
 385 different  $\text{CO}_2$  concentration ( $[\text{CO}_2]$ ) averaging time windows and their seasonal differences, where

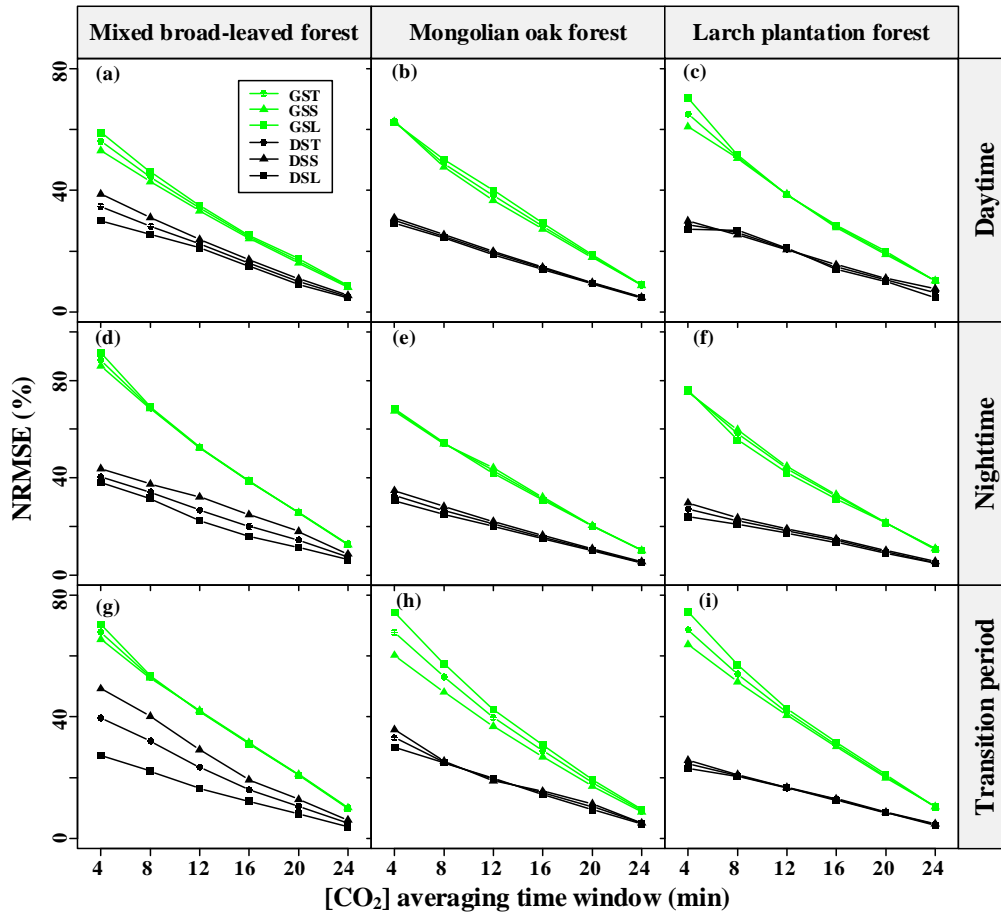
386 GS indicates the growing season and a short period of maximum amplitude ( $P_m$ ) of  $[\text{CO}_2]$   
 387 fluctuations, GL indicates the growing season and a long  $P_m$ , DS indicates the dormant season and  
 388 a short  $P_m$ , and DL indicates the dormant season and a long  $P_m$ .



389

390 Fig. 7 Random uncertainty  $\sigma(\varepsilon_s)$  of  $\text{CO}_2$  storage flux ( $F_s$ ) errors ( $\varepsilon_s$ ) at different  $\text{CO}_2$   
 391 concentration ( $[\text{CO}_2]$ ) averaging time windows as a function of the  $F_s$  magnitude for mixed broad-  
 392 leaved forest, Mongolian oak forest, and Larch plantation forest during the growing and dormant  
 393 seasons. GS indicates the growing season and a short period of maximum amplitude ( $P_m$ ) of  $[\text{CO}_2]$   
 394 fluctuations, GL indicates the growing season and a long  $P_m$ , DS indicates the dormant season and  
 395 a short  $P_m$ , and DL indicates the dormant season and a long  $P_m$ .





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Fig. 8 Seasonal and diurnal differences in the normalized root mean square error (NRMSE) of  $F_s$  versus the respective  $F_{s,28}$  values for different  $CO_2$  concentration ( $[CO_2]$ ) averaging time windows. GST indicates the growing season and does not distinguish the period of maximum amplitude ( $P_m$ ) of  $[CO_2]$  fluctuations, GSS indicates the growing season and a short  $P_m$ , GSL indicates the growing season and a long  $P_m$ , DST indicates the dormant season and does not distinguish  $P_m$ , DSS indicates the dormant season and a short  $P_m$ , and DSL indicates the dormant season and a long  $P_m$ .

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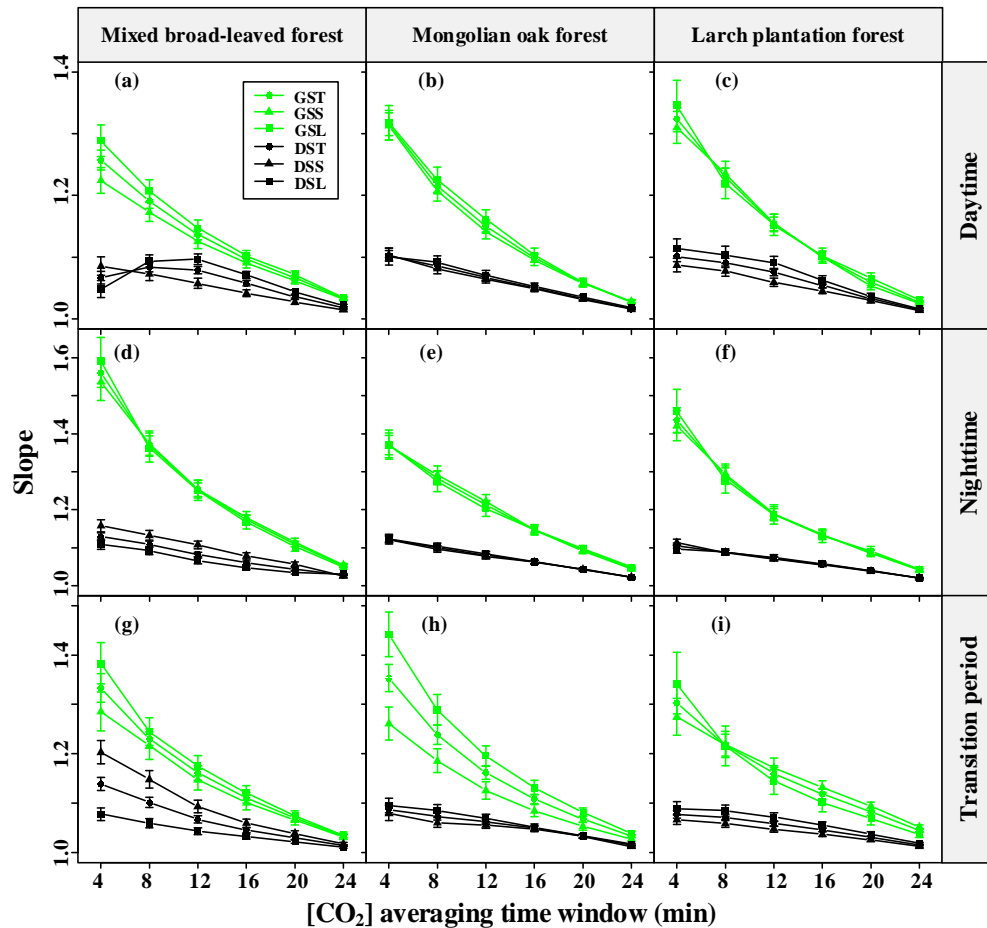
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The comparison of slopes between  $F_{s,4}$  and  $F_{s,28}$  in the three forest stands revealed interesting patterns, as depicted in Fig. 9. During the growing season, the slopes corresponding to the shorter  $P_m$  of  $[CO_2]$  fluctuations were consistently lower than those for the longer  $P_m$ , indicating that the effect of  $P_m$  on  $F_s$  uncertainty decreased with increasing  $[CO_2]$  averaging time windows. However, for the MBF stand (Fig. 9d and Fig. 9g), the slopes corresponding to the shorter  $P_m$  of  $[CO_2]$  fluctuations during the dormant season nighttime were actually greater than those for the longer  $P_m$ , primarily

411 due to diurnal variations in the daily dynamics of  $F_s$ . Overall, the influence of  $P_m$  on  $F_s$   
 412 uncertainty decreased with increasing  $[CO_2]$  averaging time windows. This suggested  
 413 that averaging  $[CO_2]$  reduced the effect of gusts on the random uncertainty in estimating  
 414  $F_s$ , but led to a systematic underestimation of  $F_s$ .



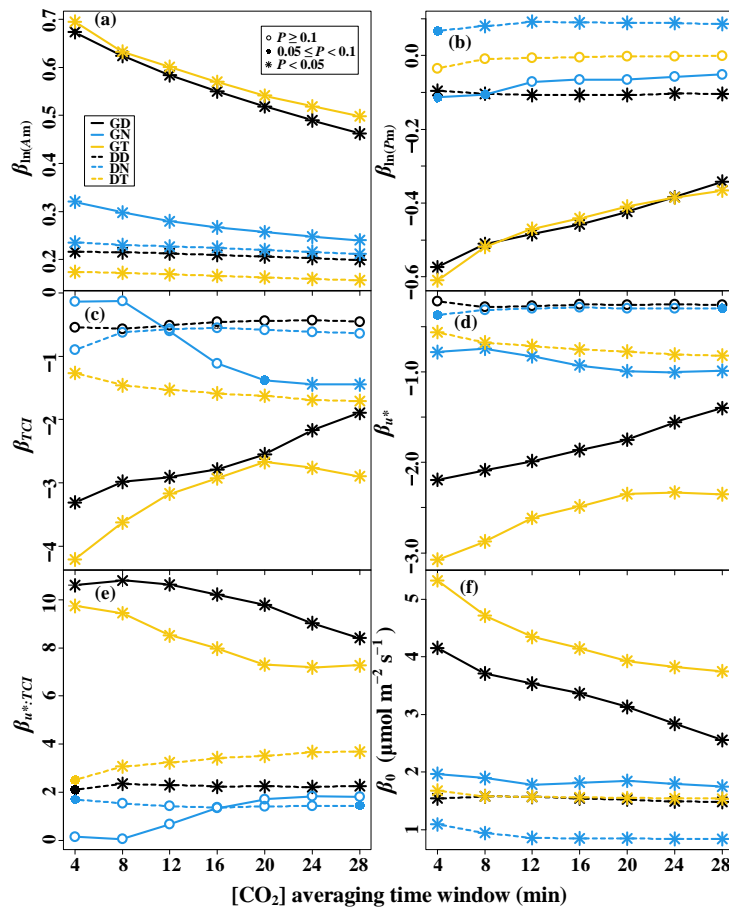
415  
 416 Fig. 9 Seasonal and diurnal differences in the slope of  $CO_2$  storage flux ( $F_s$ ) versus the  $F_{s,28}$  for the  
 417 different  $CO_2$  concentration ( $[CO_2]$ ) averaging time windows. GST indicates the growing season  
 418 and does not distinguish the period of maximum amplitude ( $P_m$ ) cases, GSS indicates the growing  
 419 season and a short  $P_m$ , GSL indicates the growing season and a long  $P_m$ , DST indicates the  
 420 dormant season and does not distinguish  $P_m$ , DSS indicates the dormant season and a short  $P_m$ ,  
 421 and DSL indicates the dormant season and a long  $P_m$ .

422 To analyze the effect of  $[CO_2]$  fluctuations on  $|F_s|$  in complex terrains, this study  
 423 developed a multiple linear regression model, considering the interaction effects of  
 424 turbulent mixing and terrain complexity on  $|F_s|$ , as shown in Fig. 10.  $A_m$  exhibited a

425 significant positive correlation with  $|F_s|$  in all time periods ( $P < 0.05$ ). Conversely,  $P_m$   
426 showed a significant negative correlation with  $|F_s|$  during the dormant season daytime,  
427 the growing season daytime, and the transition periods ( $P < 0.05$ ). Additionally, their  
428 correlation coefficient decreased with increasing  $\tau$ . In Fig. 10d and Fig. 10e, a  $u^*$   
429 threshold was observed during the growing season nighttime. When the  $u^*$  was below  
430 the threshold, higher TCI values resulted in smaller  $|F_s|$ ; whereas when the  $u^*$  was above  
431 the threshold, higher TCI values led to larger  $|F_s|$ . During the growing season nighttime  
432 and transition periods,  $u^*$  showed a significant negative correlation ( $P < 0.05$ ) with  $|F_s|$ ,  
433 and the correlation coefficient decreased with increasing TCI values. These  
434 observations suggested that the effect of turbulent mixing on the  $|F_s|$  uncertainty was  
435 regulated by terrain complexity.

436 A multiple linear regression model was used to analyze the effect of  $[CO_2]$   
437 fluctuations on the random uncertainty of  $F_s$ ,  $\sigma(\varepsilon_s)$ , in complex terrains. This model  
438 considered the interaction effects of  $[CO_2]$  fluctuations and terrain complexity on  
439  $\sigma(\varepsilon_s)$ , as shown in Fig. 11. As evident from Fig. 11a and Fig. 11e, the  $A_m$  exhibited a  
440 significant positive correlation ( $P < 0.05$ ) with  $\sigma(\varepsilon_s)$  during both the dormant season's  
441 nighttime and the growing season. Throughout the transition period of the growing  
442 season,  $P_m$  displayed a significant negative correlation with  $\sigma(\varepsilon_s)$  ( $P < 0.05$ ). The  
443 magnitude of these correlation coefficients decreased with the increasing  $[CO_2]$   
444 averaging time windows. During the transition period of the dormant season, a TCI  
445 threshold was observed, with  $P_m$  showing a significant positive correlation ( $P < 0.05$ )  
446 with  $\sigma(\varepsilon_s)$  when the TCI was below the threshold, and a significantly negative

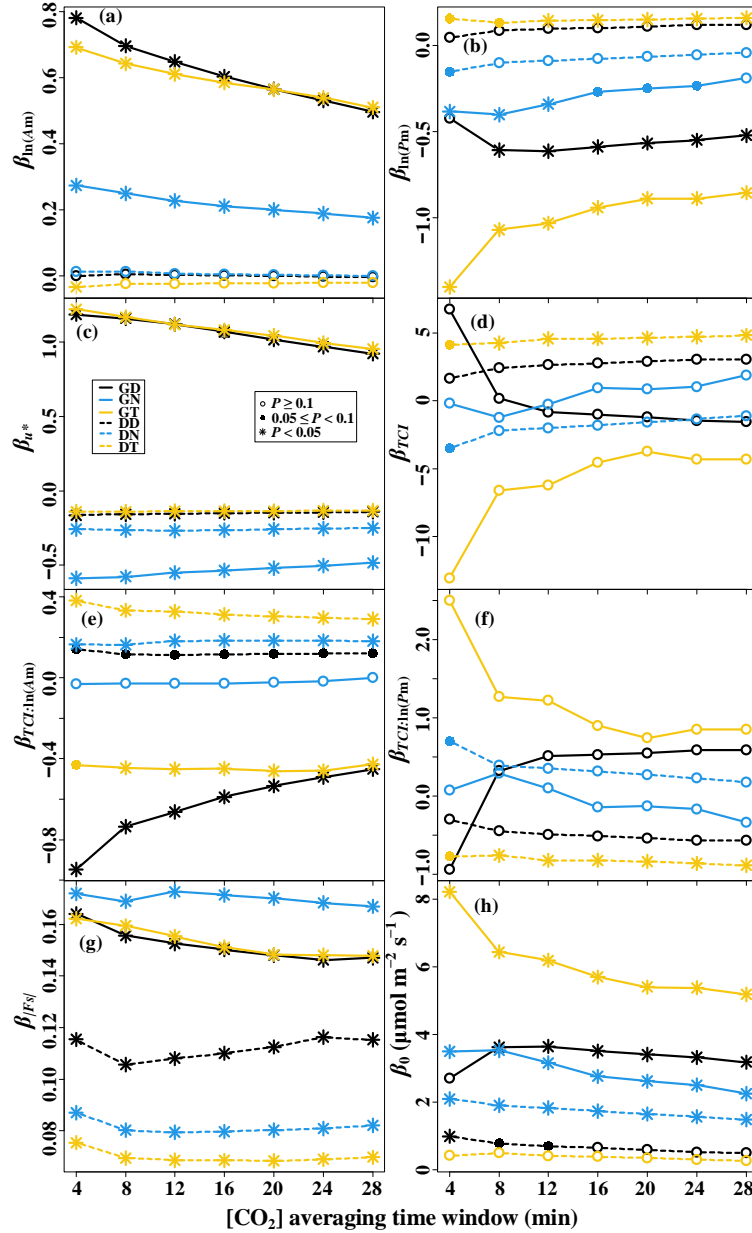
447 correlation ( $P < 0.05$ ) with  $\sigma(\varepsilon_s)$  when the TCI exceeded the threshold (Fig. 11b and  
 448 Fig. 11f). The  $u^*$  showed a significantly negative correlation with  $\sigma(\varepsilon_s)$  during the  
 449 daytime and transition periods of the growing season ( $P < 0.05$ ), while in other time  
 450 periods,  $u^*$  was significantly positively correlated with  $\sigma(\varepsilon_s)$  ( $P < 0.05$ ). The  $|F_s|$   
 451 demonstrated a significant positive correlation with  $\sigma(\varepsilon_s)$  ( $P < 0.05$ ) in all time  
 452 periods, with its correlation coefficient being greater during the growing season than  
 453 during the dormant season. These observations suggested that the relationship between  
 454 the random uncertainty in  $F_s$  and  $[\text{CO}_2]$  fluctuations was moderated by topographic  
 455 complexity. Increasing the  $[\text{CO}_2]$  averaging time window reduced the effect of  $[\text{CO}_2]$   
 456 fluctuations on the random uncertainty in  $F_s$ .



457

458 Fig. 10 Linear regression coefficients of the  $\text{CO}_2$  storage flux ( $F_s$ ) magnitude—driving factors

459 relationships for the seven CO<sub>2</sub> concentration ([CO<sub>2</sub>]) averaging time windows. The predictors of of  
 460 the multiple linear models are (a) the logarithm of maximum amplitude of [CO<sub>2</sub>] fluctuations  
 461 (ln(A<sub>m</sub>)), (b) the logarithm of the corresponding period of maximum amplitude (ln(P<sub>m</sub>)), (c) the  
 462 terrain complexity index (TCI), (d) the friction velocity (u\*), and (e) the interaction term of TCI  
 463 and u\*, respectively. (f) β<sub>0</sub> represents the intercept term.



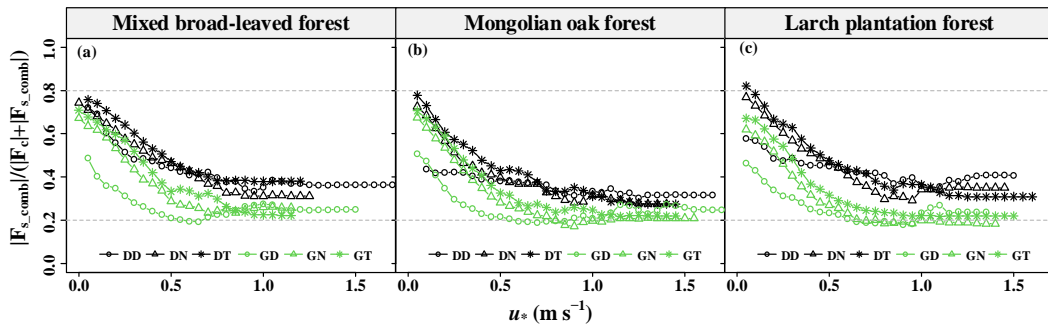
464

465 Fig. 11 Linear regression coefficients of the random uncertainty of CO<sub>2</sub> storage flux ( $\sigma(\varepsilon_s)$ )—  
 466 driving factors relationships determined with Eq. (11) for the seven CO<sub>2</sub> concentration ([CO<sub>2</sub>])  
 467 averaging time windows. The predictors of the multiple linear models are (a) the logarithm of  
 468 maximum amplitude of [CO<sub>2</sub>] fluctuations (ln(A<sub>m</sub>)), (b) the logarithm of the corresponding period  
 469 of maximum amplitude (ln(P<sub>m</sub>)), (c) the terrain complexity index (TCI), (d) the friction velocity

470 ( $u^*$ ), (e) the interaction term of TCI and  $\ln(A_m)$ , (f) the interaction term of TCI and  $\ln(P_m)$ , and the  
 471 magnitude of storage flux ( $|F_s|$ ), respectively. (h) The intercept term is represented by  $\beta_0$ .

### 472 3.3 Effect of CO<sub>2</sub> storage fluxes uncertainty on NEE observations

473 The 30-min  $F_{s\_comb}$  was obtained by weighing the bias and random error of  $F_s$  using  
 474 different [CO<sub>2</sub>] averaging time windows and  $P_m$  values. This study then focused on the  
 475 magnitude of  $F_{s\_comb}$  in relation to the  $F_c$  magnitude and its diurnal, seasonal, and site  
 476 variations. To assess the significance of  $F_s$  in NEE observations, the relative  
 477 contribution ratio of  $F_{s\_comb}$  magnitude ( $|F_{s\_comb}|/(|F_c|+|F_{s\_comb}|)$ ) was employed. The  
 478  $|F_{s\_comb}|/(|F_c|+|F_{s\_comb}|)$  showed a decreasing trend to convergence with increasing  $u^*$   
 479 (Fig. 12). On average, the  $|F_{s\_comb}|/(|F_c|+|F_{s\_comb}|)$  ranged from 17.2% to 82.0%, with a  
 480 higher value during the dormant season compared to the growing season. This indicated  
 481 that as turbulence intensity increased, the contribution of  $F_s$  to the NEE in forests  
 482 decreased to a constant value. Nevertheless, even under strong turbulence intensity,  $F_s$   
 483 still played a significant role in the NEE observations of forests in complex terrains.



484  
 485 Fig. 12 Relative contribution ratio of the CO<sub>2</sub> storage flux magnitude ( $|F_{s\_comb}|/(|F_c|+|F_{s\_comb}|)$ )  
 486 determined by decision-level fusion model as a function of the friction velocity ( $u^*$ ) moving block  
 487 averages from all 30-min data for the years 2020–2021. GD represents the growing season's  
 488 daytime; GN represents the growing season's nighttime; GT represents the growing season's  
 489 transition period; DD represents the dormant season's daytime; DN represents the dormant  
 490 season's nighttime; DT represents the dormant season's transition period.

491 As indicated in Table 3, both  $P_m$  and TCI exhibited a significant positive

492 correlation with  $|F_{s\_comb}|/(|F_c|+|F_{s\_comb}|)$  ( $P < 0.05$ ), while both  $A_m$  and  $u^*$  showed a  
493 significant negative correlation with  $|F_{s\_comb}|/(|F_c|+|F_{s\_comb}|)$  ( $P < 0.05$ ). Notably,  
494 seasonal variations in correlation coefficients were observed. The correlation between  
495 the  $u^*$  and  $|F_{s\_comb}|/(|F_c|+|F_{s\_comb}|)$  was more pronounced during both the dormant  
496 season's transition period and the growing season, and it decreased with increasing TCI  
497 values during the dormant season's daytime and nighttime.

498 Table 3 Linear regression coefficients of the relative contribution ratio of  $F_{s\_comb}$   
499 magnitudes to NEE observations ( $|F_{s\_comb}|/(|F_c|+|F_{s\_comb}|)$ ) —driving factors  
500 relationships for the six time periods.

Time period	$\beta_0$	$\ln(P_m)^7$	$\ln(A_m)^8$	$u^*{}^9$	TCI <sup>10</sup>	$u^*:TCI$	$R^2$
Total	0.292 ***	0.048 ***	-0.037 ***	-0.334 ***	0.790 ***	-1.018 ***	0.278 ***
GD <sup>1</sup>	0.299 ***	0.016	-0.041 ***	-0.183 ***	-0.293 *	0.239	0.158 ***
GN <sup>2</sup>	0.370 ***	0.029	-0.023 ***	-0.386 ***	-0.038	0.081	0.103 ***
GT <sup>3</sup>	0.161	0.060 ***	-0.014 ***	-0.182	1.056 ***	-1.754	0.186 ***
DD <sup>4</sup>	0.393 ***	0.011	-0.020 ***	-0.154 *	0.306	-0.153	0.040 ***
DN <sup>5</sup>	0.661 ***	0.012	-0.026 ***	-0.443 ***	-0.035	0.399	0.088 ***
DT <sup>6</sup>	0.495 ***	0.017	-0.036 ***	-0.294 ***	0.564	-0.852	0.149 ***

501 <sup>1</sup> GD represents the growing season's daytime; <sup>2</sup> GN represents the growing season's nighttime;  
502 <sup>3</sup> GT represents the growing season's transition period; <sup>4</sup> DD represents the dormant season's  
503 daytime; <sup>5</sup> DN represents the dormant season's nighttime; <sup>6</sup> DT represents the dormant season's  
504 transition period. <sup>7</sup>  $A_m$ : maximum amplitude; <sup>8</sup>  $P_m$ : corresponding period of maximum amplitude. <sup>9</sup>  
505  $u^*$ : friction velocity; <sup>10</sup> TCI: terrain complexity index; \*\*\* represents  $P < 0.001$ ; \*\* represents  $P <$   
506 0.01; and \* represents  $P < 0.05$ .

507 To evaluate the impact of  $F_{s\_comb}$  on  $NEE_{obs}$  ( $F_c + F_s$ ), we further evaluated the  
508 slope (with intercept terms forced to zero) and NRMSE of  $F_c + F_{s\_comb}$  compared to  $F_c$   
509 +  $F_{s\_28}$ , as presented in Supplementary Materials Table 7 and Table 8. The  $F_{s\_28}$  in the  
510 three forest stands was underestimated by 28.6%–33.3% compared to the  $F_{s\_comb}$ , and  
511 the NRMSE of  $F_{s\_comb}$  versus the  $F_{s\_28}$  ranged from 59.2% to 67.2%. The  $NEE_{obs}$  with  
512  $F_{s\_28}$  was underestimated by 1.9%–4.3% compared to the  $NEE_{obs}$  with  $F_{s\_comb}$ . The  
513 NRMSE of  $NEE_{obs}$  with the  $F_{s\_comb}$  versus the  $F_{s\_28}$  in the three forest stands ranged  
514 from 16.0% to 25.4%. The analysis suggested that combining the  $F_s$  values based on  
515 different averaging [CO<sub>2</sub>] time windows in the decision-level fusion model could  
516 successfully weigh potential underestimation bias and random uncertainties.

517 The influences of  $F_s$  on the relationship between NEE observations and  
518 meteorological drivers, indicated the effect of uncertainty in  $F_s$  estimates on NEE  
519 observations. Our analysis showed that the correlations between NEE observations  
520 derived from  $F_c + F_s$  and both photosynthetic photon flux density (PPFD) and air  
521 temperature are lower compared to those obtained from  $F_c$  alone (Figure 1 and Figure  
522 2 in the Supplementary Materials). Additionally, the estimated light saturated net CO<sub>2</sub>  
523 assimilation ( $A_{max}$ ) is greater when NEE observations are estimated by  $F_s + F_c$ , as  
524 opposed to when NEE is estimated solely by  $F_c$ . This suggests that  $F_s$  significantly  
525 affects daytime NEE and can correct the estimation of  $A_{max}$  and related parameters. The  
526 relationship between NEE observations and PPFD is influenced by the size of averaging  
527 time window the  $F_s$  measurement. A larger averaging window results in less random  
528 uncertainty in the  $F_s$  estimation, thereby increasing the correlation between NEE



529 observations and meteorological drivers, including PPFD and  $T_a$ .

## 530 **4 Discussion**

### 531 4.1 Short-term $[\text{CO}_2]$ fluctuations above the forest canopy and $F_s$ estimates in complex 532 terrains

533 Compared to flat and uniform underlying surface, complex terrain and  
534 heterogeneous canopies modify the trajectory, speed distribution, and direction of the  
535 airflow. Increased wind speeds and shifting wind directions also increase turbulent  
536 activity above the canopy, facilitating the mixing and dispersion of  $\text{CO}_2$ . This study  
537 found that short-term fluctuations of  $[\text{CO}_2]$  above the canopy exhibited a range of 1 to  
538 10 min (Fig. 2). These fluctuations were characterized by an average  $P_m$  ranging from  
539 2.313 to 2.784 min (Table 2). Our results are in line with previous research using  
540 wavelet analysis, which reported fluctuation periods of  $[\text{CO}_2]$  within and above the  
541 forest canopy to be between 14 and 116 s (Cava et al., 2004). Their observations of the  
542 canopy waves during periods of extreme atmospheric stability (when  $z/L \gg 1$ ) exhibited  
543 a dominant period of 1–2 min, consistent with our findings. The period of  $[\text{CO}_2]$   
544 fluctuations was found to be predominantly influenced by turbulent fluxes and the  
545 residence time of  $\text{CO}_2$  within the canopy. This indicated a potential correlation between  
546  $P_m$  and the residence time of  $\text{CO}_2$  within the canopy. Fuentes et al. (2006) employed a  
547 Lagrangian model and calculated the residence time of air parcels released near the  
548 ground and canopy, finding values ranging from 3 to 10 min and from 1 to 10 min,  
549 respectively. Similarly, Edburg et al. (2011) used the standard deviation of  $[\text{CO}_2]$

550 averages to determine CO<sub>2</sub> residence time at different locations, including the ground,  
551 within the canopy, and in their gas mixtures, yielding values of 8.6, 3.6, and 5.6 min,  
552 respectively. The results of these simulation experiments are consistent with our study,  
553 further supporting the association between [CO<sub>2</sub>] fluctuations above the forest canopy  
554 and CO<sub>2</sub> residence time.

555 Tree density and canopy structure also play a role in influencing the air parcel  
556 residence time; in flat terrains, the air parcel residence time correlate with  $u^*$  (Gerken  
557 et al., 2017), and an increase in vegetation leaf area leads to longer residence times  
558 when turbulence is not fully penetrative. **During the growing season, forests in our study**  
559 **site exhibit higher leaf area index and greater canopy densities than during the dormant**  
560 **season (Li et al., 2023), resulting in longer  $P_m$  of short-term [CO<sub>2</sub>] fluctuations above**  
561 **the canopy (Fig. 3).** Additionally, at night, stable atmospheric conditions lead to longer  
562 residence times due to suppressed turbulent mixing, resulting in relatively long  
563 nighttime  $P_m$  values compared to daytime and transition periods (Fig. 3).

564 Complex terrains introduce complex changes in air flow structures, including  
565 gravity-induced waves, drainage, and nonlinear waves induced by single gusts, leading  
566 to dramatic [CO<sub>2</sub>] fluctuations. These dynamics contribute to uncertainties in estimating  
567  $F_s$ . **During night, the difference between incoming and outgoing longwave radiation**  
568 **over the valley soil surface and vegetation canopy gives rise to radiative cooling.**  
569 **Subsequently, the air near the soil surface experiences a gravity-induced downslope**  
570 **acceleration, potentially causing katabatic flow.** As inertia-driven upslope winds are  
571 halted by katabatic acceleration, a local shallow drainage flow is established, reaching

572 a quasi-equilibrium state approximately 1.5 h after sunset (Nadeau et al., 2013). Under  
573 stable atmospheric conditions, even gentle slopes (around 1°) can generate strong  
574 gravity-driven waves (Belušić and Mahrt, 2012). Consequently, advection may  
575 complicate the interpretation of nighttime EC measurements at certain relatively gentle  
576 sites, but this complexity is not evident during daytime measurements (Leuning et al.,  
577 2008). Advection plays a role in depleting the CO<sub>2</sub> accumulated within the canopy,  
578 resulting in lower F<sub>s</sub> fluxes and establishing an inverse relationship between storage  
579 and advection (Van Gorsel et al., 2011). The occurrence of larger F<sub>s</sub> values for long P<sub>m</sub>  
580 values suggests weaker advection compared to short P<sub>m</sub> values (Fig. 4). In our study,  
581 we observed that the F<sub>s</sub> magnitude was relatively large during nighttime and transition  
582 periods, while it was smaller during daytime (Fig. 4), which is consistent with the  
583 findings reported by Wang et al. (2016).

584 **The terrain unevenness and the complexity of canopy structure significantly affect**  
585 **the airflow divergence in the atmospheric boundary layer.** This results in weakened air  
586 circulation within the canopy and spatial variation in the patterns and extent of airflow  
587 separation (Grant et al., 2015). During nighttime and transition periods in a closed  
588 canopy, the turbulent coupling state above and below the canopy gradually decouples,  
589 eventually reaching complete decoupling as the  $u^*$  decreases (Fig. 5). However, this  
590 decoupling does not lead to stable stratification within the canopy. Despite the  
591 occurrence of decoupling and advection in the closed canopy, waves are unlikely to  
592 exist within the canopy itself (Van Gorsel et al., 2011). As a result, a consistent trend  
593 in the variation of F<sub>s</sub> with  $\tau$  is observed across the three forest stands during the growing

594 season, independent of  $P_m$  (Fig. 9). Conversely, in an open canopy where waves are  
595 present, the observations of  $F_s$  become more complex. This complexity could be the  
596 primary reason why the variation of  $F_s$  with  $[CO_2]$  averaging time windows differs  
597 between the three forest stands for short  $P_m$  values during the dormant season daytime  
598 (Fig. 9). The presence of waves introduces additional variability in the measurements,  
599 leading to differences in  $F_s$  estimates based on different  $[CO_2]$  averaging time windows  
600 in these particular conditions.

#### 601 4.2 Uncertainty in forest ecosystem $F_s$ measurement in complex terrains

602 The random uncertainty of  $F_s$  shares similarities with NEE estimation. For  
603 example, the magnitude of  $F_s$  measurements is positively correlated with the standard  
604 deviation of random uncertainty in  $F_s$ . Additionally, the overall distribution of  $F_s$   
605 measurements exhibits a non-Gaussian distribution with a high peak, aligning with the  
606 statistical properties of NEE uncertainty (Richardson et al., 2006; Richardson et al.,  
607 2008). The uncertainty in the storage term depends a lot on the set-up used, together  
608 with the biological activity of the ecosystem, and the height of the control volume. In  
609 addition, various factors contribute to the uncertainty in  $F_s$  estimates, including flux  
610 measurement footprint variations, sampling frequency, spatial sampling resolution of  
611  $CO_2/H_2O$  concentrations, and instrumental measurement accuracy. The accuracy and  
612 precision requested for the  $CO_2$  and  $H_2O$  concentration measurements are  $\pm 1 \mu mol$   
613  $mol^{-1}$  and  $\pm 1 mmol mol^{-1}$ , respectively (Montagnani et al., 2018). The uncertainty  
614 arising from variations in the flux measurement footprint is considerable, typically on  
615 the order of tens of percentages, which is an order of magnitude higher than typical

616 sensor errors (Metzger, 2018). The AP200 adopts buffer volumes to mix the gas. The  
617 LI-850 analyzer integrated within in AP200 exhibits a sensitivity to water vapor of less  
618 than  $0.1 \mu\text{mol CO}_2$  per  $\text{mmol mol}^{-1} \text{H}_2\text{O}$ , and a sensitivity to  $\text{CO}_2$  of less than  $0.0001$   
619  $\text{mmol mol}^{-1} \text{H}_2\text{O}$  per  $\mu\text{mol CO}_2$ . Efforts to reduce random errors in  $[\text{CO}_2]$  originating  
620 from pressure fluctuations include adding buffer volumes before IRGA pumping tests  
621 (Marcolla et al., 2014). The buffer volumes are fully mixed during gas extraction and  
622 performs a weighted average of  $[\text{CO}_2]$  instantaneous measurements to minimize the  
623 sampling error for each level's  $[\text{CO}_2]$  measurement (Cescatti et al., 2016).

624 The  $F_s$  estimates can be influenced by singular eddies that penetrate inside the  
625 canopy (Finnigan, 2006). Accurate calculation of  $F_s$  requires considering the period of  
626  $[\text{CO}_2]$  fluctuations with the eddy coherence structure. The spectral energy of the  $F_s$  time  
627 series is primarily concentrated between 0.001 and 0.2 Hz (500 and 5 s, respectively).  
628 However, even with sampling frequencies of 2 Hz and below, significantly lower  $F_s$   
629 values are obtained (Bjorkegren et al., 2015). The Nyquist-Shannon sampling theorem  
630 dictates that accurate measurements of  $[\text{CO}_2]$  require a sampling period no longer than  
631 half the period of  $[\text{CO}_2]$  fluctuations. Consequently, to monitor short-term changes in  
632  $[\text{CO}_2]$ , measurements must be taken over a period no longer than half of the period  
633 corresponding to the maximum amplitude (or major energy) of  $[\text{CO}_2]$  fluctuations. In  
634 this study, the average  $P_m$  for  $[\text{CO}_2]$  fluctuations fell within the range of 2.313–2.784  
635 min (Table 2). Therefore, it is crucial to ensure that the sampling period for  $[\text{CO}_2]$  does  
636 not exceed 1.256 to 1.392 min, which corresponds to half the average  $P_m$  range.  
637 Monitoring fluctuations of  $P_m$  for less than 4 min during a 2-min monitoring period of

638 [CO<sub>2</sub>] presents a significant challenge. This is a primary reason that the systematic bias  
639 and random error in F<sub>s</sub> estimate with a single profile system are irreconcilable (Wang  
640 et al., 2016). Short-term [CO<sub>2</sub>] fluctuations are mainly influenced by boundary layer  
641 turbulence, and sampling errors in incomplete fluctuation cycles will be superimposed  
642 with the real advection flux (anisotropy) dispersion in complex terrains (Van Gorsel et  
643 al., 2011). This substantially increases the random uncertainty in F<sub>s</sub> based on shorter  
644 [CO<sub>2</sub>] averaging time windows (Fig. 6 and Fig. 8). As a result, the deviation of NEE  
645 estimates from the actual value expands.

646         Fluxes in heterogeneous regions are significantly higher than in uniform regions.  
647 The energy transfer from the ground surface to large eddies occurs primarily in areas  
648 with pronounced heterogeneity, and this energy distribution is uneven across the region  
649 (Aubinet et al., 2012). Once large-scale eddies acquire energy, their cascading of energy  
650 to smaller-scale eddies is influenced by topographic features, leading to variations in  
651 these smaller-scale eddies along different flow streams (Chen et al., 2023). In complex  
652 terrains, the bidirectional airflow within forests along slopes can cause the decoupling  
653 of soil CO<sub>2</sub> fluxes from EC measurements above the forest canopy (Feigenwinter et al.,  
654 2008; Aubinet et al., 2003), leading to significant errors in CO<sub>2</sub> flux measurements.  
655 Forest soil serves as the primary source of CO<sub>2</sub> gas and regions of high flux over  
656 complex terrains act like chimneys, transporting air parcels from the soil surface within  
657 forests (Chen et al., 2019). By increasing the number of gas concentration sampling  
658 points near the ground, the horizontal representativeness can be enhanced, thereby  
659 reducing the bias in the estimation of F<sub>s</sub> (Nicolini et al., 2018). In situations where

660 turbulence is not well-developed, and CO<sub>2</sub> mixing is inadequate, the trend of F<sub>s</sub> with  
661 turbulence intensity aligns with that of advective fluxes, which is opposite to that of  
662 turbulent fluxes (Mchugh et al., 2017). The temporal dynamics and amplitudes of F<sub>s</sub>  
663 changes are influenced by topography complexity and wind conditions above the forest  
664 canopy (Fig. 10). Locations with more complex and sloping topography at the flux  
665 tower are more likely to generate advective fluxes that may not be easily observed at a  
666 single point.

667 Estimating landscape CO<sub>2</sub> fluxes in complex terrains solely based on  
668 measurements from a single flux tower can introduce significant errors and biases that  
669 are not acceptable. The magnitude of these errors in F<sub>s</sub> estimates is dependent on the  
670 height of the forest canopy and the endogenous source/sink (Chen et al., 2020). To  
671 mitigate errors and biases associated with estimating F<sub>s</sub> in complex terrains, we  
672 employed a regression modeling approach using the decision-level fusion model. This  
673 method involves computing a weighted average of F<sub>s</sub> based on different [CO<sub>2</sub>]  
674 averaging time windows, effectively reducing errors and biases in the estimation of F<sub>s</sub>  
675 (see Table 5). In fact, from the definition of storage flux, it can be seen that weighting  
676 the storage flux is essentially weighting the [CO<sub>2</sub>] in the average time window, which  
677 means replacing spatial sequences with temporal sequences for weighting. The  
678 weighting coefficients used to construct the model were based on the relative errors and  
679 biases of F<sub>s</sub> estimation, with the weighting coefficient decreasing as the represented  
680 moment's length increased. To obtain more accurate estimates of forest ecosystem F<sub>s</sub> in  
681 complex terrains, further research should focus on understanding the spatiotemporal

682 patterns and dynamics of [CO<sub>2</sub>].

## 683 **5 Conclusions**

684 This study investigated the impact of short-term [CO<sub>2</sub>] fluctuations on the  
685 estimation of F<sub>s</sub> in temperate forest ecosystems within complex terrains. Additionally,  
686 it examined the F<sub>s</sub> uncertainty and the contribution of the F<sub>s</sub> to NEE using data from  
687 three flux towers. To enhance F<sub>s</sub> uncertainty estimation, statistical sampling techniques  
688 were applied based on the individual tower approach.

689 The results highlighted the significance of considering multiple time windows for  
690 averaging [CO<sub>2</sub>] when estimating F<sub>s</sub>, as [CO<sub>2</sub>] above the forest canopies exhibited  
691 fluctuations with periods ranging from 1 to 10 minutes. Diurnal, seasonal, and spatial  
692 variations were observed in the amplitude and periodicity of [CO<sub>2</sub>] fluctuations,  
693 highlighting the need for thoughtful sampling strategies. The use of individual gas  
694 analyzers to sample the CO<sub>2</sub> in the control volume was inadequate, leading to  
695 systematic biases and random errors in the F<sub>s</sub> estimates. Increasing [CO<sub>2</sub>] averaging  
696 time windows mitigated the effect of [CO<sub>2</sub>] fluctuations on F<sub>s</sub> estimates, reducing both  
697 their magnitude and uncertainty.

698 The study also revealed that the uncertainty of F<sub>s</sub> followed a non-normal  
699 distribution, with its standard deviation positively correlated with F<sub>s</sub> magnitude, which  
700 has important implications for quality control. To improve F<sub>s</sub> estimation, a decision-  
701 level fusion model was introduced, integrating F<sub>s</sub> estimates from multiple [CO<sub>2</sub>]  
702 averaging time windows, effectively reducing the impact of short-term [CO<sub>2</sub>]



703 fluctuations while considering underestimation bias and random errors. The  
704 contribution of  $F_s$  to NEE exhibited diurnal, seasonal, and spatial variations associated  
705 with  $u^*$ , contributing to the NEE observations at rates ranging from 17.2% to 82.0%  
706 depending on the turbulent mixing and terrain complexity. The influence of terrain  
707 complexity on the relationship between  $[CO_2]$  fluctuations, turbulent mixing, and the  
708 contribution of  $F_s$  to NEE was also evident. The findings from the three flux towers  
709 allowed for the generalization of these results beyond the study site. These insights  
710 provide crucial scientific support for the practical application of the eddy covariance  
711 technique and advance our understanding of accurately estimating NEE in forest  
712 ecosystems in complex terrains.

## 713 **Appendix A**

### 714 *A.1 the weight parameters of the decision-level fusion model*

715 For each 30-min  $CO_2$  storage flux ( $F_s$ ) estimate based on the  $CO_2$  concentration  
716 ( $[CO_2]$ ) averaging time window ( $\tau$ ), the weight in the decision-level fusion model can  
717 be obtained by weighting the random uncertainty and bias of  $F_{s_\tau}$ .

718 The weight of the random uncertainty for the  $F_{s_\tau}$  is expressed as follows:

$$w_\tau = \frac{1/\sigma(\varepsilon_\tau)}{\sum_j 1/\sigma(\varepsilon_j)}, \quad (A.1)$$

719 where  $\sigma(\varepsilon_\tau)$  is the random uncertainty of the  $F_{s_\tau}$ , qualified as the standard deviation.

720 The weight of the bias for the  $F_{s_\tau}$  is expressed as follows:

$$W_\tau = \frac{K_\tau}{\sum_j K_j}, \quad (A.2)$$

721 where  $K_\tau$  is the slope between the  $F_{s_\tau}$  and  $F_{s_{28}}$ .

722 Ultimately, the weight of the  $F_{s_\tau}$  in the decision-level fusion model can be

723 calculated using the following equation:

$$w_{\tau}^* = rw_{\tau} + (1 - r)W_{\tau}, \quad (\text{A.3})$$

724 where  $r$  represents the proportion of the weight of random uncertainty.

## 725 A.2 Complex terrain index

726 This study employed a novel descriptor called the terrain complexity index (*TCI*)  
727 to quantify the complexity of the three-dimensional terrain. For a given unit area, the  
728 *TCI* equation can be expressed as follows:

$$TCI = (1 - P_d \cos \alpha_d)(1 - Z_d^{-1})(D_f - 2)^{-H/\ln(12)}, \quad (\text{A.4})$$

729 where,  $P_d$  represents the volume of terrain above the lowest elevation of an area  
730 unit ( $V_u$ ) divided by the product of its largest vertically projected area ( $S_v$ ) and the  
731 edge length of the side of the area unit ( $d$ ), expressed as  $P_d = V_u/(S_v d)$ ;  $P_d$  was  
732 defined to be one when the  $S_v$  is zero. Given  $V_u$ , an increase in  $S_v$  correlates with a  
733 higher degree of terrain complexity. Notably, the  $P_d$  is defined as 1 when the terrain  
734 volume is 0 or when the terrain surface of the area unit was parallel to the horizontal  
735 plane and was smooth and homogeneous.  $\alpha_d$  indicates the slope of the area unit.  $Z_d$   
736 denoted the terrain roughness, which defined as the ratio of the terrain surface area to  
737 the projected horizontal plane (Loke and Chisholm, 2022). The value of  $Z_d$  is in the  
738 range of  $[1, +\infty)$ . The larger  $Z_d$ , the more complex the terrain.  $D_f$  is the fractal  
739 dimension of terrain surface area, which ranged from 2 to 3 and described the  
740 complexity in spatially self-similar structure of the local surface within the area unit  
741 and the area unit surface (B. B. Mandelbrot, 1967; Taud and Parrot, 2005). Employing  
742 terrain surface area, the box-counting method is used to estimate fractal dimension of

743 unit area.  $H$  represented the Shannon-Wiener index and expressed as  $H =$   
744  $-\sum_{i=1}^n P_i \ln(P_i)$ , capturing the uniformity of the spatial distribution of the pixel  
745 aspects within the area unit (Brown, 1997). When the aspect of each pixel is divided  
746 into  $30^\circ$  segments,  $P_i$  denotes the proportion of the  $i^{\text{th}}$  type of pixel aspects within the  
747 area unit and  $n$  was the total number of pixel aspect types within the area unit. A  
748 larger  $H$  indicates a more complex terrain. When the number of pixel aspect types in  
749 the area unit is kept constant, it's essential to recognize that greater uniformity in the  
750 distribution of all pixel aspect in the area unit results in a larger  $H$ . Similarly, when the  
751 uniformity of the distribution of pixel aspects in the area unit is kept constant, a larger  
752  $H$  is achieved with an increase in the observation of the number of pixel aspect types.

753 To quantify the terrain complexity of the underlying surface around the flux towers,  
754 we computed the quartiles of  $TCI$  for all area units within a sector (divided by  $30^\circ$ ) with  
755 a radius of 380 m. A weighted geometric mean was employed to construct  $TCIs$ , which  
756 describe the statistical distribution of  $TCI$  of the sector. The  $TCIs$  represents the  
757 topographic complexity of the sector and are calculated using the following equation:

$$758 \quad TCI_s = (TCI_5 TCI_{25} TCI_{50} TCI_{75} TCI_{95})^{1/5} \quad (\text{A.5})$$

759 where  $TCI_5$ ,  $TCI_{25}$ ,  $TCI_{50}$ ,  $TCI_{75}$ , and  $TCI_{95}$  are the quartiles of 5%, 25%, 50%, 75%,  
760 and 95%, respectively. The  $TCIs$  values range from 0 to 1, with higher values indicating  
761 greater terrain complexity.

762 *Data availability.* Data used in this paper are available at the Science Data Bank  
763 (<https://www.scidb.cn/en/s/7ZfQZv>) or upon request to the corresponding author.

764 *Author contributions.* DT developed the manuscript; JZ was responsible for

765 conceptualizing the idea and designing the research study; TG substantially structured  
766 the manuscript; FY contributed to the data collection process; YZ helped in the design  
767 and preparation of the figures and tables; XZ and BY revised the manuscript.

768 *Competing interests.* The authors declare that they have no known competing  
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